

Mathematica 11.3 Integration Test Results

Test results for the 1563 problems in "4.1.2.2 (g cos)^p (a+b sin)^m (c+d sin)^n.m"

Problem 6: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[e+fx]^2 \sqrt{a+a \sin[e+fx]}}{(c-c \sin[e+fx])^{3/2}} dx$$

Optimal (type 3, 99 leaves, 5 steps):

$$-\frac{2a \cos[e+fx] \operatorname{Log}[1-\sin[e+fx]]}{cf \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}} - \frac{\cos[e+fx] \sqrt{a+a \sin[e+fx]}}{cf \sqrt{c-c \sin[e+fx]}}$$

Result (type 3, 127 leaves):

$$-\left(\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \sqrt{a(1+\sin[e+fx])} \right. \\ \left. (-2ifx + 4i \operatorname{ArcTan}[e^{i(e+fx)}] + 2 \operatorname{Log}[1+e^{2i(e+fx)}] + \sin[e+fx]) \right) / \\ \left(f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right) (c-c \sin[e+fx])^{3/2} \right)$$

Problem 7: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[e+fx]^2 \sqrt{a+a \sin[e+fx]}}{(c-c \sin[e+fx])^{5/2}} dx$$

Optimal (type 3, 97 leaves, 5 steps):

$$\frac{\cos[e+fx] \sqrt{a+a \sin[e+fx]}}{cf (c-c \sin[e+fx])^{3/2}} + \frac{a \cos[e+fx] \operatorname{Log}[1-\sin[e+fx]]}{c^2 f \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}}$$

Result (type 3, 118 leaves):

$$\frac{1}{c^2 f \sqrt{c-c \sin[e+fx]}} \operatorname{Sec}[e+fx] \sqrt{a(1+\sin[e+fx])} (2-ifx + \operatorname{Log}[1+e^{2i(e+fx)}]) - \\ 2i \operatorname{ArcTan}[e^{i(e+fx)}] (-1+\sin[e+fx]) + (ifx - \operatorname{Log}[1+e^{2i(e+fx)}]) \sin[e+fx]$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e+f x]^2 (a+a \sin [e+f x])^{3 / 2}}{\sqrt{c-c \sin [e+f x]}} d x$$

Optimal (type 3, 45 leaves, 2 steps):

$$\frac{\cos [e+f x] (a+a \sin [e+f x])^{5 / 2}}{3 a f \sqrt{c-c \sin [e+f x]}}$$

Result (type 3, 111 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right) (a (1+\sin [e+f x]))^{3 / 2} \right. \\ \left. (-6 \cos [2 (e+f x)] + 15 \sin [e+f x] - \sin [3 (e+f x)]) \right) / \\ \left(12 f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^3 \sqrt{c-c \sin [e+f x]} \right)$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e+f x]^2 (a+a \sin [e+f x])^{3 / 2}}{(c-c \sin [e+f x])^{9 / 2}} d x$$

Optimal (type 3, 48 leaves, 2 steps):

$$\frac{\cos [e+f x] (a+a \sin [e+f x])^{5 / 2}}{6 a c f (c-c \sin [e+f x])^{7 / 2}}$$

Result (type 3, 110 leaves):

$$- \left(\left(a (-5+3 \cos [2 (e+f x)]) \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^3 \sqrt{a (1+\sin [e+f x])} \right) \right. \\ \left. \left(6 c^4 f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right) (-1+\sin [e+f x])^4 \sqrt{c-c \sin [e+f x]} \right) \right)$$

Problem 23: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e+f x]^2 (a+a \sin [e+f x])^{5 / 2}}{\sqrt{c-c \sin [e+f x]}} d x$$

Optimal (type 3, 45 leaves, 2 steps):

$$\frac{\cos [e+f x] (a+a \sin [e+f x])^{7 / 2}}{4 a f \sqrt{c-c \sin [e+f x]}}$$

Result (type 3, 119 leaves):

$$\left(\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right) \left(a(1 + \sin[e+fx]) \right)^{5/2} \right. \\ \left. (-28 \cos[2(e+fx)] + \cos[4(e+fx)] + 56 \sin[e+fx] - 8 \sin[3(e+fx)]) \right) / \\ \left(32 f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \sqrt{c - c \sin[e+fx]} \right)$$

Problem 28: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a + a \sin[e+fx])^{5/2}}{(c - c \sin[e+fx])^{11/2}} dx$$

Optimal (type 3, 48 leaves, 2 steps):

$$\frac{\cos[e+fx] (a + a \sin[e+fx])^{7/2}}{8 a c f (c - c \sin[e+fx])^{9/2}}$$

Result (type 3, 329 leaves):

$$\frac{2 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 \left(a(1 + \sin[e+fx]) \right)^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c - c \sin[e+fx])^{11/2}} - \\ \frac{4 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \left(a(1 + \sin[e+fx]) \right)^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c - c \sin[e+fx])^{11/2}} + \\ \frac{3 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 \left(a(1 + \sin[e+fx]) \right)^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c - c \sin[e+fx])^{11/2}} - \\ \frac{\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(a(1 + \sin[e+fx]) \right)^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c - c \sin[e+fx])^{11/2}}$$

Problem 29: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a + a \sin[e+fx])^{5/2}}{(c - c \sin[e+fx])^{13/2}} dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\frac{\cos[e+fx] (a + a \sin[e+fx])^{7/2}}{10 a c f (c - c \sin[e+fx])^{11/2}} + \frac{\cos[e+fx] (a + a \sin[e+fx])^{7/2}}{80 a c^2 f (c - c \sin[e+fx])^{9/2}}$$

Result (type 3, 333 leaves):

$$\frac{8 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 (a(1+\sin[e+fx]))^{5/2}}{5 f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c-c\sin[e+fx])^{13/2}} -$$

$$\frac{3 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (a(1+\sin[e+fx]))^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c-c\sin[e+fx])^{13/2}} +$$

$$\frac{2 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (a(1+\sin[e+fx]))^{5/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c-c\sin[e+fx])^{13/2}} -$$

$$\frac{\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^9 (a(1+\sin[e+fx]))^{5/2}}{2 f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (c-c\sin[e+fx])^{13/2}}$$

Problem 30: Result more than twice size of optimal antiderivative.

$$\int \cos[e+fx]^2 (a+a\sin[e+fx])^{7/2} (c-c\sin[e+fx])^{9/2} dx$$

Optimal (type 3, 236 leaves, 6 steps):

$$\frac{4 a^4 \cos[e+fx] (c-c\sin[e+fx])^{11/2}}{315 c f \sqrt{a+a\sin[e+fx]}} -$$

$$\frac{4 a^3 \cos[e+fx] \sqrt{a+a\sin[e+fx]} (c-c\sin[e+fx])^{11/2}}{105 c f} -$$

$$\frac{a^2 \cos[e+fx] (a+a\sin[e+fx])^{3/2} (c-c\sin[e+fx])^{11/2}}{15 c f} -$$

$$\frac{4 a \cos[e+fx] (a+a\sin[e+fx])^{5/2} (c-c\sin[e+fx])^{11/2}}{45 c f} -$$

$$\frac{\cos[e+fx] (a+a\sin[e+fx])^{7/2} (c-c\sin[e+fx])^{11/2}}{10 c f}$$

Result (type 3, 919 leaves):

$$\begin{aligned}
 & \left(21 \operatorname{Cos}[2(e+fx)] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(512 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(3 \operatorname{Cos}[4(e+fx)] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(128 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(9 \operatorname{Cos}[6(e+fx)] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(1024 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(\operatorname{Cos}[8(e+fx)] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(512 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(\operatorname{Cos}[10(e+fx)] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(5120 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(63 \operatorname{Sin}[e+fx] (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \right) / \\
 & \left(128 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(7 (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \operatorname{Sin}[3(e+fx)] \right) / \\
 & \left(64 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(9 (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \operatorname{Sin}[5(e+fx)] \right) / \\
 & \left(320 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left(9 (a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \operatorname{Sin}[7(e+fx)] \right) / \\
 & \left(1792 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right) + \\
 & \left((a(1+\operatorname{Sin}[e+fx]))^{7/2} (c-c\operatorname{Sin}[e+fx])^{9/2} \operatorname{Sin}[9(e+fx)] \right) / \\
 & \left(2304 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^9 \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^7 \right)
 \end{aligned}$$

Problem 35: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[e+fx]^2 (a+a\operatorname{Sin}[e+fx])^{7/2}}{\sqrt{c-c\operatorname{Sin}[e+fx]}} dx$$

Optimal (type 3, 45 leaves, 2 steps):

$$\frac{\cos [e+f x] (a+a \sin [e+f x])^{9 / 2}}{5 a f \sqrt{c-c \sin [e+f x]}}$$

Result (type 3, 142 leaves):

$$\left(a^3 \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right) \left(1 + \sin [e+f x] \right)^3 \sqrt{a (1 + \sin [e+f x])} (-120 \cos [2 (e+f x)] + 10 \cos [4 (e+f x)] + 210 \sin [e+f x] - 45 \sin [3 (e+f x)] + \sin [5 (e+f x)]) \right) / \left(80 f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 \sqrt{c-c \sin [e+f x]} \right)$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e+f x]^2 (a+a \sin [e+f x])^{7 / 2}}{(c-c \sin [e+f x])^{13 / 2}} dx$$

Optimal (type 3, 48 leaves, 2 steps):

$$\frac{\cos [e+f x] (a+a \sin [e+f x])^{9 / 2}}{10 a c f (c-c \sin [e+f x])^{11 / 2}}$$

Result (type 3, 412 leaves):

$$\frac{16 \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^3 (a (1 + \sin [e+f x]))^{7 / 2}}{5 f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (c-c \sin [e+f x])^{13 / 2}} - \frac{8 \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^5 (a (1 + \sin [e+f x]))^{7 / 2}}{f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (c-c \sin [e+f x])^{13 / 2}} + \frac{8 \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (a (1 + \sin [e+f x]))^{7 / 2}}{f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (c-c \sin [e+f x])^{13 / 2}} - \frac{4 \left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^9 (a (1 + \sin [e+f x]))^{7 / 2}}{f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (c-c \sin [e+f x])^{13 / 2}} + \frac{\left(\cos \left[\frac{1}{2} (e+f x) \right] - \sin \left[\frac{1}{2} (e+f x) \right] \right)^{11} (a (1 + \sin [e+f x]))^{7 / 2}}{f \left(\cos \left[\frac{1}{2} (e+f x) \right] + \sin \left[\frac{1}{2} (e+f x) \right] \right)^7 (c-c \sin [e+f x])^{13 / 2}}$$

Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e+f x]^2 (a+a \sin [e+f x])^{7 / 2}}{(c-c \sin [e+f x])^{15 / 2}} dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\frac{\cos[e+fx] (a+a\sin[e+fx])^{9/2}}{12acf(c-c\sin[e+fx])^{13/2}} + \frac{\cos[e+fx] (a+a\sin[e+fx])^{9/2}}{120ac^2f(c-c\sin[e+fx])^{11/2}}$$

Result (type 3, 419 leaves):

$$\begin{aligned} & \frac{8 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^3 (a(1+\sin[e+fx]))^{7/2}}{3f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (c-c\sin[e+fx])^{15/2}} - \\ & \frac{32 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 (a(1+\sin[e+fx]))^{7/2}}{5f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (c-c\sin[e+fx])^{15/2}} + \\ & \frac{6 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (a(1+\sin[e+fx]))^{7/2}}{f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (c-c\sin[e+fx])^{15/2}} - \\ & \frac{8 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^9 (a(1+\sin[e+fx]))^{7/2}}{3f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (c-c\sin[e+fx])^{15/2}} + \\ & \frac{\left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^{11} (a(1+\sin[e+fx]))^{7/2}}{2f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^7 (c-c\sin[e+fx])^{15/2}} \end{aligned}$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a+a\sin[e+fx])^{7/2}}{(c-c\sin[e+fx])^{17/2}} dx$$

Optimal (type 3, 145 leaves, 4 steps):

$$\begin{aligned} & \frac{\cos[e+fx] (a+a\sin[e+fx])^{9/2}}{14acf(c-c\sin[e+fx])^{15/2}} + \\ & \frac{\cos[e+fx] (a+a\sin[e+fx])^{9/2}}{84ac^2f(c-c\sin[e+fx])^{13/2}} + \frac{\cos[e+fx] (a+a\sin[e+fx])^{9/2}}{840ac^3f(c-c\sin[e+fx])^{11/2}} \end{aligned}$$

Result (type 3, 419 leaves):

$$\begin{aligned} & \frac{16 \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^3 (a (1 + \sin [e + f x]))^{7/2}}{7 f \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (c - c \sin [e + f x])^{17/2}} - \\ & \frac{16 \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^5 (a (1 + \sin [e + f x]))^{7/2}}{3 f \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (c - c \sin [e + f x])^{17/2}} + \\ & \frac{24 \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (a (1 + \sin [e + f x]))^{7/2}}{5 f \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (c - c \sin [e + f x])^{17/2}} - \\ & \frac{2 \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^9 (a (1 + \sin [e + f x]))^{7/2}}{f \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (c - c \sin [e + f x])^{17/2}} + \\ & \frac{\left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^{11} (a (1 + \sin [e + f x]))^{7/2}}{3 f \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right)^7 (c - c \sin [e + f x])^{17/2}} \end{aligned}$$

Problem 44: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e + f x]^2 (c - c \sin [e + f x])^{5/2}}{\sqrt{a + a \sin [e + f x]}} dx$$

Optimal (type 3, 45 leaves, 2 steps):

$$\frac{\cos [e + f x] (c - c \sin [e + f x])^{7/2}}{4 c f \sqrt{a + a \sin [e + f x]}}$$

Result (type 3, 134 leaves):

$$\begin{aligned} & \left(c^2 \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right) (-1 + \sin [e + f x])^2 \sqrt{c - c \sin [e + f x]} \right. \\ & \quad \left. (28 \cos [2 (e + f x)] - \cos [4 (e + f x)] + 56 \sin [e + f x] - 8 \sin [3 (e + f x)]) \right) / \\ & \left(32 f \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^5 \sqrt{a (1 + \sin [e + f x])} \right) \end{aligned}$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [e + f x]^2 (c - c \sin [e + f x])^{3/2}}{\sqrt{a + a \sin [e + f x]}} dx$$

Optimal (type 3, 45 leaves, 2 steps):

$$\frac{\cos [e + f x] (c - c \sin [e + f x])^{5/2}}{3 c f \sqrt{a + a \sin [e + f x]}}$$

Result (type 3, 120 leaves):

$$\begin{aligned}
 & - \left(\left(c \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right) (-1 + \sin [e + f x]) \right. \right. \\
 & \quad \left. \left. \sqrt{c - c \sin [e + f x]} (6 \cos [2 (e + f x)] + 15 \sin [e + f x] - \sin [3 (e + f x)]) \right) \right) / \\
 & \left(12 f \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right) \sqrt{a (1 + \sin [e + f x])} \right)
 \end{aligned}$$

Problem 53: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [e + f x]^2 \sqrt{c - c \sin [e + f x]}}{(a + a \sin [e + f x])^{3/2}} dx$$

Optimal (type 3, 96 leaves, 5 steps):

$$\frac{2 c \cos [e + f x] \operatorname{Log}[1 + \sin [e + f x]]}{a f \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} + \frac{\cos [e + f x] \sqrt{c - c \sin [e + f x]}}{a f \sqrt{a + a \sin [e + f x]}}$$

Result (type 3, 127 leaves):

$$\begin{aligned}
 & - \left(\left(\left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right) \right)^3 \right. \\
 & \quad \left. (2 i f x + 4 i \operatorname{ArcTan} [e^{i (e + f x)}] - 2 \operatorname{Log}[1 + e^{2 i (e + f x)}] + \sin [e + f x]) \sqrt{c - c \sin [e + f x]} \right) / \\
 & \left(f \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right) (a (1 + \sin [e + f x]))^{3/2} \right)
 \end{aligned}$$

Problem 61: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [e + f x]^2 \sqrt{c - c \sin [e + f x]}}{(a + a \sin [e + f x])^{5/2}} dx$$

Optimal (type 3, 97 leaves, 5 steps):

$$- \frac{c \cos [e + f x] \operatorname{Log}[1 + \sin [e + f x]]}{a^2 f \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} - \frac{\cos [e + f x] \sqrt{c - c \sin [e + f x]}}{a f (a + a \sin [e + f x])^{3/2}}$$

Result (type 3, 121 leaves):

$$\begin{aligned}
 & \left(i \operatorname{Sec}[e + f x] \sqrt{c - c \sin [e + f x]} \right. \\
 & \quad \left. (2 i + f x + i \operatorname{Log}[1 + e^{2 i (e + f x)}] + (f x + i \operatorname{Log}[1 + e^{2 i (e + f x)}]) \sin [e + f x] + \right. \\
 & \quad \left. 2 \operatorname{ArcTan} [e^{i (e + f x)}] (1 + \sin [e + f x])) \right) / \left(a^2 f \sqrt{a (1 + \sin [e + f x])} \right)
 \end{aligned}$$

Problem 65: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [e + f x]^2 (a + a \sin [e + f x])^m (c - c \sin [e + f x])^n dx$$

Optimal (type 5, 114 leaves, 5 steps):

$$\frac{1}{f (3 + 2 m)} 2^{\frac{3+n}{2}} c^2 \cos [e + f x]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{2} (3 + 2 m), \frac{1}{2} (-1 - 2 n), \frac{1}{2} (5 + 2 m), \frac{1}{2} (1 + \sin [e + f x])\right] (1 - \sin [e + f x])^{\frac{1}{2}-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-2+n}$$

Result (type 6, 15688 leaves):

$$\begin{aligned} & - \left(\left(4^{3+n} (3 + 2 n) \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \right. \\ & \quad \left. \left. (a + a \sin [e + f x])^m (c - c \sin [e + f x])^n \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right. \right. \\ & \quad \left. \left. \left(\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2n} \left(\frac{1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \right. \right. \\ & \quad \left. \left. \left(5 \operatorname{AppellF1} \left[\frac{1}{2} + n, -2 m, 3 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \left(- (3 + 2 n) \operatorname{AppellF1} \left[\frac{1}{2} + n, \right. \right. \right. \\ & \quad \quad \left. \left. \left. -2 m, 3 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\ & \quad \left. 2 \left(2 m \operatorname{AppellF1} \left[\frac{3}{2} + n, 1 - 2 m, 3 + 2 (m + n), \frac{5}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (3 + 2 m + 2 n) \operatorname{AppellF1} \left[\frac{3}{2} + n, -2 m, 2 (2 + m + n), \frac{5}{2} + \right. \right. \right. \\ & \quad \quad \left. \left. \left. n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\ & \quad \left(4 \operatorname{AppellF1} \left[\frac{1}{2} + n, -2 m, 5 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \left(- (3 + 2 n) \operatorname{AppellF1} \left[\frac{1}{2} + n, -2 m, \right. \right. \right. \\ & \quad \quad \left. \left. \left. 5 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\ & \quad \left. 2 \left(2 m \operatorname{AppellF1} \left[\frac{3}{2} + n, 1 - 2 m, 5 + 2 (m + n), \frac{5}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (5 + 2 m + 2 n) \operatorname{AppellF1} \left[\frac{3}{2} + n, -2 m, 2 (3 + m + n), \frac{5}{2} + \right. \right. \right. \\ & \quad \quad \left. \left. \left. n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\ & \quad \left(\operatorname{AppellF1} \left[\frac{1}{2} + n, -2 m, 2 (1 + m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \quad \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) / \end{aligned}$$

$$\begin{aligned}
 & \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+ \right. \right. \\
 & \quad \quad \left. \left. n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \\
 & \quad \left(8 \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) / \\
 & \quad \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \quad 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(2+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 5+2(m+n), \frac{5}{2}+n, \right. \right. \\
 & \quad \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) / \\
 & \quad \left(f(1+2n) \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^5 \left(-\frac{1}{(1+2n) \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^6} \right. \right. \\
 & \quad \quad \left. \left. 5 \times 2^{3+2n} (3+2n) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2n} \left(\frac{1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2m} \right. \right. \\
 & \quad \quad \left. \left. \left(\left(5 \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \right) / \right. \\
 & \quad \quad \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 3+2(m+n), \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+2m+2n) \right. \right. \\
 & \quad \quad \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(2+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+\left(4 \operatorname{AppellF1}\left[\frac{1}{2}+n,\right.\right. \\
 & \left.\left.-2 m, 5+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) / \\
 & \left(-\left(3+2 n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n,-2 m, 5+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2 m, 5+2(m+n),\right.\right.\right. \\
 & \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(5+2 m+2 n)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}+n,-2 m, 2(3+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}+n,-2 m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^3\right) / \\
 & \left(-\left(3+2 n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n,-2 m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2 m, 2(1+m+n),\right.\right.\right. \\
 & \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left.\left.(1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n,-2 m, 3+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(8 \operatorname{AppellF1}\left[\frac{1}{2}+n,-2 m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
 & \left(-\left(3+2 n\right) \operatorname{AppellF1}\left[\frac{1}{2}+n,-2 m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2 m, 2(2+m+n),\right.\right.\right. \\
 & \left.\left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left.\left.(2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n,-2 m, 5+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) + \\
 & \frac{1}{(1+2 n)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^5} 4^{1+n}(3+2 n) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2n} \\
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left(\left(5 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) / \right. \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m+n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (3 + 2m + 2n) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \left(4 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2 \right. \right. \right. \\
 & \quad \left. \left. \left. m, 5 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \right. \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 5 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 5 + 2(m+n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5 + 2m + 2n) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(3 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3 \right) / \right. \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1 + m + n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (1 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 3 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(8 \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 2(2+m+n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) / \\
 & \left(- (3+2n) \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 2(2+m+n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} + n, 1-2m, 2(2+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \right. \\
 & \quad \left. (2+m+n) \operatorname{AppellF1} \left[\frac{3}{2} + n, -2m, 5+2(m+n), \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
 & \frac{1}{(1+2n) \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)^5} 2^{5+2n} n (3+2n) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \\
 & \left(\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2} \right)^{-1+2n} \\
 & \left(\frac{1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2} \right)^{2m} \\
 & \left(- \frac{\operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2}{2 \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2} + \frac{\operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2}{4 \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)} \right) \\
 & \left(\left(5 \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 3+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) / \\
 & \left(- (3+2n) \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 3+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} + n, 1-2m, 3+2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (3+2m+2n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{3}{2} + n, -2m, 2(2+m+n), \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
 & \left(4 \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 5+2(m+n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 5+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 5+2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (5+2m+2n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(3+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3 \right) / \\
 & \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(1+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(1+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(8 \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) / \\
 & \left(-(3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(2+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 5+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \frac{1}{(1+2n) \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^5} 2^{5+2n} m (3+2n) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2n}
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-1+2m} \\
 & \left(- \left(\left(\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \right. \\
 & \quad \left. \left(2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \right) \\
 & \left(\left(5 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) / \right. \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (3 + 2m + 2n) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \quad \left(4 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 5 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 5 + 2(m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 5 + 2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5 + 2m + 2n) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 2(3 + m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3 \right) / \\
 & \quad \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1 + m + n), \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \Big] + \\
 & (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 3+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \Big] - \\
 & \left(8 \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \\
 & \left(- (3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 2(2+m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 2(2+m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 5+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \Big] + \\
 & \frac{1}{(1+2n) \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^5} 4^{2+n} (3+2n) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{2n} \\
 & \left(\frac{1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{2m} \\
 & \left(\left(5 \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) \Big] / \\
 & \left(- (3+2n) \operatorname{AppellF1}\left[\frac{1}{2}+n, -2m, 3+2(m+n), \frac{3}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2m, 3+2(m+n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3+2m+2n) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}+n, -2m, 2(2+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \Big] +
 \end{aligned}$$

$$\begin{aligned}
 & \left(5 \left(-\frac{1}{\frac{3}{2}+n} m \left(\frac{1}{2} + n \right) \text{AppellF1} \left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m+n), \frac{5}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \right. \\
 & \quad \left. \left. \left. \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 \left(\frac{3}{2} + n \right)} \left(\frac{1}{2} + n \right) (3 + 2(m+n)) \text{AppellF1} \left[\frac{3}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 4 + 2(m+n), \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left. \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \left(1 + \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) \right) / \\
 & \left(- (3 + 2n) \text{AppellF1} \left[\frac{1}{2} + n, -2m, 3 + 2(m+n), \frac{3}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \text{AppellF1} \left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m+n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (3 + 2m + 2n) \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{3}{2} + n, -2m, 2(2 + m + n), \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \right. \\
 & \left. \left(4 \left(-\frac{1}{\frac{3}{2}+n} m \left(\frac{1}{2} + n \right) \text{AppellF1} \left[\frac{3}{2} + n, 1 - 2m, 5 + 2(m+n), \frac{5}{2} + n, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \right. \\
 & \quad \left. \left. \left. \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{2 \left(\frac{3}{2} + n \right)} \left(\frac{1}{2} + n \right) (5 + 2(m+n)) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{3}{2} + n, -2m, 6 + 2(m+n), \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \right) / \\
 & \left(- (3 + 2n) \text{AppellF1} \left[\frac{1}{2} + n, -2m, 5 + 2(m+n), \frac{3}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \text{AppellF1} \left[\frac{3}{2} + n, 1 - 2m, 5 + 2(m+n), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (5 + 2m + 2n) \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{3}{2} + n, -2m, 2(3 + m + n), \frac{5}{2} + n, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \Big] + \\
 & (2 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2 m, 5 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \Big] - \\
 & \left(8 \left(-\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right) \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2 m, 2(2 + m + n), \frac{5}{2} + n, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{\frac{3}{2} + n} \left(\frac{1}{2} + n\right) (2 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2 m, \right. \right. \\
 & \left. \left. 1 + 2(2 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 \Big) / \\
 & \left(- (3 + 2 n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2 m, 2(2 + m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2 m, 2(2 + m + n), \right. \right. \right. \\
 & \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \left. (2 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2 m, 5 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2} + n, -2 m, 2(1 + m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^3 \right. \\
 & \left. \left(2 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2 m, 2(1 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (1 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2 m, \right. \right. \right. \\
 & \left. \left. 3 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - (3 + 2 n) \left(-\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2 m, 2(1 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
& \frac{1}{\frac{3}{2} + n} \left(\frac{1}{2} + n\right) (1 + m + n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 1 + 2(1 + m + n), \right. \\
& \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big) + 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
& \left(m \left(-\frac{1}{\frac{5}{2} + n} \left(\frac{3}{2} + n\right) (1 + m + n) \operatorname{AppellF1}\left[\frac{5}{2} + n, 1 - 2m, 1 + 2(1 + m + n), \right. \right. \right. \\
& \left. \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2\left(\frac{5}{2} + n\right)} \right. \\
& \left. (1 - 2m) \left(\frac{3}{2} + n\right) \operatorname{AppellF1}\left[\frac{5}{2} + n, 2 - 2m, 2(1 + m + n), \frac{7}{2} + n, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big) \right) + \\
& (1 + m + n) \left(-\frac{1}{\frac{5}{2} + n} m \left(\frac{3}{2} + n\right) \operatorname{AppellF1}\left[\frac{5}{2} + n, 1 - 2m, 3 + 2(m + n), \right. \right. \\
& \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2\left(\frac{5}{2} + n\right)} \right. \\
& \left. \left(\frac{3}{2} + n\right) (3 + 2(m + n)) \operatorname{AppellF1}\left[\frac{5}{2} + n, -2m, 4 + 2(m + n), \right. \right. \\
& \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big) \right) \Big) \Big) \Big) / \\
& \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(1 + m + n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(1 + m + n), \right. \right. \right. \\
& \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + m + n) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 3 + 2(m + n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & \left(8 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(2+m+n), \frac{3}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right. \\
 & \quad \left. \left(2 \left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(2+m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, \right. \right. \\
 & \quad \quad \left. \left. 5 + 2(m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - (3+2n) \left(-\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right)\right. \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(2+m+n), \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{\frac{3}{2} + n} \left(\frac{1}{2} + n\right) (2+m+n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 1 + 2(2+m+n), \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left(m \left(-\frac{1}{\frac{5}{2} + n} \left(\frac{3}{2} + n\right) (2+m+n) \operatorname{AppellF1}\left[\frac{5}{2} + n, 1 - 2m, 1 + 2(2+m+n), \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{7}{2} + n, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2\left(\frac{5}{2} + n\right)} \right. \\
 & \quad \quad \left. (1 - 2m) \left(\frac{3}{2} + n\right) \operatorname{AppellF1}\left[\frac{5}{2} + n, 2 - 2m, 2(2+m+n), \frac{7}{2} + n, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \right) + \\
 & \quad (2+m+n) \left(-\frac{1}{\frac{5}{2} + n} m \left(\frac{3}{2} + n\right) \operatorname{AppellF1}\left[\frac{5}{2} + n, 1 - 2m, 5 + 2(m+n), \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{7}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2\left(\frac{5}{2} + n\right)} \\
 & \left(\frac{3}{2} + n\right) (5 + 2(m + n)) \operatorname{AppellF1}\left[\frac{5}{2} + n, -2m, 6 + 2(m + n), \right. \\
 & \left. \frac{7}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left(- (3 + 2n) \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 2(2 + m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 2(2 + m + n), \right. \right. \right. \\
 & \left. \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (2 + m + n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 5 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 - \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{2} + n, -2m, 3 + 2(m + n), \frac{3}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 \right. \\
 & \left. \left(\left(2m \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3 + 2m + 2n) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, \right. \right. \right. \right. \\
 & \left. \left. \left. 2(2 + m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - (3 + 2n) \left(-\frac{1}{\frac{3}{2} + n} m \left(\frac{1}{2} + n\right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{3}{2} + n, 1 - 2m, 3 + 2(m + n), \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) - \\
 & \frac{1}{2\left(\frac{3}{2} + n\right)} \left(\frac{1}{2} + n\right) (3 + 2(m + n)) \operatorname{AppellF1}\left[\frac{3}{2} + n, -2m, 4 + 2(m + n), \right. \\
 & \left. \frac{5}{2} + n, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + 2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \left(2 m \left(-\frac{1}{2 \left(\frac{5}{2} + n \right)} \left(\frac{3}{2} + n \right) (3 + 2 (m + n)) \text{AppellF1} \left[\frac{5}{2} + n, 1 - 2 m, 4 + \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (m + n), \frac{7}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \\
 & \quad \left. \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{1}{2 \left(\frac{5}{2} + n \right)} \right. \\
 & \quad \left. (1 - 2 m) \left(\frac{3}{2} + n \right) \text{AppellF1} \left[\frac{5}{2} + n, 2 - 2 m, 3 + 2 (m + n), \frac{7}{2} + n, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \left. \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) + \\
 & (3 + 2 m + 2 n) \left(-\frac{1}{\frac{5}{2} + n} m \left(\frac{3}{2} + n \right) \text{AppellF1} \left[\frac{5}{2} + n, 1 - 2 m, 2 (2 + m + n), \right. \right. \\
 & \quad \left. \left. \frac{7}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{\frac{5}{2} + n} \right. \\
 & \quad \left. \left(\frac{3}{2} + n \right) (2 + m + n) \text{AppellF1} \left[\frac{5}{2} + n, -2 m, 1 + 2 (2 + m + n), \right. \right. \\
 & \quad \left. \left. \frac{7}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \left. \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \right) \left. \right) / \\
 & \left(- (3 + 2 n) \text{AppellF1} \left[\frac{1}{2} + n, -2 m, 3 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2 m \text{AppellF1} \left[\frac{3}{2} + n, 1 - 2 m, 3 + 2 (m + n), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (3 + 2 m + 2 n) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{3}{2} + n, -2 m, 2 (2 + m + n), \frac{5}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 - \\
 & \left(4 \text{AppellF1} \left[\frac{1}{2} + n, -2 m, 5 + 2 (m + n), \frac{3}{2} + n, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2] \\
 & \left(2 m \operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2 m, 5+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(5+2 m+2 n) \operatorname{AppellF1}\left[\frac{3}{2}+n,-2 m,\right. \\
 & \quad \left.2(3+m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-(3+2 n)\left(-\frac{1}{\frac{3}{2}+n} m\left(\frac{1}{2}+n\right)\right. \\
 & \quad \left.\operatorname{AppellF1}\left[\frac{3}{2}+n, 1-2 m, 5+2(m+n), \frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]- \\
 & \quad \frac{1}{2\left(\frac{3}{2}+n\right)}\left(\frac{1}{2}+n\right)(5+2(m+n)) \operatorname{AppellF1}\left[\frac{3}{2}+n,-2 m, 6+2(m+n),\right. \\
 & \quad \left.\frac{5}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \\
 & \left(2 m\left(-\frac{1}{2\left(\frac{5}{2}+n\right)}\left(\frac{3}{2}+n\right)(5+2(m+n)) \operatorname{AppellF1}\left[\frac{5}{2}+n, 1-2 m, 6+\right.\right.\right. \\
 & \quad \left.\left.2(m+n), \frac{7}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{1}{2\left(\frac{5}{2}+n\right)} \\
 & \quad (1-2 m)\left(\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}+n, 2-2 m, 5+2(m+n), \frac{7}{2}+n,\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+ \\
 & (5+2 m+2 n)\left(-\frac{1}{\frac{5}{2}+n} m\left(\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}+n, 1-2 m, 2(3+m+n),\right.\right. \\
 & \quad \left.\frac{7}{2}+n, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{\frac{5}{2}+n}\right)
 \end{aligned}$$

$$\begin{aligned} & \left(\frac{3}{2} + n \right) (3 + m + n) \operatorname{AppellF1} \left[\frac{5}{2} + n, -2m, 1 + 2(3 + m + n), \right. \\ & \left. \frac{7}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \\ & \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right] \bigg) \bigg) \bigg) \bigg) \bigg) / \\ & \left(-(3 + 2n) \operatorname{AppellF1} \left[\frac{1}{2} + n, -2m, 5 + 2(m + n), \frac{3}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\ & \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} + n, 1 - 2m, 5 + 2(m + n), \right. \right. \right. \right. \\ & \left. \left. \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (5 + 2m + 2n) \right. \right. \\ & \left. \left. \operatorname{AppellF1} \left[\frac{3}{2} + n, -2m, 2(3 + m + n), \frac{5}{2} + n, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\ & \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) \bigg) \bigg) \bigg) \bigg) \end{aligned}$$

Problem 66: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[e + f x]^2 (a + a \sin[e + f x])^m (c - c \sin[e + f x])^3 dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$-\frac{1}{9f} 2^{\frac{3}{2}+m} a^4 c^3 \cos[e + f x]^9 \operatorname{Hypergeometric2F1} \left[\frac{9}{2}, -\frac{1}{2} - m, \frac{11}{2}, \frac{1}{2} (1 - \sin[e + f x]) \right] (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^{-4+m}$$

Result (type 6, 17864 leaves):

$$\begin{aligned} & - \left(\left(\cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{-2m} (a + a \sin[e + f x])^m \right. \right. \\ & \left. \left. (c - c \sin[e + f x])^3 \left(\cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^{10} - \right. \right. \right. \\ & \left. \left. 6 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^9 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] + \right. \right. \\ & \left. \left. 13 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^8 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^2 - \right. \right. \\ & \left. \left. 8 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^7 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^3 - \right. \right. \\ & \left. \left. 14 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^6 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^4 + \right. \right. \\ & \left. \left. 28 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^5 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^5 - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 14 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^4 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^6 - \\
 & 8 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^3 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^7 + \\
 & 13 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^2 \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^8 - \\
 & 6 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^9 + \\
 & \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^{10} \\
 & \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \\
 & \quad \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \\
 & \quad \left. \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{7+2m} \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), \right. \right. \right. \\
 & \quad \left. \left. \left. 7+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (7+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(18 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \\
 & \quad \left. \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{9+2m} \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), \right. \right. \right. \\
 & \quad \left. \left. \left. 9+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (9+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{11+2m} \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), \right.\right. \\
& \quad \left.11+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \\
& \quad 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
& \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \\
& \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
& \left(12 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
& \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m-2(4+m)} \Big/ \left(3 \operatorname{AppellF1}\left[\right.\right. \\
& \quad \left.\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \\
& \quad 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
& \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \\
& \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
& \left(12 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
& \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m-2(5+m)} \Big/ \left(3 \operatorname{AppellF1}\left[\right.\right. \\
& \quad \left.\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \\
& \quad 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
& \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right.
\end{aligned}$$

$$\begin{aligned}
 & \left(3 (1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2(1+m)} \left(\frac{1}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{7+2m}\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \right. \\
 & \left(3(7+2m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \left(\frac{1}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{8+2m}\right) / \\
 & \left(2 \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) + \\
 & \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{9+2m}\right) / \left(2 \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2] - \\
 & 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left(18 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\frac{1}{6}(9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 10+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \\
 & \left. \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{9+2m}\right) / \right. \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \\
 & 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(18(1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2(1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{9+2m}\right) / \right. \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (9+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left(9(9+2m) \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{10+2m} \right) / \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (9+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{11+2m} \right) / \\
 & \left(4 \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (11+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \left(3 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\frac{1}{6} (11+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 12+2m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \\
 & \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 11+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \\
 & \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2(1+m)} \left(\frac{1}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{11+2m} \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \left. 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 - \\
 & \left(3(1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left. \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-1+2(1+m)} \left(\frac{1}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{11+2m} \Big/ \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \left. 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 - \\
 & \left(3(11+2m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{12+2m} \Big/ \\
 & \left(2 \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \\
 & \quad \left. 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (11+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \left(12m \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-1+2m-2(4+m)} \right) \Big/ \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad \left. 4 \left((1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (4+m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \right. \\
 & \left(6(2m-2(4+m)) \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-1+2m-2(4+m)} \right) \Big/ \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2]- \\
 & 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 8+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 9+2 m, \frac{5}{2},\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(1+m)} \\
 & \quad \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m}\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2 m-2(4+m)}\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 8+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 9+2 m, \frac{5}{2},\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(12 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(-\frac{1}{3}(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 1+2(4+m),\right.\right.\right. \\
 & \quad \left.\left.\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(4+m), \frac{5}{2},\right.\right. \\
 & \quad \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(1+m)}\right. \\
 & \quad \left.\left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m}\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2 m-2(4+m)}\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-
 \end{aligned}$$

$$\begin{aligned}
 & 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
 & \left(12(1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2m-2(4+m)} \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
 & \left(12m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2m-2(5+m)} \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (5+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(6(2m - 2(5+m)) \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-1+2m-2(5+m)} \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m-2(5+m)} \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(12 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\frac{1}{3}(5+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(5+m), \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \frac{1}{3} (1+m) \text{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(5+m), \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \left(\frac{1}{1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \\
 & \left(1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m-2(5+m)} \Big/ \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5+m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(12(1+m) \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-1+2(1+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \left(1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m-2(5+m)} \right) \Big/ \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad 4 \left((1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5+m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) - \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2)^2 - \\
 & \left(18 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{9+2m} \right. \right. \\
 & \quad \left. \left(-2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right. \right. \right. \\
 & \quad \quad \left. \left. 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 3\left(-\frac{1}{6}(9+2m) \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, -2(1+m), 10+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1-2(1+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left(2(1+m) \left(-\frac{3}{10}(9+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, 10+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \right. \\
 & \quad \quad \left. \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 9+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \right. \\
 & \quad \left. (9+2m) \left(-\frac{3}{5}(5+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(5+m), \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \quad \quad \left. \left. 2(5+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) \Big/
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^2 - \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \\
 & \quad \left. \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2(1+m)} \left(\frac{1}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{11+2m} \right. \\
 & \quad \left. \left(- \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + 3 \left(-\frac{1}{6} (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 12+2m, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3} (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 11+2m, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) - 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(2(1+m) \right. \right. \\
 & \quad \quad \left. \left(-\frac{3}{10} (11+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, 12+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \quad \quad \left. \frac{3}{10} (-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 11+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \\
 & \quad \quad \left. (11+2m) \left(-\frac{3}{5} (6+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(6+m), \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \quad \left. \left. 2(6+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) \Bigg/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 11+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 11+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (11+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(6+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 + \\
 & \left(12 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{2(1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{2m-2(4+m)} \right. \\
 & \quad \left. \left(-2 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 3 \left(-\frac{1}{3}(4+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -2(1+m), 1+2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. 1-2(1+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left((1+m) \left(-\frac{3}{10}(8+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, 9+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] + \\
 & \frac{3}{10}(-1-2 m) \operatorname{AppellF1}\left[\frac{5}{2},-2 m, 8+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right], \\
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] + \\
 & (4+m)\left(-\frac{3}{10}(9+2 m) \operatorname{AppellF1}\left[\frac{5}{2},-2(1+m), 10+2 m, \frac{7}{2},\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m),\right.\right. \\
 & \left.\left.9+2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \\
 & \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 8+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 9+2 m, \frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2)^2 + \\
 & \left(12 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(5+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(1+m)}\left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m} \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2 m-2(5+m)} \\
 & \left(-2\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 2(5+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+(5+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m),\right.\right. \\
 & \left.\left.11+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \\
 & \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+3\left(-\frac{1}{3}(5+m) \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -2(1+m), 1+2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
 & \left. 1-2(1+m), 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \\
 & \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left((1+m) \left(-\frac{3}{5}(5+m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, 1+2(5+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \right. \\
 & \left. \left. \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 2(5+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \right. \\
 & (5+m) \left(-\frac{3}{10}(11+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 12+2m, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \left. \left. 11+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \left. \left. \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \right) \right) \Bigg/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(5+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 2(5+m), \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (5+m) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 11+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \right) \right) \Bigg)
 \end{aligned}$$

Problem 67: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[e+fx]^2 (a+a \sin[e+fx])^m (c-c \sin[e+fx])^2 dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$-\frac{1}{7f} 2^{\frac{3}{2}+m} a^3 c^2 \cos[e+fx]^7 \text{Hypergeometric2F1}\left[\frac{7}{2}, -\frac{1}{2}-m, \frac{9}{2}, \frac{1}{2}(1-\sin[e+fx])\right] \\ (1+\sin[e+fx])^{-\frac{1}{2}-m} (a+a\sin[e+fx])^{-3+m}$$

Result (type 6, 13077 leaves):

$$-\left(12288 c^2 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \right. \\ (a+a\sin[e+fx])^m \left(\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^8 - \right. \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^7 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] + \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^6 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 + \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^5 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^3 - \\ 10 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^4 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^4 + \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^3 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^5 + \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^6 - \\ 4 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^7 + \\ \left. \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^8 \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\ \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)^{2(1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{9+2m} \\ \left(\left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\ \left. \left(1 + \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right) / \left(-3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), \right. \right. \\ \left. \left. 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\ \left. 2\left(2(1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\ \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (7+2m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \\ \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \right. \\ \left. \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) / \\ \left. \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \right. \right. \right.$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^3 \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), \right. \right. \\
 & \quad \left. \left. 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 7+2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \\
 & \quad \left. \left. -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big/ \\
 & \left(f \left(3072 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{2(1+m)} \right. \right. \\
 & \quad \left. \left. \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{9+2m} \right. \right. \\
 & \quad \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) \Big/ \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \\
 & \quad \left. \left. (1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{9+2m} \\
 & \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 \right) / \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \right. \\
 & \quad \left. \left. \left. (1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) - \\
 & \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \quad \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] / \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+ \right. \right. \\
 & \quad \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^3 \right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \\
 & \quad \left. \left. (1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad \left. 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 7+2m, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) \right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \\
 & \quad \left. \left. (1+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 4 \left((1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (4+m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \Bigg) - \\
 6144 & (9+2m) \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \\
 & \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{10+2m} \\
 & \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \left(-3 \operatorname{AppellF1} \left[\frac{1}{2}, -2 \right. \right. \right. \\
 & \quad \left. \left. (1+m), 7+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (7+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \Bigg) - \\
 & \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \\
 & \quad \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 9+ \right. \right. \\
 & \quad \left. \left. 2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) - \\
 & \quad 2 \left(2(1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (9+2m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \Bigg) + \\
 & \left(\operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2 \right. \right. \right. \\
 & \quad \left. \left. (1+m), 2(3+m), \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) - \\
 & \quad 4 \left((1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 6+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(3+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 7+2 m, \frac{5}{2},\right. \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m,\right.\right.\right. \\
& \left.\left.\left.8+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right. \\
& \left.\left.(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 9+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
& 12288 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(1+m)} \\
& \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{9+2 m} \\
& \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 7+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right.\right. \\
& \left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \left(-3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 7+ \right.\right.\right. \\
& \left.\left.\left.2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right. \\
& \left.\left.2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 7+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
& \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(7+2 m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 2(4+m), \frac{5}{2},\right.\right.\right.\right. \\
& \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
& \left(3\left(-\frac{1}{6}(7+2 m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 8+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
& \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{3}\right.\right.\right. \\
& \left.\left.\left.(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 7+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
& \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)
\end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \Big/ \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7 + \right.\right. \\
 & \quad \left.2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & \left(-\frac{1}{6}(9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 10+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \quad \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \\
 & 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \Big/ \\
 & \left(2\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right.\right. \\
 & \quad \left.6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & \quad (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \\
 & \left(\left(-\frac{1}{3}(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3} \\
& (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(3+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right] \\
& \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3 \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2 \right. \right. \\
& \left. \left.(3+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& \left. 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 6+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 7+2m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) + \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right] \Big/ \right. \\
& \left. \left(2 \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
& \left. \left. 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
& \left. \left.(4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) \Big) + \\
& \left(3 \left(-\frac{1}{3} (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(4+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3} \right. \right. \\
& \left. \left.(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(4+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \right. \\
& \left. \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \right. \right. \\
& \left. \left.\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& \left. 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \left(\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -1-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 3 \right. \right. \\
 & \quad \left. \left. \left(-\frac{1}{6}(7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + 2 \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(2(1+m) \left(-\frac{3}{10}(7+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 7+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + \\
 & (7+2m) \left(-\frac{3}{5}(4+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(4+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \right. \\
 & \quad \left. \left. \left. 2(4+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) / \\
 & \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
& (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
& \quad \left. -\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right. \right. \\
& \quad \quad \left. \left. 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + 3\left(-\frac{1}{6}(9+2m) \right. \\
& \quad \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 10+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
& \quad \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) - 2 \\
& \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(2(1+m) \left(-\frac{3}{10}(9+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 10+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\right. \\
& \quad \quad \left. \frac{5}{2}, -2m, 9+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \\
& (9+2m) \left(-\frac{3}{5}(5+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(5+m), \frac{7}{2}, \tan\left[\frac{1}{4} \right. \right. \right. \\
& \quad \left. \left. \left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
& \quad \left. \left. 2(5+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2 - \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3 \right. \right. \\
 & \quad \left. \left. -2\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + 3 \right. \\
 & \quad \left. \left(-\frac{1}{3}(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) - 4 \\
 & \quad \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left((1+m) \left(-\frac{3}{10}(6+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. 7+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, -2m, 6+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + (3+m) \\
 & \quad \left(-\frac{3}{10}(7+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 8+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \quad \quad \left. \left. 7+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(3+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - 4 \left((1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 6+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
& \quad \left. (3+m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 7+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 - \\
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right. \\
& \quad \left. \left(-2 \left((1+m) \operatorname{AppellF1} \left[\frac{3}{2}, -1-2m, 8+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (4+m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), \right. \right. \right. \\
& \quad \left. \left. 9+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + 3 \right. \\
& \quad \left. \left(-\frac{1}{3} (4+m) \operatorname{AppellF1} \left[\frac{3}{2}, -2(1+m), 1+2(4+m), \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \\
& \quad \left. \frac{1}{3} (1+m) \operatorname{AppellF1} \left[\frac{3}{2}, 1-2(1+m), 2(4+m), \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) - 4 \\
& \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left((1+m) \left(-\frac{3}{10} (8+2m) \operatorname{AppellF1} \left[\frac{5}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 9+2m, \frac{7}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{3}{10} (-1-2m) \operatorname{AppellF1} \left[\right. \right. \\
& \quad \left. \left. \frac{5}{2}, -2m, 8+2m, \frac{7}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + (4+m) \\
& \left(-\frac{3}{10} (9+2m) \operatorname{AppellF1} \left[\frac{5}{2}, -2(1+m), 10+2m, \frac{7}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
& \quad \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{3}{5} (1+m) \operatorname{AppellF1} \left[\frac{5}{2}, 1-2(1+m), \right. \right.
\end{aligned}$$

$$\begin{aligned} & \left. \begin{aligned} & 9 + 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\ & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \Bigg/ \\ & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\ & \quad \left. \left. 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\ & \quad \left. \left. (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\ & \quad \left. \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)^2\right) \right) \right) \right) \Bigg/ \end{aligned} \right. \end{aligned}$$

Problem 68: Attempted integration timed out after 120 seconds.

$$\int \cos[e + fx]^2 (a + a \sin[e + fx])^m (c - c \sin[e + fx]) dx$$

Optimal (type 5, 84 leaves, 4 steps):

$$\begin{aligned} & -\frac{1}{5f} 2^{\frac{3}{2}+m} a^2 c \cos[e + fx]^5 \operatorname{Hypergeometric2F1}\left[\frac{5}{2}, -\frac{1}{2}-m, \frac{7}{2}, \frac{1}{2}(1 - \sin[e + fx])\right] \\ & (1 + \sin[e + fx])^{-\frac{1}{2}-m} (a + a \sin[e + fx])^{-2+m} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 69: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[e + fx]^2 (a + a \sin[e + fx])^m dx$$

Optimal (type 5, 81 leaves, 3 steps):

$$\begin{aligned} & -\frac{1}{3f} 2^{\frac{3}{2}+m} a \cos[e + fx]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, -\frac{1}{2}-m, \frac{5}{2}, \frac{1}{2}(1 - \sin[e + fx])\right] \\ & (1 + \sin[e + fx])^{-\frac{1}{2}-m} (a + a \sin[e + fx])^{-1+m} \end{aligned}$$

Result (type 6, 6167 leaves):

$$\begin{aligned} & -\left(\left(192 \left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{5+2m} \cos[e + fx]^2 \right. \right. \\ & \quad \left. \left. (a + a \sin[e + fx])^m \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2(1+m)} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(2+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 5+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right. \\
 & \left.\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)- \\
 96(5+2 m)\left(\operatorname{Cos}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{4+2 m} \operatorname{Sin}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right. \\
 & \left.\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(1+m)}\right. \\
 & \left.-\left(\operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 5+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \right. \\
 & \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 5+2 m, \frac{3}{2},\right.\right.\right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \\
 & \left. \left. -1-2 m, 5+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. (5+2 m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 2(3+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \right. \\
 & \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)+ \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 2(2+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2\right.\right. \\
 & \left. \left.(1+m), 2(2+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]- \right. \\
 & \left. 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2},-1-2 m, 4+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(2+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m), 5+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right. \\
 & \left.\left.\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)- \\
 192(1+m) \operatorname{Cos}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^6\left(\operatorname{Cos}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2 m} \\
 & \operatorname{Sin}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \\
 & \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1+2(1+m)} \\
 & \left(-\left(\operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 5+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right],\right. \right. \\
 & \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 5+2 m, \frac{3}{2},\right.\right.\right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \\
 & \left. \left. -1-2 m, 5+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.
 \end{aligned}$$

$$\begin{aligned}
& (5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Bigg) + \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Bigg) / \right. \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
& \quad \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) + \\
192 & \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{5+2m} \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\
& \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2(1+m)} \\
& \left(- \left(\left(-\frac{1}{6} (5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3} \right. \right. \right. \\
& \quad \left. \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Bigg) / \right. \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
& \quad \left. (5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) + \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Bigg) / \right. \\
& \left(2 \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2] - 4\left((1+m)\operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right.\right. \\
 & \quad \left.\left. 4+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left.(2+m)\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left(\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(-\frac{1}{3}(2+m)\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(2+m), \right.\right.\right. \\
 & \quad \left.\left.\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \quad \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{3}(1+m)\operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), \right. \\
 & \quad \left. 2(2+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) / \left(3\operatorname{AppellF1}\left[\frac{1}{2}, -2 \right.\right. \\
 & \quad \left.\left.(1+m), 2(2+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad \left. 4\left((1+m)\operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (2+m)\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)^2 \\
 & \quad \left(-\left(2(1+m)\operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 5+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (5+2m)\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right.\right. \\
 & \quad \left.\left. 2(3+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + 3\left(-\frac{1}{6}(5+2m) \right. \\
 & \quad \left.\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 6+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
 & \quad \frac{1}{3}(1+m)\operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 5+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) - 2 \\
 & \quad \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(2(1+m)\left(-\frac{3}{10}(5+2m)\operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
& 6 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] \\
& \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10}(-1 - 2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, 5 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \\
& (5 + 2m) \left(-\frac{3}{5}(3 + m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1 + m), 1 + 2(3 + m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{5}(1 + m) \operatorname{AppellF1}\left[\frac{5}{2}, 1 - 2(1 + m), 2(3 + m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1 + m), 5 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2 \left(2(1 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -1 - 2m, 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (5 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1 + m), 2(3 + m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \right. \\
& \left. \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1 + m), 2(2 + m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
& \left. \left(-2 \left((1 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -1 - 2m, 4 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (2 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1 + m), 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \right. \\
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 3 \left(-\frac{1}{3}(2 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1 + m), 1 + 2(2 + m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
& \left. \frac{1}{3}(1 + m) \operatorname{AppellF1}\left[\frac{3}{2}, 1 - 2(1 + m), 2(2 + m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left]\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)-4 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(\left(1+m\right)\left(-\frac{3}{10}\left(4+2m\right)\operatorname{AppellF1}\left[\frac{5}{2},-1-2m,\right.\right.\right. \\
 & \quad \left.\left.\left.5+2m,\frac{7}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+\frac{3}{10}\left(-1-2m\right)\operatorname{AppellF1}\left[\right.\right.\right. \\
 & \quad \left.\left.\left.\frac{5}{2},-2m,4+2m,\frac{7}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)+\left(2+m\right) \\
 & \quad \left(-\frac{3}{10}\left(5+2m\right)\operatorname{AppellF1}\left[\frac{5}{2},-2\left(1+m\right),6+2m,\frac{7}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]-\frac{3}{5}\left(1+m\right)\operatorname{AppellF1}\left[\frac{5}{2},1-2\left(1+m\right),\right.\right. \\
 & \quad \left.\left.5+2m,\frac{7}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)\right)\right)\right) / \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},-2\left(1+m\right),2\left(2+m\right),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-4\left(\left(1+m\right)\operatorname{AppellF1}\left[\frac{3}{2},-1-2m,\right.\right.\right. \\
 & \quad \left.\left.\left.4+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+\right. \\
 & \quad \left.\left(2+m\right)\operatorname{AppellF1}\left[\frac{3}{2},-2\left(1+m\right),5+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)\right)\right)
 \end{aligned}$$

Problem 70: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a+a \sin[e+fx])^m}{c-c \sin[e+fx]} dx$$

Optimal (type 5, 77 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{1}{c f} 2^{\frac{3}{2}+m} \cos[e+fx] \operatorname{Hypergeometric2F1}\left[\frac{1}{2},-\frac{1}{2}-m,\frac{3}{2},\frac{1}{2}\left(1-\sin[e+fx]\right)\right] \\
 & \left(1+\sin[e+fx]\right)^{-\frac{1}{2}-m}\left(a+a \sin[e+fx]\right)^m
 \end{aligned}$$

Result (type 6, 6494 leaves):

$$\begin{aligned}
 & \frac{1}{f(c - c \operatorname{Sin}[e + f x])} \\
 & \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m} \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]\right)^2 (a + a \operatorname{Sin}[e + f x])^m \\
 & \left(-\frac{1}{2} i \left(-\frac{1}{1+m} 4^{-m} e^{-i\left(-e + \frac{\pi}{2} - f x\right)} \left(1 + e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right)^{-2m} \left(e^{-\frac{1}{2} i\left(-e + \frac{\pi}{2} - f x\right)} \left(1 + e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right)\right)^{2m}\right. \\
 & \quad \operatorname{Hypergeometric2F1}\left[-1 - m, -2m, -m, -e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right] - \frac{1}{-1 + m} \\
 & \quad \left. 4^{-m} e^{i\left(-e + \frac{\pi}{2} - f x\right)} \left(1 + e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right)^{-2m} \left(e^{-\frac{1}{2} i\left(-e + \frac{\pi}{2} - f x\right)} \left(1 + e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right)\right)^{2m}\right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[1 - m, -2m, 2 - m, -e^{i\left(-e + \frac{\pi}{2} - f x\right)}\right]\right) - \\
 & \left(2 \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{3+2m} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(3 + 2m), \frac{1}{2}(5 + 2m),\right. \right. \\
 & \quad \left. \left. \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] / \left((3 + 2m) \sqrt{\operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right) + \right. \\
 & \left(8 \left(\operatorname{Cos}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{3+2m} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \operatorname{Sin}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \quad \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2m} \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2 + 2m, \frac{3}{2},\right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) / \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2 + 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad \left. 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}, 1 - 2m, 2 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (1 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 3 + 2m, \frac{5}{2},\right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 - \\
 & \quad \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 3 + 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] / \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2m, 3 + 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad \left. \frac{2}{3} \left(2m \operatorname{AppellF1}\left[\frac{3}{2}, 1 - 2m, 3 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 4 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) / \\
 & \left. \left(2 \operatorname{Cos}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2m} \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2m}\right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 4 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(m \left(-\frac{3}{10} (2+2m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, \right. \right. \right. \\
& \quad \left. \left. \left. 3+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{10} (1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 2-2m, 2+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) + (1+m) \\
& \quad \left(-\frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1-2m, 3+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
& \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{3}{10} (3+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, \right. \right. \\
& \quad \left. \left. 4+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2m, 2+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 2+2m, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
& \quad \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 3+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 + \right. \\
& \quad \left. \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2m, 3+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left(-\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 3+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \right. \\
& \quad \left. \frac{1}{6} (3+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, 4+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \\
& \quad \left. \frac{1}{3} \left(2m \operatorname{AppellF1}\left[\frac{3}{2}, 1-2m, 3+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2m, \right. \right. \right. \\
& \quad \left. \left. \left. 4+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left(\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{2}{3} \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left. \left(2 m \left(-\frac{3}{10} (3 + 2 m) \text{AppellF1}\left[\frac{5}{2}, 1 - 2 m, 4 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{10} (1 - 2 m) \text{AppellF1}\left[\frac{5}{2}, 2 - 2 m, \right. \right. \right. \\
 & \quad \left. \left. \left. 3 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + (3 + 2 m) \right. \right. \\
 & \quad \left. \left. \left(-\frac{3}{5} m \text{AppellF1}\left[\frac{5}{2}, 1 - 2 m, 4 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{3}{10} (4 + 2 m) \text{AppellF1}\left[\frac{5}{2}, -2 m, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 5 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \right. \right. \\
 & \quad \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right) \right) \right) / \\
 & \left(\text{AppellF1}\left[\frac{1}{2}, -2 m, 3 + 2 m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] - \right. \\
 & \quad \frac{2}{3} \left(2 m \text{AppellF1}\left[\frac{3}{2}, 1 - 2 m, 3 + 2 m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] + \right. \\
 & \quad \left. \left. (3 + 2 m) \text{AppellF1}\left[\frac{3}{2}, -2 m, 4 + 2 m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) \right)
 \end{aligned}$$

Problem 71: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos[e + f x]^2 (a + a \sin[e + f x])^m}{(c - c \sin[e + f x])^2} dx$$

Optimal (type 5, 81 leaves, 4 steps):

$$\frac{1}{a c^2 f} 2^{\frac{3}{2}+m} \text{Hypergeometric2F1}\left[-\frac{1}{2}, -\frac{1}{2} - m, \frac{1}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \\
 \text{Sec}[e + f x] (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^{1+m}$$

Result (type 6, 6360 leaves):

$$\begin{aligned}
& - \left(\left(\left(\cos \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2m} \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{-2m} \right. \right. \\
& \quad \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(\cos \left[\frac{1}{2} \left(e + f x \right) \right] - \sin \left[\frac{1}{2} \left(e + f x \right) \right] \right)^4 \\
& \quad \left. \left(a + a \sin \left[e + f x \right] \right)^m \left(\frac{\cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^2}{\left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^2} + \right. \\
& \quad \left. \left(2 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right) \right) / \\
& \quad \left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^2 + \\
& \quad \left. \frac{\cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right]^2}{\left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^2} \right) \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \\
& \quad \left(- \left(\text{AppellF1} \left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \right. \right. \\
& \quad \left(\text{AppellF1} \left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)^2 - \\
& \quad 4 \left((1+m) \text{AppellF1} \left[\frac{1}{2}, -1-2m, 2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + m \text{AppellF1} \left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \right. \right. \\
& \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
& \quad \left(3 \text{AppellF1} \left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
& \quad \left. \sin \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \left(-3 \text{AppellF1} \left[\frac{1}{2}, -2(1+m), 1+2m, \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
& \quad \left. 2 \left(2(1+m) \text{AppellF1} \left[\frac{3}{2}, -1-2m, 1+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1+2m) \text{AppellF1} \left[\frac{3}{2}, -2(1+m), 2(1+m), \frac{5}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
& \quad \left(f (c - c \sin [e + f x])^2 \left(-m \left(\cos \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2m} \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2(1+m)} \right. \right. \\
& \quad \left. \left(- \left(\text{AppellF1} \left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
& \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \left(\text{AppellF1} \left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - 4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2},\right.\right. \\
 & \quad \left.\left.-1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] +\right. \\
 & \quad \left.m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \\
 & \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m,\right.\right. \\
 & \quad \left.\left.1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] +\right. \\
 & \quad \left.(1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(1+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & \frac{1}{4} \left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^{2m} \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^{2(1+m)} \\
 & \left(-\left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2},\right.\right. \\
 & \quad \left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2},\right.\right.\right. \\
 & \quad \left.\left.-1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] +\right. \\
 & \quad \left.\left.m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \\
 & \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m,\right.\right. \\
 & \quad \left.\left.1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] +\right.
 \end{aligned}$$

$$\begin{aligned}
& (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(1+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) - \\
(1+m) & \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2m} \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2(1+m)} \\
& \left(-\left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. -1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) + \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sin\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) / \\
& \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(1+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) + \\
& \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \\
& \left(-\left(m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \right. \\
& \quad \left. \left. (1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 1-2(1+m), 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) / \\
& \left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -1-2m, 2m, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2]+m \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m),1+2m,\frac{3}{2},\right. \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+(1+m) \operatorname{AppellF1}\left[\frac{1}{2},1-2(1+m),2m,\frac{3}{2},\right. \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]-4 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left((1+m)\left(-\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \\
& \left.\left.\left.-1-2m,1+2m,\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+\frac{1}{6}(-1-2m) \operatorname{AppellF1}\left[\right.\right. \\
& \left.\left.\frac{3}{2},-2m,2m,\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)+ \\
& m\left(-\frac{1}{6}(1+2m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m),2+2m,\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right. \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]-\frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2},1-2(1+m),\right.\right. \\
& \left.\left.1+2m,\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)\right) / \\
& \left(\operatorname{AppellF1}\left[-\frac{1}{2},-2(1+m),2m,\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2},-1-2m,2m,\right.\right.\right. \\
& \left.\left.\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+ \right. \\
& \left. m \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m),1+2m,\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)- \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m),1+2m,\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sin}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \right. \\
& \left.\left.\left.-1-2m,1+2m,\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)+ \right. \\
& \left.\left.(1+2m) \operatorname{AppellF1}\left[\frac{3}{2},-2(1+m),2(1+m),\frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 3 \right. \\
 & \left. \left(-\frac{1}{6}(1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + 2 \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(2(1+m) \left(-\frac{3}{10}(1+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 2+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{5}{2}, -2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \\
 & (1+2m) \left(-\frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(1+m), \frac{7}{2}, \tan\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left. \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \quad \left. \left. 2(1+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \left. \right) / \\
 & \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(1+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right) \right)
 \end{aligned}$$

Problem 72: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a+a\sin[e+fx])^m}{(c-c\sin[e+fx])^3} dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$\frac{1}{3a^2c^3f} 2^{\frac{3}{2}+m} \text{Hypergeometric2F1}\left[-\frac{3}{2}, -\frac{1}{2}-m, -\frac{1}{2}, \frac{1}{2}(1-\sin[e+fx])\right] \\ \text{Sec}[e+fx]^3 (1+\sin[e+fx])^{-\frac{1}{2}-m} (a+a\sin[e+fx])^{2+m}$$

Result (type 6, 6298 leaves):

$$-\left(\left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)^{2m} \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^3 \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right]\right)^6 \right. \\ \left. (a+a\sin[e+fx])^m \left(\frac{\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2}{\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)^4} + \right. \\ \left. \left(2\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right) / \right. \\ \left. \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)^4 + \right. \\ \left. \frac{\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2}{\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)^4} \right) \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)^{2(1+m)} \\ \left(-\left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] / \right. \right. \\ \left. \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left((1+m)\text{AppellF1}\left[-\frac{1}{2}, -1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\ \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + m\text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\ \left. \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\ \left. \left(3\text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\ \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) / \right. \\ \left. \left(\text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\ \left. 4\left((1+m)\text{AppellF1}\left[\frac{1}{2}, -1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\ \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + m\text{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \right. \right. \right. \right. \\ \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \right)$$

$$\begin{aligned}
 & \left(\left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big/ \\
 & \left(24 f (c - c \sin[e + fx])^3 \left(-\frac{1}{24} m \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2(1+m)} \right. \right. \\
 & \quad \left. \left(- \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \Big/ \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + 4 \left((1+m) \text{AppellF1}\left[-\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \right. \right. \\
 & \quad \quad \left. \left. m \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \right. \\
 & \quad \left. \left(3 \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big/ \left(\text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \right. \\
 & \quad \left. 4 \left((1+m) \text{AppellF1}\left[\frac{1}{2}, -1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + m \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big/ \right. \\
 & \left. \frac{1}{32} \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2(1+m)} \right. \\
 & \quad \left. \left(- \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \Big/ \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + 4 \left((1+m) \text{AppellF1}\left[-\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \right. \right. \\
 & \quad \quad \left. \left. m \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-3 \\
 & (1+m) \operatorname{AppellF1}\left[-\frac{1}{2}, 1-2(1+m), 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \\
 & \left(\operatorname{AppellF1}\left[-\frac{3}{2},-2(1+m), 2 m,-\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left((1+m) \operatorname{AppellF1}\left[-\frac{1}{2},-1-2 m,\right.\right. \\
 & \left.2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left.m \operatorname{AppellF1}\left[-\frac{1}{2},-2(1+m), 1+2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(3 \operatorname{AppellF1}\left[-\frac{1}{2},-2(1+m), 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \\
 & \left(2\left(\operatorname{AppellF1}\left[-\frac{1}{2},-2(1+m), 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2},-1-2 m, 2 m,\right.\right. \\
 & \left.\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left.m \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(3 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(m \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 1+2 m, \frac{3}{2},\right.\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+(1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 1-2(1+m), 2 m,\right.\right.\right. \\
 & \left.\left.\frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \\
 & \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2},\right.\right. \\
 & \left.-2(1+m), 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & 4\left((1+m) \operatorname{AppellF1}\left[\frac{1}{2},-1-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+m \operatorname{AppellF1}\left[\frac{1}{2},-2(1+m), 1+2 m, \frac{3}{2},\right.\right.
 \end{aligned}$$

$$\begin{aligned}
& \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
& \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \left(-3m \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 2 \right. \right. \\
& \left. \left. \left((1+m) \text{AppellF1}\left[-\frac{1}{2}, -1-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 3(1+m) \text{AppellF1}\left[-\frac{1}{2}, 1-2(1+m), 2m, \frac{1}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left((1+m) \left(m \text{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. -1-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \right. \\
& \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2}(-1-2m) \text{AppellF1}\left[\right. \right. \right. \\
& \left. \left. \left. \frac{1}{2}, -2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \right. \\
& \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + \\
& m \left(\frac{1}{2}(1+2m) \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (1+m) \text{AppellF1}\left[\frac{1}{2}, 1-2(1+m), \right. \right. \\
& \left. \left. 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right. \\
& \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \Big/ \\
& \left(\text{AppellF1}\left[-\frac{3}{2}, -2(1+m), 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left((1+m) \text{AppellF1}\left[-\frac{1}{2}, -1-2m, \right. \right. \right. \\
& \left. \left. 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \right. \\
& \left. m \text{AppellF1}\left[-\frac{1}{2}, -2(1+m), 1+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & \left(3 \operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left(m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2 \right. \right. \\
 & \quad \left. \left. \left((1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -1-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 1-2(1+m), 2m, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left((1+m) \left(-\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -1-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{6} (-1-2m) \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2}, -2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + m \right. \\
 & \quad \left. \left(-\frac{1}{6} (1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3} (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), \right. \right. \right. \\
 & \quad \left. \left. \left. 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right)\right)\right)\right)\bigg/ \\
 & \left(\operatorname{AppellF1}\left[-\frac{1}{2}, -2(1+m), 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{1}{2}, -1-2m, 2m, \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) +
 \end{aligned}$$

$$m \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 1+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\ \left. - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)$$

Problem 73: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[e + fx]^2 (a + a \sin[e + fx])^m (c - c \sin[e + fx])^{5/2} dx$$

Optimal (type 3, 244 leaves, 5 steps):

$$\frac{768 c^3 \cos[e + fx] (a + a \sin[e + fx])^{1+m}}{a f (7 + 2m) (9 + 2m) (15 + 16m + 4m^2) \sqrt{c - c \sin[e + fx]}} + \\ \frac{192 c^2 \cos[e + fx] (a + a \sin[e + fx])^{1+m} \sqrt{c - c \sin[e + fx]}}{a f (9 + 2m) (35 + 24m + 4m^2)} + \\ \frac{24 c \cos[e + fx] (a + a \sin[e + fx])^{1+m} (c - c \sin[e + fx])^{3/2}}{a f (63 + 32m + 4m^2)} + \\ \frac{2 \cos[e + fx] (a + a \sin[e + fx])^{1+m} (c - c \sin[e + fx])^{5/2}}{a f (9 + 2m)}$$

Result (type 3, 695 leaves):

$$\frac{1}{f \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^5} \left(a (1 + \sin [e + f x]) \right)^m (c - c \sin [e + f x])^{5/2}$$

$$\left(\left((2205 + 590 m + 108 m^2 + 8 m^3) \left(\left(\frac{3}{8} + \frac{3 i}{8} \right) \cos \left[\frac{1}{2} (e + f x) \right] + \left(\frac{3}{8} - \frac{3 i}{8} \right) \sin \left[\frac{1}{2} (e + f x) \right] \right) \right) / \right.$$

$$\left((3 + 2 m) (5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((2205 + 590 m + 108 m^2 + 8 m^3) \left(\left(\frac{3}{8} - \frac{3 i}{8} \right) \cos \left[\frac{1}{2} (e + f x) \right] + \left(\frac{3}{8} + \frac{3 i}{8} \right) \sin \left[\frac{1}{2} (e + f x) \right] \right) \right) /$$

$$\left((3 + 2 m) (5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((191 m + 48 m^2 + 4 m^3) \left((1 - i) \cos \left[\frac{3}{2} (e + f x) \right] - (1 + i) \sin \left[\frac{3}{2} (e + f x) \right] \right) \right) /$$

$$\left((3 + 2 m) (5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((191 m + 48 m^2 + 4 m^3) \left((1 + i) \cos \left[\frac{3}{2} (e + f x) \right] - (1 - i) \sin \left[\frac{3}{2} (e + f x) \right] \right) \right) /$$

$$\left((3 + 2 m) (5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((21 + 2 m) \left(\left(\frac{3}{2} + \frac{3 i}{2} \right) \cos \left[\frac{5}{2} (e + f x) \right] + \left(\frac{3}{2} - \frac{3 i}{2} \right) \sin \left[\frac{5}{2} (e + f x) \right] \right) \right) /$$

$$\left((5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((21 + 2 m) \left(\left(\frac{3}{2} - \frac{3 i}{2} \right) \cos \left[\frac{5}{2} (e + f x) \right] + \left(\frac{3}{2} + \frac{3 i}{2} \right) \sin \left[\frac{5}{2} (e + f x) \right] \right) \right) /$$

$$\left((5 + 2 m) (7 + 2 m) (9 + 2 m) \right) +$$

$$\left((15 + 2 m) \left(\left(\frac{3}{16} - \frac{3 i}{16} \right) \cos \left[\frac{7}{2} (e + f x) \right] - \left(\frac{3}{16} + \frac{3 i}{16} \right) \sin \left[\frac{7}{2} (e + f x) \right] \right) \right) /$$

$$\left((7 + 2 m) (9 + 2 m) \right) +$$

$$\left((15 + 2 m) \left(\left(\frac{3}{16} + \frac{3 i}{16} \right) \cos \left[\frac{7}{2} (e + f x) \right] - \left(\frac{3}{16} - \frac{3 i}{16} \right) \sin \left[\frac{7}{2} (e + f x) \right] \right) \right) /$$

$$\left((7 + 2 m) (9 + 2 m) \right) + \frac{\left(-\frac{1}{16} + \frac{i}{16} \right) \cos \left[\frac{9}{2} (e + f x) \right] - \left(\frac{1}{16} + \frac{i}{16} \right) \sin \left[\frac{9}{2} (e + f x) \right]}{9 + 2 m} +$$

$$\left. \frac{\left(-\frac{1}{16} - \frac{i}{16} \right) \cos \left[\frac{9}{2} (e + f x) \right] - \left(\frac{1}{16} - \frac{i}{16} \right) \sin \left[\frac{9}{2} (e + f x) \right]}{9 + 2 m} \right)$$

Problem 77: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos [e + f x]^2 (a + a \sin [e + f x])^m}{(c - c \sin [e + f x])^{3/2}} dx$$

Optimal (type 5, 76 leaves, 4 steps):

$$\left(\cos [e + f x] \operatorname{Hypergeometric2F1} \left[1, \frac{3}{2} + m, \frac{5}{2} + m, \frac{1}{2} (1 + \sin [e + f x]) \right] (a + a \sin [e + f x])^{1+m} \right) /$$

$$\left(a c f (3 + 2 m) \sqrt{c - c \sin [e + f x]} \right)$$

Result (type 6, 3587 leaves):

$$\begin{aligned}
& \left(2\sqrt{2} (2+m) \right. \\
& \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^3 \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(\cos\left[\frac{1}{2} (e + fx)\right] - \sin\left[\frac{1}{2} (e + fx)\right]\right)^3 \\
& (a + a \sin[e + fx])^m \left(\frac{\cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]^2}{\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]} + \right. \\
& \left. \left(2 \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] \right) / \right. \\
& \left. \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] \right) + \right. \\
& \left. \frac{\cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]^2}{\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + fx\right)\right]} \right) \Bigg) / \\
& \left(f (3+2m) \left(2 (2+m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \\
& \quad \left. \left. 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \right. \\
& \quad \left. \left. \left(\text{AppellF1}\left[4+2m, 2+2m, 2, 5+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+m) \text{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \right. \right. \\
& \quad \quad \left. \left. \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right] \right) \\
& (c - c \sin[e + fx])^{3/2} \left(\left(\sqrt{2} (2+m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \right. \right. \\
& \quad \left. \left. \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^{3+2m} \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] \csc\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) / \right. \\
& \quad \left((3+2m) \left(2 (2+m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \\
& \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \left(\text{AppellF1}\left[4+2m, 2+2m, \right. \right. \right. \\
& \quad \quad \left. \left. 2, 5+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
& \quad \quad \left. \left. (1+m) \text{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \\
& \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \\
& \quad \left. \left(\sqrt{2} (2+m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2} \left(1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \right. \\
& \quad \quad \left. \left. 1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2+2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big/ \left(2(2+m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \\
 & \quad \left. \left(\operatorname{AppellF1}\left[4+2m, 2+2m, 2, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + (1+m) \operatorname{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) - \\
 & \left(2\sqrt{2}(2+m) \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{3+2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2(4+2m)} \right. \right. \\
 & \quad \left. \left. (3+2m) \operatorname{AppellF1}\left[4+2m, 2+2m, 2, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], 1 - \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(4+2m)} \right. \right. \\
 & \quad \left. \left. (2+2m)(3+2m) \operatorname{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
 & \left((3+2m) \left(2(2+m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \left(\operatorname{AppellF1}\left[4+2m, 2+2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 2, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. (1+m) \operatorname{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big) + \\
 & \left(2\sqrt{2}(2+m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{3+2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left(- (2+m) \operatorname{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\left(\operatorname{AppellF1}\left[4+2m, 2+2m, 2, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right], \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + (1+m) \operatorname{AppellF1}\left[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] + \\
 & 2(2+m) \cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2(4+2m)} (3+2m) \operatorname{AppellF1}[4+2m, \right. \\
 & \quad \left. 2+2m, 2, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(4+2m)} (2+2m)(3+2m) \right. \\
 & \quad \left. \operatorname{AppellF1}[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\frac{1}{5+2m} (4+2m) \operatorname{AppellF1}[5+2m, 2+2m, 3, 6+2m, \right. \\
 & \quad \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(5+2m)} (2+2m)(4+2m) \right. \\
 & \quad \left. \operatorname{AppellF1}[5+2m, 3+2m, 2, 6+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & (1+m) \left(-\frac{1}{2(5+2m)} (4+2m) \operatorname{AppellF1}[5+2m, 3+2m, 2, 6+2m, \right. \\
 & \quad \left. \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(5+2m)} (3+2m)(4+2m) \right. \\
 & \quad \left. \operatorname{AppellF1}[5+2m, 4+2m, 1, 6+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \right) \Big/ \\
 & \left((3+2m) \left(2(2+m) \operatorname{AppellF1}[3+2m, 2+2m, 1, 4+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \left(\operatorname{AppellF1}[4+2m, 2+2m, 2, \right. \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}[4+2m, 3+2m, 1, 5+2m, \frac{1}{2}\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right), \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \right) \Big)
 \end{aligned}$$

Problem 78: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx]^2 (a+a \sin[e+fx])^m}{(c-c \sin[e+fx])^{5/2}} dx$$

Optimal (type 5, 79 leaves, 4 steps):

$$\frac{\left(\cos[e+fx] \operatorname{Hypergeometric2F1}\left[2, \frac{3}{2}+m, \frac{5}{2}+m, \frac{1}{2}(1+\sin[e+fx])\right] (a+a \sin[e+fx])^{1+m} \right)}{\left(2ac^2f(3+2m)\sqrt{c-c \sin[e+fx]} \right)}$$

Result (type 6, 7834 leaves):

$$\begin{aligned} & - \left(\left(\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \right)^{-2m} \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^5 \right. \\ & \quad \left(a+a \sin[e+fx] \right)^m \left(\frac{\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2}{\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^3} + \right. \\ & \quad \left. \left(2 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \right)^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right) \Big/ \\ & \quad \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^3 + \\ & \quad \frac{\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2}{\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^3} \left(\frac{1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2m} \\ & \quad \left(- \left(\operatorname{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \Big/ \right. \right. \\ & \quad \left. \left(-m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\ & \quad \left. \left. \left. -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] + \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \right. \right. \right. \\ & \quad \left. \left. \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right) + \operatorname{AppellF1}\left[1, -2m, 2m, 2, \right. \right. \\ & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big/ \right. \\ & \quad \left(\operatorname{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] \right. \\ & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Big/ \\ & \quad \left(\operatorname{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] - \right. \\ & \quad \left. m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right] + \right. \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & \left(4(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) / \\
 & \left(\left(1+2m\right) \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right)\right)\right) / \\
 & \left(4\sqrt{2} f (c - c \sin[e + fx])^{5/2} \left(\frac{1}{2\sqrt{2}} m \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{-1+2m} \right. \right. \\
 & \quad \left. \left. - \left(\left(\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right)\right) / \\
 & \left(2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \\
 & \left(-\left(\text{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \right. \\
 & \quad \left(-m \left(\text{AppellF1}\left[2, 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[2, -2m, 1+2m, \right. \right. \right. \\
 & \quad \quad \left. \left. 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) + \right. \\
 & \quad \left. \text{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) + \left(\text{AppellF1}\left[1, -2m, 2m, 2, \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \\
 & \left(\text{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & m \left(\text{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \text{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
 & \left(4(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \\
 & \left((1+2m) \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) \right) + \\
 & \frac{1}{4\sqrt{2}} \left(\frac{1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2m} \left(- \left(\left(\frac{1}{2} m \text{AppellF1}\left[2, 1-2m, 2m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \frac{1}{2} m \text{AppellF1}\left[2, -2m, 1+2m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) / \left(-m \left(\text{AppellF1}\left[2, 1-2m, 2m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \right) + \\
 & \quad \text{AppellF1}\left[1, -2m, 2m, 2, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
 & \left(\text{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) / \\
 & \left(2 \left(\text{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& m \left(\text{AppellF1} \left[2, 1 - 2m, 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \text{AppellF1} \left[2, -2m, 1 + 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. fx \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
& \left(\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \left(-\frac{1}{2} m \text{AppellF1} \left[2, 1 - 2m, 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] - \right. \right. \\
& \quad \left. \frac{1}{2} m \text{AppellF1} \left[2, -2m, 1 + 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right) \right) / \\
& \left(\text{AppellF1} \left[1, -2m, 2m, 2, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] - \right. \\
& \quad m \left(\text{AppellF1} \left[2, 1 - 2m, 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \right. \\
& \quad \left. \text{AppellF1} \left[2, -2m, 1 + 2m, 3, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
& \left(\text{AppellF1} \left[1, -2m, 2m, 2, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \\
& \left(-m \left(\frac{4}{3} m \text{AppellF1} \left[3, 1 - 2m, 1 + 2m, 4, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 - \right. \right. \\
& \quad \frac{1}{3} (1 - 2m) \text{AppellF1} \left[3, 2 - 2m, 2m, 4, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \\
& \quad \left. \left. - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 + \right. \\
& \quad \frac{1}{3} (1 + 2m) \text{AppellF1} \left[3, -2m, 2 + 2m, 4, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \\
& \quad \left. \left. - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
& \frac{1}{2} \text{AppellF1} \left[1, -2m, 2m, 2, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \\
& \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] + \left(\frac{1}{2} m \text{AppellF1} \left[2, \right. \right. \\
& \quad \left. \left. 1 - 2m, 2m, 3, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \\
& \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 + \frac{1}{2} m \text{AppellF1} \left[2, \right. \\
& \quad \left. -2m, 1 + 2m, 3, \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, - \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right]
\end{aligned}$$

$$\begin{aligned}
 & \left(\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) / \\
 & \left(-m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[1, -2m, 2m, 2, \right. \right. \\
 & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 - \\
 & \left(\operatorname{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2} m \operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2} m \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2} m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[2, -2m, 1+2m, \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - m \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \\
 & \left(-\frac{4}{3} m \operatorname{AppellF1}\left[3, 1-2m, 1+2m, 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left. \frac{1}{3} (1-2m) \operatorname{AppellF1}\left[3, 2-2m, 2m, 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{3} (1+2m) \operatorname{AppellF1}\left[3, -2m, 2+2m, 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left. \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) / \\
 & \left(\operatorname{AppellF1}\left[1, -2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad m \left(\operatorname{AppellF1}\left[2, 1-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[2, -2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\pi}{2} - f x \right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 + \\
 & \left(2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right], \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) - \\
 & \left(2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right. \\
 & \quad \left. \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) + \\
 & \left(4(1+m) \operatorname{Cot}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(-\frac{1}{2(2+2m)}(1+2m) \operatorname{AppellF1}\left[2+2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2(2+2m)} \right. \\
 & \quad \left. m(1+2m) \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \\
 & \quad \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right.\right. \\
 & \quad \left.\left.\frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) - \\
 & \left(4(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \\
 & \left.\left(\frac{1}{2}\left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \right. \\
 & \quad \left.\frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2(1+m) \\
 & \left(-\frac{1}{2(2+2m)}(1+2m) \text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right.\right. \\
 & \quad \left.\frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)}m(1+2m) \\
 & \quad \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \\
 & \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-\frac{1}{3+2m}(2+2m) \text{AppellF1}\left[3+2m, \right.\right. \\
 & \quad \left. 2m, 3, 4+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left.\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(3+2m)} \right. \\
 & \quad \left. m(2+2m) \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left. m\left(-\frac{1}{2(3+2m)}(2+2m) \text{AppellF1}\left[3+2m, 1+2m, 2, 4+2m, \right.\right.\right. \\
 & \quad \left.\left.\frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{4(3+2m)} \right. \\
 & (1+2m)(2+2m) \text{AppellF1}\left[3+2m, 2+2m, 1, 4+2m, \right. \\
 & \left. \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \left. \left. \left. \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]\right]\right)\right) / \\
 & \left((1+2m) \left(-2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \right. \\
 & \left. \left. \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left. \left. 1 - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right)\right]\right)\right)\right)\right)\right)
 \end{aligned}$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int \text{Cos}[e + f x]^2 (a + a \text{Sin}[e + f x])^m (c - c \text{Sin}[e + f x])^{-3-m} dx$$

Optimal (type 3, 54 leaves, 2 steps):

$$\frac{\text{Cos}[e + f x] (a + a \text{Sin}[e + f x])^{1+m} (c - c \text{Sin}[e + f x])^{-2-m}}{a c f (3 + 2m)}$$

Result (type 3, 109 leaves):

$$\begin{aligned}
 & \frac{1}{c^3 f (3 + 2m)} 2^{-m} \text{Cos}\left[\frac{1}{4}(2e + \pi + 2fx)\right]^{-3-2m} \left(\text{Cos}\left[\frac{1}{2}(e + fx)\right] - \text{Sin}\left[\frac{1}{2}(e + fx)\right]\right)^{2m} \\
 & (a(1 + \text{Sin}[e + fx]))^m (c - c \text{Sin}[e + fx])^{-m} \text{Sin}\left[\frac{1}{4}(2e + \pi + 2fx)\right]^3
 \end{aligned}$$

Problem 84: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Cos}[e + f x]^2 (a + a \text{Sin}[e + f x])^m (c - c \text{Sin}[e + f x])^{-2-m} dx$$

Optimal (type 5, 113 leaves, 5 steps):

$$\frac{1}{f(3+2m)} 2^{-\frac{1}{2}-m} \text{Cos}[e+fx]^3 \text{Hypergeometric2F1}\left[\frac{1}{2}(3+2m), \frac{1}{2}(3+2m), \frac{1}{2}(5+2m), \frac{1}{2}(1+\text{Sin}[e+fx])\right] \\ (1-\text{Sin}[e+fx])^{\frac{1}{2}+m} (a+a\text{Sin}[e+fx])^m (c-c\text{Sin}[e+fx])^{-2-m}$$

Result (type 6, 5056 leaves):

$$-\left(\left(2^{-m} \left(\text{Cos}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)^{2m} \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \\ \left. \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right] - \text{Sin}\left[\frac{1}{2}(e+fx)\right] \right)^{-2(-2m)} (a+a\text{Sin}[e+fx])^m \right. \\ \left. (c-c\text{Sin}[e+fx])^{-2m} \left(\text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 \right. \right. \\ \left. \left(\text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2-2m} + 2 \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \right. \\ \left. \text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \left(\text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2-2m} \right. \\ \left. \text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] + \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \right. \\ \left. \left(\text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2-2m} \text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 \right) \\ \left(-\frac{1}{1+2m} \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2(1+m), \frac{1}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\ \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sin}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \right) \right) / \\ \left((-1+2m) \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \right. \right. \right. \\ \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\ \left. 2 \left(2(1+m) \text{AppellF1}\left[\frac{3}{2}-m, -1-2m, 1, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\ \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\ \left. \left. \left. \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \right) / \\ \left(f \left(-2^{-m} m \left(\text{Cos}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)^{2m} \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \\ \left. \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-1-2m} \right. \\ \left. \left(-\frac{1}{1+2m} \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2(1+m), \frac{1}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right.$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Bigg) + \\
 & 2^{-m} \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{2m} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \sin\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \\
 & \left(\left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \right) \right) / \\
 & \left(2(-1+2m) \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \left(2(1+m) \text{AppellF1}\left[\frac{3}{2}-m, -1-2m, 1, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) + \left((-3+2m) \sin\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \left(-\frac{1}{2\left(\frac{3}{2}-m\right)} \left(\frac{1}{2}-m\right) \text{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{\frac{3}{2}-m} \left(\frac{1}{2}-m\right) (1+m) \text{AppellF1}\left[\frac{3}{2}-m, 1-2(1+m), 1, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \right) \Bigg) / \\
 & \left((-1+2m) \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \left(2(1+m) \text{AppellF1}\left[\frac{3}{2}-m, -1-2m, 1, \frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) - \left((1+m) (-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^3 \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2(1+m)} \Big/ \\
 & \left((-1+2m) \left((-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}-m, -1-2m, \right. \right. \right. \\
 & \quad \left. \left. 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \frac{1}{2(1+2m)} \left(-\frac{1}{2}-m\right) \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\
 & \left(-\operatorname{Hypergeometric2F1}\left[-\frac{1}{2}-m, -2(1+m), \frac{1}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)}\right) - \\
 & \left((-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \operatorname{Sin}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(1+m)} \left(\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}-m, -1-2m, 1, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + (-3+2m) \\
 & \left(-\frac{1}{2\left(\frac{3}{2}-m\right)} \left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{\frac{3}{2}-m} \left(\frac{1}{2}-m\right) (1+m) \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. 1-2(1+m), 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned} & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\ & \left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, -2(1+m), 3, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\ & \quad \left. \frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right)(1+m) \text{AppellF1}\left[\frac{5}{2}-m, 1-2(1+m), 2, \frac{7}{2}-m, \right. \right. \\ & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\ & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 2(1+m) \left(-\frac{1}{2\left(\frac{5}{2}-m\right)}\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, \right. \right. \right. \\ & \quad \quad \left. \left. \left. -1-2m, 2, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\ & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\ & \quad \left. \frac{1}{2\left(\frac{5}{2}-m\right)}(-1-2m)\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, -2m, 1, \frac{7}{2}-m, \right. \right. \\ & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\ & \quad \left. \left. \left. \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) \right) \right) \right) / \\ & \left((-1+2m) \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2(1+m), 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\ & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(2(1+m) \text{AppellF1}\left[\frac{3}{2}-m, -1-2m, \right. \right. \right. \right. \\ & \quad \quad \left. \left. \left. 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\ & \quad \quad \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}-m, -2(1+m), 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right) \right) \right) \end{aligned}$$

Problem 85: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[ex + f] (a + a \sin[ex + f])^m (c - c \sin[ex + f])^{-1-m} dx$$

Optimal (type 5, 114 leaves, 5 steps):

$$\frac{1}{f(3+2m)} 2^{\frac{1}{2}-m} c \cos[e+fx]^3 \text{Hypergeometric2F1}\left[\frac{1}{2}(1+2m), \frac{1}{2}(3+2m), \frac{1}{2}(5+2m), \frac{1}{2}(1+\sin[e+fx])\right] (1-\sin[e+fx])^{\frac{1}{2}+m} (a+a\sin[e+fx])^m (c-c\sin[e+fx])^{-2-m}$$

Result (type 6, 11925 leaves):

$$\begin{aligned} & - \left(8^{1-m} (-3+2m) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \right. \\ & \quad \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^{-2(-1-m)} (a+a\sin[e+fx])^m \\ & \quad (c-c\sin[e+fx])^{-1-m} \left(\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 \right. \\ & \quad \left. \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2m} + 2 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \right. \\ & \quad \left. \cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2m} \right. \\ & \quad \left. \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] + \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \right. \\ & \quad \left. \left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] - \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right] \right)^{-2m} \sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]^2 \right) \\ & \quad \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(\frac{\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{-2m} \left(\frac{1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{2m} \\ & \quad \left(- \left(\text{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\ & \quad \left. \left. \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^2 \right) / \left((-3+2m) \right. \right. \\ & \quad \left. \left. \text{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) + \right. \\ & \quad \left. 2 \left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 1, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \right. \right. \\ & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\ & \quad \left(4 \text{AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\ & \quad \left. \left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) / \left((-3+2m) \right. \\ & \quad \left. \text{AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) + \\ & \quad \left. 4 \left(m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 2, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] + \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2) - \\
 & \left(4 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) / \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Bigg) / \\
 & \left(f (-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^3 \left(-\frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^4} \right. \right. \\
 & \left. \left. 3 \times 2^{2-3m} (-3 + 2m) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \left. \left. \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \right. \right. \\
 & \left. \left. \left(- \left(\left(\text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right)^2 \right. \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) \right) / \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \right. \\
 & \left. \left. \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(4 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) / \left((-3 + 2m) \text{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + 4 \right. \\
 & \left. \left. \left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \\
 & \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \left(\left(-3+2m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \right. \\
 & \left. \left. \left. 1-2m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. 3 \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) + \\
 & \frac{1}{(-1+2m)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^3} 2^{1-3m}(-3+2m) \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{-2m} \left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right)\right) / \left(\left(-3+2m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 1, \frac{3}{2}-m, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \right. \right. \\
 & \left. \left. \left. 1-2m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) + \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \left. \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \left(\left(-3+2m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, \right. \right. \right. \\
 & \left. \left. \left. 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 3, \frac{5}{2}-m, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(4 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. 3 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \frac{1}{(-1 + 2m) \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3} 2^{4-3m} m (-3 + 2m) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \\
 & \left(\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-1-2m} \\
 & \left(\frac{1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \\
 & \left(-\frac{\operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{2 \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2} + \frac{\operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{4 \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)} \right) \\
 & - \left(\left(\operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 1, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(4 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 2, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m,\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m,\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m,\right.\right.\right. \\
 & \left.\left.\left.1-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+3 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m,\right.\right.\right. \\
 & \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \frac{1}{(-1+2 m)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^3} 2^{4-3 m} m\left(-3+2 m\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-2 m} \\
 & \left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-1+2 m} \\
 & \left(-\left(\left(\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \right. \\
 & \left.\left(2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right)\right)-\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)} \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 1, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right.\right.\right. \\
 & \left.\left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 1, \frac{3}{2}-m,\right.\right.\right.\right. \\
 & \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m,\right.\right.\right.\right. \\
 & \left.\left.\left.\left.\left.1-2 m, 1, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right.\right.\right. \\
 & \left.\left.\left.\left.\operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
 & \left.\left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)+ \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right]
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Big/ \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 2, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \Big) - \\
 & \left(4 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \Big/ \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 3 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Big) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3} 8^{1-m} (-3 + 2m) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \\
 & \left(\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-2m} \\
 & \left(\frac{1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \\
 & \left(- \left(\left(\operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \Big/ \\
 & \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 1, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(4 \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2\left(\frac{3}{2} - m\right)} 3 \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \\
 & \left. \left(\operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \left(\left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \right. \\
 & \left. \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2 \left(\frac{3}{2} - m\right)} \left(\frac{1}{2} - m\right) \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \text{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, \right. \right. \\
 & \quad \left. \left. 2, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{\frac{5}{2} - m} \right. \\
 & \quad \left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, -2m, 3, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \\
 & \quad \left. 2m \left(-\frac{1}{2 \left(\frac{5}{2} - m\right)} \left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 2, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - \right. \right. \right. \\
 & \quad \quad \left. \frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2 \left(\frac{5}{2} - m\right)} (1 - 2m) \left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, \right. \\
 & \quad \quad \left. \left. 2 - 2m, 1, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) \right) / \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 1, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 1, \right. \right. \\
 & \quad \quad \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \quad \left. \text{AppellF1}\left[\frac{3}{2} - m, -2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \right. \\
 & \quad \left(4 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \left(2 \left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \text{AppellF1}\left[\frac{3}{2} - m, \right. \\
 & \left. -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \\
 & \left(-\frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \left. \frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{\frac{5}{2} - m}\left(\frac{3}{2} - m\right) m \text{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, \right. \right. \\
 & \left. \left. 3, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2\left(\frac{5}{2} - m\right)} \right. \\
 & \left. 3\left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, -2m, 4, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \left. m\left(-\frac{1}{\frac{5}{2} - m}\left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 3, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{2\left(\frac{5}{2} - m\right)}(1 - 2m)\left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, \right. \right. \\
 & \left. \left. 2 - 2m, 2, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) \right) \right) \right) \Big/ \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4\left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \right. \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}-m, -2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
 & \left(4 \text{AppellF1}\left[\frac{1}{2}-m, -2m, 3, \frac{3}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
 & \quad \left(\left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right. \\
 & \quad \quad \left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 4,\right. \\
 & \quad \quad \left.\frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + (-3+2m) \\
 & \quad \left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right)m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 3, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \quad \left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
 & \quad \quad \frac{1}{2\left(\frac{3}{2}-m\right)}3\left(\frac{1}{2}-m\right) \text{AppellF1}\left[\frac{3}{2}-m, -2m, 4, \frac{5}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
 & \quad \quad \left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(2m \left(-\frac{1}{2\left(\frac{5}{2}-m\right)}3\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m,\right.\right.\right. \\
 & \quad \quad \left.1-2m, 4, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \quad \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \quad \left. \frac{1}{2\left(\frac{5}{2}-m\right)}(1-2m)\left(\frac{3}{2}-m\right) \text{AppellF1}\left[\frac{5}{2}-m, 2-2m, 3, \frac{7}{2}-m,\right.\right. \\
 & \quad \quad \left.\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \quad \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) + 3 \\
 & \quad \left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right)m \text{AppellF1}\left[\frac{5}{2}-m, 1-2m, 4, \frac{7}{2}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \quad \left.-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3 \Big/ \left((-3 + 2m)\right. \\
 & \quad \text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & \quad 4\left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(5 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \Big/ \left((-3 + 2m)\right. \right. \\
 & \quad \quad \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & \quad \quad 2\left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \right. \right. \\
 & \quad \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) - \\
 & \left(8 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) \Big/ \left((-3 + 2m)\right. \\
 & \quad \quad \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & \quad \quad 4\left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \right. \right. \\
 & \quad \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(4 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \Big/ \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) + \\
 & \quad 2\left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 5 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
 & \left(f (-1 + 2m) \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^5 \left(- \frac{1}{(-1 + 2m) \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^6} \right. \right. \right. \\
 & 5 \times 2^{5-3m} (-3 + 2m) \sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \left. \left(\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-2m} \left(\frac{1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \right. \\
 & \left. - \left(\left(\text{AppellF1} \left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right)^2 \right. \right. \\
 & \left. \left. \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) \right) / \left((-3 + 2m) \text{AppellF1} \left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left(m \text{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. 1 - 2m, 2, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \left. \text{AppellF1} \left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(5 \text{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \\
 & \left((-3 + 2m) \text{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \text{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 3 \text{AppellF1} \left[\frac{3}{2} - m, \right. \right. \\
 & \left. \left. -2m, 4, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \left(8 \text{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan \left[\frac{1}{4} \right. \right. \right. \\
 & \left. \left. \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
 & \left((-3 + 2m) \text{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left(m \text{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \text{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \right. \\
 & \left. \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^5} 2^{4-3m} (-3 + 2m) \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{-2m} \\
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3\right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \right. \\
 & \left. \left. 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right)^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 - \\
 & \left(8 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \left. \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, \right. \right. \right. \\
 & \left. \left. \left. 4, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \operatorname{AppellF1} \left[\right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right] \right) \\
 & \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left(4 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \left. \left. 5 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^5} 2^{7-3m} m (-3 + 2m) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \\
 & \left(\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-1-2m} \\
 & \left(\frac{1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \\
 & \left(-\frac{\sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{2 \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2} + \frac{\sec \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{4 \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)} \right) \\
 & - \left(\left(\operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \\
 & \left. \left. \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] + \\
 & \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2) + \\
 & \left(5 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) / \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \left. \left. 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. 2\left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left.\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \right. \\
 & \left. \left(8 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \right. \\
 & \left. \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4\left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \text{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \left.-2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \left(4 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \right. \\
 & \left. \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. 5 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^5} 2^{7-3m} m (-3 + 2m) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \\
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-1+2m} \\
 & \left(- \left(\left(\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \right. \\
 & \quad \left. \left(2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \right) \right) \\
 & \left(- \left(\left(\text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3 \right) / \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \text{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \\
 & \left(5 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2 \right) / \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \left(8 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \\
 & \left. -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. \left. 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^5} 8^{2-m} (-3 + 2m) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \\
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left(- \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) / \left(2 \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \left(\left(-\frac{1}{2} - \frac{3}{2} - m \right) \left(\frac{1}{2} - m \right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \\
 & \frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \Bigg) \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^3\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m,\right.\right. \\
 & \left. 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \\
 & 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 2, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+\operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m,\right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3,\right.\right. \\
 & \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \\
 & 3 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left(5\left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]- \\
 & \left. \frac{1}{2\left(\frac{3}{2}-m\right)} 3\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \Bigg) \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m,\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] + \\
 & 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(8\left(-\frac{1}{2} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2} \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \\
 & \left. \left(4\left(-\frac{1}{2} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \\
 & \frac{1}{2\left(\frac{3}{2} - m\right)} 5\left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right] \Bigg) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 2, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3 \left(2\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \\
 & \left. \left. -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \\
 & \left(-\frac{1}{2\left(\frac{3}{2} - m\right)}\left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 2, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \left. \frac{1}{\frac{3}{2} - m}\left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Bigg) + \\
 & 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\frac{1}{2\left(\frac{3}{2} - m\right)}\left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, \right. \right. \\
 & \left. \left. 3, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2\left(\frac{5}{2}-m\right)} \\
 & 3\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m,-2 m, 4, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \\
 & m\left(-\frac{1}{\frac{5}{2}-m}\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 1-2 m, 3, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \quad \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{1}{2\left(\frac{5}{2}-m\right)}(1-2 m)\left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m,\right. \right. \\
 & \quad \left. \left. 2-2 m, 2, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)\right) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 2, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \quad \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 2,\right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \\
 & \quad \left. \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2-\right. \\
 & \left.\left(5 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \right. \\
 & \left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\left(\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3, \frac{5}{2}-m,\right. \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+3 \operatorname{AppellF1}\left[\frac{3}{2}-m,\right. \right. \\
 & \quad \left. \left.-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+(-3+2 m) \right. \\
 & \left.\left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \left(2 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left. \left. \left. + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \right. \\
 & \quad \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{\frac{3}{2} - m} 2 \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \left. \right) + \\
 & 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(m \left(-\frac{1}{\frac{5}{2} - m} 2 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 5, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left. \frac{1}{2 \left(\frac{5}{2} - m\right)} (1 - 2m) \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 2 - 2m, 4, \frac{7}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + 2 \\
 & \left(-\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 5, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2 \left(\frac{5}{2} - m\right)} 5 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, \right. \right. \\
 & \quad \left. \left. - 2m, 6, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((-3+2m) \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 4, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 4, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 5, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2 - \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m, -2m, 5, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \left(\left(2m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 5, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 6, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + (-3+2m) \\
 & \left(-\frac{1}{\frac{3}{2}-m} \left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2m, 5, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2\left(\frac{3}{2}-m\right)} 5 \left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m, -2m, 6, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(2m \left(-\frac{1}{2\left(\frac{5}{2}-m\right)} 5 \left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 6, \frac{7}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \left. \frac{1}{2\left(\frac{5}{2}-m\right)} (1-2m) \left(\frac{3}{2}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}-m, 2-2m, 5, \frac{7}{2}-m, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + 5 \\
& \left(-\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 6, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right. \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{\frac{5}{2} - m} 3 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, -2m, \right. \right. \\
& \quad \left. \left. 7, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \quad \left. \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right) \right) / \\
& \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2,\right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)\right)\right) \right) \right) \right)
\end{aligned}$$

Problem 87: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[ex + fx]^2 (a + a \sin[ex + fx])^m (c - c \sin[ex + fx])^{1-m} dx$$

Optimal (type 5, 116 leaves, 5 steps):

$$\frac{1}{f(3 + 2m)} 2^{\frac{5}{2}-m} c^3 \cos[ex + fx]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-3 + 2m), \frac{1}{2}(3 + 2m), \frac{1}{2}(5 + 2m), \frac{1}{2}(1 + \sin[ex + fx])\right] \\
(1 - \sin[ex + fx])^{\frac{1}{2}+m} (a + a \sin[ex + fx])^m (c - c \sin[ex + fx])^{-2-m}$$

Result (type 6, 19668 leaves):

$$- \left(\left(8^{3-m} (-3 + 2m) \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-2m} \left(\cos\left[\frac{1}{2}(ex + fx)\right] - \sin\left[\frac{1}{2}(ex + fx)\right] \right)^{-2(1-m)} \right) \right)$$

$$\begin{aligned}
 & (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{1-m} \left(\cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^6 \right. \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} - 2 \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \\
 & \quad \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^5 \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \\
 & \quad \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^4 \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^2 + \\
 & \quad 4 \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^3 \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^3 - \\
 & \quad \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^2 \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^4 - \\
 & \quad 2 \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^5 + \\
 & \quad \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-2m} \\
 & \quad \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right]^6 \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right] \right) \\
 & \quad \left(\frac{\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]}{1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{-2m} \left(\frac{1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{2m} \\
 & \quad \left(- \left(\text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right. \\
 & \quad \quad \left. \left(1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^4 \right) / \left((-3 + 2m) \right. \\
 & \quad \quad \text{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \\
 & \quad \quad 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \right. \right. \\
 & \quad \quad \quad \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) + \\
 & \quad \quad \left(6 \text{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \quad \left. \left(1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^3 \right) / \left((-3 + 2m) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{2}-m, -2m, 4, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & 4\left(m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 4, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 5, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \\
 & \left(13 \text{AppellF1}\left[\frac{1}{2}-m, -2m, 5, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^2\right) / \left((-3+2m)\right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1}{2}-m, -2m, 5, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad 2\left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 5, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 5 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 6, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
 & \left(12 \text{AppellF1}\left[\frac{1}{2}-m, -2m, 6, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \left((-3+2m)\right. \\
 & \quad \left. \text{AppellF1}\left[\frac{1}{2}-m, -2m, 6, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad 4\left(m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 6, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 7, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \\
 & \left(4 \text{AppellF1}\left[\frac{1}{2}-m, -2m, 7, \frac{3}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) / \\
 & \left((-3+2m) \text{AppellF1}\left[\frac{1}{2}-m, -2m, 7, \frac{3}{2}-m, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad 2\left(2m \text{AppellF1}\left[\frac{3}{2}-m, 1-2m, 7, \frac{5}{2}-m, \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 7 \text{AppellF1}\left[\frac{3}{2}-m, -2m, 8, \frac{5}{2}-m, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(f (-1+2m) \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right)^2 \right)^7 \left(- \frac{1}{(-1+2m) \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right)^2} \right)^8 \\
 & 7 \times 2^{8-3m} (-3+2m) \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \left(\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]} \right)^{-2m} \left(\frac{1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]} \right)^{2m} \\
 & \left(- \left(\left(\operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^4 \right) / \left((-3+2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 3 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \left(6 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) / \left((-3+2m) \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \right. \\
 & \quad \left. \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \\
 & \left(13 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2 \right) / \left((-3+2m) \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \right. \\
 & \quad \left. \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 5 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(12 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 4 \left(m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 3 \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. - 2m, 7, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - \left(4 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \right. \\
 & \quad \left. \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, 1 - 2m, 7, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 7 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^7} 2^{7-3m} (-3 + 2m) \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \left(\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{-2m} \left(\frac{1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{2m} \\
 & \left(- \left(\left(\operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^4 \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 3 \operatorname{AppellF1} \left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) + \\
 & \left(6 \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^3 \right) / \left((-3 + 2m) \operatorname{AppellF1} \left[\frac{1}{2} - m, -2m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] + \\
 & 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(13 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \Big/ \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(12 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \Big/ \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. \left. -2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \Big/ \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 7 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(-1+2m) \left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^7} 2^{10-3m} m (-3+2m) \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{-1-2m} \\
 & \left(\frac{1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{2m} \\
 & \left(-\frac{\operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}{2 \left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}{4 \left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)}\right) \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right.\right.\right. \\
 & \quad \left.\left.\left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^4\right) / \left(\left(-3 + 2m\right) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right.\right.\right. \\
 & \quad \left.\left.\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, \right.\right.\right. \\
 & \quad \left.\left.\left.1 - 2m, 3, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \left.\left(6 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^3\right) / \left(\left(-3 + 2m\right) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right.\right.\right. \\
 & \quad \left.\left.\left.4, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right. \right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \right. \\
 & \left.\left(13 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\left(1 + \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) / \left(\left(-3 + 2m\right) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right.\right.\right. \\
 & \quad \left.\left.\left.5, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2]+5 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 6, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \\
 & \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left(12 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 6, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 6, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 6, \frac{5}{2}-m, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+3 \operatorname{AppellF1}\left[\frac{3}{2}-m, \right. \right. \right. \\
 & \left. \left. -2 m, 7, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right)\right) \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)-\left(4 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 7, \frac{3}{2}-m, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 7, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 7, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. \left. 7 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 8, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) + \\
 & \frac{1}{(-1+2 m)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^7} 2^{10-3 m} m(-3+2 m) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \left(\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-2 m} \\
 & \left(\frac{1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{-1+2 m} \\
 & \left(-\left(\left(\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) / \right. \\
 & \left.\left(2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right)\right)-\frac{\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]}{2\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)}\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \\
 & \left. -2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \right. \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. 7 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \frac{1}{(-1 + 2m) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^7} 8^{3-m} (-3 + 2m) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left(\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{-2m} \\
 & \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{2m} \\
 & \left(- \left(\left(2 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^3 \right) \right) / \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 3, \frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \\
 & \left. \left. 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] + \right. \\
 & \left. \left. 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \left(\left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m \right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 3, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] - \\
 & \frac{1}{2\left(\frac{3}{2}-m\right)} 3\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \\
 & \left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^4\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m,\right.\right. \\
 & \left.\left. 3, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. 2\left(2 m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 3, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+3 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left(9 \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 4, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2) / \\
 & \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m, 4, \frac{3}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 4,\right.\right.\right. \\
 & \left.\left.\frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 5, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left(6\left(-\frac{1}{\frac{3}{2}-m}\left(\frac{1}{2}-m\right) m \operatorname{AppellF1}\left[\frac{3}{2}-m, 1-2 m, 4, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]- \right. \\
 & \left. \frac{1}{\frac{3}{2}-m} 2\left(\frac{1}{2}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}-m,-2 m, 5, \frac{5}{2}-m, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) \\
 & \left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^3\right) / \left(\left(-3+2 m\right) \operatorname{AppellF1}\left[\frac{1}{2}-m,-2 m,\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] + \\
 & 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(13 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big/ \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \left(13 \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m \right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \right. \\
 & \quad \left. \left. \frac{1}{2 \left(\frac{3}{2} - m \right)} 5 \left(\frac{1}{2} - m \right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) \Big/ \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big/ \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + 4 \left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \quad 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 7, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \\
 & \quad \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(12 \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{\frac{3}{2} - m} 3 \left(\frac{1}{2} - m\right) \text{AppellF1}\left[\frac{3}{2} - m, -2m, 7, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \Big) \\
 & \left(1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big/ \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 6, \frac{3}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \quad 4 \left(m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + 3 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 7, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \\
 & \quad \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) - \\
 & \left(4 \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2\left(\frac{3}{2} - m\right)} 7 \left(\frac{1}{2} - m\right) \text{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. \left. - \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \Big) \Big/ \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+2\left(2m\operatorname{AppellF1}\left[\frac{3}{2}-m,1-2m,7,\right.\right. \\
 & \quad \left.\left.\frac{5}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+7\operatorname{AppellF1}\left[\frac{3}{2}-m,-2m,8,\right.\right. \\
 & \quad \left.\left.\frac{5}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}-m,-2m,3,\frac{3}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right. \\
 & \quad \left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^4\left(\left(2m\operatorname{AppellF1}\left[\frac{3}{2}-m,1-2m,3,\frac{5}{2}-m,\right.\right.\right.\right. \\
 & \quad \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+3\operatorname{AppellF1}\left[\frac{3}{2}-m,\right.\right.\right. \\
 & \quad \left.\left.\left.-2m,4,\frac{5}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+(-3+2m) \\
 & \quad \left(-\frac{1}{2}\left(\frac{1}{2}-m\right)m\operatorname{AppellF1}\left[\frac{3}{2}-m,1-2m,3,\frac{5}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]-\right. \\
 & \quad \left.\frac{1}{2}\left(\frac{3}{2}-m\right)3\left(\frac{1}{2}-m\right)\operatorname{AppellF1}\left[\frac{3}{2}-m,-2m,4,\frac{5}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)+ \\
 & 2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(2m\left(-\frac{1}{2}\left(\frac{5}{2}-m\right)3\left(\frac{3}{2}-m\right)\operatorname{AppellF1}\left[\frac{5}{2}-m,\right.\right.\right. \\
 & \quad \left.\left.1-2m,4,\frac{7}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+\frac{1}{2}\left(\frac{5}{2}-m\right)(1-2m) \\
 & \quad \left(\frac{3}{2}-m\right)\operatorname{AppellF1}\left[\frac{5}{2}-m,2-2m,3,\frac{7}{2}-m,\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \\
 & \quad \left.\left.\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)+3\left(-\frac{1}{2}\left(\frac{3}{2}-m\right)m\operatorname{AppellF1}\left[\frac{5}{2}-m,1-2m,4,\right.\right. \\
 & \quad \left.\left.\frac{5}{2}-m\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{7}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{\frac{5}{2} - m} 2 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, -2 m, 5, \frac{7}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] \right) \right) \right) \right) \right) / \\
 & \left((-3 + 2 m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2 m, 3, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 2 \left(2 m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2 m, 3, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2 m, 4, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right) \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 - \right. \\
 & \left. \left(6 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2 m, 4, \frac{3}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right. \\
 & \left. \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^3 \left(2 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2 m, 4, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2 m, 5, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + (-3 + 2 m) \right. \\
 & \left. \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2 m, 4, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{\frac{3}{2} - m} 2 \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2 m, 5, \frac{5}{2} - m, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \right. \\
 & \left. \left. - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right) + \\
 & 4 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(m \left(-\frac{1}{\frac{5}{2} - m} 2 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2 m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 5, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2] \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \\
 & \frac{1}{2\left(\frac{5}{2} - m\right)}(1 - 2m)\left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 2 - 2m, 4, \frac{7}{2} - m, \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] + 2 \\
 & \left(-\frac{1}{\frac{5}{2} - m}\left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 5, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{2\left(\frac{5}{2} - m\right)} 5\left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, \right. \right. \\
 & \left. \left. -2m, 6, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]\right) \Bigg/ \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 4, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 4\left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 4, \right. \right. \right. \\
 & \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \left. \left. 2 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 5, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^2 + \\
 & \left(13 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 5, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right)^2 \left(\left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 5, \frac{5}{2} - m, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \\
 & \left. \left. -2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \\
 & \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + (-3 + 2m) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{1}{\frac{3}{2}-m} \left(\frac{1}{2}-m \right) m \operatorname{AppellF1} \left[\frac{3}{2}-m, 1-2m, 5, \frac{5}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \\
 & \quad \left. \frac{1}{2 \left(\frac{3}{2}-m \right)} 5 \left(\frac{1}{2}-m \right) \operatorname{AppellF1} \left[\frac{3}{2}-m, -2m, 6, \frac{5}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + \\
 & 2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left(2m \left(-\frac{1}{2 \left(\frac{5}{2}-m \right)} 5 \left(\frac{3}{2}-m \right) \operatorname{AppellF1} \left[\frac{5}{2}-m, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 6, \frac{7}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \right. \\
 & \quad \left. \frac{1}{2 \left(\frac{5}{2}-m \right)} (1-2m) \left(\frac{3}{2}-m \right) \operatorname{AppellF1} \left[\frac{5}{2}-m, 2-2m, 5, \frac{7}{2}-m, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + 5 \\
 & \left(-\frac{1}{\frac{5}{2}-m} \left(\frac{3}{2}-m \right) m \operatorname{AppellF1} \left[\frac{5}{2}-m, 1-2m, 6, \frac{7}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{\frac{5}{2}-m} 3 \left(\frac{3}{2}-m \right) \operatorname{AppellF1} \left[\frac{5}{2}-m, -2m, \right. \right. \\
 & \quad \left. \left. 7, \frac{7}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \Big/ \\
 & \left((-3+2m) \operatorname{AppellF1} \left[\frac{1}{2}-m, -2m, 5, \frac{3}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left(2m \operatorname{AppellF1} \left[\frac{3}{2}-m, 1-2m, 5, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. 5 \operatorname{AppellF1} \left[\frac{3}{2}-m, -2m, 6, \frac{5}{2}-m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \left(12 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(2 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, \right. \right. \right. \right. \\
 & \left. \left. \left. -2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \\
 & \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \left. \frac{1}{\frac{3}{2} - m} 3 \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + \\
 & 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(m \left(-\frac{1}{\frac{5}{2} - m} 3 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, \right. \right. \right. \right. \\
 & \left. \left. \left. 7, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \left. \frac{1}{2 \left(\frac{5}{2} - m\right)} (1 - 2m) \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, 2 - 2m, 6, \frac{7}{2} - m, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + 3 \\
 & \left(-\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \operatorname{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 7, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2 \left(\frac{5}{2} - m\right)} 7 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -2m, 8, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left((-3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 6, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 6, \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 3 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 + \\
 & \left(4 \operatorname{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \\
 & \left(\left(2m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 7 \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right) \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (-3 + 2m) \\
 & \left(-\frac{1}{\frac{3}{2} - m} \left(\frac{1}{2} - m\right) m \operatorname{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{2\left(\frac{3}{2} - m\right)} 7 \left(\frac{1}{2} - m\right) \operatorname{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(2m \left(-\frac{1}{2\left(\frac{5}{2} - m\right)} 7 \left(\frac{3}{2} - m\right) \operatorname{AppellF1}\left[\frac{5}{2} - m, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2m, 8, \frac{7}{2} - m, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2 \left(\frac{5}{2} - m\right)} (1 - 2m) \left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, 2 - 2m, 7, \frac{7}{2} - m, \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \quad \left. \text{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]\right] + 7 \\
 & \left(-\frac{1}{\frac{5}{2} - m} \left(\frac{3}{2} - m\right) m \text{AppellF1}\left[\frac{5}{2} - m, 1 - 2m, 8, \frac{7}{2} - m, \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{1}{\frac{5}{2} - m} 4 \left(\frac{3}{2} - m\right) \text{AppellF1}\left[\frac{5}{2} - m, -2m, \right. \right. \\
 & \quad \left. \left. 9, \frac{7}{2} - m, \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]\right] \right) \right) \right) \Big/ \\
 & \left((-3 + 2m) \text{AppellF1}\left[\frac{1}{2} - m, -2m, 7, \frac{3}{2} - m, \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + 2 \left(2m \text{AppellF1}\left[\frac{3}{2} - m, 1 - 2m, 7, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \quad \left. \left. 7 \text{AppellF1}\left[\frac{3}{2} - m, -2m, 8, \frac{5}{2} - m, \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right) \right) \Big/
 \end{aligned}$$

Problem 88: Result unnecessarily involves higher level functions.

$$\int (g \cos[e + f x])^{3/2} \sqrt{a + a \sin[e + f x]} (c - c \sin[e + f x])^{7/2} dx$$

Optimal (type 4, 343 leaves, 8 steps):

$$\frac{2 a c^4 (g \operatorname{Cos}[e+f x])^{5/2}}{3 f g \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}} + \frac{2 a c^4 g \sqrt{\operatorname{Cos}[e+f x]} \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{f \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}} + \frac{2 a c^3 (g \operatorname{Cos}[e+f x])^{5/2} \sqrt{c-c \operatorname{Sin}[e+f x]}}{7 f g \sqrt{a+a \operatorname{Sin}[e+f x]}} + \frac{10 a c^2 (g \operatorname{Cos}[e+f x])^{5/2} (c-c \operatorname{Sin}[e+f x])^{3/2}}{77 f g \sqrt{a+a \operatorname{Sin}[e+f x]}} + \frac{2 a c (g \operatorname{Cos}[e+f x])^{5/2} (c-c \operatorname{Sin}[e+f x])^{5/2}}{33 f g \sqrt{a+a \operatorname{Sin}[e+f x]}} - \frac{2 a (g \operatorname{Cos}[e+f x])^{5/2} (c-c \operatorname{Sin}[e+f x])^{7/2}}{11 f g \sqrt{a+a \operatorname{Sin}[e+f x]}}$$

Result (type 5, 673 leaves):

$$\begin{aligned} & - \left(\left((2-2i) c^4 e^{-\frac{3}{2}i(e+fx)} (-i+e^{i(e+fx)}) (g \operatorname{Cos}[e+fx])^{3/2} \right. \right. \\ & \quad \left. \left(1+e^{2i(e+fx)} + (-1+e^{2ie}) \sqrt{1+e^{2i(e+fx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)}\right] \right) \right. \\ & \quad \left. \sqrt{a(1+\operatorname{Sin}[e+fx])} \right) / \left((-1+e^{2ie}) \sqrt{ic e^{-i(e+fx)} (-i+e^{i(e+fx)})^2} \right. \\ & \quad \left. \sqrt{e^{-i(e+fx)} (1+e^{2i(e+fx)})} f \operatorname{Cos}[e+fx]^{3/2} \left(\operatorname{Cos}\left[\frac{e}{2} + \frac{fx}{2}\right] + \operatorname{Sin}\left[\frac{e}{2} + \frac{fx}{2}\right] \right) \right) + \\ & \frac{1}{\operatorname{Cos}\left[\frac{e}{2} + \frac{fx}{2}\right] + \operatorname{Sin}\left[\frac{e}{2} + \frac{fx}{2}\right]} (g \operatorname{Cos}[e+fx])^{3/2} \operatorname{Sec}[e+fx] \\ & \left(\frac{58 c^3 \operatorname{Cos}\left[\frac{fx}{2}\right] \left(\operatorname{Cos}\left[\frac{e}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}\right]\right)}{77 f} - \frac{3 c^3 \operatorname{Cos}\left[\frac{3fx}{2}\right] \left(\operatorname{Cos}\left[\frac{3e}{2}\right] - \operatorname{Sin}\left[\frac{3e}{2}\right]\right)}{308 f} + \right. \\ & \frac{145 c^3 \operatorname{Cos}\left[\frac{5fx}{2}\right] \left(\operatorname{Cos}\left[\frac{5e}{2}\right] + \operatorname{Sin}\left[\frac{5e}{2}\right]\right)}{924 f} + \frac{19 c^3 \operatorname{Cos}\left[\frac{7fx}{2}\right] \left(\operatorname{Cos}\left[\frac{7e}{2}\right] - \operatorname{Sin}\left[\frac{7e}{2}\right]\right)}{264 f} - \\ & \frac{c^3 \operatorname{Cos}\left[\frac{9fx}{2}\right] \left(\operatorname{Cos}\left[\frac{9e}{2}\right] + \operatorname{Sin}\left[\frac{9e}{2}\right]\right)}{88 f} + \frac{58 c^3 \left(\operatorname{Cos}\left[\frac{e}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}\right]\right) \operatorname{Sin}\left[\frac{fx}{2}\right]}{77 f} + \\ & \frac{3 c^3 \left(\operatorname{Cos}\left[\frac{3e}{2}\right] + \operatorname{Sin}\left[\frac{3e}{2}\right]\right) \operatorname{Sin}\left[\frac{3fx}{2}\right]}{308 f} + \frac{145 c^3 \left(\operatorname{Cos}\left[\frac{5e}{2}\right] - \operatorname{Sin}\left[\frac{5e}{2}\right]\right) \operatorname{Sin}\left[\frac{5fx}{2}\right]}{924 f} - \\ & \left. \frac{19 c^3 \left(\operatorname{Cos}\left[\frac{7e}{2}\right] + \operatorname{Sin}\left[\frac{7e}{2}\right]\right) \operatorname{Sin}\left[\frac{7fx}{2}\right]}{264 f} - \frac{c^3 \left(\operatorname{Cos}\left[\frac{9e}{2}\right] - \operatorname{Sin}\left[\frac{9e}{2}\right]\right) \operatorname{Sin}\left[\frac{9fx}{2}\right]}{88 f} \right) \\ & \left. \frac{2 c^3 \operatorname{Cot}[e]}{f \left(\operatorname{Cos}\left[\frac{e}{2} + \frac{fx}{2}\right] - \operatorname{Sin}\left[\frac{e}{2} + \frac{fx}{2}\right]\right)} \sqrt{a(1+\operatorname{Sin}[e+fx])} \sqrt{c-c \operatorname{Sin}[e+fx]} \right) \end{aligned}$$

Problem 89: Result unnecessarily involves higher level functions.

$$\int (g \operatorname{Cos}[e+fx])^{3/2} \sqrt{a+a \operatorname{Sin}[e+fx]} (c-c \operatorname{Sin}[e+fx])^{5/2} dx$$

Optimal (type 4, 290 leaves, 7 steps):

$$\frac{22 a c^3 (g \cos [e+f x])^{5/2}}{45 f g \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} + \frac{22 a c^3 g \sqrt{\cos [e+f x]} \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{21 f g \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} + \frac{22 a c^2 (g \cos [e+f x])^{5/2} \sqrt{c-c \sin [e+f x]}}{105 f g \sqrt{a+a \sin [e+f x]}} + \frac{2 a c (g \cos [e+f x])^{5/2} (c-c \sin [e+f x])^{3/2}}{21 f g \sqrt{a+a \sin [e+f x]}} - \frac{2 a (g \cos [e+f x])^{5/2} (c-c \sin [e+f x])^{5/2}}{9 f g \sqrt{a+a \sin [e+f x]}}$$

Result (type 5, 205 leaves):

$$\left(c^3 g^2 \left(\cos \left[\frac{1}{2}(e+f x) \right] - \sin \left[\frac{1}{2}(e+f x) \right] \right) \sqrt{a(1+\sin [e+f x])} \left(3696 i e^{-i(e+f x)} \sqrt{1+e^{2i(e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+f x)}\right] + 4 \cos [e+f x] (-924 i + \cos [e+f x] (180 + 180 \cos [2(e+f x)] + 273 \sin [e+f x] - 35 \sin [3(e+f x)])) \right) \right) / \left(2520 f \sqrt{g \cos [e+f x]} \left(\cos \left[\frac{1}{2}(e+f x) \right] + \sin \left[\frac{1}{2}(e+f x) \right] \right) \sqrt{c-c \sin [e+f x]} \right)$$

Problem 90: Result unnecessarily involves higher level functions.

$$\int (g \cos [e+f x])^{3/2} \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{3/2} dx$$

Optimal (type 4, 235 leaves, 6 steps):

$$\frac{2 a c^2 (g \cos [e+f x])^{5/2}}{5 f g \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} + \frac{6 a c^2 g \sqrt{\cos [e+f x]} \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{5 f \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} + \frac{6 a c (g \cos [e+f x])^{5/2} \sqrt{c-c \sin [e+f x]}}{35 f g \sqrt{a+a \sin [e+f x]}} - \frac{2 a (g \cos [e+f x])^{5/2} (c-c \sin [e+f x])^{3/2}}{7 f g \sqrt{a+a \sin [e+f x]}}$$

Result (type 5, 147 leaves):

$$\left(c g^3 \sqrt{a(1+\sin [e+f x])} \sqrt{c-c \sin [e+f x]} \left(168 i e^{-i(e+f x)} \sqrt{1+e^{2i(e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+f x)}\right] + 4 \cos [e+f x] (-42 i + \cos [e+f x] (5 + 5 \cos [2(e+f x)] + 14 \sin [e+f x])) \right) \right) / \left(140 f (g \cos [e+f x])^{3/2} \right)$$

Problem 91: Result unnecessarily involves higher level functions.

$$\int (g \cos[e + f x])^{3/2} \sqrt{a + a \sin[e + f x]} \sqrt{c - c \sin[e + f x]} dx$$

Optimal (type 4, 178 leaves, 5 steps):

$$\frac{2 a c (g \cos [e + f x])^{5/2}}{5 f g \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} + \frac{6 a c g \sqrt{\cos [e + f x]} \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{5 f \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} - \frac{2 a (g \cos [e + f x])^{5/2} \sqrt{c - c \sin [e + f x]}}{5 f g \sqrt{a + a \sin [e + f x]}}$$

Result (type 5, 249 leaves):

$$\frac{1}{40 f} (g \cos [e + f x])^{3/2} \operatorname{Csc}\left[\frac{e}{2}\right] \operatorname{Sec}\left[\frac{e}{2}\right] \operatorname{Sec}[e + f x]^3 \sqrt{a (1 + \sin [e + f x])} \sqrt{c - c \sin [e + f x]} \left(-11 \cos [f x] - 13 \cos [2 e + f x] + \cos [2 e + 3 f x] - \cos [4 e + 3 f x] + 12 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i f x} (\cos [e] + i \sin [e])^2\right] (\cos [f x] - i \sin [f x]) \sqrt{1 + \cos [2 (e + f x)] + i \sin [2 (e + f x)]} \right) + 4 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i f x} (\cos [e] + i \sin [e])^2\right] (\cos [f x] + i \sin [f x]) \sqrt{1 + \cos [2 (e + f x)] + i \sin [2 (e + f x)]} \right)$$

Problem 92: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos [e + f x])^{3/2} \sqrt{a + a \sin [e + f x]}}{\sqrt{c - c \sin [e + f x]}} dx$$

Optimal (type 4, 122 leaves, 4 steps):

$$-\frac{2 a (g \cos [e + f x])^{5/2}}{3 f g \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}} + \frac{2 a g \sqrt{\cos [e + f x]} \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{f \sqrt{a + a \sin [e + f x]} \sqrt{c - c \sin [e + f x]}}$$

Result (type 5, 147 leaves):

$$- \left(\left(g \sqrt{g \cos[e+fx]} \left(1 + 6 i \cos[e+fx] + \cos[2(e+fx)] - 6 i e^{-i(e+fx)} \sqrt{1+e^{2i(e+fx)}} \right. \right. \right. \\ \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)}\right] \sqrt{a(1+\sin[e+fx])} \right) \right) / \right. \\ \left. \left(3 f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{c-c \sin[e+fx]} \right) \right)$$

Problem 93: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos[e+fx])^{3/2} \sqrt{a+a \sin[e+fx]}}{(c-c \sin[e+fx])^{3/2}} dx$$

Optimal (type 4, 123 leaves, 4 steps):

$$\frac{4 a (g \cos[e+fx])^{5/2}}{f g \sqrt{a+a \sin[e+fx]} (c-c \sin[e+fx])^{3/2}} - \\ \frac{6 a g \sqrt{\cos[e+fx]} \sqrt{g \cos[e+fx]} \text{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{c f \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}}$$

Result (type 5, 184 leaves):

$$\left(2 i g \sqrt{g \cos[e+fx]} \left(\cos\left[\frac{1}{2}(e+fx)\right] - \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 \right. \\ \left. \sqrt{a(1+\sin[e+fx])} \left(-3 \cos[e+fx] + 3 e^{-i(e+fx)} \sqrt{1+e^{2i(e+fx)}} \right. \right. \\ \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)}\right] + 2 i (1+\sin[e+fx]) \right) \right) / \\ \left(c f \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 (-1+\sin[e+fx]) \sqrt{c-c \sin[e+fx]} \right)$$

Problem 94: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos[e+fx])^{3/2} \sqrt{a+a \sin[e+fx]}}{(c-c \sin[e+fx])^{5/2}} dx$$

Optimal (type 4, 182 leaves, 5 steps):

$$\frac{4 a (g \cos[e+fx])^{5/2}}{5 f g \sqrt{a+a \sin[e+fx]} (c-c \sin[e+fx])^{5/2}} - \frac{6 a (g \cos[e+fx])^{5/2}}{5 c f g \sqrt{a+a \sin[e+fx]} (c-c \sin[e+fx])^{3/2}} + \\ \frac{6 a g \sqrt{\cos[e+fx]} \sqrt{g \cos[e+fx]} \text{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{5 c^2 f \sqrt{a+a \sin[e+fx]} \sqrt{c-c \sin[e+fx]}}$$

Result (type 5, 194 leaves):

$$\left(e^{-\frac{3}{2}i(e+fx)} g^3 \left(-3 - i e^{i(e+fx)} + e^{2i(e+fx)} - 5 i e^{3i(e+fx)} - \right. \right. \\ \left. \left. 3 \left(-i + e^{i(e+fx)} \right)^2 \sqrt{1 + e^{2i(e+fx)}} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)} \right] \right) \right) \\ \left(\operatorname{Cos} \left[\frac{1}{2}(e+fx) \right] - i \operatorname{Sin} \left[\frac{1}{2}(e+fx) \right] \right) \sqrt{a(1 + \operatorname{Sin}[e+fx])} \Big/ \\ \left(5 c^2 f (g \operatorname{Cos}[e+fx]) \right)^{3/2} \sqrt{c - c \operatorname{Sin}[e+fx]} \Big)$$

Problem 95: Result unnecessarily involves higher level functions.

$$\int \frac{(g \operatorname{Cos}[e+fx])^{3/2} \sqrt{a+a \operatorname{Sin}[e+fx]}}{(c-c \operatorname{Sin}[e+fx])^{7/2}} dx$$

Optimal (type 4, 237 leaves, 6 steps):

$$\frac{4 a (g \operatorname{Cos}[e+fx])^{5/2}}{9 f g \sqrt{a+a \operatorname{Sin}[e+fx]} (c-c \operatorname{Sin}[e+fx])^{7/2}} - \frac{2 a (g \operatorname{Cos}[e+fx])^{5/2}}{15 c f g \sqrt{a+a \operatorname{Sin}[e+fx]} (c-c \operatorname{Sin}[e+fx])^{5/2}} - \\ \frac{2 a (g \operatorname{Cos}[e+fx])^{5/2}}{15 c^2 f g \sqrt{a+a \operatorname{Sin}[e+fx]} (c-c \operatorname{Sin}[e+fx])^{3/2}} + \\ \frac{2 a g \sqrt{\operatorname{Cos}[e+fx]} \sqrt{g \operatorname{Cos}[e+fx]} \operatorname{EllipticE} \left[\frac{1}{2}(e+fx), 2 \right]}{15 c^3 f \sqrt{a+a \operatorname{Sin}[e+fx]} \sqrt{c-c \operatorname{Sin}[e+fx]}}$$

Result (type 5, 237 leaves):

$$\left(g^2 (\operatorname{Cos}[e+fx] - i \operatorname{Sin}[e+fx]) \sqrt{a(1 + \operatorname{Sin}[e+fx])} \right. \\ \left(7 i + 8 \operatorname{Cos}[e+fx] - 13 i \operatorname{Cos}[2(e+fx)] - \frac{3}{2} i e^{-2i(e+fx)} (-i + e^{i(e+fx)})^4 \sqrt{1 + e^{2i(e+fx)}} \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)} \right] + 20 i \operatorname{Sin}[e+fx] + 16 \operatorname{Sin}[2(e+fx)] \right] \right) \Big/ \\ \left(45 c^3 f \sqrt{g \operatorname{Cos}[e+fx]} \left(\operatorname{Cos} \left[\frac{1}{2}(e+fx) \right] - \operatorname{Sin} \left[\frac{1}{2}(e+fx) \right] \right)^3 \right. \\ \left. \left(\operatorname{Cos} \left[\frac{1}{2}(e+fx) \right] + \operatorname{Sin} \left[\frac{1}{2}(e+fx) \right] \right) \sqrt{c-c \operatorname{Sin}[e+fx]} \right)$$

Problem 96: Result unnecessarily involves higher level functions.

$$\int \frac{(g \operatorname{Cos}[e+fx])^{3/2} \sqrt{a+a \operatorname{Sin}[e+fx]}}{(c-c \operatorname{Sin}[e+fx])^{9/2}} dx$$

Optimal (type 4, 292 leaves, 7 steps):

$$\frac{4 a (g \cos [e+f x])^{5/2}}{13 f g \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{9/2}} -$$

$$\frac{2 a (g \cos [e+f x])^{5/2}}{39 c f g \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{7/2}} -$$

$$\frac{2 a (g \cos [e+f x])^{5/2}}{65 c^2 f g \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{5/2}} -$$

$$\frac{2 a (g \cos [e+f x])^{5/2}}{65 c^3 f g \sqrt{a+a \sin [e+f x]} (c-c \sin [e+f x])^{3/2}} +$$

$$\frac{2 a g \sqrt{\cos [e+f x]} \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{65 c^4 f \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}}$$

Result (type 5, 255 leaves):

$$\left(g^2 (\cos [e+f x] - i \sin [e+f x]) \sqrt{a(1+\sin [e+f x])} \right.$$

$$\left(54 i + 75 \cos [e+f x] - 66 i \cos [2(e+f x)] + \cos [3(e+f x)] + \right.$$

$$\left. \frac{3}{2} e^{-3 i(e+f x)} (-i + e^{i(e+f x)})^6 \sqrt{1+e^{2 i(e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(e+f x)}\right] + \right.$$

$$\left. 118 i \sin [e+f x] + 84 \sin [2(e+f x)] - 2 i \sin [3(e+f x)] \right) /$$

$$\left(390 c^4 f \sqrt{g \cos [e+f x]} \left(\cos \left[\frac{1}{2}(e+f x) \right] - \sin \left[\frac{1}{2}(e+f x) \right] \right)^5 \right.$$

$$\left. \left(\cos \left[\frac{1}{2}(e+f x) \right] + \sin \left[\frac{1}{2}(e+f x) \right] \right) \sqrt{c-c \sin [e+f x]} \right)$$

Problem 99: Result unnecessarily involves higher level functions.

$$\int (g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^{3/2} \sqrt{c-c \sin [e+f x]} dx$$

Optimal (type 4, 235 leaves, 6 steps):

$$-\frac{2 a^2 c (g \cos [e+f x])^{5/2}}{5 f g \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} +$$

$$\frac{6 a^2 c g \sqrt{\cos [e+f x]} \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{5 f \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}} -$$

$$\frac{6 a c (g \cos [e+f x])^{5/2} \sqrt{a+a \sin [e+f x]}}{35 f g \sqrt{c-c \sin [e+f x]}} + \frac{2 c (g \cos [e+f x])^{5/2} (a+a \sin [e+f x])^{3/2}}{7 f g \sqrt{c-c \sin [e+f x]}}$$

Result (type 5, 195 leaves):

$$\left(a^2 g^2 \left(\cos \left[\frac{1}{2} (e + f x) \right] + \sin \left[\frac{1}{2} (e + f x) \right] \right) \sqrt{c - c \sin[e + f x]} \right. \\ \left. \left(168 i e^{-i (e + f x)} \sqrt{1 + e^{2 i (e + f x)}} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (e + f x)} \right] + \right. \right. \\ \left. \left. 4 \cos[e + f x] (-42 i + \cos[e + f x] (-5 - 5 \cos[2 (e + f x)] + 14 \sin[e + f x])) \right) \right) / \\ \left(140 f \sqrt{g \cos[e + f x]} \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right) \sqrt{a (1 + \sin[e + f x])} \right)$$

Problem 108: Result unnecessarily involves higher level functions.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^{5/2} \sqrt{c - c \sin[e + f x]} dx$$

Optimal (type 4, 290 leaves, 7 steps):

$$- \frac{22 a^3 c (g \cos[e + f x])^{5/2}}{45 f g \sqrt{a + a \sin[e + f x]} \sqrt{c - c \sin[e + f x]}} + \\ \frac{22 a^3 c g \sqrt{\cos[e + f x]} \sqrt{g \cos[e + f x]} \operatorname{EllipticE} \left[\frac{1}{2} (e + f x), 2 \right]}{15 f \sqrt{a + a \sin[e + f x]} \sqrt{c - c \sin[e + f x]}} - \\ \frac{22 a^2 c (g \cos[e + f x])^{5/2} \sqrt{a + a \sin[e + f x]}}{105 f g \sqrt{c - c \sin[e + f x]}} - \\ \frac{2 a c (g \cos[e + f x])^{5/2} (a + a \sin[e + f x])^{3/2}}{21 f g \sqrt{c - c \sin[e + f x]}} + \frac{2 c (g \cos[e + f x])^{5/2} (a + a \sin[e + f x])^{5/2}}{9 f g \sqrt{c - c \sin[e + f x]}}$$

Result (type 5, 182 leaves):

$$- \left(\left(a^3 g \sqrt{g \cos[e + f x]} \sqrt{c - c \sin[e + f x]} \left(-3696 i e^{-i (e + f x)} \sqrt{1 + e^{2 i (e + f x)}} \right. \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (e + f x)} \right] + 4 \cos[e + f x] (924 i + \right. \right. \\ \left. \left. \cos[e + f x] (180 + 180 \cos[2 (e + f x)] - 273 \sin[e + f x] + 35 \sin[3 (e + f x)]) \right) \right) \right) / \\ \left(2520 f \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^2 \sqrt{a (1 + \sin[e + f x])} \right)$$

Problem 118: Result unnecessarily involves higher level functions.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^{7/2} \sqrt{c - c \sin[e + f x]} dx$$

Optimal (type 4, 343 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{2 a^4 c (g \operatorname{Cos}[e+f x])^{5/2}}{3 f g \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}} + \\
 & \frac{2 a^4 c g \sqrt{\operatorname{Cos}[e+f x]} \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{f \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}} - \\
 & \frac{2 a^3 c (g \operatorname{Cos}[e+f x])^{5/2} \sqrt{a+a \operatorname{Sin}[e+f x]}}{7 f g \sqrt{c-c \operatorname{Sin}[e+f x]}} - \frac{10 a^2 c (g \operatorname{Cos}[e+f x])^{5/2} (a+a \operatorname{Sin}[e+f x])^{3/2}}{77 f g \sqrt{c-c \operatorname{Sin}[e+f x]}} - \\
 & \frac{2 a c (g \operatorname{Cos}[e+f x])^{5/2} (a+a \operatorname{Sin}[e+f x])^{5/2}}{33 f g \sqrt{c-c \operatorname{Sin}[e+f x]}} + \frac{2 c (g \operatorname{Cos}[e+f x])^{5/2} (a+a \operatorname{Sin}[e+f x])^{7/2}}{11 f g \sqrt{c-c \operatorname{Sin}[e+f x]}}
 \end{aligned}$$

Result (type 5, 676 leaves):

$$\begin{aligned}
 & \left((2+2i) a^4 e^{-\frac{3}{2}i(e+fx)} (i+e^{i(e+fx)}) (g \operatorname{Cos}[e+f x])^{3/2} \right. \\
 & \left. \left(1+e^{2i(e+fx)} + (-1+e^{2ie}) \sqrt{1+e^{2i(e+fx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(e+fx)}\right] \right) \right. \\
 & \left. \sqrt{c-c \operatorname{Sin}[e+f x]} \right) / \left((-1+e^{2ie}) \sqrt{-i a e^{-i(e+fx)} (i+e^{i(e+fx)})^2} \right. \\
 & \left. \sqrt{e^{-i(e+fx)} (1+e^{2i(e+fx)})} f \operatorname{Cos}[e+f x]^{3/2} \left(\operatorname{Cos}\left[\frac{e}{2}+\frac{fx}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}+\frac{fx}{2}\right] \right) \right) + \\
 & \frac{1}{\operatorname{Cos}\left[\frac{e}{2}+\frac{fx}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}+\frac{fx}{2}\right]} (g \operatorname{Cos}[e+f x])^{3/2} \operatorname{Sec}[e+f x] \\
 & \left(-\frac{58 a^3 \operatorname{Cos}\left[\frac{fx}{2}\right] \left(\operatorname{Cos}\left[\frac{e}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}\right]\right)}{77 f} + \frac{3 a^3 \operatorname{Cos}\left[\frac{3fx}{2}\right] \left(\operatorname{Cos}\left[\frac{3e}{2}\right] + \operatorname{Sin}\left[\frac{3e}{2}\right]\right)}{308 f} - \right. \\
 & \frac{145 a^3 \operatorname{Cos}\left[\frac{5fx}{2}\right] \left(\operatorname{Cos}\left[\frac{5e}{2}\right] - \operatorname{Sin}\left[\frac{5e}{2}\right]\right)}{924 f} - \frac{19 a^3 \operatorname{Cos}\left[\frac{7fx}{2}\right] \left(\operatorname{Cos}\left[\frac{7e}{2}\right] + \operatorname{Sin}\left[\frac{7e}{2}\right]\right)}{264 f} + \\
 & \frac{a^3 \operatorname{Cos}\left[\frac{9fx}{2}\right] \left(\operatorname{Cos}\left[\frac{9e}{2}\right] - \operatorname{Sin}\left[\frac{9e}{2}\right]\right)}{88 f} + \frac{58 a^3 \left(\operatorname{Cos}\left[\frac{e}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}\right]\right) \operatorname{Sin}\left[\frac{fx}{2}\right]}{77 f} + \\
 & \frac{3 a^3 \left(\operatorname{Cos}\left[\frac{3e}{2}\right] - \operatorname{Sin}\left[\frac{3e}{2}\right]\right) \operatorname{Sin}\left[\frac{3fx}{2}\right]}{308 f} + \frac{145 a^3 \left(\operatorname{Cos}\left[\frac{5e}{2}\right] + \operatorname{Sin}\left[\frac{5e}{2}\right]\right) \operatorname{Sin}\left[\frac{5fx}{2}\right]}{924 f} - \\
 & \left. \frac{19 a^3 \left(\operatorname{Cos}\left[\frac{7e}{2}\right] - \operatorname{Sin}\left[\frac{7e}{2}\right]\right) \operatorname{Sin}\left[\frac{7fx}{2}\right]}{264 f} - \frac{a^3 \left(\operatorname{Cos}\left[\frac{9e}{2}\right] + \operatorname{Sin}\left[\frac{9e}{2}\right]\right) \operatorname{Sin}\left[\frac{9fx}{2}\right]}{88 f} \right) \\
 & \left. \frac{2 a^3 \operatorname{Cot}[e]}{f \left(\operatorname{Cos}\left[\frac{e}{2}+\frac{fx}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}+\frac{fx}{2}\right]\right)} \right) \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}
 \end{aligned}$$

Problem 129: Result unnecessarily involves higher level functions.

$$\int \frac{(g \operatorname{Cos}[e+f x])^{3/2} \sqrt{c-c \operatorname{Sin}[e+f x]}}{\sqrt{a+a \operatorname{Sin}[e+f x]}} dx$$

Optimal (type 4, 122 leaves, 4 steps):

$$\frac{2 c (g \operatorname{Cos}[e+f x])^{5/2}}{3 f g \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}} + \frac{2 c g \sqrt{\operatorname{Cos}[e+f x]} \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{f \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}}$$

Result (type 5, 149 leaves):

$$\left(g \sqrt{g \operatorname{Cos}[e+f x]} \left(1 - 6 i \operatorname{Cos}[e+f x] + \operatorname{Cos}[2(e+f x)] + 6 i e^{-i(e+f x)} \sqrt{1+e^{2 i(e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(e+f x)}\right] \right) \sqrt{c-c \operatorname{Sin}[e+f x]} \right) / \left(3 f \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^2 \sqrt{a(1+\operatorname{Sin}[e+f x])} \right)$$

Problem 137: Result unnecessarily involves higher level functions.

$$\int \frac{(g \operatorname{Cos}[e+f x])^{3/2} \sqrt{c-c \operatorname{Sin}[e+f x]}}{(a+a \operatorname{Sin}[e+f x])^{3/2}} dx$$

Optimal (type 4, 123 leaves, 4 steps):

$$\frac{4 c (g \operatorname{Cos}[e+f x])^{5/2}}{f g (a+a \operatorname{Sin}[e+f x])^{3/2} \sqrt{c-c \operatorname{Sin}[e+f x]}} - \frac{6 c g \sqrt{\operatorname{Cos}[e+f x]} \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{a f \sqrt{a+a \operatorname{Sin}[e+f x]} \sqrt{c-c \operatorname{Sin}[e+f x]}}$$

Result (type 5, 170 leaves):

$$\left(2 g \sqrt{g \operatorname{Cos}[e+f x]} \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] + \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^2 \left(-2 + 3 i \operatorname{Cos}[e+f x] - 3 i e^{-i(e+f x)} \sqrt{1+e^{2 i(e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(e+f x)}\right] + 2 \operatorname{Sin}[e+f x] \right) \sqrt{c-c \operatorname{Sin}[e+f x]} \right) / \left(f \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right] - \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right] \right)^2 (a(1+\operatorname{Sin}[e+f x]))^{3/2} \right)$$

Problem 146: Result unnecessarily involves higher level functions.

$$\int \frac{(g \operatorname{Cos}[e+f x])^{3/2} \sqrt{c-c \operatorname{Sin}[e+f x]}}{(a+a \operatorname{Sin}[e+f x])^{5/2}} dx$$

Optimal (type 4, 182 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{4 c (g \cos [e+f x])^{5/2}}{5 f g (a+a \sin [e+f x])^{5/2} \sqrt{c-c \sin [e+f x]}} + \frac{6 c (g \cos [e+f x])^{5/2}}{5 a f g (a+a \sin [e+f x])^{3/2} \sqrt{c-c \sin [e+f x]}} + \\
 & \frac{6 c g \sqrt{\cos [e+f x]} \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e+f x), 2\right]}{5 a^2 f \sqrt{a+a \sin [e+f x]} \sqrt{c-c \sin [e+f x]}}
 \end{aligned}$$

Result (type 5, 194 leaves):

$$\begin{aligned}
 & - \left(\left(e^{-\frac{3}{2} i (e+f x)} g^3 \left(-3 + i e^{i (e+f x)} + e^{2 i (e+f x)} + 5 i e^{3 i (e+f x)} - \right. \right. \right. \\
 & \quad \left. \left. \left. 3 (i + e^{i (e+f x)})^2 \sqrt{1 + e^{2 i (e+f x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (e+f x)}\right] \right) \right) \right. \\
 & \quad \left. \left(\cos \left[\frac{1}{2} (e+f x) \right] - i \sin \left[\frac{1}{2} (e+f x) \right] \right) \sqrt{c-c \sin [e+f x]} \right) / \\
 & \quad \left(5 a^2 f (g \cos [e+f x])^{3/2} \sqrt{a(1+\sin [e+f x])} \right)
 \end{aligned}$$

Problem 152: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m (c-c \sin [e+f x])^3 dx$$

Optimal (type 5, 93 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{1}{17 f g^7} 2^{\frac{9}{4}+m} a^4 c^3 (g \cos [e+f x])^{17/2} \operatorname{Hypergeometric2F1}\left[\frac{17}{4}, -\frac{1}{4}-m, \frac{21}{4}, \frac{1}{2}(1-\sin [e+f x])\right] \\
 & (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^{-4+m}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 153: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m (c-c \sin [e+f x])^2 dx$$

Optimal (type 5, 93 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{1}{13 f g^5} 2^{\frac{9}{4}+m} a^3 c^2 (g \cos [e+f x])^{13/2} \operatorname{Hypergeometric2F1}\left[\frac{13}{4}, -\frac{1}{4}-m, \frac{17}{4}, \frac{1}{2}(1-\sin [e+f x])\right] \\
 & (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^{-3+m}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 154: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m (c-c \sin [e+f x]) dx$$

Optimal (type 5, 91 leaves, 4 steps):

$$-\frac{1}{9fg^3} 2^{9+m} a^2 c (g \cos [e+fx])^{9/2} \text{Hypergeometric2F1}\left[\frac{9}{4}, -\frac{1}{4}-m, \frac{13}{4}, \frac{1}{2}(1-\sin [e+fx])\right] \\ (1+\sin [e+fx])^{-\frac{1}{4}-m} (a+a \sin [e+fx])^{-2+m}$$

Result (type 1, 1 leaves):

???

Problem 155: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (g \cos [e+fx])^{3/2} (a+a \sin [e+fx])^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$-\frac{1}{5fg} 2^{9+m} a (g \cos [e+fx])^{5/2} \text{Hypergeometric2F1}\left[\frac{5}{4}, -\frac{1}{4}-m, \frac{9}{4}, \frac{1}{2}(1-\sin [e+fx])\right] \\ (1+\sin [e+fx])^{-\frac{1}{4}-m} (a+a \sin [e+fx])^{-1+m}$$

Result (type 6, 13703 leaves):

$$\left(64 \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx \right) \right]^{-2m} (g \cos [e+fx])^{3/2} (a+a \sin [e+fx])^m \right. \\ \left(\cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx \right) \right]^{2m} \cos [e+fx]^{7/2} + \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx \right) \right]^{2m} \cos [e+fx]^{3/2} \sin [e+fx]^2 \right) \\ \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right)^{2m} \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2} \right)^{3+2m} \\ \sqrt{\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^3}{\left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)^2}} \\ \left(\left(25 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}-2m, 3+2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \right. \\ \left. \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) / \\ \left(-5 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}-2m, 3+2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + \right. \\ 2 \left((6+4m) \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\ \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (1+4m) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \right. \\ \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) +$$

$$\begin{aligned} & \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) / \\ & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\ & \quad 2 \left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right. \right. \\ & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\ & 9 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(- \left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \right) / \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}- \right. \right. \\ & \quad \left. \left. 2m, 3+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) + \\ & 2 \left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\ & \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] / \\ & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right. \right. \\ & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\ & \quad 2 \left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\ & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) \right) / \end{aligned}$$

$$\left(5 f \operatorname{Cos}[e+fx]^{3/2} \left(\frac{64}{5} m \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right. \\ \left. \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)^{-1+2m} \right)$$

$$\begin{aligned}
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{3+2m} \\
& \sqrt{\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2}} \\
& \left(\left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \left(-5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \quad \left. \left. \left. 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) + \right. \\
& \quad 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
& \quad \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \\
& \quad \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) - \\
& \quad 2 \left(4(2 + m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
& \quad 9 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(- \left(\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) / \\
& \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \quad \quad \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \\
& \quad \left(1 + 4m \right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) +
\end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] / \\
 & \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2\left(4(2+m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) \right) + \\
 & \frac{32}{5} (3+2m) \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \\
 & \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{4+2m} \\
 & \sqrt{\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2}} \\
 & \left(\left(25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \left(-5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2\left((6+4m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \\
 & \left(25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] / \right. \\
 & \quad \left. \left(5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2\left(4(2+m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & 9 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(- \left(\text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \right. \\
 & \quad \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left((6 + 4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] / \\
 & \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(4(2 + m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \frac{1}{5 \sqrt{\frac{\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2}}} 32 \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{2m} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2} \right)^{3+2m} \\
 & \left(\left(\frac{1}{4} \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \frac{3}{4} \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) / \right. \\
 & \quad \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^2 - \left(\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^3 \right) \right) / \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^3 \right) \\
 & \left(\left(25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right) / \left(-5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big] + \\
 & 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) / \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & 2 \left(4(2 + m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & 9 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(- \left(\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right) / \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \right. \\
 & \quad \left. (1 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big) + \operatorname{AppellF1}\left[\frac{5}{4}, \right. \\
 & \quad \left. -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right] / \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(4(2 + m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \right. \\
 & \quad \left. (1 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{64}{5} \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2m} \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right)^{3+2m} \\
 & \sqrt{\frac{\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^3}{\left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^2}} \\
 & \left(\left(25 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) / \\
 & \left(2 \left(-5 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + 2 \left((6 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. (1 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(25 \left(-\frac{1}{10} (3 + 2m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \right. \\
 & \quad \left. \frac{1}{10} \left(-\frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \\
 & \left(1 + \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) / \left(-5 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{5}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left((6 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left(25 \left(-\frac{1}{10} (4 + 2m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \right. \\
 & \quad \left. \frac{1}{10} \left(-\frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \Bigg) \Bigg/ \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & 2 \left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right. \\
 & \left. \frac{9}{2} \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
 & \left. \left. \left. 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) \Bigg) \Bigg/ \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) + \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \Bigg) \Bigg/ \right. \\
 & \left. \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
 & \left. \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) - \right. \\
 & \left. \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right. \right. \right. \\
 & \left. \left. \left(\left((6+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \left. \left. \left. \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 5\left(-\frac{1}{10}(3+2m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right.\right. \\
 & \quad \left.\left.\frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{10}\left(-\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 2\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\left((6+4m)\right. \\
 & \quad \left. - \frac{5}{18}(4+2m)\operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \left.\frac{5}{18}\left(-\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & \quad (1+4m)\left(-\frac{5}{18}(3+2m)\operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \right.\right. \\
 & \quad \left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{5}{18}\left(\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}-2m, \right. \\
 & \quad \left.3+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right) / \\
 & \quad \left(-5\operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 3+2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) + \\
 & \quad 2\left((6+4m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) + (1+4m)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \\
 & \quad \left(25\operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. - \left(4(2+m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right.\right. \right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) + (1+4m)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 5\left(-\frac{1}{10}(4+2m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}\right], \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{10}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}\right], \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (4(2+m) \\
 & \quad \left(-\frac{5}{18}(5+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 6+2m, \frac{13}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \quad \quad \left. \frac{5}{18}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 5+2m, \frac{13}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & (1+4m)\left(-\frac{5}{18}(4+2m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 5+2m, \frac{13}{4}\right], \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{5}{18}\left(\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}-2m, \right. \\
 & \quad \quad \left. 4+2m, \frac{13}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & 2\left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}\right], \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \\
 & 9 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
 & \left(2\left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + 2\left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \quad \left. \left. 4+2m, \frac{13}{4}\right], \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Bigg) - \\
 & \left(\left(-\frac{5}{18}(3+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \left. \frac{5}{18}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) / \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. 2 \left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
 & \left(-\frac{5}{18}(4+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \left. \frac{5}{18}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Bigg) / \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \quad \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
 & \quad \left. \left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \right) \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \Bigg) \left(\left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 4+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
 & 9\left(-\frac{5}{18}(3+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right. \\
 & \quad \left. \frac{5}{18}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) + \\
 & 2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left((6+4m) \left(-\frac{9}{26}(4+2m) \operatorname{AppellF1}\left[\frac{13}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{9}{26}\left(-\frac{1}{2}-2m\right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{13}{4}, \frac{1}{2}-2m, 4+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \\
 & \quad \left. \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right) + (1+4m) \left(-\frac{9}{26}(3+2m) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{1}{2}-2m, \right. \right. \\
 & \quad \left. \left. 4+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{9}{26}\left(\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{3}{2}-2m, \right. \right. \\
 & \quad \left. \left. 3+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \Big/ \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 2 \left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \right. \\
 & \quad \left. \left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(1+4 m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, \right. \\
 & \left. 4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]- \\
 & 9\left(-\frac{5}{18}(4+2 m) \operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2 m, 5+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \right. \\
 & \left. \frac{5}{18}\left(-\frac{1}{2}-2 m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, 4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+ \\
 & 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(4(2+m)\left(-\frac{9}{26}(5+2 m) \operatorname{AppellF1}\left[\frac{13}{4},-\frac{1}{2}-2 m, \right. \right. \right. \\
 & \left. \left. 6+2 m, \frac{17}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{9}{26}\left(-\frac{1}{2}-2 m\right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{13}{4}, \frac{1}{2}-2 m, 5+2 m, \frac{17}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+ \\
 & \left. (1+4 m)\left(-\frac{9}{26}(4+2 m) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{1}{2}-2 m, \right. \right. \right. \\
 & \left. \left. 5+2 m, \frac{17}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{9}{26}\left(\frac{1}{2}-2 m\right) \operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{13}{4}, \frac{3}{2}-2 m, 4+2 m, \frac{17}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}- \right. \right. \right. \\
 & \left. \left. \left. f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right)\right) / \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 4+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+2\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2 m, \right. \right. \right. \\
 & \left. \left. 5+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. (1+4 m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, 4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)\right)$$

Problem 156: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{3/2} (a+a \sin[e+fx])^m}{c-c \sin[e+fx]} dx$$

Optimal (type 5, 84 leaves, 4 steps):

$$-\frac{1}{c f} 2^{9/4+m} g \sqrt{g \cos[e+fx]} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, -\frac{1}{4}-m, \frac{5}{4}, \frac{1}{2}(1-\sin[e+fx])\right] \\ (1+\sin[e+fx])^{-1/4-m} (a+a \sin[e+fx])^m$$

Result (type 6, 9339 leaves):

$$\frac{1}{f \cos[e+fx]^{3/2} (c-c \sin[e+fx])} \\ \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} (g \cos[e+fx])^{3/2} \left(\cos\left[\frac{1}{2}(e+fx)\right]-\sin\left[\frac{1}{2}(e+fx)\right]\right)^2 \\ (a+a \sin[e+fx])^m \left(-\left(\left(10\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.\right.\right. \\ \left.\left.\left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2+4m} \cos[e+fx]\right.\right.\right.\right. \\ \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)\right)\right)\right) / \left(\left(\cos\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]-\sin\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)\right) \\ \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{3}{2}-2m, 3+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.\right. \\ \left.\left.\left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-2(3+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 2+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.\right. \\ \left.\left.\left.\left.\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m,\right.\right.\right.\right. \\ \left.\left.\left.\left.\frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) \\ \left(-\left(\left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.\right.\right. \\ \left.\left.\left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{1+2m} \sqrt{\cos[e+fx]}\right.\right.\right.\right. \\ \left.\left.\left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right)\right) / \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4},\right.\right.\right.\right. \\ \left.\left.\left.\left.-\frac{3}{2}-2m, 3+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-\right.\right.\right.\right.$$

$$\begin{aligned}
& 2(3+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 2+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
& \quad \left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
& \quad \left.\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \\
& \left(10 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{1+2m} \sqrt{\cos[e+fx]} \left(\frac{1}{10}(2+2m) \operatorname{AppellF1}\left[\frac{5}{4},\right.\right.\right. \\
& \quad \left.\left.\left.-\frac{3}{2}-2m, 3+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right.\right. \\
& \quad \left.\left.\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \frac{1}{10}\left(-\frac{3}{2}-2m\right) \operatorname{AppellF1}\left[\frac{5}{4},\right.\right.\right. \\
& \quad \left.\left.\left.-\frac{1}{2}-2m, 2+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right.\right. \\
& \quad \left.\left.\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) / \\
& \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{3}{2}-2m, 3+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2(3+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m,\right.\right. \\
& \quad \left.\left.2+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 5\right. \\
& \quad \left.\operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
& \left(5(1+2m) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sqrt{\cos[e+fx]} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) / \\
& \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4},\right.\right. \\
& \quad \left.\left.-\frac{3}{2}-2m, 3+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2\right. \\
& \quad \left.(3+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 2+2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4},\right.\right. \\
& \quad \left.\left.\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
& \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2}-2m, 2+2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{1+2m} \sin[e+fx] \right. \\
& \quad \left.\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) / \left(\sqrt{\cos[e+fx]} \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4},\right.\right.\right.
\end{aligned}$$

$$\begin{aligned}
 & -\frac{3}{2} - 2m, 3 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] - \\
 & 2(3 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2} - 2m, 2 + 2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \\
 & \left(10 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2} - 2m, 2 + 2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{1+2m} \sqrt{\cos[e + fx]} \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(-8(1+m) \left(\frac{5}{18}(3+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{3}{2} - 2m, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 4 + 2m, \frac{13}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \frac{5}{18}\left(-\frac{3}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \right. \\
 & \quad \left. 2(3 + 4m) \left(\frac{5}{18}(2 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \frac{5}{18}\left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{13}{4}, \right. \right. \\
 & \quad \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left. \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \frac{5}{2} \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{2} - 2m, 2 + 2m, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 5\left(\frac{1}{10}(2 + 2m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{3}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left. \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \frac{1}{10}\left(-\frac{3}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 2 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) / \\
 & \left(-8(1+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{3}{2} - 2m, 3 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-2(3+4m)\text{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2m, \right. \\
 & \left. 2+2m,\frac{9}{4},\text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+ \\
 & 5\text{AppellF1}\left[\frac{1}{4},-\frac{3}{2}-2m,2+2m,\frac{5}{4},\text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \left. -\text{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)+ \\
 & \left(7\sqrt{2}\text{AppellF1}\left[\frac{3}{4},-\frac{1}{2}-2m,2+2m,\frac{7}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{4m} \\
 & \text{Cos}[\\
 & \quad e+fx] \\
 & \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)/ \\
 & \left(\left(\text{Cos}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]-\text{Sin}\left[\frac{\pi}{4}+\frac{1}{2}\left(e-\frac{\pi}{2}+fx\right)\right]\right)\right) \\
 & \left(21\text{AppellF1}\left[\frac{3}{4},-\frac{1}{2}-2m,2+2m,\frac{7}{4}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]- \right. \\
 & \left. 6\left(4(1+m)\text{AppellF1}\left[\frac{7}{4},-\frac{1}{2}-2m,3+2m,\frac{11}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(1+4m)\text{AppellF1}\left[\frac{7}{4},\frac{1}{2}-2m,2+2m,\frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \\
 & \left(\left(7\text{AppellF1}\left[\frac{3}{4},-\frac{1}{2}-2m,2+2m,\frac{7}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) \right. \\
 & \quad \left. \text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{1+2m}\sqrt{\text{Cos}[e+fx]}\right)/\left(21\text{AppellF1}\left[\frac{3}{4},-\frac{1}{2}- \right. \right. \\
 & \quad \left. \left. 2m,2+2m,\frac{7}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]- \right. \\
 & \left. 6\left(4(1+m)\text{AppellF1}\left[\frac{7}{4},-\frac{1}{2}-2m,3+2m,\frac{11}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(1+4m)\text{AppellF1}\left[\frac{7}{4},\frac{1}{2}-2m,2+2m,\frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
 & \left(14m\text{AppellF1}\left[\frac{3}{4},-\frac{1}{2}-2m,2+2m,\frac{7}{4},\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\text{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-1+2m}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\cos[e+fx]} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big/ \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad \left. 6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \right. \\
 & \left. \left(7 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \sin[e+fx]\right) \Big/ \right. \\
 & \left. \left(\sqrt{\cos[e+fx]} \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) + \right. \\
 & \left. \left(14 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sqrt{\cos[e+fx]} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \right. \\
 & \quad \left. \left(-\frac{3}{14}(2+2m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{3}{14} \right. \right. \\
 & \quad \left. \left(-\frac{1}{2}-2m \right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Big/ \right) \Big/ \\
 & \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
 & \quad \left. 6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \right. \\
 & \left. \left(14 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Cos}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sqrt{\operatorname{Cos}[e+fx]} \\
 & \operatorname{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-3\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}-2m,3+2m,\frac{11}{4},\right.\right.\right. \\
 & \quad \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(1+4m) \operatorname{AppellF1}\left[\frac{7}{4},\right.\right.\right. \\
 & \quad \left.\left.\left.\frac{1}{2}-2m,2+2m,\frac{11}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right)\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+21 \\
 & \left(-\frac{3}{14}(2+2m) \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}-2m,3+2m,\frac{11}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+ \right. \\
 & \quad \left.\frac{3}{14}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{7}{4},\frac{1}{2}-2m,2+2m,\frac{11}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)-6 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(4(1+m)\left(-\frac{7}{22}(3+2m) \operatorname{AppellF1}\left[\frac{11}{4},-\frac{1}{2}-2m,\right.\right.\right. \\
 & \quad \left.\left.\left.4+2m,\frac{15}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \right. \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+\frac{7}{22}\left(-\frac{1}{2}-2m\right) \right. \\
 & \quad \left.\operatorname{AppellF1}\left[\frac{11}{4},\frac{1}{2}-2m,3+2m,\frac{15}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\right.\right.\right. \\
 & \quad \left.\left.\left.(-e+\frac{\pi}{2}-fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right) \\
 & (1+4m)\left(-\frac{7}{22}(2+2m) \operatorname{AppellF1}\left[\frac{11}{4},\frac{1}{2}-2m,3+2m,\frac{15}{4},\operatorname{Tan}\left[\frac{1}{4}\right.\right.\right. \\
 & \quad \left.\left.\left.(-e+\frac{\pi}{2}-fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]+\frac{7}{22}\left(\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{11}{4},\frac{3}{2}-2m,\right.\right. \\
 & \quad \left.\left.2+2m,\frac{15}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right) \Big/ \\
 & \left(21 \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}-2m,2+2m,\frac{7}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]-6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}-2m,\right.\right.\right. \\
 & \quad \left.\left.\left.3+2m,\frac{11}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+ \right. \\
 & \quad \left.\left.(1+4m) \operatorname{AppellF1}\left[\frac{7}{4},\frac{1}{2}-2m,2+2m,\frac{11}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) - \\
 & \left(7\sqrt{2} \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{4m} \right. \\
 & \quad \left. \cos\left[e + fx\right] \right. \\
 & \quad \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) / \\
 & \left(\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + fx\right)\right]\right) \right. \\
 & \quad \left(-21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \\
 & \quad \left.\left(7 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{1+2m} \sqrt{\cos[e + fx]}\right) / \\
 & \quad \left(-21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. 6\left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & \quad \left(14m \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \right. \\
 & \quad \quad \left. \sqrt{\cos[e + fx]} \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) / \left(-21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - \right. \right. \\
 & \quad \quad \left. \left. 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \right. \\
 & \left. \frac{1}{2} - 2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 21 \\
 & \left(-\frac{3}{14} (2+2m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
 & \left. \frac{3}{14} \left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + 6 \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(4(1+m) \left(-\frac{7}{22} (3+2m) \operatorname{AppellF1}\left[\frac{11}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \left. \left. 4+2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{7}{22} \left(-\frac{1}{2} - 2m\right) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2} - 2m, 3+2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) + \right. \\
 & \left. (1+4m) \left(-\frac{7}{22} (2+2m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2} - 2m, 3+2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{7}{22} \left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, \right. \right. \right. \\
 & \left. \left. 2+2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \right) / \\
 & \left(-21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \left. \left. 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \left. (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right)
 \end{aligned}$$

Problem 157: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m}{(c - c \sin[e + f x])^2} dx$$

Optimal (type 5, 93 leaves, 4 steps):

$$\left(2^{9/4+m} g^3 \text{Hypergeometric2F1} \left[-\frac{3}{4}, -\frac{1}{4} - m, \frac{1}{4}, \frac{1}{2} (1 - \sin[e + f x]) \right] \right) (1 + \sin[e + f x])^{-1/4 - m} (a + a \sin[e + f x])^{1+m} / \left(3 a c^2 f (g \cos[e + f x])^{3/2} \right)$$

Result (type 6, 13626 leaves):

$$\frac{1}{f \cos[e + f x]^{3/2} (c - c \sin[e + f x])^2} \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{-2m} (g \cos[e + f x])^{3/2} \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^4 (a + a \sin[e + f x])^m \left(\left(3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{4m} \cos[e + f x] \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) / \left(2 \sqrt{2} \left(8m \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + (2 + 8m) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - 3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^3 \left(- \left(\left(3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2m} \sqrt{\cos[e + f x]} \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \csc \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) / \left(4 \left(8m \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + (2 + 8m) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) - 3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right]^2, -\tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right)$$

$$\begin{aligned}
 & \left(-\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \\
 & \quad \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \Big) / \\
 & \left(2 \left(8m \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (2 + 8m) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] - 3 \right. \\
 & \quad \left. \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) - \\
 & \left(3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \\
 & \quad \left. \text{Cos} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx \right) \right]^{2m} \sqrt{\text{Cos} \left[e + fx \right]} \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right. \\
 & \quad \left. \text{Csc} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \left(\frac{3}{2} \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right. \\
 & \quad \left. \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \text{Csc} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 - 3 \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right. \\
 & \quad \left. \left(\frac{1}{3} m \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] - \right. \\
 & \quad \left. \frac{1}{6} \left(-\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right) + 8 \\
 & m \left(-\frac{3}{14} (1 + 2m) \text{AppellF1} \left[\frac{7}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] + \right. \\
 & \quad \left. \frac{3}{14} \left(-\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{7}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right) + \\
 & (2 + 8m) \left(-\frac{3}{7} m \text{AppellF1} \left[\frac{7}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] + \right. \\
 & \quad \left. \frac{3}{14} \left(\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right)^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \Bigg) \Bigg) / \\
 & \left(2 \left(8 m \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (2 + 8 m) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2 m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 3 \operatorname{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) + \\
 & \left(3 \operatorname{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \\
 & \quad \operatorname{Cos} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{4 m} \\
 & \quad \operatorname{Cos} [e + f x] \\
 & \quad \operatorname{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \\
 & \quad \operatorname{Csc} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \quad \left. \operatorname{Sin} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \Bigg) / \\
 & \left(2 \sqrt{2} \left(8 m \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (2 + 8 m) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2 m, 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 3 \operatorname{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \right) \right) \\
 & \left(\operatorname{Cos} \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \operatorname{Sin} \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^3 \\
 & \left(\left(3 \operatorname{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right. \\
 & \quad \operatorname{Cos} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{2 m} \sqrt{\operatorname{Cos} [e + f x]} \\
 & \quad \left. \operatorname{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Csc} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) / \\
 & \left(4 \left(8 m \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (2 + 8 m) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2 m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2 m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - 3 \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \\
 & \left(3 \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \sqrt{\cos[efx]} \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \Big) / \right. \\
 & \left(8 \left(8m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (2 + 8m) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 3 \right. \right. \\
 & \quad \left. \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \right. \\
 & \left(3m \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{-1+2m} \sqrt{\cos[efx]} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \Big) / \right. \\
 & \left(2 \left(8m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (2 + 8m) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 3 \right. \right. \\
 & \quad \left. \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) - \right. \\
 & \left(3 \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^{2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[efx] \Big) / \right. \\
 & \left(4 \sqrt{\cos[efx]} \left(8m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (2 + 8m) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 3 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2}-2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) - \\
 & \left(3 \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sqrt{\cos[e+fx]} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left(\frac{1}{3} m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 1+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \frac{1}{6} \right. \\
 & \quad \left(-\frac{1}{2}-2m\right) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}-2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\Big) \Big) / \\
 & \left(2 \left(8 m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 1+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (2+8 m) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 3 \right. \right. \\
 & \quad \left. \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2}-2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right) + \\
 & \left(3 \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2}-2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \sqrt{\cos[e+fx]} \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right. \\
 & \quad \left. \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(\frac{3}{2} \text{AppellF1}\left[-\frac{1}{4}, -\frac{1}{2}-2m, 2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - 3 \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left(\frac{1}{3} m \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 1+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \\
 & \quad \quad \left. \frac{1}{6} \left(-\frac{1}{2}-2m\right) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}-2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right) + 8 \\
 & m \left(-\frac{3}{14} (1+2m) \text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{3}{14} \left(-\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{7}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \\
 & \quad \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right) + \\
 & (2 + 8m) \left(-\frac{3}{7} m \text{AppellF1} \left[\frac{7}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] + \right. \\
 & \quad \left. \frac{3}{14} \left(\frac{1}{2} - 2m \right) \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right] \right) \right) / \\
 & \left(2 \left(8m \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (2 + 8m) \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] - \right. \\
 & \quad \left. 3 \text{AppellF1} \left[-\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{3}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) \right) - \\
 & \left(\left(\text{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)^{-1+2m} \text{Cos} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx \right) \right]^{1+2m} \sqrt{\text{Cos} [e + fx]} \right. \\
 & \quad \left. \sqrt{\left(\text{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \left(-\text{Sin} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] + \text{Sin} \left[\frac{3}{4} \left(-e + \frac{\pi}{2} - fx \right) \right] \right) \right)} \right) \\
 & \left(1 - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right)^{2m} \\
 & \left(\left(\text{AppellF1} \left[-\frac{3}{4}, -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \text{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) / \right. \\
 & \quad \left(\text{AppellF1} \left[-\frac{3}{4}, -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] - \right. \\
 & \quad \left. 2 \left(4m \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{5}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] + (1 + 4m) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right) + \\
 & \left(15 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] \right) / \\
 & \left(5 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - fx \right) \right]^2 \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(4 m \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 4 m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2 m, 2 m, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{4} \right. \right. \right. \\
 & \quad \left. \left. \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) \Bigg) / \\
 & \left(6 \left(\operatorname{Cos} \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \operatorname{Sin} \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right) \right)^3 \left(\frac{1}{12 \sqrt{2}} (-1 + 2 m) \right. \\
 & \quad \operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(\operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-2+2 m} \operatorname{Sin} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \\
 & \quad \left. \sqrt{\left(\operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\operatorname{Sin} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \operatorname{Sin} \left[\frac{3}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right)} \right) \\
 & \quad \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2 m} \left(\left(\operatorname{AppellF1} \left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) / \\
 & \quad \left(\operatorname{AppellF1} \left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - 2 \left(4 m \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{5}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 4 m) \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{1}{4}, \frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \left(15 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \Bigg) / \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] - \right. \\
 & \quad \left. 2 \left(4 m \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1 + 4 m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2 m, \right. \right. \\
 & \quad \left. \left. 2 m, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \Bigg) - \left(\left(\operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-1+2 m} \right. \\
 & \quad \left(\operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\frac{1}{4} \operatorname{Cos} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{3}{4} \operatorname{Cos} \left[\frac{3}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) - \right. \\
 & \quad \left. \frac{1}{4} \operatorname{Sin} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\operatorname{Sin} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] + \operatorname{Sin} \left[\frac{3}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \Bigg) \\
 & \quad \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{2 m} \left(\left(\operatorname{AppellF1} \left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big/ \\
 & \left(\text{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - 2 \left(4m \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{5}{4}, \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \text{AppellF1}\left[\right. \\
 & \quad \left. \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big) + \left(15 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \Big/ \\
 & \left(5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2 \left(4m \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 1 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big) \Big/ \left(12\sqrt{2} \right. \\
 & \quad \left. \sqrt{\left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \sin\left[\frac{3}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right)} \right) + \\
 & \frac{1}{6\sqrt{2}} m \left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{2m} \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \\
 & \sqrt{\left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-\sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \sin\left[\frac{3}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right)} \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{-1+2m} \\
 & \left(\left(\text{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \Big/ \left(\text{AppellF1}\left[-\frac{3}{4}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(4m \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 + \left(15 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \right.\right. \\
 & \left.\left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, \right.\right. \\
 & \left.\left. -\frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & 2 \left(4 m \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right. \\
 & \left.\left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (1 + 4 m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2 m, \right.\right. \\
 & \left.\left. 2 m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) - \frac{1}{6\sqrt{2}} \left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-1+2 m} \\
 & \sqrt{\left(\cos\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\sin\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \sin\left[\frac{3}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)} \\
 & \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{2 m} \\
 & \left(-\left(\operatorname{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right. \\
 & \left.\left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] \csc\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \\
 & \left(2 \left(\operatorname{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right. \\
 & \left.\left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 2 \left(4 m \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \right.\right.\right. \\
 & \left.\left. \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\
 & \left.\left. (1 + 4 m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right. \\
 & \left.\left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \\
 & \left(\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(3 m \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2 m, 1 + 2 m, \frac{5}{4}, \right.\right.\right. \\
 & \left.\left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - \frac{3}{2}\left(-\frac{1}{2} - 2 m\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2 m, 2 m, \frac{5}{4}, \right.\right. \\
 & \left.\left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right. \\
 & \left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right) / \left(\operatorname{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2 m, 2 m, \frac{1}{4}, \right.\right. \\
 & \left.\left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 2 \left(4 m \operatorname{AppellF1}\left[\frac{1}{4}, \right.\right.\right. \\
 & \left.\left. -\frac{1}{2} - 2 m, 1 + 2 m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (1+4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}-2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 + \\
 & \left(15\left(-\frac{1}{5}m \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 1+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \\
 & \quad \frac{1}{10}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) / \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 1+2m, \frac{9}{4},\right.\right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \left(\operatorname{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2}-2m, 2m, \frac{1}{4},\right.\right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left. 3m \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 1+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
 & \quad \frac{3}{2}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}-2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - \\
 & \left. 4m \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 1+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}-2m,\right. \\
 & \quad \left. 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - 2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left. 4m\left(-\frac{1}{10}(1+2m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 2+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-\right.\right.\right.\right. \right. \\
 & \quad \left. \left. \left. fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{10}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m,\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2] \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (1 + 4m) \\
 & \left(-\frac{1}{5} m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{10}\left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2} - 2m, \right. \\
 & \quad \left. 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) / \\
 & \left(\operatorname{AppellF1}\left[-\frac{3}{4}, -\frac{1}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 1 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. (1 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \left(15 \operatorname{AppellF1}\left[\frac{1}{4}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \left. - \left(4m \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 5\left(-\frac{1}{5} m \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - \right. \right. \\
 & \quad \left. \left. 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{10}\left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{5}{4}, \frac{1}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) - \\
 & 2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(4m\left(-\frac{5}{18}(1 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 2 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \\
 & \frac{5}{18}\left(-\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{13}{4}, \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + (1 + 4m) \\
 & \left(-\frac{5}{9}m \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{13}{4}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{5}{18}\left(\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{3}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{13}{4}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) \Bigg/ \\
 & \left(5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 2m, \frac{5}{4}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - 2\left(4m \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 1 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{4}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. \left. (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 2m, \frac{9}{4}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right) \Bigg)
 \end{aligned}$$

Problem 158: Attempted integration timed out after 120 seconds.

$$\int \frac{(g \cos[e + fx])^{3/2} (a + a \sin[e + fx])^m}{(c - c \sin[e + fx])^3} dx$$

Optimal (type 5, 93 leaves, 4 steps):

$$\left(2^{4+m} g^5 \text{Hypergeometric2F1}\left[-\frac{7}{4}, -\frac{1}{4} - m, -\frac{3}{4}, \frac{1}{2} (1 - \sin[e + fx])\right] \right. \\
 \left. (1 + \sin[e + fx])^{-\frac{1}{4}-m} (a + a \sin[e + fx])^{2+m}\right) / \left(7 a^2 c^3 f (g \cos[e + fx])^{7/2}\right)$$

Result (type 1, 1 leaves):

???

Problem 159: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{5/2} dx$$

Optimal (type 5, 114 leaves, 4 steps):

$$-\frac{1}{15 f g^6} 2^{\frac{9}{4}+m} a^3 c^2 (g \cos[e + f x])^{15/2} \text{Hypergeometric2F1}\left[\frac{15}{4}, -\frac{1}{4}-m, \frac{19}{4}, \frac{1}{2}(1 - \sin[e + f x])\right] \\ \sec[e + f x] (1 + \sin[e + f x])^{-\frac{1}{4}-m} (a + a \sin[e + f x])^{-3+m} \sqrt{c - c \sin[e + f x]}$$

Result (type 1, 1 leaves):

???

Problem 160: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{3/2} dx$$

Optimal (type 5, 112 leaves, 4 steps):

$$-\frac{1}{11 f g^4} 2^{\frac{9}{4}+m} a^2 c (g \cos[e + f x])^{11/2} \text{Hypergeometric2F1}\left[\frac{11}{4}, -\frac{1}{4}-m, \frac{15}{4}, \frac{1}{2}(1 - \sin[e + f x])\right] \\ \sec[e + f x] (1 + \sin[e + f x])^{-\frac{1}{4}-m} (a + a \sin[e + f x])^{-2+m} \sqrt{c - c \sin[e + f x]}$$

Result (type 1, 1 leaves):

???

Problem 161: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m \sqrt{c - c \sin[e + f x]} dx$$

Optimal (type 5, 109 leaves, 4 steps):

$$-\frac{1}{7 f g^2} 2^{\frac{9}{4}+m} a (g \cos[e + f x])^{7/2} \text{Hypergeometric2F1}\left[\frac{7}{4}, -\frac{1}{4}-m, \frac{11}{4}, \frac{1}{2}(1 - \sin[e + f x])\right] \\ \sec[e + f x] (1 + \sin[e + f x])^{-\frac{1}{4}-m} (a + a \sin[e + f x])^{-1+m} \sqrt{c - c \sin[e + f x]}$$

Result (type 1, 1 leaves):

???

Problem 162: Attempted integration timed out after 120 seconds.

$$\int \frac{(g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m}{\sqrt{c - c \sin[e + f x]}} dx$$

Optimal (type 5, 106 leaves, 4 steps):

$$- \left(\left(2^{4+m} a \cos [e+f x] (g \cos [e+f x])^{3/2} \text{Hypergeometric2F1} \left[\frac{3}{4}, -\frac{1}{4}-m, \frac{7}{4}, \frac{1}{2} (1-\sin [e+f x]) \right] \right) (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^{-1+m} \right) / \left(3 f \sqrt{c-c \sin [e+f x]} \right)$$

Result (type 1, 1 leaves):

???

Problem 163: Attempted integration timed out after 120 seconds.

$$\int \frac{(g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m}{(c-c \sin [e+f x])^{3/2}} dx$$

Optimal (type 5, 106 leaves, 4 steps):

$$\left(2^{4+m} g^2 \cos [e+f x] \text{Hypergeometric2F1} \left[-\frac{1}{4}, -\frac{1}{4}-m, \frac{3}{4}, \frac{1}{2} (1-\sin [e+f x]) \right] (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^m \right) / \left(c f \sqrt{g \cos [e+f x]} \sqrt{c-c \sin [e+f x]} \right)$$

Result (type 1, 1 leaves):

???

Problem 164: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m}{(c-c \sin [e+f x])^{5/2}} dx$$

Optimal (type 5, 114 leaves, 4 steps):

$$\left(2^{9+m} g^4 \cos [e+f x] \text{Hypergeometric2F1} \left[-\frac{5}{4}, -\frac{1}{4}-m, -\frac{1}{4}, \frac{1}{2} (1-\sin [e+f x]) \right] (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^{1+m} \right) / \left(5 a c^2 f (g \cos [e+f x])^{5/2} \sqrt{c-c \sin [e+f x]} \right)$$

Result (type 6, 20476 leaves): Display of huge result suppressed!

Problem 165: Attempted integration timed out after 120 seconds.

$$\int \frac{(g \cos [e+f x])^{3/2} (a+a \sin [e+f x])^m}{\sqrt{c-c \sin [e+f x]}} dx$$

Optimal (type 5, 106 leaves, 4 steps):

$$- \left(\left(2^{4+m} a \cos [e+f x] (g \cos [e+f x])^{3/2} \text{Hypergeometric2F1} \left[\frac{3}{4}, -\frac{1}{4}-m, \frac{7}{4}, \frac{1}{2} (1-\sin [e+f x]) \right] \right) (1+\sin [e+f x])^{-\frac{1}{4}-m} (a+a \sin [e+f x])^{-1+m} \right) / \left(3 f \sqrt{c-c \sin [e+f x]} \right)$$

Result (type 1, 1 leaves):

???

Problem 166: Attempted integration timed out after 120 seconds.

$$\int \frac{(g \cos[e + f x])^{3/2} (c + c \sin[e + f x])^m}{\sqrt{a - a \sin[e + f x]}} dx$$

Optimal (type 5, 106 leaves, 4 steps):

$$- \left(\left(2^{3/4+m} c \cos[e + f x] (g \cos[e + f x])^{3/2} \text{Hypergeometric2F1} \left[\frac{3}{4}, -\frac{1}{4} - m, \frac{7}{4}, \frac{1}{2} (1 - \sin[e + f x]) \right] \right) (1 + \sin[e + f x])^{-1/4-m} (c + c \sin[e + f x])^{-1+m} \right) / \left(3 f \sqrt{a - a \sin[e + f x]} \right)$$

Result (type 1, 1 leaves):

???

Problem 167: Result more than twice size of optimal antiderivative.

$$\int (g \cos[e + f x])^{3/2} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-3-m} dx$$

Optimal (type 5, 123 leaves, 4 steps):

$$\frac{1}{c^2 f g (5 + 4 m)} 2^{-3/4-m} (g \cos[e + f x])^{5/2} \text{Hypergeometric2F1} \left[\frac{1}{4} (5 + 4 m), \frac{1}{4} (11 + 4 m), \frac{1}{4} (9 + 4 m), \frac{1}{2} (1 + \sin[e + f x]) \right] (1 - \sin[e + f x])^{-1/4-m} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-1-m}$$

Result (type 5, 2502 leaves):

$$\left(2^{-4-m} \left(\cos \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-1+2m} \sqrt{\cos[e + f x]} (g \cos[e + f x])^{3/2} \left((-3 + 8 m + 16 m^2) \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \text{Hypergeometric2F1} \left[-\frac{3}{2} - 2 m, -\frac{7}{4} - m, -\frac{3}{4} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (7 + 4 m) \left(2 (-1 + 4 m) \cot \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) \text{Hypergeometric2F1} \left[-\frac{3}{2} - 2 m, -\frac{3}{4} - m, \frac{1}{4} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (3 + 4 m) \text{Hypergeometric2F1} \left[-\frac{3}{2} - 2 m, \frac{1}{4} - m, \frac{5}{4} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \right) \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^{-2m} \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^{-2(-3-m)} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-3-m} \left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] - \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)^{-6-2m} /$$

$$\left(f (-1 + 4 m) (3 + 4 m) (7 + 4 m) \sqrt{1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right.$$

$$\left. - \frac{1}{(-1 + 4 m) (3 + 4 m) (7 + 4 m) \left(1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{3/2}} \right.$$

$$\left. 2^{-6-m} \left(\operatorname{Cos}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-1+2m} \sqrt{\operatorname{Cos}[e + f x]} \right.$$

$$\left. \left((-3 + 8 m + 16 m^2) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^4 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, -\frac{7}{4} - m, -\frac{3}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (7 + 4 m) \left(2 (-1 + 4 m) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, -\frac{3}{4} - m, \frac{1}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3 + 4 m) \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, \frac{1}{4} - m, \frac{5}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \right)$$

$$\left. \operatorname{Sec}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{-2m} \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{1}{(-1 + 4 m) (3 + 4 m) (7 + 4 m) \sqrt{1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}} \right.$$

$$\left. 2^{-4-m} m \left(\operatorname{Cos}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-1+2m} \operatorname{Cos}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right] \sqrt{\operatorname{Cos}[e + f x]} \right.$$

$$\left. \left((-3 + 8 m + 16 m^2) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^4 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, -\frac{7}{4} - m, -\frac{3}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (7 + 4 m) \left(2 (-1 + 4 m) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, -\frac{3}{4} - m, \frac{1}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (3 + 4 m) \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, \frac{1}{4} - m, \frac{5}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \right)$$

$$\left. \operatorname{Sin}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{-1-2m} + \frac{1}{(-1 + 4 m) (3 + 4 m) (7 + 4 m) \sqrt{1 - \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}} \right.$$

$$\left. 2^{-5-m} (-1 + 2 m) \operatorname{Cos}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right] \left(\operatorname{Cos}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-2+2m} \sqrt{\operatorname{Cos}[e + f x]} \right.$$

$$\left. \left((-3 + 8 m + 16 m^2) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^4 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2} - 2 m, -\frac{7}{4} - m, -\frac{3}{4} - m, \operatorname{Tan}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (7 + 4 m) \left(2 (-1 + 4 m) \operatorname{Cot}\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right)$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{3}{4}-m, \frac{1}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & (3+4m) \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, \frac{1}{4}-m, \frac{5}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \Bigg) \\
 & \sin\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} - \\
 & \left(2^{-5-m} \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2m} \left((-3+8m+16m^2) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^4\right. \right. \\
 & \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{7}{4}-m, -\frac{3}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & (7+4m) \left(2(-1+4m) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{3}{4}- \right. \right. \\
 & m, \frac{1}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (3+4m) \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, \frac{1}{4}- \right. \\
 & m, \frac{5}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \Bigg) \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \sin[e+fx] \Bigg) / \\
 & \left((-1+4m) (3+4m) (7+4m) \sqrt{\cos[e+fx]} \sqrt{1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right) - \\
 & \frac{1}{(-1+4m) (3+4m) (7+4m) \sqrt{1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}} \\
 & 2^{-4-m} \left(\cos\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-1+2m} \sqrt{\cos[e+fx]} \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-2m} \\
 & \left(-(-3+8m+16m^2) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^3 \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{7}{4}-m, -\frac{3}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & \frac{1}{2} \left(-\frac{7}{4}-m\right) (-3+8m+16m^2) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^3 \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left(-\text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{7}{4}-m, -\frac{3}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
 & \left. \left(1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{\frac{3}{2}+2m} \right) + \\
 & (7+4m) \left(-(-1+4m) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \\
 & \text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{3}{4}-m, \frac{1}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \\
 & \left(-\frac{3}{4}-m\right) (-1+4m) \cot\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \csc\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
 & \left. \left(-\text{Hypergeometric2F1}\left[-\frac{3}{2}-2m, -\frac{3}{4}-m, \frac{1}{4}-m, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\left(\left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{3}{2} + 2m} + \frac{1}{2} \left(\frac{1}{4} - m \right) (3 + 4m) \operatorname{Csc} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \operatorname{Sec} \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\operatorname{Hypergeometric2F1} \left[-\frac{3}{2} - 2m, \frac{1}{4} - m, \frac{5}{4} - m, \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + \left(1 - \tan \left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{\frac{3}{2} + 2m} \right) \right)$$

Problem 169: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e + f x])^{3/2} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1-m} dx$$

Optimal (type 5, 120 leaves, 4 steps):

$$\frac{1}{f g (5 + 4 m)} 2^{\frac{5}{4} - m} (g \cos [e + f x])^{5/2} \operatorname{Hypergeometric2F1} \left[\frac{1}{4} (3 + 4 m), \frac{1}{4} (5 + 4 m), \frac{1}{4} (9 + 4 m), \frac{1}{2} (1 + \sin [e + f x]) \right] (1 - \sin [e + f x])^{-\frac{1}{4} + m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1-m}$$

Result (type 1, 1 leaves):

???

Problem 170: Unable to integrate problem.

$$\int (g \cos [e + f x])^{3/2} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-m} dx$$

Optimal (type 5, 121 leaves, 4 steps):

$$\frac{1}{f g (5 + 4 m)} 2^{\frac{9}{4} - m} c (g \cos [e + f x])^{5/2} \operatorname{Hypergeometric2F1} \left[\frac{1}{4} (-1 + 4 m), \frac{1}{4} (5 + 4 m), \frac{1}{4} (9 + 4 m), \frac{1}{2} (1 + \sin [e + f x]) \right] (1 - \sin [e + f x])^{-\frac{1}{4} + m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1-m}$$

Result (type 8, 42 leaves):

$$\int (g \cos [e + f x])^{3/2} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-m} dx$$

Problem 171: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e + f x])^{3/2} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{1-m} dx$$

Optimal (type 5, 123 leaves, 4 steps):

$$\frac{1}{f g (5 + 4 m)} 2^{\frac{13}{4}-m} c^2 (g \cos [e + f x])^{5/2}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{4}(-5 + 4 m), \frac{1}{4}(5 + 4 m), \frac{1}{4}(9 + 4 m), \frac{1}{2}(1 + \sin [e + f x])\right]$$

$$(1 - \sin [e + f x])^{-\frac{1}{4}+m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1-m}$$

Result (type 1, 1 leaves):

???

Problem 172: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e + f x])^{3/2} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{2-m} dx$$

Optimal (type 5, 123 leaves, 4 steps):

$$\frac{1}{f g (5 + 4 m)} 2^{\frac{17}{4}-m} c^3 (g \cos [e + f x])^{5/2}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{4}(-9 + 4 m), \frac{1}{4}(5 + 4 m), \frac{1}{4}(9 + 4 m), \frac{1}{2}(1 + \sin [e + f x])\right]$$

$$(1 - \sin [e + f x])^{-\frac{1}{4}+m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1-m}$$

Result (type 1, 1 leaves):

???

Problem 174: Attempted integration timed out after 120 seconds.

$$\int (g \cos [e + f x])^{1-2m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1+m} dx$$

Optimal (type 3, 57 leaves, 4 steps):

$$-\frac{1}{c f} g (g \cos [e + f x])^{-2m} \text{Log}[1 - \sin [e + f x]] (a + a \sin [e + f x])^m (c - c \sin [e + f x])^m$$

Result (type 1, 1 leaves):

???

Problem 175: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (g \cos [e + f x])^{5-2m} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^n dx$$

Optimal (type 3, 203 leaves, 3 steps):

$$\frac{8 a^3 (g \cos [e+f x])^{6-2 m} (a+a \sin [e+f x])^{-3+m} (c-c \sin [e+f x])^n}{f g (3-m+n)(4-m+n)(5-m+n)}$$

$$\frac{4 a^2 (g \cos [e+f x])^{6-2 m} (a+a \sin [e+f x])^{-2+m} (c-c \sin [e+f x])^n}{f g (4-m+n)(5-m+n)}$$

$$\frac{a (g \cos [e+f x])^{6-2 m} (a+a \sin [e+f x])^{-1+m} (c-c \sin [e+f x])^n}{f g (5-m+n)}$$

Result (type 3, 1513 leaves):

$$\frac{1}{f} \cos [e+f x]^{-5+2 n} (g \cos [e+f x])^{5-2 m}$$

$$\left(a (1+\sin [e+f x]) \right)^m (c-c \sin [e+f x])^{n-\frac{n(\log [a(1+\sin [e+f x])]+\log [c-c \sin [e+f x]])}{\log [c-c \sin [e+f x]]}}$$

$$\left(\left(e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} (256-41 m+3 m^2+41 n-6 m n+3 n^2) \right) / \right.$$

$$\left(8(-5+m-n)(-4+m-n)(-3+m-n) \right) +$$

$$\left((300-23 m+m^2+23 n-2 m n+n^2) \left(-\frac{1}{16} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \right. \right.$$

$$\left. \left. \cos [e+f x] - \frac{1}{16} e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \sin [e+f x] \right) \right) /$$

$$\left((-5+m-n)(-4+m-n)(-3+m-n) \right) + \left((300-23 m+m^2+23 n-2 m n+n^2) \right.$$

$$\left(\frac{1}{16} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \cos [e+f x] - \right.$$

$$\left. \frac{1}{16} e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \sin [e+f x] \right) \right) /$$

$$\left((-5+m-n)(-4+m-n)(-3+m-n) \right) + \left((-11 m+m^2+11 n-2 m n+n^2) \right.$$

$$\left(\frac{1}{4} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \cos [2(e+f x)] - \right.$$

$$\left. \frac{1}{4} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \sin [2(e+f x)] \right) \right) /$$

$$\left((-5+m-n)(-4+m-n)(-3+m-n) \right) + \left((-11 m+m^2+11 n-2 m n+n^2) \right.$$

$$\left(\frac{1}{4} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \cos [2(e+f x)] + \right.$$

$$\left. \frac{1}{4} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \sin [2(e+f x)] \right) \right) /$$

$$\left((-5+m-n)(-4+m-n)(-3+m-n) \right) + \left((100-53 m+3 m^2+53 n-6 m n+3 n^2) \right.$$

$$\left(-\frac{1}{32} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \cos [3(e+f x)] - \right.$$

$$\left. \frac{1}{32} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \sin [3(e+f x)] \right) \right) /$$

$$\left((-5+m-n)(-4+m-n)(-3+m-n) \right) + \left((100-53 m+3 m^2+53 n-6 m n+3 n^2) \right.$$

$$\left(\frac{1}{32} \int e^{n(-2 \log [\cos [e+f x]]+\log [a(1+\sin [e+f x]])+\log [c-c \sin [e+f x]])} \cos [3(e+f x)] - \right.$$

$$\begin{aligned}
 & \left. \frac{1}{32} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \sin[3(e+fx)] \right) \Bigg/ \\
 & \left((-5+m-n)(-4+m-n)(-3+m-n) + \right. \\
 & \left. \left((m-n) \left(\frac{1}{16} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \cos[4(e+fx)] - \right. \right. \right. \\
 & \left. \left. \frac{1}{16} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \sin[4(e+fx)] \right) \right) \Bigg/ \\
 & \left((-5+m-n)(-4+m-n) + \left((m-n) \left(\frac{1}{16} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \right. \right. \right. \\
 & \left. \left. \cos[4(e+fx)] + \frac{1}{16} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \right. \right. \\
 & \left. \left. \sin[4(e+fx)] \right) \right) \Bigg/ \left((-5+m-n)(-4+m-n) + \frac{1}{-5+m-n} \right. \\
 & \left. \left(-\frac{1}{32} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \cos[5(e+fx)] - \right. \right. \\
 & \left. \left. \frac{1}{32} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \sin[5(e+fx)] \right) + \right. \\
 & \left. \frac{1}{-5+m-n} \left(\frac{1}{32} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \cos[5(e+fx)] - \right. \right. \\
 & \left. \left. \frac{1}{32} e^{n(-2 \operatorname{Log}[\cos[e+fx]] + \operatorname{Log}[a(1+\sin[e+fx])] + \operatorname{Log}[c-c \sin[e+fx]])} \sin[5(e+fx)] \right) \right)
 \end{aligned}$$

Problem 178: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e+fx])^{-1-2m} (a+a \sin[e+fx])^m (c-c \sin[e+fx])^n dx$$

Optimal (type 5, 81 leaves, 4 steps):

$$\frac{1}{2fg(m-n)} (g \cos[e+fx])^{-2m} \operatorname{Hypergeometric2F1}\left[1, -m+n, 1-m+n, \frac{1}{2}(1-\sin[e+fx])\right] \\
 (a+a \sin[e+fx])^m (c-c \sin[e+fx])^n$$

Result (type 1, 1 leaves):

???

Problem 179: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e+fx])^{-3-2m} (a+a \sin[e+fx])^m (c-c \sin[e+fx])^n dx$$

Optimal (type 5, 85 leaves, 4 steps):

$$\frac{1}{4fg^3(1+m-n)} c (g \cos[e+fx])^{-2m} \operatorname{Hypergeometric2F1}\left[2, -1-m+n, -m+n, \frac{1}{2}(1-\sin[e+fx])\right] \\
 (a+a \sin[e+fx])^m (c-c \sin[e+fx])^{-1+n}$$

Result (type 1, 1 leaves):

???

Problem 180: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{-5-2m} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n dx$$

Optimal (type 5, 88 leaves, 4 steps):

$$\frac{1}{8 f g^5 (2 + m - n)}$$

$$c^2 (g \cos[e + f x])^{-2m} \text{Hypergeometric2F1}\left[3, -2 - m + n, -1 - m + n, \frac{1}{2} (1 - \sin[e + f x])\right] \\ (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-2+n}$$

Result (type 1, 1 leaves):

???

Problem 182: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{-1-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{3+n} dx$$

Optimal (type 5, 134 leaves, 4 steps):

$$\frac{1}{f g (m - n)} 2^{3 - \frac{m}{2} + \frac{n}{2}} c^3 (g \cos[e + f x])^{-m-n}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{2} (-4 + m - n), \frac{m - n}{2}, \frac{1}{2} (2 + m - n), \frac{1}{2} (1 + \sin[e + f x])\right] \\ (1 - \sin[e + f x])^{\frac{m-n}{2}} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n$$

Result (type 1, 1 leaves):

???

Problem 183: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{-1-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{2+n} dx$$

Optimal (type 5, 134 leaves, 4 steps):

$$\frac{1}{f g (m - n)} 2^{2 - \frac{m}{2} + \frac{n}{2}} c^2 (g \cos[e + f x])^{-m-n}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{2} (-2 + m - n), \frac{m - n}{2}, \frac{1}{2} (2 + m - n), \frac{1}{2} (1 + \sin[e + f x])\right] \\ (1 - \sin[e + f x])^{\frac{m-n}{2}} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n$$

Result (type 1, 1 leaves):

???

Problem 184: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^{-1-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{1+n} dx$$

Optimal (type 5, 131 leaves, 4 steps):

$$\frac{1}{f g (m-n)} 2^{1-\frac{m}{2}+\frac{n}{2}} c (g \cos[e + f x])^{-m-n} \text{Hypergeometric2F1}\left[\frac{m-n}{2}, \frac{m-n}{2}, \frac{1}{2}(2+m-n), \frac{1}{2}(1+\sin[e + f x])\right] (1 - \sin[e + f x])^{\frac{m-n}{2}} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n$$

Result (type 1, 1 leaves):

???

Problem 187: Result more than twice size of optimal antiderivative.

$$\int (g \cos[e + f x])^{-1-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-2+n} dx$$

Optimal (type 3, 204 leaves, 3 steps):

$$\frac{(g \cos[e + f x])^{-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-2+n}}{f g (4+m-n)} + \frac{2 (g \cos[e + f x])^{-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-1+n}}{c f g (2+m-n) (4+m-n)} + \frac{2 (g \cos[e + f x])^{-m-n} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^n}{c^2 f g (m-n) (2+m-n) (4+m-n)}$$

Result (type 3, 2259 leaves):

$$\left(2^{-2-m+2n} \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{2m} \cos[e + f x] (g \cos[e + f x])^{-1-m-n} \csc\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^4 \left(\cos\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \sin\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{2n} \left(\cos\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \sin\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \sin\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \sin\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{-m-n} \left(\cos\left[\frac{1}{2}(e + f x)\right] - \sin\left[\frac{1}{2}(e + f x)\right]\right)^{-2(-2+n)} (a + a \sin[e + f x])^m (c - c \sin[e + f x])^{-2+n} \left(3 + 4m + m^2 - 4n - 2mn + n^2 + \cos\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] - 2(2+m-n) \sin[e + f x]\right) \left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)^{-5+2n} / \left(f (m-n) (2+m-n) (4+m-n)\right)$$

$$\begin{aligned}
 & \left(-\frac{1}{(m-n)(2+m-n)(4+m-n)} 2^{-2-m+2n} \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{2n} \right. \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \left. \sin\left[\frac{5}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{7}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{-m-n} \\
 & \quad \left(2(2+m-n) \cos[e+fx] - 2 \sin\left[2\left(-e+\frac{\pi}{2}-fx\right)\right] \right) + \frac{1}{(m-n)(2+m-n)(4+m-n)} \\
 & 2^{-2-m+2n} m \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{-1+2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^3 \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{2n} \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \left. \sin\left[\frac{5}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{7}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{-m-n} \\
 & \quad \left(3+4m+m^2-4n-2mn+n^2 + \cos\left[2\left(-e+\frac{\pi}{2}-fx\right)\right] - 2(2+m-n) \sin[e+fx] \right) + \\
 & \frac{1}{(m-n)(2+m-n)(4+m-n)} 2^{-1-m+2n} \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{1+2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^5 \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{2n} \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \left. \sin\left[\frac{5}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{7}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{-m-n} \\
 & \quad \left(3+4m+m^2-4n-2mn+n^2 + \cos\left[2\left(-e+\frac{\pi}{2}-fx\right)\right] - 2(2+m-n) \sin[e+fx] \right) - \\
 & \frac{1}{(m-n)(2+m-n)(4+m-n)} 2^{-1-m+2n} n \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{-1+2n} \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\frac{1}{8} \cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{3}{8} \cos\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) - \right. \\
 & \quad \quad \left. \frac{1}{8} \sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right) \\
 & \quad \left(\cos\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \left(-\sin\left[\frac{1}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{3}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] - \right. \right. \\
 & \quad \quad \left. \left. \sin\left[\frac{5}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] + \sin\left[\frac{7}{8}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \right)^{-m-n} \\
 & \quad \left(3+4m+m^2-4n-2mn+n^2 + \cos\left[2\left(-e+\frac{\pi}{2}-fx\right)\right] - 2(2+m-n) \sin[e+fx] \right) - \\
 & \frac{1}{(m-n)(2+m-n)(4+m-n)} 2^{-2-m+2n} (-m-n) \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^{2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4
 \end{aligned}$$

$$\begin{aligned}
 & \left(\cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right)^{2n} \\
 & \left(\cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \\
 & \quad \left. \left. \sin \left[\frac{5}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{7}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right)^{-1-m-n} \\
 & \left(\cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\frac{1}{8} \cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{3}{8} \cos \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \\
 & \quad \left. \left. \frac{5}{8} \cos \left[\frac{5}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{7}{8} \cos \left[\frac{7}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) - \right. \\
 & \quad \left. \frac{1}{8} \sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \\
 & \quad \left. \left. \sin \left[\frac{5}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{7}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right) \\
 & \left(3 + 4m + m^2 - 4n - 2mn + n^2 + \cos \left[2 \left(-e + \frac{\pi}{2} - f x \right) \right] - 2(2+m-n) \sin \left[e + f x \right] \right) \\
 & \left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] + \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x \right) \right] \right)
 \end{aligned}$$

Problem 188: Result more than twice size of optimal antiderivative.

$$\int (g \cos [e + f x])^{-1-m-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-3+n} dx$$

Optimal (type 3, 290 leaves, 4 steps):

$$\begin{aligned}
 & \frac{(g \cos [e + f x])^{-m-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-3+n}}{f g (6 + m - n)} + \\
 & \frac{3 (g \cos [e + f x])^{-m-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-2+n}}{c f g (4 + m - n) (6 + m - n)} + \\
 & \frac{6 (g \cos [e + f x])^{-m-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-1+n}}{c^2 f g (2 + m - n) (4 + m - n) (6 + m - n)} + \\
 & \frac{6 (g \cos [e + f x])^{-m-n} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^n}{c^3 f g (m - n) (2 + m - n) (4 + m - n) (6 + m - n)}
 \end{aligned}$$

Result (type 3, 2681 leaves):

$$\begin{aligned}
 & - \left(\left(2^{-4-m+2n} \cos \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] \right)^{2m} \cos [e + f x] (g \cos [e + f x])^{-1-m-n} \csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^6 \right. \\
 & \quad \left(\cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right)^{2n} \\
 & \quad \left(\cos \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \left(-\sin \left[\frac{1}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{3}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] - \right. \right. \\
 & \quad \left. \left. \sin \left[\frac{5}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] + \sin \left[\frac{7}{8} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) \right)^{-m-n} \\
 & \left(\cos \left[\frac{1}{2} (e + f x) \right] - \sin \left[\frac{1}{2} (e + f x) \right] \right)^{-2(-3+n)} (a + a \sin [e + f x])^m (c - c \sin [e + f x])^{-3+n}
 \end{aligned}$$

$$\begin{aligned}
 & \left(-30 - 46 m - 18 m^2 - 2 m^3 + 46 n + 36 m n + 6 m^2 n - 18 n^2 - 6 m n^2 + \right. \\
 & \quad \left. 2 n^3 - 6 (3 + m - n) \operatorname{Cos}\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] + 3 \operatorname{Cos}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] + \right. \\
 & \quad \left. 3 (15 + 2 m^2 - 4 m (-3 + n) - 12 n + 2 n^2) \operatorname{Sin}[e + f x] \right) \\
 & \left(\operatorname{Cos}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \operatorname{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] \right)^{-7+2n} / \\
 & \left(f (m - n) (2 + m - n) (4 + m - n) (6 + m - n) \left(\frac{1}{(m - n) (2 + m - n) (4 + m - n) (6 + m - n)} \right. \right. \\
 & \quad \left. \left. 2^{-4-m+2n} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^6 \right. \right. \\
 & \quad \left. \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{2n} \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Sin}\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{-m-n} \\
 & \quad \left(-3 (15 + 2 m^2 - 4 m (-3 + n) - 12 n + 2 n^2) \operatorname{Cos}[e + f x] + 12 (3 + m - n) \operatorname{Sin}\left[\right. \right. \\
 & \quad \left. \left. 2\left(-e + \frac{\pi}{2} - f x\right)\right] - 9 \operatorname{Sin}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] \right) - \frac{1}{(m - n) (2 + m - n) (4 + m - n) (6 + m - n)} \\
 & \quad \left. 2^{-4-m+2n} m \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{-1+2m} \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^5 \right. \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{2n} \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \operatorname{Sin}\left[\right. \right. \\
 & \quad \left. \left. \frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{-m-n} \left(-30 - 46 m - 18 m^2 - 2 m^3 + \right. \\
 & \quad \left. 46 n + 36 m n + 6 m^2 n - 18 n^2 - 6 m n^2 + 2 n^3 - 6 (3 + m - n) \operatorname{Cos}\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] + \right. \\
 & \quad \left. 3 \operatorname{Cos}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] + 3 (15 + 2 m^2 - 4 m (-3 + n) - 12 n + 2 n^2) \operatorname{Sin}[e + f x] \right) - \\
 & \quad \frac{1}{(m - n) (2 + m - n) (4 + m - n) (6 + m - n)} 3 \times 2^{-4-m+2n} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{1+2m} \\
 & \quad \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^7 \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{2n} \\
 & \quad \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \operatorname{Sin}\left[\right. \right. \\
 & \quad \left. \left. \frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right)^{-m-n} \left(-30 - 46 m - 18 m^2 - 2 m^3 + \right. \\
 & \quad \left. 46 n + 36 m n + 6 m^2 n - 18 n^2 - 6 m n^2 + 2 n^3 - 6 (3 + m - n) \operatorname{Cos}\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{3 \operatorname{Cos}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(15 + 2 m^2 - 4 m(-3+n) - 12 n + 2 n^2\right) \operatorname{Sin}\left[e + f x\right]}{(m-n)(2+m-n)(4+m-n)(6+m-n)} 2^{-3-m+2 n} \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2 m} \\
 & \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^6 \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{-1+2 n} \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\frac{1}{8} \operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{8} \operatorname{Cos}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) - \right. \\
 & \left. \frac{1}{8} \operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right) \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \operatorname{Sin}\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{-m-n} \\
 & \left(-30 - 46 m - 18 m^2 - 2 m^3 + 46 n + 36 m n + 6 m^2 n - 18 n^2 - 6 m n^2 + 2 n^3 - 6(3+m-n) \operatorname{Cos}\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] + \right. \\
 & \left. 3 \operatorname{Cos}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(15 + 2 m^2 - 4 m(-3+n) - 12 n + 2 n^2\right) \operatorname{Sin}\left[e + f x\right]\right) \\
 & \frac{1}{(m-n)(2+m-n)(4+m-n)(6+m-n)} 2^{-4-m+2 n} (-m-n) \\
 & \operatorname{Cos}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^{2 m} \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]^6 \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{2 n} \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \\
 & \left. \operatorname{Sin}\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)^{-1-m-n} \\
 & \left(\operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\frac{1}{8} \operatorname{Cos}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{8} \operatorname{Cos}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \\
 & \left. \frac{5}{8} \operatorname{Cos}\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{7}{8} \operatorname{Cos}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) - \right. \\
 & \left. \frac{1}{8} \operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\left(-\operatorname{Sin}\left[\frac{1}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{3}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] - \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{5}{8}\left(-e + \frac{\pi}{2} - f x\right)\right] + \operatorname{Sin}\left[\frac{7}{8}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\left(-30 - 46 m - 18 m^2 - 2 m^3 + \right. \\
 & \left. 46 n + 36 m n + 6 m^2 n - 18 n^2 - 6 m n^2 + 2 n^3 - 6(3+m-n) \operatorname{Cos}\left[2\left(-e + \frac{\pi}{2} - f x\right)\right] + \right. \\
 & \left. 3 \operatorname{Cos}\left[3\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(15 + 2 m^2 - 4 m(-3+n) - 12 n + 2 n^2\right) \operatorname{Sin}\left[e + f x\right]\right) \\
 & \left(\operatorname{Cos}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] + \operatorname{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)
 \end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + d x] \text{Csc}[c + d x]^3 (a + a \text{Sin}[c + d x])^3 dx$$

Optimal (type 3, 65 leaves, 4 steps):

$$-\frac{3 a^3 \text{Csc}[c + d x]}{d} - \frac{3 a^3 \text{Csc}[c + d x]^2}{2 d} - \frac{a^3 \text{Csc}[c + d x]^3}{3 d} + \frac{a^3 \text{Log}[\text{Sin}[c + d x]]}{d}$$

Result (type 3, 146 leaves):

$$a^3 \left(-\frac{19 \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{12 d} - \frac{3 \text{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{8 d} - \frac{\text{Cot}\left[\frac{1}{2}(c + d x)\right] \text{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{24 d} + \frac{\text{Log}[\text{Sin}[c + d x]]}{d} - \frac{3 \text{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{8 d} - \frac{19 \text{Tan}\left[\frac{1}{2}(c + d x)\right]}{12 d} - \frac{\text{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \text{Tan}\left[\frac{1}{2}(c + d x)\right]}{24 d} \right)$$

Problem 230: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x] \text{Csc}[c + d x]^2}{a + a \text{Sin}[c + d x]} dx$$

Optimal (type 3, 63 leaves, 4 steps):

$$\frac{\text{Csc}[c + d x]}{a d} - \frac{\text{Csc}[c + d x]^2}{2 a d} + \frac{\text{Log}[\text{Sin}[c + d x]]}{a d} - \frac{\text{Log}[1 + \text{Sin}[c + d x]]}{a d}$$

Result (type 3, 127 leaves):

$$\left(\left(\text{Csc}\left[\frac{1}{2}(c + d x)\right] + \text{Sec}\left[\frac{1}{2}(c + d x)\right] \right)^2 \left(-1 - 2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \text{Cos}[2(c + d x)] \left(2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}[\text{Sin}[c + d x]] \right) + \text{Log}[\text{Sin}[c + d x]] + 2 \text{Sin}[c + d x] \right) / (8 a d (1 + \text{Sin}[c + d x]))$$

Problem 235: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cos}[c + d x] \text{Sin}[c + d x]}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 37 leaves, 4 steps):

$$\frac{\text{Log}[1 + \text{Sin}[c + d x]]}{a^2 d} + \frac{1}{d (a^2 + a^2 \text{Sin}[c + d x])}$$

Result (type 3, 88 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right. \\ \left. \left(1 + 2 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) \right) / \left(d \right. \\ \left. (a + a \sin [c + d x])^2 \right)$$

Problem 236: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x]}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 52 leaves, 3 steps):

$$\frac{\operatorname{Log}[\sin [c + d x]]}{a^2 d} - \frac{\operatorname{Log}[1 + \sin [c + d x]]}{a^2 d} + \frac{1}{d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 112 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right. \\ \left(1 - 2 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + \operatorname{Log}[\sin [c + d x]] + \right. \\ \left. \left(-2 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + \operatorname{Log}[\sin [c + d x]] \right) \sin [c + d x] \right) \right) / \\ (a^2 d (1 + \sin [c + d x])^2)$$

Problem 238: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 85 leaves, 4 steps):

$$\frac{2 \operatorname{Csc}[c + d x]}{a^2 d} - \frac{\operatorname{Csc}[c + d x]^2}{2 a^2 d} + \frac{3 \operatorname{Log}[\sin [c + d x]]}{a^2 d} - \\ \frac{3 \operatorname{Log}[1 + \sin [c + d x]]}{a^2 d} + \frac{1}{d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 214 leaves):

$$\frac{1}{16 a^2 d (1 + \sin [c + d x])^2} \left(\csc \left[\frac{1}{2} (c + d x) \right] + \sec \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(4 - 12 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \right) + 6 \cos [2 (c + d x)] \left(-1 + 2 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] - \log [\sin [c + d x]] \right) + 6 \log [\sin [c + d x]] + \left(6 - 18 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + 9 \log [\sin [c + d x]] \right) \sin [c + d x] + 6 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \sin [3 (c + d x)] - 3 \log [\sin [c + d x]] \sin [3 (c + d x)] \right)$$

Problem 239: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x] \csc [c + d x]^3}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 101 leaves, 4 steps):

$$-\frac{3 \csc [c + d x]}{a^2 d} + \frac{\csc [c + d x]^2}{a^2 d} - \frac{\csc [c + d x]^3}{3 a^2 d} - \frac{4 \log [\sin [c + d x]]}{a^2 d} + \frac{4 \log [1 + \sin [c + d x]]}{a^2 d} - \frac{1}{d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 298 leaves):

$$-\frac{1}{48 a^2 d (1 + \sin [c + d x])^2} \csc \left[\frac{1}{2} (c + d x) \right] \sec \left[\frac{1}{2} (c + d x) \right] \left(\csc \left[\frac{1}{2} (c + d x) \right] + \sec \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(8 - 18 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \right) + 6 \cos [2 (c + d x)] \left(-1 + 4 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] - 2 \log [\sin [c + d x]] \right) + 9 \log [\sin [c + d x]] + \cos [4 (c + d x)] \left(-6 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + 3 \log [\sin [c + d x]] \right) + 14 \sin [c + d x] - 36 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \sin [c + d x] + 18 \log [\sin [c + d x]] \sin [c + d x] - 6 \sin [3 (c + d x)] + 12 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \sin [3 (c + d x)] - 6 \log [\sin [c + d x]] \sin [3 (c + d x)] \right)$$

Problem 240: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x] \sin [c + d x]^5}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 111 leaves, 4 steps):

$$-\frac{10 \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{a^3 d} + \frac{6 \operatorname{Sin}[c + d x]}{a^3 d} - \frac{3 \operatorname{Sin}[c + d x]^2}{2 a^3 d} + \frac{\operatorname{Sin}[c + d x]^3}{3 a^3 d} + \frac{1}{2 a d (a + a \operatorname{Sin}[c + d x])^2} - \frac{5}{d (a^3 + a^3 \operatorname{Sin}[c + d x])}$$

Result (type 3, 450 leaves):

$$\frac{1}{32} \left(\frac{24 \operatorname{Cos}[2 c] \operatorname{Cos}[2 d x]}{a^3 d} - \frac{448 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{a^3 d} + \right. \\ \left. x \left(\frac{224 \operatorname{Cos}\left[\frac{c}{2}\right]}{a^3 \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)} - \frac{224 \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)}{a^3 \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)} - \frac{224 \operatorname{Sin}\left[\frac{c}{2}\right]}{a^3 \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)} \right) + \right. \\ \left. \frac{168 \operatorname{Cos}[d x] \operatorname{Sin}[c]}{a^3 d} - \frac{8 \operatorname{Cos}[3 d x] \operatorname{Sin}[3 c]}{3 a^3 d} + \frac{168 \operatorname{Cos}[c] \operatorname{Sin}[d x]}{a^3 d} - \right. \\ \left. \frac{24 \operatorname{Sin}[2 c] \operatorname{Sin}[2 d x]}{a^3 d} - \frac{8 \operatorname{Cos}[3 c] \operatorname{Sin}[3 d x]}{3 a^3 d} + \right. \\ \left. \frac{3}{a^3 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right)^4} - \frac{70}{a^3 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right)^2} \right) - \frac{1}{4 a^3 d} \\ \left(24 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 4 \operatorname{Cos}[d x] \operatorname{Sin}[c] - 4 \operatorname{Cos}[c] \operatorname{Sin}[d x] - \right. \\ \left. \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{10}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} \right) + \\ \frac{5(-1 - 2 \operatorname{Sin}[c + d x])}{32 a^3 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4}$$

Problem 246: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]}{(a + a \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 90 leaves, 4 steps):

$$-\frac{\operatorname{Csc}[c + d x]}{a^3 d} - \frac{3 \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^3 d} + \frac{3 \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{a^3 d} - \frac{1}{2 a d (a + a \operatorname{Sin}[c + d x])^2} - \frac{2}{d (a^3 + a^3 \operatorname{Sin}[c + d x])}$$

Result (type 3, 218 leaves):

$$\frac{1}{2 d (a + a \operatorname{Sin}[c + d x])^3} \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \left(-1 - 4 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right)^2 - \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 + 12 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 - 6 \operatorname{Log}\left[\operatorname{Sin}[c + d x]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 - \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right)$$

Problem 247: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2}{(a + a \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 108 leaves, 4 steps):

$$\frac{3 \operatorname{Csc}[c + d x]}{a^3 d} - \frac{\operatorname{Csc}[c + d x]^2}{2 a^3 d} + \frac{6 \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^3 d} - \frac{6 \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{a^3 d} + \frac{1}{2 a d (a + a \operatorname{Sin}[c + d x])^2} + \frac{3}{d (a^3 + a^3 \operatorname{Sin}[c + d x])}$$

Result (type 3, 275 leaves):

$$\frac{1}{8 a^3 d (1 + \operatorname{Sin}[c + d x])^3} \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \left(4 - \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right)^4 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]^2 + 24 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 + 12 \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 - 96 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 + 48 \operatorname{Log}\left[\operatorname{Sin}[c + d x]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 + 12 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right)$$

Problem 248: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3}{(a + a \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 126 leaves, 4 steps):

$$-\frac{6 \operatorname{Csc}[c+dx]}{a^3 d} + \frac{3 \operatorname{Csc}[c+dx]^2}{2 a^3 d} - \frac{\operatorname{Csc}[c+dx]^3}{3 a^3 d} - \frac{10 \operatorname{Log}[\operatorname{Sin}[c+dx]]}{a^3 d} + \frac{10 \operatorname{Log}[1+\operatorname{Sin}[c+dx]]}{a^3 d} - \frac{1}{2 a d (a+a \operatorname{Sin}[c+dx])^2} - \frac{4}{d (a^3+a^3 \operatorname{Sin}[c+dx])}$$

Result (type 3, 335 leaves):

$$\frac{1}{24 a^3 d (1+\operatorname{Sin}[c+dx])^3} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \left(-12 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right)^4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 9 \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right)^4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]^2 - 96 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 - 74 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 + 480 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 - 240 \operatorname{Log}[\operatorname{Sin}[c+dx]] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 - 74 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 9 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)^4 - \frac{1}{2} \operatorname{Sin}[c+dx] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)$$

Problem 255: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{(a+a \operatorname{Sin}[c+dx])^4} dx$$

Optimal (type 3, 111 leaves, 4 steps):

$$-\frac{\operatorname{Csc}[c+dx]}{a^4 d} - \frac{4 \operatorname{Log}[\operatorname{Sin}[c+dx]]}{a^4 d} + \frac{4 \operatorname{Log}[1+\operatorname{Sin}[c+dx]]}{a^4 d} - \frac{1}{3 a d (a+a \operatorname{Sin}[c+dx])^3} - \frac{1}{d (a^2+a^2 \operatorname{Sin}[c+dx])^2} - \frac{3}{d (a^4+a^4 \operatorname{Sin}[c+dx])}$$

Result (type 3, 243 leaves):

$$\frac{1}{6 d (a + a \sin [c + d x])^4} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2$$

$$\left(-2 - 6 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)^2 - 18 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 -$$

$$3 \cot \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 +$$

$$48 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 -$$

$$24 \log [\sin [c + d x]] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 -$$

$$3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 \tan \left[\frac{1}{2} (c + d x) \right]$$

Problem 256: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x] \operatorname{Csc} [c + d x]^2}{(a + a \sin [c + d x])^4} dx$$

Optimal (type 3, 131 leaves, 4 steps):

$$\frac{4 \operatorname{Csc} [c + d x]}{a^4 d} - \frac{\operatorname{Csc} [c + d x]^2}{2 a^4 d} + \frac{10 \log [\sin [c + d x]]}{a^4 d} - \frac{10 \log [1 + \sin [c + d x]]}{a^4 d} +$$

$$\frac{1}{3 a d (a + a \sin [c + d x])^3} + \frac{1}{2 d (a^2 + a^2 \sin [c + d x])^2} + \frac{1}{d (a^4 + a^4 \sin [c + d x])}$$

Result (type 3, 300 leaves):

$$\frac{1}{24 a^4 d (1 + \sin [c + d x])^4}$$

$$\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(8 - 3 \left(1 + \cot \left[\frac{1}{2} (c + d x) \right] \right)^6 \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 +$$

$$36 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 144 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 +$$

$$48 \cot \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 -$$

$$480 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 +$$

$$240 \log [\sin [c + d x]] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 +$$

$$48 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 \tan \left[\frac{1}{2} (c + d x) \right] -$$

$$3 \cos \left[\frac{1}{2} (c + d x) \right]^4 \left(1 + \tan \left[\frac{1}{2} (c + d x) \right] \right)^6$$

Problem 257: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x] \sqrt{a + a \sin [c + d x]} dx$$

Optimal (type 3, 51 leaves, 4 steps):

$$-\frac{2 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{a}}\right]}{d} + \frac{2 \sqrt{a+a \sin [c+d x]}}{d}$$

Result (type 3, 118 leaves):

$$\left(\left(2 \cos \left[\frac{1}{2} (c + d x) \right] + \log \left[1 - \cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] - \right. \right. \\ \left. \log \left[1 + \cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + 2 \sin \left[\frac{1}{2} (c + d x) \right] \right) \\ \left. \sqrt{a (1 + \sin [c + d x])} \right) / \left(d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)$$

Problem 258: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c + d x] \sin [c + d x]^n (a + a \sin [c + d x])^4 dx$$

Optimal (type 3, 114 leaves, 3 steps):

$$\frac{a^4 \sin [c + d x]^{1+n}}{d (1+n)} + \frac{4 a^4 \sin [c + d x]^{2+n}}{d (2+n)} + \frac{6 a^4 \sin [c + d x]^{3+n}}{d (3+n)} + \frac{4 a^4 \sin [c + d x]^{4+n}}{d (4+n)} + \frac{a^4 \sin [c + d x]^{5+n}}{d (5+n)}$$

Result (type 3, 457 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} \sin [c + d x]^n (a + a \sin [c + d x])^4$$

$$\left(\frac{22 + 7 n}{2 (2 + n) (4 + n)} + \frac{(315 + 300 n + 49 n^2) \left(-\frac{1}{16} \operatorname{Im} \cos [c + d x] + \frac{1}{16} \operatorname{Im} \sin [c + d x] \right)}{(1 + n) (3 + n) (5 + n)} + \right.$$

$$\frac{(315 + 300 n + 49 n^2) \left(\frac{1}{16} \operatorname{Im} \cos [c + d x] + \frac{1}{16} \operatorname{Im} \sin [c + d x] \right)}{(1 + n) (3 + n) (5 + n)} +$$

$$\frac{(3 + n) (-2 \operatorname{Cos} [2 (c + d x)] - 2 \operatorname{Im} \sin [2 (c + d x)])}{(2 + n) (4 + n)} +$$

$$\frac{(3 + n) (-2 \operatorname{Cos} [2 (c + d x)] + 2 \operatorname{Im} \sin [2 (c + d x)])}{(2 + n) (4 + n)} +$$

$$\frac{(135 + 29 n) \left(-\frac{1}{32} \operatorname{Im} \cos [3 (c + d x)] - \frac{1}{32} \operatorname{Im} \sin [3 (c + d x)] \right)}{(3 + n) (5 + n)} +$$

$$\frac{(135 + 29 n) \left(\frac{1}{32} \operatorname{Im} \cos [3 (c + d x)] - \frac{1}{32} \operatorname{Im} \sin [3 (c + d x)] \right)}{(3 + n) (5 + n)} +$$

$$\frac{\frac{1}{4} \operatorname{Cos} [4 (c + d x)] - \frac{1}{4} \operatorname{Im} \sin [4 (c + d x)]}{4 + n} + \frac{\frac{1}{4} \operatorname{Cos} [4 (c + d x)] + \frac{1}{4} \operatorname{Im} \sin [4 (c + d x)]}{4 + n} +$$

$$\left. \frac{-\frac{1}{32} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{32} \operatorname{Im} \sin [5 (c + d x)]}{5 + n} + \frac{\frac{1}{32} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{32} \operatorname{Im} \sin [5 (c + d x)]}{5 + n} \right)$$

Problem 259: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c + d x] \sin [c + d x]^n (a + a \sin [c + d x])^3 dx$$

Optimal (type 3, 91 leaves, 3 steps):

$$\frac{a^3 \sin [c + d x]^{1+n}}{d (1 + n)} + \frac{3 a^3 \sin [c + d x]^{2+n}}{d (2 + n)} + \frac{3 a^3 \sin [c + d x]^{3+n}}{d (3 + n)} + \frac{a^3 \sin [c + d x]^{4+n}}{d (4 + n)}$$

Result (type 3, 363 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} \sin [c + d x]^n (a + a \sin [c + d x])^3$$

$$\left(\frac{3 (18 + 5 n)}{8 (2 + n) (4 + n)} + \frac{(21 + 13 n) \left(-\frac{1}{8} i \cos [c + d x] + \frac{1}{8} \sin [c + d x] \right)}{(1 + n) (3 + n)} + \right.$$

$$\frac{(21 + 13 n) \left(\frac{1}{8} i \cos [c + d x] + \frac{1}{8} \sin [c + d x] \right)}{(1 + n) (3 + n)} +$$

$$\frac{(-7 - 2 n) \left(\frac{1}{2} \cos [2 (c + d x)] - \frac{1}{2} i \sin [2 (c + d x)] \right)}{(2 + n) (4 + n)} +$$

$$\frac{(-7 - 2 n) \left(\frac{1}{2} \cos [2 (c + d x)] + \frac{1}{2} i \sin [2 (c + d x)] \right)}{(2 + n) (4 + n)} +$$

$$\frac{-\frac{3}{8} i \cos [3 (c + d x)] - \frac{3}{8} \sin [3 (c + d x)]}{3 + n} + \frac{\frac{3}{8} i \cos [3 (c + d x)] - \frac{3}{8} \sin [3 (c + d x)]}{3 + n} +$$

$$\left. \frac{\frac{1}{16} \cos [4 (c + d x)] - \frac{1}{16} i \sin [4 (c + d x)]}{4 + n} + \frac{\frac{1}{16} \cos [4 (c + d x)] + \frac{1}{16} i \sin [4 (c + d x)]}{4 + n} \right)$$

Problem 262: Unable to integrate problem.

$$\int \frac{\cos [c + d x] \sin [c + d x]^n}{a + a \sin [c + d x]} dx$$

Optimal (type 5, 38 leaves, 2 steps):

$$\frac{\text{Hypergeometric2F1}[1, 1 + n, 2 + n, -\sin [c + d x]] \sin [c + d x]^{1+n}}{a d (1 + n)}$$

Result (type 8, 29 leaves):

$$\int \frac{\cos [c + d x] \sin [c + d x]^n}{a + a \sin [c + d x]} dx$$

Problem 263: Unable to integrate problem.

$$\int \frac{\cos [c + d x] \sin [c + d x]^n}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 5, 38 leaves, 2 steps):

$$\frac{\text{Hypergeometric2F1}[2, 1 + n, 2 + n, -\sin [c + d x]] \sin [c + d x]^{1+n}}{a^2 d (1 + n)}$$

Result (type 8, 29 leaves):

$$\int \frac{\cos [c + d x] \sin [c + d x]^n}{(a + a \sin [c + d x])^2} dx$$

Problem 264: Unable to integrate problem.

$$\int \frac{\cos [c+d x] \sin [c+d x]^n}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 5, 38 leaves, 2 steps):

$$\frac{\text{Hypergeometric2F1}[3, 1+n, 2+n, -\sin [c+d x]] \sin [c+d x]^{1+n}}{a^3 d (1+n)}$$

Result (type 8, 29 leaves):

$$\int \frac{\cos [c+d x] \sin [c+d x]^n}{(a+a \sin [c+d x])^3} dx$$

Problem 265: Unable to integrate problem.

$$\int \frac{\cos [c+d x] \sin [c+d x]^n}{(a+a \sin [c+d x])^4} dx$$

Optimal (type 5, 38 leaves, 2 steps):

$$\frac{\text{Hypergeometric2F1}[4, 1+n, 2+n, -\sin [c+d x]] \sin [c+d x]^{1+n}}{a^4 d (1+n)}$$

Result (type 8, 29 leaves):

$$\int \frac{\cos [c+d x] \sin [c+d x]^n}{(a+a \sin [c+d x])^4} dx$$

Problem 282: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^2 \csc [c+d x]^3 (a+a \sin [c+d x])^2 dx$$

Optimal (type 3, 82 leaves, 9 steps):

$$\frac{5 a^2 \text{ArcTanh}[\cos [c+d x]]}{8 d} - \frac{2 a^2 \cot [c+d x]^3}{3 d} - \frac{3 a^2 \cot [c+d x] \csc [c+d x]}{8 d} - \frac{a^2 \cot [c+d x] \csc [c+d x]^3}{4 d}$$

Result (type 3, 209 leaves):

$$a^2 \left(\frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{3d} - \frac{3 \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{32d} - \frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{12d} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64d} + \right. \\ \left. \frac{5 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} - \frac{5 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{3 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{32d} + \right. \\ \left. \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64d} - \frac{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{3d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{12d} \right)$$

Problem 292: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c+dx]^2 \text{Csc}[c+dx]^4 (a+a \text{Sin}[c+dx])^3 dx$$

Optimal (type 3, 100 leaves, 12 steps):

$$\frac{7 a^3 \text{ArcTanh}[\text{Cos}[c+dx]]}{8d} - \frac{4 a^3 \text{Cot}[c+dx]^3}{3d} - \frac{a^3 \text{Cot}[c+dx]^5}{5d} - \frac{a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]}{8d} - \frac{3 a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]^3}{4d}$$

Result (type 3, 267 leaves):

$$a^3 \left(\frac{17 \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{30d} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{32d} - \frac{59 \text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{480d} - \right. \\ \left. \frac{3 \text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64d} - \frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{160d} + \frac{7 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} - \right. \\ \left. \frac{7 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{32d} + \frac{3 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64d} - \frac{17 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{30d} + \right. \\ \left. \frac{59 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{480d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{160d} \right)$$

Problem 293: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c+dx]^2 \text{Csc}[c+dx]^5 (a+a \text{Sin}[c+dx])^3 dx$$

Optimal (type 3, 124 leaves, 14 steps):

$$\frac{7 a^3 \text{ArcTanh}[\text{Cos}[c+dx]]}{16d} - \frac{4 a^3 \text{Cot}[c+dx]^3}{3d} - \frac{3 a^3 \text{Cot}[c+dx]^5}{5d} + \frac{7 a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]}{16d} - \frac{17 a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]^3}{24d} - \frac{a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]^5}{6d}$$

Result (type 3, 252 leaves):

$$\frac{1}{1920 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} a^3 \left(\csc \left[\frac{1}{2} (c + d x) \right]^6 (18 + 5 \csc [c + d x]) + \csc \left[\frac{1}{2} (c + d x) \right]^4 (34 + 90 \csc [c + d x]) - 2 \csc \left[\frac{1}{2} (c + d x) \right]^2 (176 + 105 \csc [c + d x]) - 840 \csc [c + d x] \left(\log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \right) + (97 + 159 \cos [c + d x] + 44 \cos [2 (c + d x)]) \sec \left[\frac{1}{2} (c + d x) \right]^6 + 840 \csc [c + d x]^3 \sin \left[\frac{1}{2} (c + d x) \right]^2 - 1440 \csc [c + d x]^5 \sin \left[\frac{1}{2} (c + d x) \right]^4 - 320 \csc [c + d x]^7 \sin \left[\frac{1}{2} (c + d x) \right]^6 \right) \sin [c + d x] (1 + \sin [c + d x])^3$$

Problem 297: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^2 \sin [c + d x]^4}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 104 leaves, 6 steps):

$$\frac{3 x}{8 a} + \frac{\cos [c + d x]}{a d} - \frac{2 \cos [c + d x]^3}{3 a d} + \frac{\cos [c + d x]^5}{5 a d} - \frac{3 \cos [c + d x] \sin [c + d x]}{8 a d} - \frac{\cos [c + d x] \sin [c + d x]^3}{4 a d}$$

Result (type 3, 281 leaves):

$$\frac{1}{480} \left(\frac{180 x}{a} + \frac{300 \cos [c] \cos [d x]}{a d} - \frac{50 \cos [3 c] \cos [3 d x]}{a d} + \frac{6 \cos [5 c] \cos [5 d x]}{a d} - \frac{120 \cos [2 d x] \sin [2 c]}{a d} + \frac{15 \cos [4 d x] \sin [4 c]}{a d} - \frac{300 \sin [c] \sin [d x]}{a d} - \frac{120 \cos [2 c] \sin [2 d x]}{a d} + \frac{50 \sin [3 c] \sin [3 d x]}{a d} + \frac{15 \cos [4 c] \sin [4 d x]}{a d} - \frac{6 \sin [5 c] \sin [5 d x]}{a d} - \frac{60 \sin \left[\frac{d x}{2} \right]}{a d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)} + \frac{30 \sin [c + d x]}{a d (1 + \sin [c + d x])} + \frac{60 \sin \left[\frac{1}{2} (c + d x) \right]^2}{d (a + a \sin [c + d x])} \right)$$

Problem 298: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^2 \sin [c + d x]^3}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 87 leaves, 6 steps):

$$-\frac{3x}{8a} - \frac{\cos[c+dx]}{ad} + \frac{\cos[c+dx]^3}{3ad} + \frac{3\cos[c+dx]\sin[c+dx]}{8ad} + \frac{\cos[c+dx]\sin[c+dx]^3}{4ad}$$

Result (type 3, 271 leaves):

$$\frac{1}{192ad \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(24(c-3dx)\cos\left[\frac{c}{2}\right] - 72\cos\left[\frac{c}{2}+dx\right] - 72\cos\left[\frac{3c}{2}+dx\right] + 24\cos\left[\frac{3c}{2}+2dx\right] - 24\cos\left[\frac{5c}{2}+2dx\right] + 8\cos\left[\frac{5c}{2}+3dx\right] + 8\cos\left[\frac{7c}{2}+3dx\right] - 3\cos\left[\frac{7c}{2}+4dx\right] + 3\cos\left[\frac{9c}{2}+4dx\right] - 48\sin\left[\frac{c}{2}\right] + 24c\sin\left[\frac{c}{2}\right] - 72dx\sin\left[\frac{c}{2}\right] + 72\sin\left[\frac{c}{2}+dx\right] - 72\sin\left[\frac{3c}{2}+dx\right] + 24\sin\left[\frac{3c}{2}+2dx\right] + 24\sin\left[\frac{5c}{2}+2dx\right] - 8\sin\left[\frac{5c}{2}+3dx\right] + 8\sin\left[\frac{7c}{2}+3dx\right] - 3\sin\left[\frac{7c}{2}+4dx\right] - 3\sin\left[\frac{9c}{2}+4dx\right] \right)$$

Problem 300: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^2 \sin[c+dx]}{a+a\sin[c+dx]} dx$$

Optimal (type 3, 45 leaves, 4 steps):

$$-\frac{x}{2a} - \frac{\cos[c+dx]}{ad} + \frac{\cos[c+dx]\sin[c+dx]}{2ad}$$

Result (type 3, 161 leaves):

$$\left(2(c-2dx)\cos\left[\frac{c}{2}\right] - 4\cos\left[\frac{c}{2}+dx\right] - 4\cos\left[\frac{3c}{2}+dx\right] + \cos\left[\frac{3c}{2}+2dx\right] - \cos\left[\frac{5c}{2}+2dx\right] - 4\sin\left[\frac{c}{2}\right] + 2c\sin\left[\frac{c}{2}\right] - 4dx\sin\left[\frac{c}{2}\right] + 4\sin\left[\frac{c}{2}+dx\right] - 4\sin\left[\frac{3c}{2}+dx\right] + \sin\left[\frac{3c}{2}+2dx\right] + \sin\left[\frac{5c}{2}+2dx\right] \right) / \left(8ad \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right)$$

Problem 302: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot[c+dx]^2}{a+a\sin[c+dx]} dx$$

Optimal (type 3, 29 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\cos[c+dx]]}{ad} - \frac{\cot[c+dx]}{ad}$$

Result (type 3, 69 leaves):

$$-\frac{1}{2ad} \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(\cos[c+dx] + \left(-\operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right]\right) \sin[c+dx]\right)$$

Problem 308: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^2 \sin[c+dx]^3}{(a+a\sin[c+dx])^2} dx$$

Optimal (type 3, 83 leaves, 9 steps):

$$\frac{3x}{a^2} + \frac{3\cos[c+dx]}{a^2d} - \frac{\cos[c+dx]^3}{3a^2d} - \frac{\cos[c+dx]\sin[c+dx]}{a^2d} + \frac{2\cos[c+dx]}{a^2d(1+\sin[c+dx])}$$

Result (type 3, 183 leaves):

$$\left((2+72dx) \cos\left[\frac{dx}{2}\right] + 31 \cos\left[c+\frac{dx}{2}\right] + 27 \cos\left[c+\frac{3dx}{2}\right] + 5 \cos\left[3c+\frac{5dx}{2}\right] - \cos\left[3c+\frac{7dx}{2}\right] - 131 \sin\left[\frac{dx}{2}\right] + 2 \sin\left[c+\frac{dx}{2}\right] + 72dx \sin\left[c+\frac{dx}{2}\right] + 27 \sin\left[2c+\frac{3dx}{2}\right] - 5 \sin\left[2c+\frac{5dx}{2}\right] - \sin\left[4c+\frac{7dx}{2}\right] \right) / \left(24a^2d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right)$$

Problem 310: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^2 \sin[c+dx]}{(a+a\sin[c+dx])^2} dx$$

Optimal (type 3, 47 leaves, 3 steps):

$$\frac{2x}{a^2} + \frac{\cos[c+dx]}{a^2d} + \frac{2\cos[c+dx]}{d(a^2+a^2\sin[c+dx])}$$

Result (type 3, 129 leaves):

$$\left((1+12dx) \cos\left[\frac{dx}{2}\right] + 2 \cos\left[c+\frac{dx}{2}\right] + 3 \cos\left[c+\frac{3dx}{2}\right] - 28 \sin\left[\frac{dx}{2}\right] + \sin\left[c+\frac{dx}{2}\right] + 12dx \sin\left[c+\frac{dx}{2}\right] + 3 \sin\left[2c+\frac{3dx}{2}\right] \right) / \left(6a^2d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right)$$

Problem 311: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx] \operatorname{Cot}[c+dx]}{(a+a\sin[c+dx])^2} dx$$

Optimal (type 3, 40 leaves, 5 steps):

$$-\frac{\text{ArcTanh}[\text{Cos}[c + d x]]}{a^2 d} + \frac{2 \text{Cos}[c + d x]}{a^2 d (1 + \text{Sin}[c + d x])}$$

Result (type 3, 115 leaves):

$$-\left(\left(\left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right. \right. \\ \left. \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] \left(\text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right) + \right. \\ \left. \left(4 + \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right. \\ \left. \left. \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \left(a^2 d (1 + \text{Sin}[c + d x])^2 \right)$$

Problem 312: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^2}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 54 leaves, 7 steps):

$$\frac{2 \text{ArcTanh}[\text{Cos}[c + d x]]}{a^2 d} - \frac{\text{Cot}[c + d x]}{a^2 d} - \frac{2 \text{Cot}[c + d x]}{a^2 d (1 + \text{Csc}[c + d x])}$$

Result (type 3, 216 leaves):

$$-\frac{1}{4 a^2 d (1 + \text{Sin}[c + d x])^2} \text{Csc}\left[\frac{1}{2}(c + d x)\right] \text{Sec}\left[\frac{1}{2}(c + d x)\right] \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \\ \left(\text{Cos}\left[\frac{3}{2}(c + d x)\right] \left(5 + 2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - 2 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\ \left. \text{Cos}\left[\frac{1}{2}(c + d x)\right] \left(-3 - 2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 2 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right) + \\ 2 \left(-2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 2 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \\ \text{Cos}[c + d x] \left(1 - 2 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 2 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \text{Sin}\left[\frac{1}{2}(c + d x)\right]$$

Problem 313: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^2 \text{Csc}[c + d x]}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 78 leaves, 9 steps):

$$-\frac{5 \text{ArcTanh}[\text{Cos}[c + d x]]}{2 a^2 d} + \frac{2 \text{Cot}[c + d x]}{a^2 d} - \frac{\text{Cot}[c + d x] \text{Csc}[c + d x]}{2 a^2 d} + \frac{2 \text{Cos}[c + d x]}{a^2 d (1 + \text{Sin}[c + d x])}$$

Result (type 3, 364 leaves):

$$\begin{aligned}
 & - \frac{4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3}{d (a+a \operatorname{Sin}[c+dx])^2} + \\
 & \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{d (a+a \operatorname{Sin}[c+dx])^2} - \\
 & \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{8 d (a+a \operatorname{Sin}[c+dx])^2} - \\
 & \frac{5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{2 d (a+a \operatorname{Sin}[c+dx])^2} + \\
 & \frac{5 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{2 d (a+a \operatorname{Sin}[c+dx])^2} + \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{8 d (a+a \operatorname{Sin}[c+dx])^2} - \\
 & \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{d (a+a \operatorname{Sin}[c+dx])^2}
 \end{aligned}$$

Problem 314: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx]^2}{(a+a \operatorname{Sin}[c+dx])^2} dx$$

Optimal (type 3, 91 leaves, 11 steps):

$$\frac{3 \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{a^2 d} - \frac{3 \operatorname{Cot}[c+dx]}{a^2 d} - \frac{\operatorname{Cot}[c+dx]^3}{3 a^2 d} + \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{a^2 d} - \frac{2 \operatorname{Cos}[c+dx]}{a^2 d (1+\operatorname{Sin}[c+dx])}$$

Result (type 3, 472 leaves):

$$\frac{1}{192 a^2 d (1 + \sin [c + d x])^2} \left(\operatorname{Csc} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right] \right)^3 \left(-10 \operatorname{Cos} \left[\frac{5}{2} (c + d x) \right] + 20 \operatorname{Cos} \left[\frac{7}{2} (c + d x) \right] - \right. \\
 9 \operatorname{Cos} \left[\frac{5}{2} (c + d x) \right] \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] + 9 \operatorname{Cos} \left[\frac{7}{2} (c + d x) \right] \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] + \\
 3 \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \left(8 + 9 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] - 9 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \right) - \\
 3 \operatorname{Cos} \left[\frac{3}{2} (c + d x) \right] \left(14 + 9 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] - 9 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \right) + \\
 9 \operatorname{Cos} \left[\frac{5}{2} (c + d x) \right] \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - 9 \operatorname{Cos} \left[\frac{7}{2} (c + d x) \right] \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \\
 12 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] + 27 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] - \\
 27 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] - 6 \operatorname{Sin} \left[\frac{3}{2} (c + d x) \right] + \\
 27 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{3}{2} (c + d x) \right] - 27 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{3}{2} (c + d x) \right] - \\
 2 \operatorname{Sin} \left[\frac{5}{2} (c + d x) \right] - 9 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{5}{2} (c + d x) \right] + \\
 9 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{5}{2} (c + d x) \right] + 8 \operatorname{Sin} \left[\frac{7}{2} (c + d x) \right] - \\
 9 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{7}{2} (c + d x) \right] + 9 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} \left[\frac{7}{2} (c + d x) \right] \left. \right)$$

Problem 315: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos} [c + d x]^2 \operatorname{Sin} [c + d x]^3}{(a + a \operatorname{Sin} [c + d x])^3} dx$$

Optimal (type 3, 97 leaves, 9 steps):

$$\frac{11 x}{2 a^3} - \frac{3 \operatorname{Cos} [c + d x]}{a^3 d} + \frac{\operatorname{Cos} [c + d x] \operatorname{Sin} [c + d x]}{2 a^3 d} + \\
\frac{2 \operatorname{Cos} [c + d x]}{3 a^3 d (1 + \operatorname{Sin} [c + d x])^2} - \frac{19 \operatorname{Cos} [c + d x]}{3 a^3 d (1 + \operatorname{Sin} [c + d x])}$$

Result (type 3, 235 leaves):

$$\frac{1}{240 a^3 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} \left((9 - 1980 d x) \cos \left[\frac{d x}{2} \right] + 1326 \cos \left[c + \frac{d x}{2} \right] - 2012 \cos \left[c + \frac{3 d x}{2} \right] - 3 \cos \left[2 c + \frac{3 d x}{2} \right] + 660 d x \cos \left[2 c + \frac{3 d x}{2} \right] + 135 \cos \left[3 c + \frac{5 d x}{2} \right] - 15 \cos \left[3 c + \frac{7 d x}{2} \right] + 3216 \sin \left[\frac{d x}{2} \right] + 9 \sin \left[c + \frac{d x}{2} \right] - 1980 d x \sin \left[c + \frac{d x}{2} \right] + 3 \sin \left[c + \frac{3 d x}{2} \right] - 660 d x \sin \left[c + \frac{3 d x}{2} \right] - 498 \sin \left[2 c + \frac{3 d x}{2} \right] - 135 \sin \left[2 c + \frac{5 d x}{2} \right] - 15 \sin \left[4 c + \frac{7 d x}{2} \right] \right)$$

Problem 317: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^2 \sin [c + d x]}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 61 leaves, 3 steps):

$$-\frac{x}{a^3} - \frac{7 \cos [c + d x]}{3 a^3 d (1 + \sin [c + d x])} + \frac{2 \cos [c + d x]}{3 a d (a + a \sin [c + d x])^2}$$

Result (type 3, 183 leaves):

$$\left((9 - 180 d x) \cos \left[\frac{d x}{2} \right] + 351 \cos \left[c + \frac{d x}{2} \right] - 277 \cos \left[c + \frac{3 d x}{2} \right] - 3 \cos \left[2 c + \frac{3 d x}{2} \right] + 60 d x \cos \left[2 c + \frac{3 d x}{2} \right] + 471 \sin \left[\frac{d x}{2} \right] + 9 \sin \left[c + \frac{d x}{2} \right] - 180 d x \sin \left[c + \frac{d x}{2} \right] + 3 \sin \left[c + \frac{3 d x}{2} \right] - 60 d x \sin \left[c + \frac{3 d x}{2} \right] - 3 \sin \left[2 c + \frac{3 d x}{2} \right] \right) / \left(120 a^3 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \right)$$

Problem 318: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x] \cot [c + d x]}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 68 leaves, 7 steps):

$$-\frac{\text{ArcTanh} [\cos [c + d x]]}{a^3 d} + \frac{2 \cos [c + d x]}{3 a^3 d (1 + \sin [c + d x])^2} + \frac{5 \cos [c + d x]}{3 a^3 d (1 + \sin [c + d x])}$$

Result (type 3, 185 leaves):

$$\begin{aligned} & \frac{1}{3 d (a + a \sin [c + d x])^3} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \\ & \left(-4 \sin \left[\frac{1}{2} (c + d x) \right] + 2 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) - \right. \\ & \quad \left. 10 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \right. \\ & \quad \left. 3 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \right. \\ & \quad \left. 3 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \right) \end{aligned}$$

Problem 319: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x]^2}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 82 leaves, 10 steps):

$$\frac{3 \operatorname{ArcTanh}[\cos [c + d x]]}{a^3 d} - \frac{\cot [c + d x]}{a^3 d} + \frac{2 \cot [c + d x]}{3 a^3 d (1 + \operatorname{Csc} [c + d x])^2} - \frac{13 \cot [c + d x]}{3 a^3 d (1 + \operatorname{Csc} [c + d x])}$$

Result (type 3, 255 leaves):

$$\begin{aligned} & \frac{1}{6 d (a + a \sin [c + d x])^3} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \\ & \left(8 \sin \left[\frac{1}{2} (c + d x) \right] - 4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) + \right. \\ & \quad \left. 44 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \right. \\ & \quad \left. 3 \cot \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \right. \\ & \quad \left. 18 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \right. \\ & \quad \left. 18 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \right. \\ & \quad \left. 3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \tan \left[\frac{1}{2} (c + d x) \right] \right) \end{aligned}$$

Problem 320: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x]^2 \operatorname{Csc} [c + d x]}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 106 leaves, 11 steps):

$$-\frac{11 \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{2 a^3 d} + \frac{3 \operatorname{Cot}[c+dx]}{a^3 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{2 a^3 d} + \frac{a^3 d}{2 \operatorname{Cos}[c+dx]} + \frac{17 \operatorname{Cos}[c+dx]}{3 a^3 d (1+\operatorname{Sin}[c+dx])^2} + \frac{17 \operatorname{Cos}[c+dx]}{3 a^3 d (1+\operatorname{Sin}[c+dx])}$$

Result (type 3, 465 leaves):

$$-\frac{4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3}{3 d (a+a \operatorname{Sin}[c+dx])^3} + \frac{2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 d (a+a \operatorname{Sin}[c+dx])^3} - \frac{34 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{3 d (a+a \operatorname{Sin}[c+dx])^3} + \frac{3 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2 d (a+a \operatorname{Sin}[c+dx])^3} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8 d (a+a \operatorname{Sin}[c+dx])^3} - \frac{11 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2 d (a+a \operatorname{Sin}[c+dx])^3} + \frac{11 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2 d (a+a \operatorname{Sin}[c+dx])^3} - \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8 d (a+a \operatorname{Sin}[c+dx])^3} - \frac{3 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2 d (a+a \operatorname{Sin}[c+dx])^3}$$

Problem 326: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^2 \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 89 leaves, 4 steps):

$$-\frac{\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+dx]}{\sqrt{a+a \operatorname{Sin}[c+dx]}}\right]}{d} + \frac{3 a \operatorname{Cos}[c+dx]}{d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{\operatorname{Cot}[c+dx] \sqrt{a+a \operatorname{Sin}[c+dx]}}{d}$$

Result (type 3, 206 leaves):

$$\begin{aligned} & \left(\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \sqrt{a(1+\sin[c+dx])} \left(-4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + 2 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] + \right. \right. \\ & \quad 4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + \\ & \quad \left. \left. \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + 2 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \right) / \\ & \left(d \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \left(\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right] \right) \right) \\ & \left(\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right] \right) \end{aligned}$$

Problem 327: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx] \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 101 leaves, 5 steps):

$$\frac{5 \sqrt{a} \operatorname{ArcTanh}\left[\frac{-\sqrt{a} \operatorname{Cos}[c+dx]}{\sqrt{a+a \operatorname{Sin}[c+dx]}}\right]}{4 d} - \frac{a \operatorname{Cot}[c+dx]}{4 d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx] \sqrt{a+a \operatorname{Sin}[c+dx]}}{2 d}$$

Result (type 3, 249 leaves):

$$\begin{aligned} & \frac{1}{4 d \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \left(\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 - \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \right)^2} \\ & \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^7 \sqrt{a(1+\sin[c+dx])} \\ & \left(2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + 6 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 5 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\ & \quad 5 \operatorname{Cos}[2(c+dx)] \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \quad 5 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 5 \operatorname{Cos}[2(c+dx)] \\ & \quad \left. \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 6 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \end{aligned}$$

Problem 328: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx]^2 \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 137 leaves, 6 steps):

$$\frac{3 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{8 d} + \frac{3 a \operatorname{Cot}[c+d x]}{8 d \sqrt{a+a \sin [c+d x]}} - \frac{a \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{12 d \sqrt{a+a \sin [c+d x]}} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2 \sqrt{a+a \sin [c+d x]}}{3 d}$$

Result (type 3, 285 leaves):

$$\frac{1}{24 d \left(1 + \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]\right) \left(\operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2 - \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2\right)^3 \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10} \sqrt{a(1 + \sin [c+d x])} \left(-12 \cos \left[\frac{1}{2}(c+d x)\right] + 58 \cos \left[\frac{3}{2}(c+d x)\right] + 18 \cos \left[\frac{5}{2}(c+d x)\right] + 12 \sin \left[\frac{1}{2}(c+d x)\right] - 27 \log \left[1 + \cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x] + 27 \log \left[1 - \cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x] + 58 \sin \left[\frac{3}{2}(c+d x)\right] - 18 \sin \left[\frac{5}{2}(c+d x)\right] + 9 \log \left[1 + \cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [3(c+d x)] - 9 \log \left[1 - \cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [3(c+d x)]\right)}$$

Problem 334: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^2 \operatorname{Csc}[c+d x] (a+a \sin [c+d x])^{3/2} dx$$

Optimal (type 3, 131 leaves, 6 steps):

$$\frac{a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{4 d} + \frac{13 a^2 \cos [c+d x]}{4 d \sqrt{a+a \sin [c+d x]}} - \frac{3 a \operatorname{Cot}[c+d x] \sqrt{a+a \sin [c+d x]}}{4 d} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x] (a+a \sin [c+d x])^{3/2}}{2 d}$$

Result (type 3, 271 leaves):

$$\frac{1}{4 d \left(1 + \cot \left[\frac{1}{2} (c + d x)\right]\right) \left(\csc \left[\frac{1}{4} (c + d x)\right]^2 - \sec \left[\frac{1}{4} (c + d x)\right]^2\right)^2}$$

$$a \csc \left[\frac{1}{2} (c + d x)\right]^7 \sqrt{a (1 + \sin [c + d x])} \left(-22 \cos \left[\frac{1}{2} (c + d x)\right] + 22 \cos \left[\frac{3}{2} (c + d x)\right] +\right.$$

$$8 \cos \left[\frac{5}{2} (c + d x)\right] - \log \left[1 + \cos \left[\frac{1}{2} (c + d x)\right] - \sin \left[\frac{1}{2} (c + d x)\right]\right] + \cos [2 (c + d x)]$$

$$\log \left[1 + \cos \left[\frac{1}{2} (c + d x)\right] - \sin \left[\frac{1}{2} (c + d x)\right]\right] + \log \left[1 - \cos \left[\frac{1}{2} (c + d x)\right] + \sin \left[\frac{1}{2} (c + d x)\right]\right] -$$

$$\cos [2 (c + d x)] \log \left[1 - \cos \left[\frac{1}{2} (c + d x)\right] + \sin \left[\frac{1}{2} (c + d x)\right]\right] +$$

$$\left.22 \sin \left[\frac{1}{2} (c + d x)\right] + 22 \sin \left[\frac{3}{2} (c + d x)\right] - 8 \sin \left[\frac{5}{2} (c + d x)\right]\right)$$

Problem 335: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^2 \csc [c + d x]^2 (a + a \sin [c + d x])^{3/2} dx$$

Optimal (type 3, 139 leaves, 6 steps):

$$\frac{13 a^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{a + a \sin [c + d x]}} \right]}{8 d} + \frac{5 a^2 \cot [c + d x]}{24 d \sqrt{a + a \sin [c + d x]}} -$$

$$\frac{a \cot [c + d x] \csc [c + d x] \sqrt{a + a \sin [c + d x]}}{4 d} - \frac{\cot [c + d x] \csc [c + d x]^2 (a + a \sin [c + d x])^{3/2}}{3 d}$$

Result (type 3, 286 leaves):

$$\frac{1}{24 d \left(1 + \cot \left[\frac{1}{2} (c + d x)\right]\right) \left(\csc \left[\frac{1}{4} (c + d x)\right]^2 - \sec \left[\frac{1}{4} (c + d x)\right]^2\right)^3}$$

$$a \csc \left[\frac{1}{2} (c + d x)\right]^{10} \sqrt{a (1 + \sin [c + d x])}$$

$$\left(12 \cos \left[\frac{1}{2} (c + d x)\right] + 70 \cos \left[\frac{3}{2} (c + d x)\right] - 18 \cos \left[\frac{5}{2} (c + d x)\right] - 12 \sin \left[\frac{1}{2} (c + d x)\right] -\right.$$

$$117 \log \left[1 + \cos \left[\frac{1}{2} (c + d x)\right] - \sin \left[\frac{1}{2} (c + d x)\right]\right] \sin [c + d x] +$$

$$117 \log \left[1 - \cos \left[\frac{1}{2} (c + d x)\right] + \sin \left[\frac{1}{2} (c + d x)\right]\right] \sin [c + d x] + 70 \sin \left[\frac{3}{2} (c + d x)\right] +$$

$$18 \sin \left[\frac{5}{2} (c + d x)\right] + 39 \log \left[1 + \cos \left[\frac{1}{2} (c + d x)\right] - \sin \left[\frac{1}{2} (c + d x)\right]\right] \sin [3 (c + d x)] -$$

$$\left.39 \log \left[1 - \cos \left[\frac{1}{2} (c + d x)\right] + \sin \left[\frac{1}{2} (c + d x)\right]\right] \sin [3 (c + d x)]\right)$$

Problem 340: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x]^2}{\sqrt{a + a \sin [c + d x]}} dx$$

Optimal (type 3, 62 leaves, 4 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{\sqrt{a} d} - \frac{\text{Cot}[c+dx]}{d \sqrt{a+a \sin[c+dx]}}$$

Result (type 3, 138 leaves):

$$\left(\text{Csc}\left[\frac{1}{4}(c+dx)\right] \text{Sec}\left[\frac{1}{4}(c+dx)\right] \left(-2 \cos\left[\frac{1}{2}(c+dx)\right] + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right) + \right. \\ \left. \left(\text{Log}\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - \text{Log}\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]\right) \right. \\ \left. \sin[c+dx] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right) \Big/ \left(8 d \sqrt{a(1 + \sin[c+dx])}\right)$$

Problem 341: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c+dx]^2 \text{Csc}[c+dx]}{\sqrt{a+a \sin[c+dx]}} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{4 \sqrt{a} d} + \frac{\text{Cot}[c+dx]}{4 d \sqrt{a+a \sin[c+dx]}} - \frac{\text{Cot}[c+dx] \text{Csc}[c+dx]}{2 d \sqrt{a+a \sin[c+dx]}}$$

Result (type 3, 272 leaves):

$$\frac{1}{32 d \sqrt{a(1 + \sin[c+dx])}} \\ \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \left(-8 + 4 \text{Cot}\left[\frac{1}{4}(c+dx)\right] - \text{Csc}\left[\frac{1}{4}(c+dx)\right] \right)^2 + \\ 4 \text{Log}\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - 4 \text{Log}\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\ \text{Sec}\left[\frac{1}{4}(c+dx)\right]^2 + \frac{2}{\left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} - \\ \frac{8 \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} - \frac{2}{\left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\ \frac{8 \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]} + 4 \tan\left[\frac{1}{4}(c+dx)\right] \Big/ \left(8 d \sqrt{a(1 + \sin[c+dx])}\right)$$

Problem 342: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^2 \operatorname{Csc}[c+d x]^2}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{8 \sqrt{a} d} + \frac{\cot [c+d x]}{8 d \sqrt{a+a \sin [c+d x]}} + \frac{\cot [c+d x] \operatorname{Csc}[c+d x]}{12 d \sqrt{a+a \sin [c+d x]}} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^2}{3 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 292 leaves):

$$\frac{1}{24 d \left(\operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2 - \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \right)^3 \sqrt{a(1+\sin [c+d x])} \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^9 \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right] \right) \left(-60 \cos\left[\frac{1}{2}(c+d x)\right] + 2 \cos\left[\frac{3}{2}(c+d x)\right] - 6 \cos\left[\frac{5}{2}(c+d x)\right] + 60 \sin\left[\frac{1}{2}(c+d x)\right] + 9 \log\left[1 + \cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x] - 9 \log\left[1 - \cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x] + 2 \sin\left[\frac{3}{2}(c+d x)\right] + 6 \sin\left[\frac{5}{2}(c+d x)\right] - 3 \log\left[1 + \cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]\right] \sin [3(c+d x)] + 3 \log\left[1 - \cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right] \sin [3(c+d x)] \right)}$$

Problem 343: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^2 \sin [c+d x]^3}{(a+a \sin [c+d x])^{3/2}} dx$$

Optimal (type 3, 184 leaves, 8 steps):

$$\frac{2 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{a^{3/2} d} - \frac{344 \cos [c+d x]}{105 a d \sqrt{a+a \sin [c+d x]}} - \frac{16 \cos [c+d x] \sin [c+d x]^2}{35 a d \sqrt{a+a \sin [c+d x]}} + \frac{2 \cos [c+d x] \sin [c+d x]^3}{7 a d \sqrt{a+a \sin [c+d x]}} + \frac{76 \cos [c+d x] \sqrt{a+a \sin [c+d x]}}{105 a^2 d}$$

Result (type 3, 201 leaves):

$$\frac{1}{420 a^2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)} \sqrt{a (1 + \sin [c + d x])} \left((1680 + 1680 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \operatorname{Sec} \left[\frac{d x}{4} \right] \left(\cos \left[\frac{1}{4} (2 c + d x) \right] - \sin \left[\frac{1}{4} (2 c + d x) \right] \right) \right] - 1365 \cos \left[\frac{1}{2} (c + d x) \right] + 245 \cos \left[\frac{3}{2} (c + d x) \right] + 63 \cos \left[\frac{5}{2} (c + d x) \right] - 15 \cos \left[\frac{7}{2} (c + d x) \right] + 1365 \sin \left[\frac{1}{2} (c + d x) \right] + 245 \sin \left[\frac{3}{2} (c + d x) \right] - 63 \sin \left[\frac{5}{2} (c + d x) \right] - 15 \sin \left[\frac{7}{2} (c + d x) \right] \right)$$

Problem 344: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c + d x]^2 \sin [c + d x]^2}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 140 leaves, 5 steps):

$$-\frac{2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{2} \sqrt{a + a \sin [c + d x]}} \right]}{a^{3/2} d} + \frac{18 \cos [c + d x]}{5 a d \sqrt{a + a \sin [c + d x]}} - \frac{2 \cos [c + d x]^3}{5 a d \sqrt{a + a \sin [c + d x]}} - \frac{4 \cos [c + d x] \sqrt{a + a \sin [c + d x]}}{5 a^2 d}$$

Result (type 3, 150 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \left((40 + 40 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] + 30 \cos \left[\frac{1}{2} (c + d x) \right] - 5 \cos \left[\frac{3}{2} (c + d x) \right] - \cos \left[\frac{5}{2} (c + d x) \right] - 30 \sin \left[\frac{1}{2} (c + d x) \right] - 5 \sin \left[\frac{3}{2} (c + d x) \right] + \sin \left[\frac{5}{2} (c + d x) \right] \right) \right) / \left(10 d (a (1 + \sin [c + d x]))^{3/2} \right)$$

Problem 345: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c + d x]^2 \sin [c + d x]}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 108 leaves, 4 steps):

$$\frac{2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{2} \sqrt{a + a \sin [c + d x]}} \right]}{a^{3/2} d} - \frac{10 \cos [c + d x]}{3 a d \sqrt{a + a \sin [c + d x]}} + \frac{2 \cos [c + d x] \sqrt{a + a \sin [c + d x]}}{3 a^2 d}$$

Result (type 3, 149 leaves):

$$\left(\sqrt{a(1 + \sin[c + dx])} \left((12 + 12i) (-1)^{3/4} \right. \right. \\ \left. \left. \text{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \text{Sec} \left[\frac{dx}{4} \right] \left(\cos \left[\frac{1}{4} (2c + dx) \right] - \sin \left[\frac{1}{4} (2c + dx) \right] \right) \right] - \right. \right. \\ \left. \left. 9 \cos \left[\frac{1}{2} (c + dx) \right] + \cos \left[\frac{3}{2} (c + dx) \right] + 9 \sin \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{3}{2} (c + dx) \right] \right) \right) / \\ \left(3a^2 d \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right) \right)$$

Problem 346: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c + dx] \cot[c + dx]}{(a + a \sin[c + dx])^{3/2}} dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$-\frac{2 \text{ArcTanh} \left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}} \right]}{a^{3/2} d} + \frac{2 \sqrt{2} \text{ArcTanh} \left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}} \right]}{a^{3/2} d}$$

Result (type 3, 130 leaves):

$$-\left(\left((4 + 4i) (-1)^{3/4} \text{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + dx) \right] \right) \right] \right) + \right. \\ \left. \log \left[1 + \cos \left[\frac{1}{2} (c + dx) \right] - \sin \left[\frac{1}{2} (c + dx) \right] \right] - \log \left[1 - \cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right] \right) \\ \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^3 / \left(d (a (1 + \sin[c + dx]))^{3/2} \right)$$

Problem 347: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cot[c + dx]^2}{(a + a \sin[c + dx])^{3/2}} dx$$

Optimal (type 3, 113 leaves, 6 steps):

$$\frac{3 \text{ArcTanh} \left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}} \right]}{a^{3/2} d} - \frac{2 \sqrt{2} \text{ArcTanh} \left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}} \right]}{a^{3/2} d} - \frac{\cot[c + dx]}{a d \sqrt{a + a \sin[c + dx]}}$$

Result (type 3, 206 leaves):

$$\frac{1}{4 d (a (1 + \sin [c + d x]))^{3/2}} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3$$

$$\left((16 + 16 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \right) -$$

$$\operatorname{Cot} \left[\frac{1}{4} (c + d x) \right] + 2 \left(3 \operatorname{Log} \left[1 + \cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] - \right.$$

$$3 \operatorname{Log} \left[1 - \cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right] +$$

$$\left. \left. \operatorname{Csc} [c + d x] \sin \left[\frac{1}{4} (c + d x) \right]^2 - \operatorname{Csc} [c + d x] \sin \left[\frac{1}{4} (c + d x) \right] \sin \left[\frac{3}{4} (c + d x) \right] \right) \right)$$

Problem 348: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot} [c + d x]^2 \operatorname{Csc} [c + d x]}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 153 leaves, 8 steps):

$$-\frac{11 \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{a + a \sin [c + d x]}} \right]}{4 a^{3/2} d} + \frac{2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{2} \sqrt{a + a \sin [c + d x]}} \right]}{a^{3/2} d} +$$

$$\frac{5 \operatorname{Cot} [c + d x]}{4 a d \sqrt{a + a \sin [c + d x]}} - \frac{\operatorname{Cot} [c + d x] \operatorname{Csc} [c + d x]}{2 a d \sqrt{a + a \sin [c + d x]}}$$

Result (type 3, 791 leaves):

$$\begin{aligned}
 & - \frac{3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{4d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} + \left((4+4i) (-1)^{3/4} \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right) \right] \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) / \left(d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) + \\
 & \quad \frac{3 \operatorname{Cot}\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{8d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} - \\
 & \quad \frac{\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{32d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} - \\
 & \quad \frac{\left(11 \operatorname{Log}\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) /}{\left(8d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) +} \\
 & \quad \frac{\left(11 \operatorname{Log}\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) /}{\left(8d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) +} \\
 & \quad \frac{\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{32d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} + \\
 & \quad \frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{16d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} - \\
 & \quad \frac{3 \sin\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{4d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right) \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} - \\
 & \quad \frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{16d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} + \\
 & \quad \frac{3 \sin\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{4d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right) \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}} + \\
 & \quad \frac{3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{8d \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2}}
 \end{aligned}$$

Problem 349: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx]^2}{(a+a \sin[c+dx])^{3/2}} dx$$

Optimal (type 3, 191 leaves, 9 steps):

$$\frac{23 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{8 a^{3/2} d} - \frac{2 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{a^{3/2} d} - \frac{9 \cot[c+dx]}{8 a d \sqrt{a+a \sin[c+dx]}} + \frac{7 \cot[c+dx] \csc[c+dx]}{12 a d \sqrt{a+a \sin[c+dx]}} - \frac{\cot[c+dx] \csc[c+dx]^2}{3 a d \sqrt{a+a \sin[c+dx]}}$$

Result (type 3, 332 leaves):

$$\frac{1}{192 d (a (1 + \sin[c+dx]))^{3/2}} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \left((768 + 768 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\frac{1+i}{2}\right] (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(c+dx)\right]\right) \right) - \frac{1}{\left(\csc\left[\frac{1}{4}(c+dx)\right]^2 - \sec\left[\frac{1}{4}(c+dx)\right]^2\right)^3} \left(8 \csc\left[\frac{1}{2}(c+dx)\right]^9 \left(228 \cos\left[\frac{1}{2}(c+dx)\right] - 110 \cos\left[\frac{3}{2}(c+dx)\right] - 54 \cos\left[\frac{5}{2}(c+dx)\right] - 228 \sin\left[\frac{1}{2}(c+dx)\right] - 207 \log\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[c+dx] + 207 \log\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[c+dx] - 110 \sin\left[\frac{3}{2}(c+dx)\right] + 54 \sin\left[\frac{5}{2}(c+dx)\right] + 69 \log\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[3(c+dx)] - 69 \log\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[3(c+dx)] \right) \right)$$

Problem 376: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^4 \csc[c+dx]^4 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 114 leaves, 8 steps):

$$-\frac{a \operatorname{ArcTanh}[\cos[c+dx]]}{16 d} - \frac{a \cot[c+dx]^5}{5 d} - \frac{a \cot[c+dx]^7}{7 d} - \frac{a \cot[c+dx] \csc[c+dx]}{16 d} + \frac{a \cot[c+dx] \csc[c+dx]^3}{8 d} - \frac{a \cot[c+dx]^3 \csc[c+dx]^3}{6 d}$$

Result (type 3, 239 leaves):

$$\begin{aligned}
 & - \frac{2 a \cot [c+d x]}{35 d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{64 d} + \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{64 d} - \\
 & \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{384 d} - \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^2}{35 d} + \frac{8 a \cot [c+d x] \operatorname{Csc}[c+d x]^4}{35 d} - \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^6}{7 d} - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]}{16 d} + \frac{a \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{16 d} + \\
 & \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{64 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{64 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6}{384 d}
 \end{aligned}$$

Problem 377: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^4 \operatorname{Csc}[c+d x]^5 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 136 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{3 a \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{128 d} - \frac{a \cot [c+d x]^5}{5 d} - \frac{a \cot [c+d x]^7}{7 d} - \frac{3 a \cot [c+d x] \operatorname{Csc}[c+d x]}{128 d} - \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^3}{64 d} + \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^5}{16 d} - \frac{a \cot [c+d x]^3 \operatorname{Csc}[c+d x]^5}{8 d}
 \end{aligned}$$

Result (type 3, 279 leaves):

$$\begin{aligned}
 & - \frac{2 a \cot [c+d x]}{35 d} - \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{512 d} + \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} + \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{512 d} - \\
 & \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{2048 d} - \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^2}{35 d} + \frac{8 a \cot [c+d x] \operatorname{Csc}[c+d x]^4}{35 d} - \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^6}{7 d} - \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]}{128 d} + \frac{3 a \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{128 d} + \\
 & \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{512 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6}{512 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8}{2048 d}
 \end{aligned}$$

Problem 388: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^4 \operatorname{Csc}[c+d x]^3 (a+a \sin [c+d x])^2 dx$$

Optimal (type 3, 132 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{7 a^2 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{16 d} - \frac{2 a^2 \cot [c+d x]^5}{5 d} + \frac{5 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]}{16 d} - \\
 & \frac{a^2 \cot [c+d x]^3 \operatorname{Csc}[c+d x]}{4 d} + \frac{a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^3}{8 d} - \frac{a^2 \cot [c+d x]^3 \operatorname{Csc}[c+d x]^3}{6 d}
 \end{aligned}$$

Result (type 3, 267 leaves):

$$a^2 \left(-\frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{5d} + \frac{9\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{7\text{Cot}\left[\frac{1}{2}(c+dx)\right]\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{80d} - \frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right]\text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{80d} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{384d} - \frac{7\text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{16d} + \frac{7\text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{16d} - \frac{9\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{384d} + \frac{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{5d} - \frac{7\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{80d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^4\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{80d} \right)$$

Problem 398: Result more than twice size of optimal antiderivative.

$$\int \text{Cos}[c+dx] \text{Cot}[c+dx]^3 (a+a\text{Sin}[c+dx])^3 dx$$

Optimal (type 3, 137 leaves, 15 steps):

$$\frac{33 a^3 x}{8} - \frac{3 a^3 \text{ArcTanh}[\text{Cos}[c+dx]]}{2d} + \frac{2 a^3 \text{Cos}[c+dx]}{d} + \frac{a^3 \text{Cos}[c+dx]^3}{d} - \frac{3 a^3 \text{Cot}[c+dx]}{d} - \frac{a^3 \text{Cot}[c+dx] \text{Csc}[c+dx]}{2d} - \frac{7 a^3 \text{Cos}[c+dx] \text{Sin}[c+dx]}{8d} - \frac{a^3 \text{Cos}[c+dx] \text{Sin}[c+dx]^3}{4d}$$

Result (type 3, 564 leaves):

$$\frac{33(c+dx)(a+a\text{Sin}[c+dx])^3}{8d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{11\text{Cos}[c+dx](a+a\text{Sin}[c+dx])^3}{4d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{\text{Cos}[3(c+dx)](a+a\text{Sin}[c+dx])^3}{4d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \frac{3\text{Cot}\left[\frac{1}{2}(c+dx)\right](a+a\text{Sin}[c+dx])^3}{2d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2(a+a\text{Sin}[c+dx])^3}{8d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{3\text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right](a+a\text{Sin}[c+dx])^3}{2d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{3\text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right](a+a\text{Sin}[c+dx])^3}{2d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2(a+a\text{Sin}[c+dx])^3}{8d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \frac{(a+a\text{Sin}[c+dx])^3\text{Sin}[2(c+dx)]}{2d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{(a+a\text{Sin}[c+dx])^3\text{Sin}[4(c+dx)]}{32d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{3(a+a\text{Sin}[c+dx])^3\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]+\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}$$

Problem 403: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + dx]^4 \text{Csc}[c + dx]^4 (a + a \text{Sin}[c + dx])^3 dx$$

Optimal (type 3, 150 leaves, 14 steps):

$$\begin{aligned} & -\frac{9 a^3 \text{ArcTanh}[\text{Cos}[c + dx]]}{16 d} - \frac{4 a^3 \text{Cot}[c + dx]^5}{5 d} - \frac{a^3 \text{Cot}[c + dx]^7}{7 d} + \frac{3 a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]}{16 d} \\ & - \frac{a^3 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]}{4 d} + \frac{3 a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]^3}{8 d} - \frac{a^3 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]^3}{2 d} \end{aligned}$$

Result (type 3, 363 leaves):

$$\begin{aligned} & a^3 \left(-\frac{23 \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{70 d} + \frac{7 \text{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{64 d} + \frac{297 \text{Cot}\left[\frac{1}{2}(c + dx)\right] \text{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{2240 d} + \right. \\ & \frac{\text{Csc}\left[\frac{1}{2}(c + dx)\right]^4}{32 d} - \frac{31 \text{Cot}\left[\frac{1}{2}(c + dx)\right] \text{Csc}\left[\frac{1}{2}(c + dx)\right]^4}{2240 d} - \frac{\text{Csc}\left[\frac{1}{2}(c + dx)\right]^6}{128 d} - \\ & \frac{\text{Cot}\left[\frac{1}{2}(c + dx)\right] \text{Csc}\left[\frac{1}{2}(c + dx)\right]^6}{896 d} - \frac{9 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right]}{16 d} + \\ & \frac{9 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{16 d} - \frac{7 \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2}{64 d} - \frac{\text{Sec}\left[\frac{1}{2}(c + dx)\right]^4}{32 d} + \\ & \frac{\text{Sec}\left[\frac{1}{2}(c + dx)\right]^6}{128 d} + \frac{23 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{70 d} - \frac{297 \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{2240 d} + \\ & \left. \frac{31 \text{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{2240 d} + \frac{\text{Sec}\left[\frac{1}{2}(c + dx)\right]^6 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{896 d} \right) \end{aligned}$$

Problem 404: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + dx]^4 \text{Csc}[c + dx]^5 (a + a \text{Sin}[c + dx])^3 dx$$

Optimal (type 3, 176 leaves, 16 steps):

$$\begin{aligned} & -\frac{27 a^3 \text{ArcTanh}[\text{Cos}[c + dx]]}{128 d} - \frac{4 a^3 \text{Cot}[c + dx]^5}{5 d} - \frac{3 a^3 \text{Cot}[c + dx]^7}{7 d} - \\ & \frac{27 a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]}{128 d} + \frac{23 a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]^3}{64 d} - \\ & \frac{a^3 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]^3}{2 d} + \frac{a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]^5}{16 d} - \frac{a^3 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]^5}{8 d} \end{aligned}$$

Result (type 3, 1027 leaves):

$$\begin{aligned}
& - \frac{13 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] (a+a \operatorname{Sin}[c+dx])^3}{70 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \frac{27 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \operatorname{Sin}[c+dx])^3}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{107 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \operatorname{Sin}[c+dx])^3}{2240 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{49 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 (a+a \operatorname{Sin}[c+dx])^3}{1024 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{19 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 (a+a \operatorname{Sin}[c+dx])^3}{2240 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6 (a+a \operatorname{Sin}[c+dx])^3}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{3 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6 (a+a \operatorname{Sin}[c+dx])^3}{896 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8 (a+a \operatorname{Sin}[c+dx])^3}{2048 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \frac{27 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] (a+a \operatorname{Sin}[c+dx])^3}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{27 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+a \operatorname{Sin}[c+dx])^3}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{27 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \operatorname{Sin}[c+dx])^3}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{49 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a+a \operatorname{Sin}[c+dx])^3}{1024 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 (a+a \operatorname{Sin}[c+dx])^3}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^8 (a+a \operatorname{Sin}[c+dx])^3}{2048 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{13 (a+a \operatorname{Sin}[c+dx])^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{70 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{107 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \operatorname{Sin}[c+dx])^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2240 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} - \\
& \frac{19 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a+a \operatorname{Sin}[c+dx])^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2240 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \\
& \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 (a+a \operatorname{Sin}[c+dx])^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{896 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}
\end{aligned}$$

Problem 410: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^3}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 117 leaves, 8 steps):

$$\frac{x}{16 a} - \frac{\cos [c+d x]^3}{3 a d} + \frac{\cos [c+d x]^5}{5 a d} - \frac{\cos [c+d x] \sin [c+d x]}{16 a d} + \frac{\cos [c+d x]^3 \sin [c+d x]}{8 a d} + \frac{\cos [c+d x]^3 \sin [c+d x]^3}{6 a d}$$

Result (type 3, 377 leaves):

$$\frac{1}{1920 a d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \left(30 (3 c - 4 d x) \cos \left[\frac{c}{2} \right] - 120 \cos \left[\frac{c}{2} + d x \right] - 120 \cos \left[\frac{3 c}{2} + d x \right] + 15 \cos \left[\frac{3 c}{2} + 2 d x \right] - 15 \cos \left[\frac{5 c}{2} + 2 d x \right] - 20 \cos \left[\frac{5 c}{2} + 3 d x \right] - 20 \cos \left[\frac{7 c}{2} + 3 d x \right] + 15 \cos \left[\frac{7 c}{2} + 4 d x \right] - 15 \cos \left[\frac{9 c}{2} + 4 d x \right] + 12 \cos \left[\frac{9 c}{2} + 5 d x \right] + 12 \cos \left[\frac{11 c}{2} + 5 d x \right] - 5 \cos \left[\frac{11 c}{2} + 6 d x \right] + 5 \cos \left[\frac{13 c}{2} + 6 d x \right] - 180 \sin \left[\frac{c}{2} \right] + 90 c \sin \left[\frac{c}{2} \right] - 120 d x \sin \left[\frac{c}{2} \right] + 120 \sin \left[\frac{c}{2} + d x \right] - 120 \sin \left[\frac{3 c}{2} + d x \right] + 15 \sin \left[\frac{3 c}{2} + 2 d x \right] + 15 \sin \left[\frac{5 c}{2} + 2 d x \right] + 20 \sin \left[\frac{5 c}{2} + 3 d x \right] - 20 \sin \left[\frac{7 c}{2} + 3 d x \right] + 15 \sin \left[\frac{7 c}{2} + 4 d x \right] + 15 \sin \left[\frac{9 c}{2} + 4 d x \right] - 12 \sin \left[\frac{9 c}{2} + 5 d x \right] + 12 \sin \left[\frac{11 c}{2} + 5 d x \right] - 5 \sin \left[\frac{11 c}{2} + 6 d x \right] - 5 \sin \left[\frac{13 c}{2} + 6 d x \right] \right)$$

Problem 411: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^2}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 91 leaves, 7 steps):

$$\frac{x}{8 a} + \frac{\cos [c+d x]^3}{3 a d} - \frac{\cos [c+d x]^5}{5 a d} + \frac{\cos [c+d x] \sin [c+d x]}{8 a d} - \frac{\cos [c+d x]^3 \sin [c+d x]}{4 a d}$$

Result (type 3, 258 leaves):

$$\frac{1}{960 a d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \left(120 d x \cos \left[\frac{c}{2} \right] + 60 \cos \left[\frac{c}{2} + d x \right] + 60 \cos \left[\frac{3 c}{2} + d x \right] + 10 \cos \left[\frac{5 c}{2} + 3 d x \right] + 10 \cos \left[\frac{7 c}{2} + 3 d x \right] - 15 \cos \left[\frac{7 c}{2} + 4 d x \right] + 15 \cos \left[\frac{9 c}{2} + 4 d x \right] - 6 \cos \left[\frac{9 c}{2} + 5 d x \right] - 6 \cos \left[\frac{11 c}{2} + 5 d x \right] + 120 \sin \left[\frac{c}{2} \right] + 120 d x \sin \left[\frac{c}{2} \right] - 60 \sin \left[\frac{c}{2} + d x \right] + 60 \sin \left[\frac{3 c}{2} + d x \right] - 10 \sin \left[\frac{5 c}{2} + 3 d x \right] + 10 \sin \left[\frac{7 c}{2} + 3 d x \right] - 15 \sin \left[\frac{7 c}{2} + 4 d x \right] - 15 \sin \left[\frac{9 c}{2} + 4 d x \right] + 6 \sin \left[\frac{9 c}{2} + 5 d x \right] - 6 \sin \left[\frac{11 c}{2} + 5 d x \right] \right)$$

Problem 412: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 73 leaves, 6 steps):

$$\frac{x}{8 a} - \frac{\cos [c+d x]^3}{3 a d} - \frac{\cos [c+d x] \sin [c+d x]}{8 a d} + \frac{\cos [c+d x]^3 \sin [c+d x]}{4 a d}$$

Result (type 3, 219 leaves):

$$\begin{aligned} & - \left(\left(-24 (c-d x) \cos \left[\frac{c}{2} \right] + 24 \cos \left[\frac{c}{2} + d x \right] + 24 \cos \left[\frac{3 c}{2} + d x \right] + 8 \cos \left[\frac{5 c}{2} + 3 d x \right] + \right. \\ & \quad 8 \cos \left[\frac{7 c}{2} + 3 d x \right] - 3 \cos \left[\frac{7 c}{2} + 4 d x \right] + 3 \cos \left[\frac{9 c}{2} + 4 d x \right] + 48 \sin \left[\frac{c}{2} \right] - 24 c \sin \left[\frac{c}{2} \right] + \\ & \quad 24 d x \sin \left[\frac{c}{2} \right] - 24 \sin \left[\frac{c}{2} + d x \right] + 24 \sin \left[\frac{3 c}{2} + d x \right] - 8 \sin \left[\frac{5 c}{2} + 3 d x \right] + 8 \sin \left[\frac{7 c}{2} + 3 d x \right] - \\ & \quad \left. \left. 3 \sin \left[\frac{7 c}{2} + 4 d x \right] - 3 \sin \left[\frac{9 c}{2} + 4 d x \right] \right) / \left(192 a d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \right) \end{aligned}$$

Problem 416: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^4}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 58 leaves, 5 steps):

$$\frac{\text{ArcTanh}[\cos [c+d x]]}{2 a d} - \frac{\cot [c+d x]^3}{3 a d} + \frac{\cot [c+d x] \csc [c+d x]}{2 a d}$$

Result (type 3, 124 leaves):

$$\begin{aligned} & - \left(\left(\csc \left[\frac{1}{2} (c+d x) \right] \sec \left[\frac{1}{2} (c+d x) \right] \left(\csc \left[\frac{1}{2} (c+d x) \right] + \sec \left[\frac{1}{2} (c+d x) \right] \right) \right)^2 \right. \\ & \quad \left(\cos [3 (c+d x)] + \cos [c+d x] (3-6 \sin [c+d x]) + 6 \left(\log \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] - \right. \right. \\ & \quad \left. \left. \log \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) \sin [c+d x]^3 \right) / \left(96 a d (1+\sin [c+d x]) \right) \end{aligned}$$

Problem 420: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^5}{(a+a \sin [c+d x])^2} d x$$

Optimal (type 3, 147 leaves, 11 steps):

$$\begin{aligned} & -\frac{5 x}{8 a^2} - \frac{2 \cos [c+d x]}{a^2 d} + \frac{5 \cos [c+d x]^3}{3 a^2 d} - \frac{4 \cos [c+d x]^5}{5 a^2 d} + \frac{\cos [c+d x]^7}{7 a^2 d} + \\ & \frac{5 \cos [c+d x] \sin [c+d x]}{8 a^2 d} + \frac{5 \cos [c+d x] \sin [c+d x]^3}{12 a^2 d} + \frac{\cos [c+d x] \sin [c+d x]^5}{3 a^2 d} \end{aligned}$$

Result (type 3, 414 leaves):

$$\begin{aligned} & \frac{1}{13440 a^2 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \\ & \left(-8400 d x \cos \left[\frac{c}{2} \right] - 7875 \cos \left[\frac{c}{2} + d x \right] - 7875 \cos \left[\frac{3 c}{2} + d x \right] + 3150 \cos \left[\frac{3 c}{2} + 2 d x \right] - \right. \\ & 3150 \cos \left[\frac{5 c}{2} + 2 d x \right] + 1435 \cos \left[\frac{5 c}{2} + 3 d x \right] + 1435 \cos \left[\frac{7 c}{2} + 3 d x \right] - 630 \cos \left[\frac{7 c}{2} + 4 d x \right] + \\ & 630 \cos \left[\frac{9 c}{2} + 4 d x \right] - 231 \cos \left[\frac{9 c}{2} + 5 d x \right] - 231 \cos \left[\frac{11 c}{2} + 5 d x \right] + 70 \cos \left[\frac{11 c}{2} + 6 d x \right] - \\ & 70 \cos \left[\frac{13 c}{2} + 6 d x \right] + 15 \cos \left[\frac{13 c}{2} + 7 d x \right] + 15 \cos \left[\frac{15 c}{2} + 7 d x \right] + 420 \sin \left[\frac{c}{2} \right] - \\ & 8400 d x \sin \left[\frac{c}{2} \right] + 7875 \sin \left[\frac{c}{2} + d x \right] - 7875 \sin \left[\frac{3 c}{2} + d x \right] + 3150 \sin \left[\frac{3 c}{2} + 2 d x \right] + \\ & 3150 \sin \left[\frac{5 c}{2} + 2 d x \right] - 1435 \sin \left[\frac{5 c}{2} + 3 d x \right] + 1435 \sin \left[\frac{7 c}{2} + 3 d x \right] - \\ & 630 \sin \left[\frac{7 c}{2} + 4 d x \right] - 630 \sin \left[\frac{9 c}{2} + 4 d x \right] + 231 \sin \left[\frac{9 c}{2} + 5 d x \right] - 231 \sin \left[\frac{11 c}{2} + 5 d x \right] + \\ & \left. 70 \sin \left[\frac{11 c}{2} + 6 d x \right] + 70 \sin \left[\frac{13 c}{2} + 6 d x \right] - 15 \sin \left[\frac{13 c}{2} + 7 d x \right] + 15 \sin \left[\frac{15 c}{2} + 7 d x \right] \right) \end{aligned}$$

Problem 422: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^3}{(a+a \sin [c+d x])^2} d x$$

Optimal (type 3, 102 leaves, 10 steps):

$$\begin{aligned} & -\frac{3 x}{4 a^2} - \frac{2 \cos [c+d x]}{a^2 d} + \frac{\cos [c+d x]^3}{a^2 d} - \frac{\cos [c+d x]^5}{5 a^2 d} + \\ & \frac{3 \cos [c+d x] \sin [c+d x]}{4 a^2 d} + \frac{\cos [c+d x] \sin [c+d x]^3}{2 a^2 d} \end{aligned}$$

Result (type 3, 304 leaves):

$$\frac{1}{160 a^2 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \left(120 d x \cos \left[\frac{c}{2} \right] + 110 \cos \left[\frac{c}{2} + d x \right] + 110 \cos \left[\frac{3c}{2} + d x \right] - 40 \cos \left[\frac{3c}{2} + 2 d x \right] + 40 \cos \left[\frac{5c}{2} + 2 d x \right] - 15 \cos \left[\frac{5c}{2} + 3 d x \right] - 15 \cos \left[\frac{7c}{2} + 3 d x \right] + 5 \cos \left[\frac{7c}{2} + 4 d x \right] - 5 \cos \left[\frac{9c}{2} + 4 d x \right] + \cos \left[\frac{9c}{2} + 5 d x \right] + \cos \left[\frac{11c}{2} + 5 d x \right] - 10 \sin \left[\frac{c}{2} \right] + 120 d x \sin \left[\frac{c}{2} \right] - 110 \sin \left[\frac{c}{2} + d x \right] + 110 \sin \left[\frac{3c}{2} + d x \right] - 40 \sin \left[\frac{3c}{2} + 2 d x \right] - 40 \sin \left[\frac{5c}{2} + 2 d x \right] + 15 \sin \left[\frac{5c}{2} + 3 d x \right] - 15 \sin \left[\frac{7c}{2} + 3 d x \right] + 5 \sin \left[\frac{7c}{2} + 4 d x \right] + 5 \sin \left[\frac{9c}{2} + 4 d x \right] - \sin \left[\frac{9c}{2} + 5 d x \right] + \sin \left[\frac{11c}{2} + 5 d x \right] \right)$$

Problem 423: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^2}{(a+a \sin [c+d x])^2} d x$$

Optimal (type 3, 87 leaves, 10 steps):

$$\frac{7 x}{8 a^2} + \frac{2 \cos [c+d x]}{a^2 d} - \frac{2 \cos [c+d x]^3}{3 a^2 d} - \frac{7 \cos [c+d x] \sin [c+d x]}{8 a^2 d} - \frac{\cos [c+d x] \sin [c+d x]^3}{4 a^2 d}$$

Result (type 3, 258 leaves):

$$\frac{1}{192 a^2 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \left(168 d x \cos \left[\frac{c}{2} \right] + 144 \cos \left[\frac{c}{2} + d x \right] + 144 \cos \left[\frac{3c}{2} + d x \right] - 48 \cos \left[\frac{3c}{2} + 2 d x \right] + 48 \cos \left[\frac{5c}{2} + 2 d x \right] - 16 \cos \left[\frac{5c}{2} + 3 d x \right] - 16 \cos \left[\frac{7c}{2} + 3 d x \right] + 3 \cos \left[\frac{7c}{2} + 4 d x \right] - 3 \cos \left[\frac{9c}{2} + 4 d x \right] + 8 \sin \left[\frac{c}{2} \right] + 168 d x \sin \left[\frac{c}{2} \right] - 144 \sin \left[\frac{c}{2} + d x \right] + 144 \sin \left[\frac{3c}{2} + d x \right] - 48 \sin \left[\frac{3c}{2} + 2 d x \right] - 48 \sin \left[\frac{5c}{2} + 2 d x \right] + 16 \sin \left[\frac{5c}{2} + 3 d x \right] - 16 \sin \left[\frac{7c}{2} + 3 d x \right] + 3 \sin \left[\frac{7c}{2} + 4 d x \right] + 3 \sin \left[\frac{9c}{2} + 4 d x \right] \right)$$

Problem 424: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]}{(a+a \sin [c+d x])^2} d x$$

Optimal (type 3, 70 leaves, 4 steps):

$$-\frac{x}{a^2} - \frac{2 \cos [c+d x]^3}{3 a^2 d} - \frac{\cos [c+d x] \sin [c+d x]}{a^2 d} - \frac{\cos [c+d x]^5}{d (a+a \sin [c+d x])^2}$$

Result (type 3, 200 leaves):

$$\begin{aligned} & \left(-24 d x \cos\left[\frac{c}{2}\right] - 21 \cos\left[\frac{c}{2} + d x\right] - 21 \cos\left[\frac{3c}{2} + d x\right] + 6 \cos\left[\frac{3c}{2} + 2 d x\right] - \right. \\ & 6 \cos\left[\frac{5c}{2} + 2 d x\right] + \cos\left[\frac{5c}{2} + 3 d x\right] + \cos\left[\frac{7c}{2} + 3 d x\right] + 4 \sin\left[\frac{c}{2}\right] - 24 d x \sin\left[\frac{c}{2}\right] + \\ & 21 \sin\left[\frac{c}{2} + d x\right] - 21 \sin\left[\frac{3c}{2} + d x\right] + 6 \sin\left[\frac{3c}{2} + 2 d x\right] + 6 \sin\left[\frac{5c}{2} + 2 d x\right] - \\ & \left. \sin\left[\frac{5c}{2} + 3 d x\right] + \sin\left[\frac{7c}{2} + 3 d x\right] \right) / \left(24 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \end{aligned}$$

Problem 426: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^2 \cot[c + d x]^2}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 35 leaves, 6 steps):

$$\frac{x}{a^2} + \frac{2 \operatorname{ArcTanh}[\cos[c + d x]]}{a^2 d} - \frac{\cot[c + d x]}{a^2 d}$$

Result (type 3, 98 leaves):

$$\begin{aligned} & \left(\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 \left(2(c + d x) - \cot\left[\frac{1}{2}(c + d x)\right] + 4 \log\left[\cos\left[\frac{1}{2}(c + d x)\right]\right] - \right. \right. \\ & \left. \left. 4 \log\left[\sin\left[\frac{1}{2}(c + d x)\right]\right] + \tan\left[\frac{1}{2}(c + d x)\right] \right) \right) / \left(2 d (a + a \sin[c + d x])^2 \right) \end{aligned}$$

Problem 433: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^4 \sin[c + d x]^2}{(a + a \sin[c + d x])^3} dx$$

Optimal (type 3, 87 leaves, 9 steps):

$$-\frac{11 x}{2 a^3} - \frac{5 \cos[c + d x]}{a^3 d} + \frac{\cos[c + d x]^3}{3 a^3 d} + \frac{3 \cos[c + d x] \sin[c + d x]}{2 a^3 d} - \frac{4 \cos[c + d x]}{a^3 d (1 + \sin[c + d x])}$$

Result (type 3, 181 leaves):

$$\begin{aligned} & \left((1 - 660 d x) \cos\left[\frac{d x}{2}\right] - 286 \cos\left[c + \frac{d x}{2}\right] - 240 \cos\left[c + \frac{3 d x}{2}\right] - \right. \\ & 40 \cos\left[3 c + \frac{5 d x}{2}\right] + 5 \cos\left[3 c + \frac{7 d x}{2}\right] + 1244 \sin\left[\frac{d x}{2}\right] + \sin\left[c + \frac{d x}{2}\right] - \\ & 660 d x \sin\left[c + \frac{d x}{2}\right] - 240 \sin\left[2 c + \frac{3 d x}{2}\right] + 40 \sin\left[2 c + \frac{5 d x}{2}\right] + 5 \sin\left[4 c + \frac{7 d x}{2}\right] \left. \right) / \\ & \left(120 a^3 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right) \right) \end{aligned}$$

Problem 435: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 45 leaves, 5 steps):

$$\frac{x}{a^3} - \frac{\text{ArcTanh}[\cos [c+d x]]}{a^3 d} + \frac{4 \cos [c+d x]}{a^3 d (1+\sin [c+d x])}$$

Result (type 3, 122 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^5 \right. \\ \left(\cos \left[\frac{1}{2} (c+d x) \right] \left(c+d x - \log \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + \log \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) + \right. \\ \left. \left(-8+c+d x - \log \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + \log \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) \right. \\ \left. \left. \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) / \left(a^3 d (1+\sin [c+d x])^3 \right)$$

Problem 436: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2 \cot [c+d x]^2}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 54 leaves, 7 steps):

$$\frac{3 \text{ArcTanh}[\cos [c+d x]]}{a^3 d} - \frac{\cot [c+d x]}{a^3 d} - \frac{4 \cos [c+d x]}{a^3 d (1+\sin [c+d x])}$$

Result (type 3, 156 leaves):

$$- \left(\left(\cos \left[\frac{1}{2} (c+d x) \right] \left(-17 + \cot \left[\frac{1}{2} (c+d x) \right]^2 - 6 \log \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + 6 \log \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) + \right. \\ \left. \cot \left[\frac{1}{2} (c+d x) \right] \left(1 - 6 \log \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + 6 \log \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) \right) - \\ \sin \left[\frac{1}{2} (c+d x) \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^5 \\ \tan \left[\frac{1}{2} (c+d x) \right] \right) / \left(2 a^3 d (1+\sin [c+d x])^3 \right)$$

Problem 437: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \cot [c+d x]^3}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 78 leaves, 9 steps):

$$-\frac{9 \operatorname{ArcTanh}[\cos [c+d x]]}{2 a^3 d} + \frac{3 \cot [c+d x]}{a^3 d} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]}{2 a^3 d} + \frac{4 \cos [c+d x]}{a^3 d (1+\sin [c+d x])}$$

Result (type 3, 369 leaves):

$$\begin{aligned} & -\frac{8 \sin \left[\frac{1}{2}(c+d x)\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^5}{d (a+a \sin [c+d x])^3} + \\ & \frac{3 \cot \left[\frac{1}{2}(c+d x)\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6}{2 d (a+a \sin [c+d x])^3} - \\ & \frac{\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6}{8 d (a+a \sin [c+d x])^3} - \\ & \frac{9 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6}{2 d (a+a \sin [c+d x])^3} + \\ & \frac{9 \operatorname{Log}\left[\sin \left[\frac{1}{2}(c+d x)\right]\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6}{2 d (a+a \sin [c+d x])^3} + \\ & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6}{8 d (a+a \sin [c+d x])^3} - \\ & \frac{3 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{2 d (a+a \sin [c+d x])^3} \end{aligned}$$

Problem 438: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^4}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 96 leaves, 11 steps):

$$\frac{11 \operatorname{ArcTanh}[\cos [c+d x]]}{2 a^3 d} - \frac{5 \cot [c+d x]}{a^3 d} - \frac{\cot [c+d x]^3}{3 a^3 d} + \frac{3 \cot [c+d x] \operatorname{Csc}[c+d x]}{2 a^3 d} - \frac{4 \cot [c+d x]}{a^3 d (1+\operatorname{Csc}[c+d x])}$$

Result (type 3, 497 leaves):

$$\begin{aligned}
 & \frac{8 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{d(a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{7 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{3d(a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8d(a+a \operatorname{Sin}[c+dx])^3} - \\
 & \left(\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) / \\
 & \left(24d(a+a \operatorname{Sin}[c+dx])^3\right) + \frac{11 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2d(a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{11 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2d(a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8d(a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{7 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{3d(a+a \operatorname{Sin}[c+dx])^3} + \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \\
 & \left(24d(a+a \operatorname{Sin}[c+dx])^3\right)
 \end{aligned}$$

Problem 439: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^4 \operatorname{Csc}[c+dx]}{(a+a \operatorname{Sin}[c+dx])^3} dx$$

Optimal (type 3, 117 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{51 \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{8a^3d} + \frac{7 \operatorname{Cot}[c+dx]}{a^3d} + \frac{\operatorname{Cot}[c+dx]^3}{a^3d} - \\
 & \frac{19 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8a^3d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4a^3d} + \frac{4 \operatorname{Cos}[c+dx]}{a^3d(1+\operatorname{Sin}[c+dx])}
 \end{aligned}$$

Result (type 3, 601 leaves):

$$\begin{aligned}
 & - \frac{8 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{d (a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{3 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{d (a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{19 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32 d (a+a \operatorname{Sin}[c+dx])^3} + \\
 & \left(\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) / \\
 & \left(8 d (a+a \operatorname{Sin}[c+dx])^3\right) - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64 d (a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{51 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8 d (a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{51 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8 d (a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{19 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32 d (a+a \operatorname{Sin}[c+dx])^3} + \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64 d (a+a \operatorname{Sin}[c+dx])^3} - \\
 & \frac{3 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{d (a+a \operatorname{Sin}[c+dx])^3} - \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \\
 & \left(8 d (a+a \operatorname{Sin}[c+dx])^3\right)
 \end{aligned}$$

Problem 440: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[e+fx]^4 \operatorname{Sin}[e+fx]}{(a+a \operatorname{Sin}[e+fx])^6} dx$$

Optimal (type 3, 58 leaves, 2 steps):

$$\frac{\operatorname{Cos}[e+fx]^5}{7 f (a+a \operatorname{Sin}[e+fx])^6} - \frac{6 \operatorname{Cos}[e+fx]^5}{35 a f (a+a \operatorname{Sin}[e+fx])^5}$$

Result (type 3, 237 leaves):

$$\frac{1}{4620 a^6 f \left(\cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \left(\cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^7} \left(35 \cos\left[\frac{f x}{2}\right] + 4585 \cos\left[e + \frac{f x}{2}\right] - 2982 \cos\left[e + \frac{3 f x}{2}\right] - 21 \cos\left[2 e + \frac{3 f x}{2}\right] - 7 \cos\left[2 e + \frac{5 f x}{2}\right] - 1148 \cos\left[3 e + \frac{5 f x}{2}\right] + 197 \cos\left[3 e + \frac{7 f x}{2}\right] + \cos\left[4 e + \frac{7 f x}{2}\right] + 2275 \sin\left[\frac{f x}{2}\right] + 35 \sin\left[e + \frac{f x}{2}\right] + 21 \sin\left[e + \frac{3 f x}{2}\right] + 1134 \sin\left[2 e + \frac{3 f x}{2}\right] - 224 \sin\left[2 e + \frac{5 f x}{2}\right] - 7 \sin\left[3 e + \frac{5 f x}{2}\right] - \sin\left[3 e + \frac{7 f x}{2}\right] + \sin\left[4 e + \frac{7 f x}{2}\right] \right)$$

Problem 441: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e + f x]^4 \sin[e + f x]^2}{(a + a \sin[e + f x])^7} dx$$

Optimal (type 3, 89 leaves, 18 steps):

$$-\frac{a \cos[e + f x]^7}{18 f (a + a \sin[e + f x])^8} + \frac{25 \cos[e + f x]^5}{126 a f (a + a \sin[e + f x])^6} - \frac{47 \cos[e + f x]^5}{315 a^2 f (a + a \sin[e + f x])^5}$$

Result (type 3, 293 leaves):

$$\frac{1}{720720 a^7 f \left(\cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \left(\cos\left[\frac{1}{2}(e + f x)\right] + \sin\left[\frac{1}{2}(e + f x)\right] \right)^9} \left(1890 \cos\left[\frac{f x}{2}\right] + 718830 \cos\left[e + \frac{f x}{2}\right] - 467208 \cos\left[e + \frac{3 f x}{2}\right] - 1260 \cos\left[2 e + \frac{3 f x}{2}\right] - 540 \cos\left[2 e + \frac{5 f x}{2}\right] - 179640 \cos\left[3 e + \frac{5 f x}{2}\right] + 30753 \cos\left[3 e + \frac{7 f x}{2}\right] + 135 \cos\left[4 e + \frac{7 f x}{2}\right] + 15 \cos\left[4 e + \frac{9 f x}{2}\right] - 15 \cos\left[5 e + \frac{9 f x}{2}\right] + 971082 \sin\left[\frac{f x}{2}\right] + 1890 \sin\left[e + \frac{f x}{2}\right] + 1260 \sin\left[e + \frac{3 f x}{2}\right] + 659400 \sin\left[2 e + \frac{3 f x}{2}\right] - 303192 \sin\left[2 e + \frac{5 f x}{2}\right] - 540 \sin\left[3 e + \frac{5 f x}{2}\right] - 135 \sin\left[3 e + \frac{7 f x}{2}\right] - 89955 \sin\left[4 e + \frac{7 f x}{2}\right] + 13427 \sin\left[4 e + \frac{9 f x}{2}\right] + 15 \sin\left[5 e + \frac{9 f x}{2}\right] \right)$$

Problem 442: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e + f x]^4 \sin[e + f x]^3}{(a + a \sin[e + f x])^8} dx$$

Optimal (type 3, 157 leaves, 24 steps):

$$\frac{4 \cos[e + f x]}{11 a^8 f (1 + \sin[e + f x])^6} - \frac{52 \cos[e + f x]}{33 a^8 f (1 + \sin[e + f x])^5} + \frac{617 \cos[e + f x]}{231 a^8 f (1 + \sin[e + f x])^4} - \frac{846 \cos[e + f x]}{385 a^8 f (1 + \sin[e + f x])^3} + \frac{1003 \cos[e + f x]}{1155 a^8 f (1 + \sin[e + f x])^2} - \frac{152 \cos[e + f x]}{1155 a^8 f (1 + \sin[e + f x])}$$

Result (type 3, 343 leaves):

$$\begin{aligned} & \left(\frac{1}{\left(240240 a^8 f \left(\cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^{11} \right)} \right) \\ & \left(462 \cos\left[\frac{fx}{2}\right] + 486024 \cos\left[e + \frac{fx}{2}\right] - 351450 \cos\left[e + \frac{3fx}{2}\right] - 330 \cos\left[2e + \frac{3fx}{2}\right] - \right. \\ & \quad 165 \cos\left[2e + \frac{5fx}{2}\right] - 180015 \cos\left[3e + \frac{5fx}{2}\right] + 63580 \cos\left[3e + \frac{7fx}{2}\right] + 55 \cos\left[4e + \frac{7fx}{2}\right] + \\ & \quad 11 \cos\left[4e + \frac{9fx}{2}\right] + 15004 \cos\left[5e + \frac{9fx}{2}\right] - 1975 \cos\left[5e + \frac{11fx}{2}\right] - \cos\left[6e + \frac{11fx}{2}\right] + \\ & \quad 425964 \sin\left[\frac{fx}{2}\right] + 462 \sin\left[e + \frac{fx}{2}\right] + 330 \sin\left[e + \frac{3fx}{2}\right] + 299970 \sin\left[2e + \frac{3fx}{2}\right] - \\ & \quad 145695 \sin\left[2e + \frac{5fx}{2}\right] - 165 \sin\left[3e + \frac{5fx}{2}\right] - 55 \sin\left[3e + \frac{7fx}{2}\right] - 44990 \sin\left[4e + \frac{7fx}{2}\right] + \\ & \quad \left. 6710 \sin\left[4e + \frac{9fx}{2}\right] + 11 \sin\left[5e + \frac{9fx}{2}\right] + \sin\left[5e + \frac{11fx}{2}\right] - \sin\left[6e + \frac{11fx}{2}\right] \right) \end{aligned}$$

Problem 443: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^4 \sin[c+dx]^2 \sqrt{a+a \sin[c+dx]} dx$$

Optimal (type 3, 156 leaves, 5 steps):

$$\begin{aligned} & -\frac{1472 a^3 \cos[c+dx]^5}{45045 d (a+a \sin[c+dx])^{5/2}} - \frac{368 a^2 \cos[c+dx]^5}{9009 d (a+a \sin[c+dx])^{3/2}} - \frac{46 a \cos[c+dx]^5}{1287 d \sqrt{a+a \sin[c+dx]}} + \\ & \frac{20 \cos[c+dx]^5 \sqrt{a+a \sin[c+dx]}}{143 d} - \frac{2 \cos[c+dx]^5 (a+a \sin[c+dx])^{3/2}}{13 a d} \end{aligned}$$

Result (type 3, 619 leaves):

$$\frac{\left(5 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 3 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right]\right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{480 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} -$$

$$\frac{\left(9 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] - 7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right]\right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{1008 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} -$$

$$\frac{\left(13 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] - 11 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right]\right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{4576 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} +$$

$$\frac{\left(\frac{2 \operatorname{Cos}\left[\frac{dx}{2}\right] \operatorname{Sin}\left[\frac{c}{2}\right]}{d} + \frac{2 \operatorname{Cos}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right]}{d}\right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{16 \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} +$$

$$\frac{\left(-\frac{2 \operatorname{Cos}\left[\frac{c}{2}\right] \operatorname{Cos}\left[\frac{dx}{2}\right]}{d} + \frac{2 \operatorname{Sin}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right]}{d}\right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{16 \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} +$$

$$\frac{\sqrt{a(1+\operatorname{Sin}[c+dx])} \left(5 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + 3 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]\right)}{480 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} -$$

$$\frac{\sqrt{a(1+\operatorname{Sin}[c+dx])} \left(9 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + 7 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]\right)}{1008 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} -$$

$$\frac{\sqrt{a(1+\operatorname{Sin}[c+dx])} \left(13 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] + 11 \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]\right)}{4576 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)}$$

Problem 449: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^4 \operatorname{Csc}[c+dx] \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 173 leaves, 9 steps):

$$-\frac{67 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+dx]}{\sqrt{a+a \operatorname{Sin}[c+dx]}}\right]}{64 d} + \frac{61 a \operatorname{Cot}[c+dx]}{64 d \sqrt{a+a \operatorname{Sin}[c+dx]}} + \frac{61 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{96 d \sqrt{a+a \operatorname{Sin}[c+dx]}} -$$

$$\frac{a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{24 d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3 \sqrt{a+a \operatorname{Sin}[c+dx]}}{4 d}$$

Result (type 3, 367 leaves):

$$\begin{aligned}
 & \frac{1}{192 d \left(1 + \cot\left[\frac{1}{2}(c + dx)\right]\right) \left(\csc\left[\frac{1}{4}(c + dx)\right]^2 - \sec\left[\frac{1}{4}(c + dx)\right]^2\right)^4} \\
 & \csc\left[\frac{1}{2}(c + dx)\right]^{13} \sqrt{a(1 + \sin[c + dx])} \left(442 \cos\left[\frac{1}{2}(c + dx)\right] - 162 \cos\left[\frac{3}{2}(c + dx)\right] + \right. \\
 & \quad 122 \cos\left[\frac{5}{2}(c + dx)\right] + 366 \cos\left[\frac{7}{2}(c + dx)\right] + 603 \log\left[1 + \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] - \\
 & \quad 804 \cos[2(c + dx)] \log\left[1 + \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] + \\
 & \quad 201 \cos[4(c + dx)] \log\left[1 + \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] - \\
 & \quad 603 \log\left[1 - \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] + \\
 & \quad 804 \cos[2(c + dx)] \log\left[1 - \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] - \\
 & \quad 201 \cos[4(c + dx)] \log\left[1 - \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] - 442 \sin\left[\frac{1}{2}(c + dx)\right] - \\
 & \quad \left. 162 \sin\left[\frac{3}{2}(c + dx)\right] - 122 \sin\left[\frac{5}{2}(c + dx)\right] + 366 \sin\left[\frac{7}{2}(c + dx)\right]\right)
 \end{aligned}$$

Problem 453: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^4 \sin[c + dx]^2 (a + a \sin[c + dx])^{3/2} dx$$

Optimal (type 3, 188 leaves, 6 steps):

$$\begin{aligned}
 & \frac{256 a^4 \cos[c + dx]^5}{6435 d (a + a \sin[c + dx])^{5/2}} - \frac{64 a^3 \cos[c + dx]^5}{1287 d (a + a \sin[c + dx])^{3/2}} - \\
 & \frac{56 a^2 \cos[c + dx]^5}{1287 d \sqrt{a + a \sin[c + dx]}} - \frac{14 a \cos[c + dx]^5 \sqrt{a + a \sin[c + dx]}}{429 d} + \\
 & \frac{4 \cos[c + dx]^5 (a + a \sin[c + dx])^{3/2}}{39 d} - \frac{2 \cos[c + dx]^5 (a + a \sin[c + dx])^{5/2}}{15 a d}
 \end{aligned}$$

Result (type 3, 859 leaves):

$$\begin{aligned}
 & \frac{a \left(-\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{a(1+\operatorname{Sin}[c+dx])}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)} - \\
 & \left(a \left(3 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]^3 \right) \sqrt{a(1+\operatorname{Sin}[c+dx])} \right) / \\
 & \left(48d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \\
 & \left. \left(5 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 3 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] + 5 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + 3 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] \right) \right) / \\
 & \left(480d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \\
 & \left. \left(105 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + 35 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 21 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] - 15 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] - \right. \right. \\
 & \left. \left. 105 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 35 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + 21 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] - 15 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] \right) \right) / \\
 & \left(6720d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) - \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \\
 & \left. \left(9 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] - 7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] + 9 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + 7 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] \right) \right) / \\
 & \left(1008d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
 & \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right) \left(693 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] + 495 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] - \right. \\
 & \left. 385 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] - 315 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] - 693 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \right. \\
 & \left. 495 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + 385 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] - 315 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] \right) / \\
 & \left(110880d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) - \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \\
 & \left. \left(13 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] - 11 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] + 13 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] + 11 \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right] \right) \right) / \\
 & \left(4576d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
 & \left(a \sqrt{a(1+\operatorname{Sin}[c+dx])} \right) \left(715 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] + 585 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] - 495 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] - \right. \\
 & \left. 429 \operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] - 715 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] + 585 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] + 495 \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right] - \right. \\
 & \left. 429 \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right] \right) / \left(411840d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right)
 \end{aligned}$$

Problem 454: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^4 \operatorname{Sin}[c+dx] (a+a \operatorname{Sin}[c+dx])^{3/2} dx$$

Optimal (type 3, 156 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{256 a^4 \cos [c+d x]^5}{5005 d (a+a \sin [c+d x])^{5/2}} - \frac{64 a^3 \cos [c+d x]^5}{1001 d (a+a \sin [c+d x])^{3/2}} - \frac{8 a^2 \cos [c+d x]^5}{143 d \sqrt{a+a \sin [c+d x]}} - \\
 & \frac{6 a \cos [c+d x]^5 \sqrt{a+a \sin [c+d x]}}{143 d} - \frac{2 \cos [c+d x]^5 (a+a \sin [c+d x])^{3/2}}{13 d}
 \end{aligned}$$

Result (type 3, 673 leaves):

$$\begin{aligned}
 & - \left(\left(a \left(3 \cos \left[\frac{1}{2} (c+d x) \right] + \cos \left[\frac{3}{2} (c+d x) \right] - 4 \sin \left[\frac{1}{2} (c+d x) \right]^3 \right) \sqrt{a (1+\sin [c+d x])} \right) / \right. \\
 & \quad \left. \left(24 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) \right) - \\
 & \left(a \sqrt{a (1+\sin [c+d x])} \left(30 \cos \left[\frac{1}{2} (c+d x) \right] + 5 \cos \left[\frac{3}{2} (c+d x) \right] - 3 \cos \left[\frac{5}{2} (c+d x) \right] - \right. \right. \\
 & \quad \left. \left. 30 \sin \left[\frac{1}{2} (c+d x) \right] + 5 \sin \left[\frac{3}{2} (c+d x) \right] + 3 \sin \left[\frac{5}{2} (c+d x) \right] \right) \right) / \\
 & \left(240 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) - \left(3 a \sqrt{a (1+\sin [c+d x])} \right. \\
 & \quad \left. \left(7 \cos \left[\frac{5}{2} (c+d x) \right] + 5 \cos \left[\frac{7}{2} (c+d x) \right] - 7 \sin \left[\frac{5}{2} (c+d x) \right] + 5 \sin \left[\frac{7}{2} (c+d x) \right] \right) \right) / \\
 & \left(560 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) + \left(a \sqrt{a (1+\sin [c+d x])} \right. \\
 & \quad \left(105 \cos \left[\frac{3}{2} (c+d x) \right] - 63 \cos \left[\frac{5}{2} (c+d x) \right] - 45 \cos \left[\frac{7}{2} (c+d x) \right] + 35 \cos \left[\frac{9}{2} (c+d x) \right] + \right. \\
 & \quad \left. 105 \sin \left[\frac{3}{2} (c+d x) \right] + 63 \sin \left[\frac{5}{2} (c+d x) \right] - 45 \sin \left[\frac{7}{2} (c+d x) \right] - 35 \sin \left[\frac{9}{2} (c+d x) \right] \right) \right) / \\
 & \left(3360 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) - \left(a \sqrt{a (1+\sin [c+d x])} \right. \\
 & \quad \left. \left(11 \cos \left[\frac{9}{2} (c+d x) \right] + 9 \cos \left[\frac{11}{2} (c+d x) \right] - 11 \sin \left[\frac{9}{2} (c+d x) \right] + 9 \sin \left[\frac{11}{2} (c+d x) \right] \right) \right) / \\
 & \left(1584 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right) + \\
 & \left(a \sqrt{a (1+\sin [c+d x])} \left(1287 \cos \left[\frac{7}{2} (c+d x) \right] - 1001 \cos \left[\frac{9}{2} (c+d x) \right] - \right. \right. \\
 & \quad \left. \left. 819 \cos \left[\frac{11}{2} (c+d x) \right] + 693 \cos \left[\frac{13}{2} (c+d x) \right] + 1287 \sin \left[\frac{7}{2} (c+d x) \right] + \right. \right. \\
 & \quad \left. \left. 1001 \sin \left[\frac{9}{2} (c+d x) \right] - 819 \sin \left[\frac{11}{2} (c+d x) \right] - 693 \sin \left[\frac{13}{2} (c+d x) \right] \right) \right) / \\
 & \left(288288 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right)
 \end{aligned}$$

Problem 462: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^4 \csc [c+d x]^4 (a+a \sin [c+d x])^{3/2} dx$$

Optimal (type 3, 291 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{171 a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{1024 d} - \frac{171 a^2 \cot [c+d x]}{1024 d \sqrt{a+a \sin [c+d x]}} - \\
 & \frac{57 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]}{512 d \sqrt{a+a \sin [c+d x]}} + \frac{199 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^2}{640 d \sqrt{a+a \sin [c+d x]}} + \\
 & \frac{1237 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^3}{2240 d \sqrt{a+a \sin [c+d x]}} + \frac{9 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^4}{40 d \sqrt{a+a \sin [c+d x]}} - \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^5 \sqrt{a+a \sin [c+d x]}}{28 d} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^6 (a+a \sin [c+d x])^{3/2}}{7 d}
 \end{aligned}$$

Result (type 3, 2055 leaves):

$$\begin{aligned}
 & \frac{3861 (a (1 + \sin [c+d x]))^{3/2}}{71680 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
 & \frac{3861 \cot \left[\frac{1}{4}(c+d x)\right] (a (1 + \sin [c+d x]))^{3/2}}{143360 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} - \frac{43 \operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2 (a (1 + \sin [c+d x]))^{3/2}}{8192 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
 & \frac{619 \cot \left[\frac{1}{4}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2 (a (1 + \sin [c+d x]))^{3/2}}{286720 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
 & \frac{11 \operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^4 (a (1 + \sin [c+d x]))^{3/2}}{8192 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
 & \frac{9 \cot \left[\frac{1}{4}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^4 (a (1 + \sin [c+d x]))^{3/2}}{143360 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
 & \frac{\operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^6 (a (1 + \sin [c+d x]))^{3/2}}{16384 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
 & \frac{\cot \left[\frac{1}{4}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^6 (a (1 + \sin [c+d x]))^{3/2}}{114688 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
 & \left(171 \log \left[1 + \cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] (a (1 + \sin [c+d x]))^{3/2}\right) / \\
 & \left(2048 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3\right) + \\
 & \left(171 \log \left[1 - \cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] (a (1 + \sin [c+d x]))^{3/2}\right) / \\
 & \left(2048 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^3\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{43 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 (a(1+\sin[c+dx]))^{3/2}}{8192 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{11 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 (a(1+\sin[c+dx]))^{3/2}}{8192 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^6 (a(1+\sin[c+dx]))^{3/2}}{16384 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + (a(1+\sin[c+dx]))^{3/2} / \\
 & \left(1792 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^6 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) - \\
 & \left(403 (a(1+\sin[c+dx]))^{3/2}\right) / \left(71680 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^4 \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) + \left(443 (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(71680 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) + \\
 & \left(\sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(7168 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^7 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) - \\
 & \left(9 \sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(17920 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^5 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) - \\
 & \left(619 \sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(71680 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) + \\
 & \left(3861 \sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(71680 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) - \\
 & \left(\sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(7168 d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^7 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) - \\
 & \left(3 (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(7168 d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^6 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) + \\
 & \left(9 \sin\left[\frac{1}{4}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}\right) / \\
 & \left(17920 d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^5 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3\right) + \\
 & \left(367 (a(1+\sin[c+dx]))^{3/2}\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(71\,680\,d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) + \\
 & \left(619 \sin\left[\frac{1}{4}(c+dx)\right] \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) / \\
 & \left(71\,680\,d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) - \\
 & \left(531 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) / \\
 & \left(35\,840\,d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) - \\
 & \left(3861 \sin\left[\frac{1}{4}(c+dx)\right] \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \right) / \\
 & \left(71\,680\,d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) - \\
 & \frac{3861 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \tan\left[\frac{1}{4}(c+dx)\right]}{143\,360\,d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
 & \frac{619 \sec\left[\frac{1}{4}(c+dx)\right]^2 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \tan\left[\frac{1}{4}(c+dx)\right]}{286\,720\,d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
 & \frac{9 \sec\left[\frac{1}{4}(c+dx)\right]^4 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \tan\left[\frac{1}{4}(c+dx)\right]}{143\,360\,d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} - \\
 & \frac{\sec\left[\frac{1}{4}(c+dx)\right]^6 \left(a \left(1 + \sin[c+dx] \right) \right)^{3/2} \tan\left[\frac{1}{4}(c+dx)\right]}{114\,688\,d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}
 \end{aligned}$$

Problem 463: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^4 \csc[c+dx]^5 (a+a \sin[c+dx])^{3/2} dx$$

Optimal (type 3, 329 leaves, 18 steps):

$$\begin{aligned}
 & \frac{1587 a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{16\,384\,d} - \frac{1587 a^2 \cot[c+dx]}{16\,384\,d \sqrt{a+a \sin[c+dx]}} - \frac{529 a^2 \cot[c+dx] \csc[c+dx]}{8192\,d \sqrt{a+a \sin[c+dx]}} - \\
 & \frac{529 a^2 \cot[c+dx] \csc[c+dx]^2}{10\,240\,d \sqrt{a+a \sin[c+dx]}} + \frac{8653 a^2 \cot[c+dx] \csc[c+dx]^3}{35\,840\,d \sqrt{a+a \sin[c+dx]}} + \\
 & \frac{1957 a^2 \cot[c+dx] \csc[c+dx]^4}{4480\,d \sqrt{a+a \sin[c+dx]}} + \frac{83 a^2 \cot[c+dx] \csc[c+dx]^5}{448\,d \sqrt{a+a \sin[c+dx]}} - \\
 & \frac{3 a \cot[c+dx] \csc[c+dx]^6 \sqrt{a+a \sin[c+dx]}}{112\,d} - \frac{\cot[c+dx] \csc[c+dx]^7 (a+a \sin[c+dx])^{3/2}}{8\,d}
 \end{aligned}$$

Result (type 3, 2303 leaves):

$$\begin{aligned}
 & \frac{6053 (a (1 + \sin [c + d x]))^{3/2}}{143360 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \\
 & \frac{6053 \cot \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2}}{286720 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \frac{179 \operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^2 (a (1 + \sin [c + d x]))^{3/2}}{131072 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{107 \cot \left[\frac{1}{4} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^2 (a (1 + \sin [c + d x]))^{3/2}}{573440 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{113 \operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^4 (a (1 + \sin [c + d x]))^{3/2}}{262144 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{31 \cot \left[\frac{1}{4} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^4 (a (1 + \sin [c + d x]))^{3/2}}{143360 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{\operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^6 (a (1 + \sin [c + d x]))^{3/2}}{131072 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \\
 & \frac{3 \cot \left[\frac{1}{4} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^6 (a (1 + \sin [c + d x]))^{3/2}}{229376 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \\
 & \frac{\operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^8 (a (1 + \sin [c + d x]))^{3/2}}{524288 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \\
 & \left(\frac{1587 \log \left[1 + \cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] (a (1 + \sin [c + d x]))^{3/2}}{32768 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} \right) + \\
 & \left(\frac{1587 \log \left[1 - \cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] (a (1 + \sin [c + d x]))^{3/2}}{32768 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} \right) + \\
 & \frac{179 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 (a (1 + \sin [c + d x]))^{3/2}}{131072 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \frac{113 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^4 (a (1 + \sin [c + d x]))^{3/2}}{262144 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} - \\
 & \frac{\operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^6 (a (1 + \sin [c + d x]))^{3/2}}{131072 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{\operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^8 (a (1 + \sin [c + d x]))^{3/2}}{524288 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} + (a (1 + \sin [c + d x]))^{3/2} /
 \end{aligned}$$

$$\begin{aligned}
& \left(32768 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^8 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(5 (a (1 + \sin [c + d x]))^{3/2} \right) / \left(114688 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^6 \\
& \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \left(5939 (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(2293760 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(5409 (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(2293760 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^2 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(3 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(14336 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^7 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \\
& \left(31 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(17920 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^5 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \\
& \left(107 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(143360 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(6053 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(143360 d \left(\cos \left[\frac{1}{4} (c + d x) \right] - \sin \left[\frac{1}{4} (c + d x) \right] \right) \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \\
& (a (1 + \sin [c + d x]))^{3/2} / \\
& \left(32768 d \left(\cos \left[\frac{1}{4} (c + d x) \right] + \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^8 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \\
& \left(3 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(14336 d \left(\cos \left[\frac{1}{4} (c + d x) \right] + \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^7 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(19 (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(114688 d \left(\cos \left[\frac{1}{4} (c + d x) \right] + \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^6 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(31 \sin \left[\frac{1}{4} (c + d x) \right] (a (1 + \sin [c + d x]))^{3/2} \right) / \\
& \left(17920 d \left(\cos \left[\frac{1}{4} (c + d x) \right] + \sin \left[\frac{1}{4} (c + d x) \right] \right) \right)^5 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + \\
& \left(1971 (a (1 + \sin [c + d x]))^{3/2} \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left(2293760 d \left(\cos \left[\frac{1}{4} (c+dx) \right] + \sin \left[\frac{1}{4} (c+dx) \right] \right)^4 \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3 \right) + \\
 & \left(107 \sin \left[\frac{1}{4} (c+dx) \right] (a(1+\sin[c+dx]))^{3/2} \right) / \\
 & \left(143360 d \left(\cos \left[\frac{1}{4} (c+dx) \right] + \sin \left[\frac{1}{4} (c+dx) \right] \right)^3 \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3 \right) - \\
 & \left(7121 (a(1+\sin[c+dx]))^{3/2} \right) / \\
 & \left(2293760 d \left(\cos \left[\frac{1}{4} (c+dx) \right] + \sin \left[\frac{1}{4} (c+dx) \right] \right)^2 \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3 \right) - \\
 & \left(6053 \sin \left[\frac{1}{4} (c+dx) \right] (a(1+\sin[c+dx]))^{3/2} \right) / \\
 & \left(143360 d \left(\cos \left[\frac{1}{4} (c+dx) \right] + \sin \left[\frac{1}{4} (c+dx) \right] \right) \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3 \right) - \\
 & \frac{6053 (a(1+\sin[c+dx]))^{3/2} \tan \left[\frac{1}{4} (c+dx) \right]}{286720 d \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3} + \\
 & \frac{107 \sec \left[\frac{1}{4} (c+dx) \right]^2 (a(1+\sin[c+dx]))^{3/2} \tan \left[\frac{1}{4} (c+dx) \right]}{573440 d \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3} + \\
 & \frac{31 \sec \left[\frac{1}{4} (c+dx) \right]^4 (a(1+\sin[c+dx]))^{3/2} \tan \left[\frac{1}{4} (c+dx) \right]}{143360 d \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3} - \\
 & \frac{3 \sec \left[\frac{1}{4} (c+dx) \right]^6 (a(1+\sin[c+dx]))^{3/2} \tan \left[\frac{1}{4} (c+dx) \right]}{229376 d \left(\cos \left[\frac{1}{2} (c+dx) \right] + \sin \left[\frac{1}{2} (c+dx) \right] \right)^3}
 \end{aligned}$$

Problem 468: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx] \cot[c+dx]^3}{\sqrt{a+a \sin[c+dx]}} dx$$

Optimal (type 3, 125 leaves, 11 steps):

$$\frac{9 \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}} \right]}{4 \sqrt{a} d} - \frac{2 \cos[c+dx]}{d \sqrt{a+a \sin[c+dx]}} + \\
 \frac{\cot[c+dx]}{4 d \sqrt{a+a \sin[c+dx]}} - \frac{\cot[c+dx] \operatorname{Csc}[c+dx]}{2 d \sqrt{a+a \sin[c+dx]}}$$

Result (type 3, 773 leaves):

$$\begin{aligned}
& - \frac{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]}{4d\sqrt{a(1+\sin[c+dx])}} - \frac{2\cos\left[\frac{1}{2}(c+dx)\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{d\sqrt{a(1+\sin[c+dx])}} + \\
& \frac{\cot\left[\frac{1}{4}(c+dx)\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{8d\sqrt{a(1+\sin[c+dx])}} - \\
& \frac{\csc\left[\frac{1}{4}(c+dx)\right]^2\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{32d\sqrt{a(1+\sin[c+dx])}} + \\
& \left(9\log\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
& \left(8d\sqrt{a(1+\sin[c+dx])}\right) - \\
& \left(9\log\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
& \left(8d\sqrt{a(1+\sin[c+dx])}\right) + \frac{\sec\left[\frac{1}{4}(c+dx)\right]^2\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{32d\sqrt{a(1+\sin[c+dx])}} + \\
& \frac{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]}{16d\left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2\sqrt{a(1+\sin[c+dx])}} - \\
& \frac{\sin\left[\frac{1}{4}(c+dx)\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{4d\left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)\sqrt{a(1+\sin[c+dx])}} - \\
& \frac{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]}{16d\left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^2\sqrt{a(1+\sin[c+dx])}} + \\
& \frac{\sin\left[\frac{1}{4}(c+dx)\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{4d\left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)\sqrt{a(1+\sin[c+dx])}} + \\
& \frac{2\sin\left[\frac{1}{2}(c+dx)\right]\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}{d\sqrt{a(1+\sin[c+dx])}} + \\
& \frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\tan\left[\frac{1}{4}(c+dx)\right]}{8d\sqrt{a(1+\sin[c+dx])}}
\end{aligned}$$

Problem 469: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot[c+dx]^4}{\sqrt{a+a\sin[c+dx]}} dx$$

Optimal (type 3, 135 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{7 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{8 \sqrt{a} d} + \frac{9 \cot [c+d x]}{8 d \sqrt{a+a \sin [c+d x]}} + \\
 & \frac{\cot [c+d x] \csc [c+d x]}{12 d \sqrt{a+a \sin [c+d x]}} - \frac{\cot [c+d x] \csc [c+d x]^2}{3 d \sqrt{a+a \sin [c+d x]}}
 \end{aligned}$$

Result (type 3, 292 leaves):

$$\begin{aligned}
 & \frac{1}{24 d \left(\csc \left[\frac{1}{4} (c+d x) \right]^2 - \sec \left[\frac{1}{4} (c+d x) \right]^2 \right)^3 \sqrt{a (1+\sin [c+d x])}} \\
 & \csc \left[\frac{1}{2} (c+d x) \right]^9 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \\
 & \left(36 \cos \left[\frac{1}{2} (c+d x) \right] - 46 \cos \left[\frac{3}{2} (c+d x) \right] - 54 \cos \left[\frac{5}{2} (c+d x) \right] - \right. \\
 & \quad \left. 36 \sin \left[\frac{1}{2} (c+d x) \right] - 63 \log \left[1 + \cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] \sin [c+d x] + \right. \\
 & \quad \left. 63 \log \left[1 - \cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right] \sin [c+d x] - 46 \sin \left[\frac{3}{2} (c+d x) \right] + \right. \\
 & \quad \left. 54 \sin \left[\frac{5}{2} (c+d x) \right] + 21 \log \left[1 + \cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] \sin [3(c+d x)] - \right. \\
 & \quad \left. 21 \log \left[1 - \cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right] \sin [3(c+d x)] \right)
 \end{aligned}$$

Problem 470: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^4 \csc [c+d x]}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 170 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{11 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{64 \sqrt{a} d} - \frac{11 \cot [c+d x]}{64 d \sqrt{a+a \sin [c+d x]}} + \\
 & \frac{53 \cot [c+d x] \csc [c+d x]}{96 d \sqrt{a+a \sin [c+d x]}} + \frac{\cot [c+d x] \csc [c+d x]^2}{24 d \sqrt{a+a \sin [c+d x]}} - \frac{\cot [c+d x] \csc [c+d x]^3}{4 d \sqrt{a+a \sin [c+d x]}}
 \end{aligned}$$

Result (type 3, 374 leaves):

$$\frac{1}{192 d \left(\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 - \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \right)^4 \sqrt{a(1+\sin[c+dx])}}$$

$$\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^{12} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)$$

$$\left(214 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - 558 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 490 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] + \right.$$

$$66 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] - 99 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$132 \operatorname{Cos}\left[2(c+dx)\right] \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] -$$

$$33 \operatorname{Cos}\left[4(c+dx)\right] \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$99 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] -$$

$$132 \operatorname{Cos}\left[2(c+dx)\right] \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$33 \operatorname{Cos}\left[4(c+dx)\right] \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 214 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] -$$

$$558 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + 490 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + 66 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] \Big)$$

Problem 476: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx]^2 \operatorname{Cot}[c+dx]^2}{(a+a \operatorname{Sin}[c+dx])^{3/2}} dx$$

Optimal (type 3, 94 leaves, 9 steps):

$$\frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+dx]}{\sqrt{a+a \operatorname{Sin}[c+dx]}}\right]}{a^{3/2} d} - \frac{\operatorname{Cos}[c+dx]}{a d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{\operatorname{Cot}[c+dx] \sqrt{a+a \operatorname{Sin}[c+dx]}}{a^2 d}$$

Result (type 3, 220 leaves):

$$\left(\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3 \right.$$

$$\left(2 - 8 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Cot}\left[\frac{1}{4}(c+dx)\right] + 6 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right.$$

$$6 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$\frac{2 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} - \frac{2 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} +$$

$$\left. \left. \left. 8 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right) \right) \right) / (4 d (a (1 + \operatorname{Sin}[c+dx]))^{3/2})$$

Problem 477: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \cot [c+d x]^3}{(a+a \sin [c+d x])^{3 / 2}} d x$$

Optimal (type 3, 106 leaves, 8 steps):

$$-\frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{4 a^{3 / 2} d}+\frac{7 \cot [c+d x]}{4 a d \sqrt{a+a \sin [c+d x]}}-\frac{\cot [c+d x] \operatorname{Csc}[c+d x] \sqrt{a+a \sin [c+d x]}}{2 a^2 d}$$

Result (type 3, 274 leaves):

$$\frac{1}{32 d(a(1+\sin [c+d x]))^{3 / 2}}\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^3$$

$$\left(-24+12 \cot \left[\frac{1}{4}(c+d x)\right]-\operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2-12 \log \left[1+\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]+12 \log \left[1-\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]+\operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2+\frac{2}{\left(\cos \left[\frac{1}{4}(c+d x)\right]-\sin \left[\frac{1}{4}(c+d x)\right]\right)^2}-\frac{24 \sin \left[\frac{1}{4}(c+d x)\right]}{\cos \left[\frac{1}{4}(c+d x)\right]-\sin \left[\frac{1}{4}(c+d x)\right]}-\frac{2}{\left(\cos \left[\frac{1}{4}(c+d x)\right]+\sin \left[\frac{1}{4}(c+d x)\right]\right)^2}+\frac{24 \sin \left[\frac{1}{4}(c+d x)\right]}{\cos \left[\frac{1}{4}(c+d x)\right]+\sin \left[\frac{1}{4}(c+d x)\right]}+12 \tan \left[\frac{1}{4}(c+d x)\right]\right)$$

Problem 478: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^4}{(a+a \sin [c+d x])^{3 / 2}} d x$$

Optimal (type 3, 144 leaves, 10 steps):

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{8 a^{3 / 2} d}-\frac{\cot [c+d x]}{8 a d \sqrt{a+a \sin [c+d x]}}+\frac{11 \cot [c+d x] \operatorname{Csc}[c+d x]}{12 a d \sqrt{a+a \sin [c+d x]}}-\frac{\cot [c+d x] \operatorname{Csc}[c+d x]^2 \sqrt{a+a \sin [c+d x]}}{3 a^2 d}$$

Result (type 3, 294 leaves):

$$\frac{1}{24 d \left(\operatorname{Csc}\left[\frac{1}{4}(c+d x)\right]^2 - \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \right)^3 \left(a \left(1 + \operatorname{Sin}[c+d x] \right) \right)^{3/2}}$$

$$\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^9 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3$$

$$\left(-132 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + 62 \operatorname{Cos}\left[\frac{3}{2}(c+d x)\right] + 6 \operatorname{Cos}\left[\frac{5}{2}(c+d x)\right] + \right.$$

$$132 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - 9 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x] +$$

$$9 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x] + 62 \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right] -$$

$$6 \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right] + 3 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[3(c+d x)] -$$

$$\left. 3 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[3(c+d x)] \right)$$

Problem 479: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+d x]^4 \operatorname{Csc}[c+d x]}{(a+a \operatorname{Sin}[c+d x])^{3/2}} dx$$

Optimal (type 3, 182 leaves, 12 steps):

$$-\frac{3 \operatorname{ArcTanh}\left[\frac{-\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{a+a \operatorname{Sin}[c+d x]}}\right]}{64 a^{3/2} d} - \frac{3 \operatorname{Cot}[c+d x]}{64 a d \sqrt{a+a \operatorname{Sin}[c+d x]}} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{32 a d \sqrt{a+a \operatorname{Sin}[c+d x]}} +$$

$$\frac{5 \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2}{8 a d \sqrt{a+a \operatorname{Sin}[c+d x]}} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3 \sqrt{a+a \operatorname{Sin}[c+d x]}}{4 a^2 d}$$

Result (type 3, 376 leaves):

$$\begin{aligned}
 & - \left(1 / \left(64 d \left(\operatorname{Csc} \left[\frac{1}{4} (c + d x) \right]^2 - \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \right)^4 (a (1 + \operatorname{Sin}[c + d x]))^{3/2} \right) \right) \\
 & \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^{12} \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^3 \\
 & \left(446 \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - 182 \operatorname{Cos} \left[\frac{3}{2} (c + d x) \right] - 2 \operatorname{Cos} \left[\frac{5}{2} (c + d x) \right] - \right. \\
 & \quad \left. 6 \operatorname{Cos} \left[\frac{7}{2} (c + d x) \right] + 9 \operatorname{Log} \left[1 + \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad \left. 12 \operatorname{Cos} \left[2 (c + d x) \right] \operatorname{Log} \left[1 + \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \right. \\
 & \quad \left. 3 \operatorname{Cos} \left[4 (c + d x) \right] \operatorname{Log} \left[1 + \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad \left. 9 \operatorname{Log} \left[1 - \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \right. \\
 & \quad \left. 12 \operatorname{Cos} \left[2 (c + d x) \right] \operatorname{Log} \left[1 - \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad \left. 3 \operatorname{Cos} \left[4 (c + d x) \right] \operatorname{Log} \left[1 - \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad \left. 446 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] - 182 \operatorname{Sin} \left[\frac{3}{2} (c + d x) \right] + 2 \operatorname{Sin} \left[\frac{5}{2} (c + d x) \right] - 6 \operatorname{Sin} \left[\frac{7}{2} (c + d x) \right] \right)
 \end{aligned}$$

Problem 481: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c + d x]^4 \operatorname{Sin}[c + d x]^4}{(a + a \operatorname{Sin}[c + d x])^{5/2}} dx$$

Optimal (type 3, 260 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{4 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \operatorname{Cos}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sin}[c + d x]}} \right]}{a^{5/2} d} + \frac{4496 \operatorname{Cos}[c + d x]}{693 a^2 d \sqrt{a + a \operatorname{Sin}[c + d x]}} + \\
 & \frac{200 \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^2}{231 a^2 d \sqrt{a + a \operatorname{Sin}[c + d x]}} - \frac{424 \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^3}{693 a^2 d \sqrt{a + a \operatorname{Sin}[c + d x]}} + \frac{46 \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^4}{99 a^2 d \sqrt{a + a \operatorname{Sin}[c + d x]}} - \\
 & \frac{2 \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^5}{11 a^2 d \sqrt{a + a \operatorname{Sin}[c + d x]}} - \frac{1048 \operatorname{Cos}[c + d x] \sqrt{a + a \operatorname{Sin}[c + d x]}}{693 a^3 d}
 \end{aligned}$$

Result (type 3, 224 leaves):

$$\frac{1}{11088 d (a (1 + \sin [c + d x]))^{5/2}} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5$$

$$\left((88704 + 88704 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \right) +$$

$$73458 \cos \left[\frac{1}{2} (c + d x) \right] - 15246 \cos \left[\frac{3}{2} (c + d x) \right] - 4851 \cos \left[\frac{5}{2} (c + d x) \right] +$$

$$1485 \cos \left[\frac{7}{2} (c + d x) \right] + 385 \cos \left[\frac{9}{2} (c + d x) \right] - 63 \cos \left[\frac{11}{2} (c + d x) \right] -$$

$$73458 \sin \left[\frac{1}{2} (c + d x) \right] - 15246 \sin \left[\frac{3}{2} (c + d x) \right] + 4851 \sin \left[\frac{5}{2} (c + d x) \right] +$$

$$1485 \sin \left[\frac{7}{2} (c + d x) \right] - 385 \sin \left[\frac{9}{2} (c + d x) \right] - 63 \sin \left[\frac{11}{2} (c + d x) \right]$$

Problem 482: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c + d x]^4 \sin [c + d x]^3}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 222 leaves, 16 steps):

$$\frac{4 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{2} \sqrt{a + a \sin [c + d x]}} \right]}{a^{5/2} d} - \frac{2048 \cos [c + d x]}{315 a^2 d \sqrt{a + a \sin [c + d x]}} - \frac{92 \cos [c + d x] \sin [c + d x]^2}{105 a^2 d \sqrt{a + a \sin [c + d x]}} +$$

$$\frac{38 \cos [c + d x] \sin [c + d x]^3}{63 a^2 d \sqrt{a + a \sin [c + d x]}} - \frac{2 \cos [c + d x] \sin [c + d x]^4}{9 a^2 d \sqrt{a + a \sin [c + d x]}} + \frac{472 \cos [c + d x] \sqrt{a + a \sin [c + d x]}}{315 a^3 d}$$

Result (type 3, 225 leaves):

$$\frac{1}{2520 a^3 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)}$$

$$\sqrt{a (1 + \sin [c + d x])} \left((20160 + 20160 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \operatorname{Sec} \left[\frac{d x}{4} \right] \left(\cos \left[\frac{1}{4} (2 c + d x) \right] - \sin \left[\frac{1}{4} (2 c + d x) \right] \right) \right] \right) -$$

$$16380 \cos \left[\frac{1}{2} (c + d x) \right] + 3150 \cos \left[\frac{3}{2} (c + d x) \right] + 882 \cos \left[\frac{5}{2} (c + d x) \right] -$$

$$225 \cos \left[\frac{7}{2} (c + d x) \right] - 35 \cos \left[\frac{9}{2} (c + d x) \right] + 16380 \sin \left[\frac{1}{2} (c + d x) \right] +$$

$$3150 \sin \left[\frac{3}{2} (c + d x) \right] - 882 \sin \left[\frac{5}{2} (c + d x) \right] - 225 \sin \left[\frac{7}{2} (c + d x) \right] + 35 \sin \left[\frac{9}{2} (c + d x) \right]$$

Problem 483: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c + d x]^4 \sin [c + d x]^2}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} + \frac{4 \cos [c+d x]^5}{7 d (a+a \sin [c+d x])^{5/2}} + \\
 & \frac{2 \cos [c+d x]^3}{3 a d (a+a \sin [c+d x])^{3/2}} - \frac{2 \cos [c+d x]^5}{7 a d (a+a \sin [c+d x])^{3/2}} + \frac{4 \cos [c+d x]}{a^2 d \sqrt{a+a \sin [c+d x]}}
 \end{aligned}$$

Result (type 3, 201 leaves):

$$\begin{aligned}
 & - \frac{1}{84 a^3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)} \sqrt{a(1+\sin [c+d x])} \left((672+672 i) (-1)^{3/4} \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \sec \left[\frac{d x}{4}\right] \left(\cos \left[\frac{1}{4}(2 c+d x)\right] - \sin \left[\frac{1}{4}(2 c+d x)\right]\right)\right] - \right. \\
 & \quad \left. 525 \cos \left[\frac{1}{2}(c+d x)\right] + 91 \cos \left[\frac{3}{2}(c+d x)\right] + 21 \cos \left[\frac{5}{2}(c+d x)\right] - 3 \cos \left[\frac{7}{2}(c+d x)\right] + \right. \\
 & \quad \left. 525 \sin \left[\frac{1}{2}(c+d x)\right] + 91 \sin \left[\frac{3}{2}(c+d x)\right] - 21 \sin \left[\frac{5}{2}(c+d x)\right] - 3 \sin \left[\frac{7}{2}(c+d x)\right] \right)
 \end{aligned}$$

Problem 484: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]}{(a+a \sin [c+d x])^{5/2}} dx$$

Optimal (type 3, 137 leaves, 5 steps):

$$\begin{aligned}
 & \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} - \frac{2 \cos [c+d x]^5}{5 d (a+a \sin [c+d x])^{5/2}} - \\
 & \frac{2 \cos [c+d x]^3}{3 a d (a+a \sin [c+d x])^{3/2}} - \frac{4 \cos [c+d x]}{a^2 d \sqrt{a+a \sin [c+d x]}}
 \end{aligned}$$

Result (type 3, 177 leaves):

$$\begin{aligned}
 & \left(\sqrt{a(1+\sin [c+d x])} \left((240+240 i) (-1)^{3/4} \right. \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \sec \left[\frac{d x}{4}\right] \left(\cos \left[\frac{1}{4}(2 c+d x)\right] - \sin \left[\frac{1}{4}(2 c+d x)\right]\right)\right] - \right. \\
 & \quad \left. 180 \cos \left[\frac{1}{2}(c+d x)\right] + 25 \cos \left[\frac{3}{2}(c+d x)\right] + 3 \cos \left[\frac{5}{2}(c+d x)\right] + \right. \\
 & \quad \left. 180 \sin \left[\frac{1}{2}(c+d x)\right] + 25 \sin \left[\frac{3}{2}(c+d x)\right] - 3 \sin \left[\frac{5}{2}(c+d x)\right] \right) \Big/ \\
 & \left(30 a^3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right) \right)
 \end{aligned}$$

Problem 485: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]}{(a+a \sin [c+d x])^{5/2}} dx$$

Optimal (type 3, 113 leaves, 9 steps):

$$-\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} + \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} - \frac{2 \cos [c+d x]}{a^2 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 154 leaves):

$$-\left(\left(\left((8+8 i)(-1)^{3/4} \operatorname{ArcTanh}\left[\frac{1}{2}+\frac{i}{2}\right](-1)^{3/4}\left(-1+\tan \left[\frac{1}{4}(c+d x)\right]\right)\right)\right)+\right. \\ \left.2 \cos \left[\frac{1}{2}(c+d x)\right]+\log \left[1+\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]-\right. \\ \left.\log \left[1-\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]-2 \sin \left[\frac{1}{2}(c+d x)\right]\right) \\ \left.\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^5\right) / \left(d\left(a\left(1+\sin [c+d x]\right)\right)^{5/2}\right)$$

Problem 486: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^2 \cot [c+d x]^2}{(a+a \sin [c+d x])^{5/2}} dx$$

Optimal (type 3, 113 leaves, 12 steps):

$$\frac{5 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} - \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{a^{5/2} d} - \frac{\cot [c+d x]}{a^2 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 170 leaves):

$$\left(\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^5\right. \\ \left.\left(\left(32+32 i\right)(-1)^{3/4} \operatorname{ArcTanh}\left[\frac{1}{2}+\frac{i}{2}\right](-1)^{3/4}\left(-1+\tan \left[\frac{1}{4}(c+d x)\right]\right)\right)\right)- \\ \cot \left[\frac{1}{4}(c+d x)\right]+10 \log \left[1+\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]- \\ 10 \log \left[1-\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]+2 \sec \left[\frac{1}{2}(c+d x)\right]- \\ \tan \left[\frac{1}{4}(c+d x)\right]\right) / \left(4 d\left(a\left(1+\sin [c+d x]\right)\right)^{5/2}\right)$$

Problem 487: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \cot [c+d x]^3}{(a+a \sin [c+d x])^{5/2}} dx$$

Optimal (type 3, 153 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{23 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{4 a^{5/2} d} + \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{a^{5/2} d} + \\
 & \frac{9 \cot[c+dx]}{4 a^2 d \sqrt{a+a \sin[c+dx]}} - \frac{\cot[c+dx] \operatorname{Csc}[c+dx]}{2 a^2 d \sqrt{a+a \sin[c+dx]}}
 \end{aligned}$$

Result (type 3, 791 leaves):

$$\begin{aligned}
 & - \frac{5 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{4 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} + \left((8+8i) (-1)^{3/4} \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)\right] \right) \\
 & \quad \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \Big/ \left(d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2} \right) + \\
 & \frac{5 \cot\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{8 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} - \\
 & \frac{\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{32 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} - \\
 & \frac{\left(23 \operatorname{Log}\left[1 + \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) \Big/}{\left(8 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2} \right) +} \\
 & \frac{\left(23 \operatorname{Log}\left[1 - \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) \Big/}{\left(8 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2} \right) +} \\
 & \frac{\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{32 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} + \\
 & \frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{16 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} - \\
 & \frac{5 \sin\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{4 d \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right) \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} - \\
 & \frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{16 d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} + \\
 & \frac{5 \sin\left[\frac{1}{4}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5}{4 d \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right) \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}} + \\
 & \frac{5 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{8 d \left(a \left(1 + \sin[c+dx] \right) \right)^{5/2}}
 \end{aligned}$$

Problem 488: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Cot}[c + d x]^4}{(a + a \text{Sin}[c + d x])^{5/2}} dx$$

Optimal (type 3, 191 leaves, 16 steps):

$$\frac{45 \text{ArcTanh}\left[\frac{\sqrt{a} \text{Cos}[c+dx]}{\sqrt{a+a \text{Sin}[c+dx]}}\right]}{8 a^{5/2} d} - \frac{4 \sqrt{2} \text{ArcTanh}\left[\frac{\sqrt{a} \text{Cos}[c+dx]}{\sqrt{2} \sqrt{a+a \text{Sin}[c+dx]}}\right]}{a^{5/2} d} - \frac{19 \text{Cot}[c+dx]}{8 a^2 d \sqrt{a+a \text{Sin}[c+dx]}} + \frac{13 \text{Cot}[c+dx] \text{Csc}[c+dx]}{12 a^2 d \sqrt{a+a \text{Sin}[c+dx]}} - \frac{\text{Cot}[c+dx] \text{Csc}[c+dx]^2}{3 a^2 d \sqrt{a+a \text{Sin}[c+dx]}}$$

Result (type 3, 332 leaves):

$$\frac{1}{192 d (a (1 + \text{Sin}[c + d x]))^{5/2}} \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right] \right)^5 \left((1536 + 1536 i) (-1)^{3/4} \text{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \text{Tan}\left[\frac{1}{4} (c + d x)\right]\right)\right] - \frac{1}{\left(\text{Csc}\left[\frac{1}{4} (c + d x)\right]^2 - \text{Sec}\left[\frac{1}{4} (c + d x)\right]^2\right)^3} 8 \text{Csc}\left[\frac{1}{2} (c + d x)\right]^9 \left(396 \text{Cos}\left[\frac{1}{2} (c + d x)\right] - 218 \text{Cos}\left[\frac{3}{2} (c + d x)\right] - 114 \text{Cos}\left[\frac{5}{2} (c + d x)\right] - 396 \text{Sin}\left[\frac{1}{2} (c + d x)\right] - 405 \text{Log}\left[1 + \text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \text{Sin}[c + d x] + 405 \text{Log}\left[1 - \text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \text{Sin}[c + d x] - 218 \text{Sin}\left[\frac{3}{2} (c + d x)\right] + 114 \text{Sin}\left[\frac{5}{2} (c + d x)\right] + 135 \text{Log}\left[1 + \text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \text{Sin}[3 (c + d x)] - 135 \text{Log}\left[1 - \text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \text{Sin}[3 (c + d x)] \right) \right)$$

Problem 489: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^4 \text{Csc}[c + d x]}{(a + a \text{Sin}[c + d x])^{5/2}} dx$$

Optimal (type 3, 229 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{363 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{a+a \sin[c+dx]}}\right]}{64 a^{5/2} d} + \frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{a^{5/2} d} + \frac{149 \operatorname{Cot}[c+dx]}{64 a^2 d \sqrt{a+a \sin[c+dx]}} - \\
 & \frac{107 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{96 a^2 d \sqrt{a+a \sin[c+dx]}} + \frac{17 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{24 a^2 d \sqrt{a+a \sin[c+dx]}} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4 a^2 d \sqrt{a+a \sin[c+dx]}}
 \end{aligned}$$

Result (type 3, 1327 leaves):

$$\begin{aligned}
 & - \frac{155 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{96 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} + \left((8+8i) (-1)^{3/4} \right. \\
 & \quad \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \right)\right] \\
 & \quad \left. \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) / \left(d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2} \right) + \\
 & \frac{155 \operatorname{Cot}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{192 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} - \\
 & \frac{51 \operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{512 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} + \\
 & \left(5 \operatorname{Cot}\left[\frac{1}{4}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) / \\
 & \left(384 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2} \right) - \frac{\operatorname{Csc}\left[\frac{1}{4}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{1024 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} - \\
 & \left(363 \operatorname{Log}\left[1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) / \\
 & \left(128 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2} \right) + \\
 & \left(363 \operatorname{Log}\left[1 - \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5 \right) / \\
 & \left(128 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2} \right) + \frac{51 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{512 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} + \\
 & \frac{\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{1024 d \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} + \\
 & \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{256 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \right)^4 \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} + \\
 & \frac{133 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5}{768 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \right)^2 \left(a \left(1 + \operatorname{Sin}[c+dx] \right) \right)^{5/2}} -
 \end{aligned}$$

$$\frac{5 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{96 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right)^3 \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} -$$

$$\frac{155 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{96 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right) \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} -$$

$$\frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{256 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right)^4 \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} +$$

$$\frac{5 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{96 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right)^3 \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} -$$

$$\frac{173 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{768 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right)^2 \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} +$$

$$\frac{155 \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{96 d \left(\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right) \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} +$$

$$\frac{155 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{192 d \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}} +$$

$$\left(5 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]\right)^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \Big/$$

$$\left(384 d \left(a(1 + \operatorname{Sin}[c+dx])\right)^{5/2}\right)$$

Problem 490: Unable to integrate problem.

$$\int \operatorname{Cos}[c+dx]^4 \operatorname{Sin}[c+dx]^n \left(a + a \operatorname{Sin}[c+dx]\right)^2 dx$$

Optimal (type 5, 200 leaves, 5 steps):

$$\left(a^2 \operatorname{Cos}[c+dx] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \operatorname{Sin}[c+dx]^2\right] \operatorname{Sin}[c+dx]^{1+n}\right) \Big/$$

$$\left(d(1+n) \sqrt{\operatorname{Cos}[c+dx]^2}\right) +$$

$$\left(2 a^2 \operatorname{Cos}[c+dx] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \operatorname{Sin}[c+dx]^2\right] \operatorname{Sin}[c+dx]^{2+n}\right) \Big/$$

$$\left(d(2+n) \sqrt{\operatorname{Cos}[c+dx]^2}\right) +$$

$$\left(a^2 \operatorname{Cos}[c+dx] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{3+n}{2}, \frac{5+n}{2}, \operatorname{Sin}[c+dx]^2\right] \operatorname{Sin}[c+dx]^{3+n}\right) \Big/$$

$$\left(d(3+n) \sqrt{\operatorname{Cos}[c+dx]^2}\right)$$

Result (type 8, 31 leaves):

$$\int \cos [c+d x]^4 \sin [c+d x]^n (a+a \sin [c+d x])^2 d x$$

Problem 491: Unable to integrate problem.

$$\int \cos [c+d x]^4 \sin [c+d x]^n (a+a \sin [c+d x]) d x$$

Optimal (type 5, 129 leaves, 3 steps):

$$\begin{aligned} & \left(a \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [c+d x]^2\right] \sin [c+d x]^{1+n}\right) / \\ & \left(d(1+n) \sqrt{\cos [c+d x]^2}\right) + \\ & \left(a \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [c+d x]^2\right] \sin [c+d x]^{2+n}\right) / \\ & \left(d(2+n) \sqrt{\cos [c+d x]^2}\right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \cos [c+d x]^4 \sin [c+d x]^n (a+a \sin [c+d x]) d x$$

Problem 492: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^4 \sin [c+d x]^n}{a+a \sin [c+d x]} d x$$

Optimal (type 5, 134 leaves, 3 steps):

$$\begin{aligned} & \left(\cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [c+d x]^2\right] \sin [c+d x]^{1+n}\right) / \\ & \left(a d(1+n) \sqrt{\cos [c+d x]^2}\right) - \\ & \left(\cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [c+d x]^2\right] \sin [c+d x]^{2+n}\right) / \\ & \left(a d(2+n) \sqrt{\cos [c+d x]^2}\right) \end{aligned}$$

Result (type 9, 23962 leaves): Display of huge result suppressed!

Problem 504: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \csc [c+d x] (a+a \sin [c+d x]) d x$$

Optimal (type 3, 86 leaves, 4 steps):

$$-\frac{a \operatorname{Csc}[c+d x]}{d} + \frac{a \operatorname{Csc}[c+d x]^2}{d} + \frac{2 a \operatorname{Csc}[c+d x]^3}{3 d} - \frac{a \operatorname{Csc}[c+d x]^4}{4 d} - \frac{a \operatorname{Csc}[c+d x]^5}{5 d} + \frac{a \operatorname{Log}[\operatorname{Sin}[c+d x]]}{d}$$

Result (type 3, 198 leaves):

$$-\frac{89 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{240 d} + \frac{31 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{480 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{160 d} + \frac{a \operatorname{Csc}[c+d x]^2}{d} - \frac{a \operatorname{Csc}[c+d x]^4}{4 d} + \frac{a \operatorname{Log}[\operatorname{Sin}[c+d x]]}{d} - \frac{89 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{240 d} + \frac{31 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{480 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{160 d}$$

Problem 505: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^5 \operatorname{Csc}[c+d x]^2 (a+a \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 61 leaves, 6 steps):

$$-\frac{a \operatorname{Cot}[c+d x]^6}{6 d} - \frac{a \operatorname{Csc}[c+d x]}{d} + \frac{2 a \operatorname{Csc}[c+d x]^3}{3 d} - \frac{a \operatorname{Csc}[c+d x]^5}{5 d}$$

Result (type 3, 173 leaves):

$$-\frac{89 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{240 d} - \frac{a \operatorname{Cot}[c+d x]^6}{6 d} + \frac{31 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{480 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{160 d} - \frac{89 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{240 d} + \frac{31 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{480 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{160 d}$$

Problem 506: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^5 \operatorname{Csc}[c+d x]^3 (a+a \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 65 leaves, 6 steps):

$$-\frac{a \operatorname{Cot}[c+d x]^6}{6 d} - \frac{a \operatorname{Csc}[c+d x]^3}{3 d} + \frac{2 a \operatorname{Csc}[c+d x]^5}{5 d} - \frac{a \operatorname{Csc}[c+d x]^7}{7 d}$$

Result (type 3, 233 leaves):

$$\begin{aligned}
 & - \frac{103 a \cot \left[\frac{1}{2} (c+d x) \right]}{3360 d} - \frac{a \cot [c+d x]^6}{6 d} - \frac{103 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2}{6720 d} + \\
 & \frac{9 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^4}{1120 d} - \frac{a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^6}{896 d} - \\
 & \frac{103 a \tan \left[\frac{1}{2} (c+d x) \right]}{3360 d} - \frac{103 a \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right]}{6720 d} + \\
 & \frac{9 a \sec \left[\frac{1}{2} (c+d x) \right]^4 \tan \left[\frac{1}{2} (c+d x) \right]}{1120 d} - \frac{a \sec \left[\frac{1}{2} (c+d x) \right]^6 \tan \left[\frac{1}{2} (c+d x) \right]}{896 d}
 \end{aligned}$$

Problem 507: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc} [c+d x]^4 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 81 leaves, 7 steps):

$$- \frac{a \cot [c+d x]^6}{6 d} - \frac{a \cot [c+d x]^8}{8 d} - \frac{a \operatorname{Csc} [c+d x]^3}{3 d} + \frac{2 a \operatorname{Csc} [c+d x]^5}{5 d} - \frac{a \operatorname{Csc} [c+d x]^7}{7 d}$$

Result (type 3, 265 leaves):

$$\begin{aligned}
 & - \frac{103 a \cot \left[\frac{1}{2} (c+d x) \right]}{3360 d} - \frac{103 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2}{6720 d} + \\
 & \frac{9 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^4}{1120 d} - \frac{a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^6}{896 d} - \\
 & \frac{a \operatorname{Csc} [c+d x]^4}{4 d} + \frac{a \operatorname{Csc} [c+d x]^6}{3 d} - \frac{a \operatorname{Csc} [c+d x]^8}{8 d} - \\
 & \frac{103 a \tan \left[\frac{1}{2} (c+d x) \right]}{3360 d} - \frac{103 a \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right]}{6720 d} + \\
 & \frac{9 a \sec \left[\frac{1}{2} (c+d x) \right]^4 \tan \left[\frac{1}{2} (c+d x) \right]}{1120 d} - \frac{a \sec \left[\frac{1}{2} (c+d x) \right]^6 \tan \left[\frac{1}{2} (c+d x) \right]}{896 d}
 \end{aligned}$$

Problem 508: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc} [c+d x]^5 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 81 leaves, 7 steps):

$$- \frac{a \cot [c+d x]^6}{6 d} - \frac{a \cot [c+d x]^8}{8 d} - \frac{a \operatorname{Csc} [c+d x]^5}{5 d} + \frac{2 a \operatorname{Csc} [c+d x]^7}{7 d} - \frac{a \operatorname{Csc} [c+d x]^9}{9 d}$$

Result (type 3, 325 leaves):

$$\begin{aligned}
 & - \frac{649 a \cot\left[\frac{1}{2}(c+dx)\right]}{80640 d} - \frac{649 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{161280 d} \\
 & \frac{31 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{53760 d} + \frac{37 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{32256 d} \\
 & \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{4608 d} - \frac{a \operatorname{Csc}[c+dx]^4}{4 d} + \\
 & \frac{a \operatorname{Csc}[c+dx]^6}{3 d} - \frac{a \operatorname{Csc}[c+dx]^8}{8 d} - \frac{649 a \tan\left[\frac{1}{2}(c+dx)\right]}{80640 d} \\
 & \frac{649 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{161280 d} - \frac{31 a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{53760 d} + \\
 & \frac{37 a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{32256 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^8 \tan\left[\frac{1}{2}(c+dx)\right]}{4608 d}
 \end{aligned}$$

Problem 509: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^5 \operatorname{Csc}[c+dx]^6 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 97 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{a \operatorname{Csc}[c+dx]^5}{5 d} - \frac{a \operatorname{Csc}[c+dx]^6}{6 d} + \frac{2 a \operatorname{Csc}[c+dx]^7}{7 d} + \\
 & \frac{a \operatorname{Csc}[c+dx]^8}{4 d} - \frac{a \operatorname{Csc}[c+dx]^9}{9 d} - \frac{a \operatorname{Csc}[c+dx]^{10}}{10 d}
 \end{aligned}$$

Result (type 3, 325 leaves):

$$\begin{aligned}
 & - \frac{649 a \cot\left[\frac{1}{2}(c+dx)\right]}{80640 d} - \frac{649 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{161280 d} \\
 & \frac{31 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{53760 d} + \frac{37 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{32256 d} \\
 & \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{4608 d} - \frac{a \operatorname{Csc}[c+dx]^6}{6 d} + \\
 & \frac{a \operatorname{Csc}[c+dx]^8}{4 d} - \frac{a \operatorname{Csc}[c+dx]^{10}}{10 d} - \frac{649 a \tan\left[\frac{1}{2}(c+dx)\right]}{80640 d} \\
 & \frac{649 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{161280 d} - \frac{31 a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{53760 d} + \\
 & \frac{37 a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{32256 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^8 \tan\left[\frac{1}{2}(c+dx)\right]}{4608 d}
 \end{aligned}$$

Problem 510: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^5 \operatorname{Csc} [c + d x]^7 (a + a \sin [c + d x]) dx$$

Optimal (type 3, 97 leaves, 4 steps):

$$-\frac{a \operatorname{Csc} [c + d x]^6}{6 d} - \frac{a \operatorname{Csc} [c + d x]^7}{7 d} + \frac{a \operatorname{Csc} [c + d x]^8}{4 d} + \frac{2 a \operatorname{Csc} [c + d x]^9}{9 d} - \frac{a \operatorname{Csc} [c + d x]^{10}}{10 d} - \frac{a \operatorname{Csc} [c + d x]^{11}}{11 d}$$

Result (type 3, 385 leaves):

$$\begin{aligned} & -\frac{1109 a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right]}{354816 d} - \frac{1109 a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2}{709632 d} \\ & - \frac{13 a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4}{29568 d} + \frac{173 a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^6}{1419264 d} \\ & + \frac{17 a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^8}{101376 d} - \frac{a \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^{10}}{22528 d} \\ & - \frac{a \operatorname{Csc} [c + d x]^6}{6 d} + \frac{a \operatorname{Csc} [c + d x]^8}{4 d} - \frac{a \operatorname{Csc} [c + d x]^{10}}{10 d} \\ & - \frac{1109 a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{354816 d} - \frac{1109 a \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{709632 d} \\ & - \frac{13 a \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{29568 d} + \frac{173 a \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^6 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{1419264 d} \\ & + \frac{17 a \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^8 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{101376 d} - \frac{a \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^{10} \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{22528 d} \end{aligned}$$

Problem 520: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^5 \operatorname{Csc} [c + d x]^2 (a + a \sin [c + d x])^2 dx$$

Optimal (type 3, 119 leaves, 4 steps):

$$-\frac{2 a^2 \operatorname{Csc} [c + d x]}{d} + \frac{a^2 \operatorname{Csc} [c + d x]^2}{2 d} + \frac{4 a^2 \operatorname{Csc} [c + d x]^3}{3 d} + \frac{a^2 \operatorname{Csc} [c + d x]^4}{4 d} - \frac{2 a^2 \operatorname{Csc} [c + d x]^5}{5 d} - \frac{a^2 \operatorname{Csc} [c + d x]^6}{6 d} + \frac{a^2 \operatorname{Log} [\operatorname{Sin} [c + d x]]}{d}$$

Result (type 3, 280 leaves):

$$a^2 \left(-\frac{89 \cot\left[\frac{1}{2}(c+dx)\right]}{120d} + \frac{9 \csc\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{31 \cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^2}{240d} + \frac{\csc\left[\frac{1}{2}(c+dx)\right]^4}{128d} - \frac{\cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^4}{80d} - \frac{\csc\left[\frac{1}{2}(c+dx)\right]^6}{384d} + \frac{\log[\sin[c+dx]]}{d} + \frac{9 \sec\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^4}{128d} - \frac{\sec\left[\frac{1}{2}(c+dx)\right]^6}{384d} - \frac{89 \tan\left[\frac{1}{2}(c+dx)\right]}{120d} + \frac{31 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{240d} - \frac{\sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{80d} \right)$$

Problem 529: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^5 \csc[c+dx]^2 (a+a \sin[c+dx])^3 dx$$

Optimal (type 3, 133 leaves, 4 steps):

$$-\frac{a^3 \csc[c+dx]}{d} + \frac{5a^3 \csc[c+dx]^2}{2d} + \frac{5a^3 \csc[c+dx]^3}{3d} - \frac{a^3 \csc[c+dx]^4}{4d} - \frac{3a^3 \csc[c+dx]^5}{5d} - \frac{a^3 \csc[c+dx]^6}{6d} + \frac{3a^3 \log[\sin[c+dx]]}{d} + \frac{a^3 \sin[c+dx]}{d}$$

Result (type 3, 291 leaves):

$$a^3 \left(-\frac{47 \cot\left[\frac{1}{2}(c+dx)\right]}{240d} + \frac{37 \csc\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{73 \cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^2}{480d} - \frac{3 \csc\left[\frac{1}{2}(c+dx)\right]^4}{128d} - \frac{3 \cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^4}{160d} - \frac{\csc\left[\frac{1}{2}(c+dx)\right]^6}{384d} + \frac{3 \log[\sin[c+dx]]}{d} + \frac{37 \sec\left[\frac{1}{2}(c+dx)\right]^2}{64d} - \frac{3 \sec\left[\frac{1}{2}(c+dx)\right]^4}{128d} - \frac{\sec\left[\frac{1}{2}(c+dx)\right]^6}{384d} + \frac{\sin[c+dx]}{d} - \frac{47 \tan\left[\frac{1}{2}(c+dx)\right]}{240d} + \frac{73 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{480d} - \frac{3 \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{160d} \right)$$

Problem 530: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx] \cot[c+dx]^4 (a+a \sin[c+dx])^4 dx$$

Optimal (type 3, 145 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{4 a^4 \operatorname{Csc}[c+d x]}{d} - \frac{2 a^4 \operatorname{Csc}[c+d x]^2}{d} - \frac{a^4 \operatorname{Csc}[c+d x]^3}{3 d} - \frac{4 a^4 \operatorname{Log}[\operatorname{Sin}[c+d x]]}{d} \\
 & \frac{10 a^4 \operatorname{Sin}[c+d x]}{d} - \frac{2 a^4 \operatorname{Sin}[c+d x]^2}{d} + \frac{4 a^4 \operatorname{Sin}[c+d x]^3}{3 d} + \frac{a^4 \operatorname{Sin}[c+d x]^4}{d} + \frac{a^4 \operatorname{Sin}[c+d x]^5}{5 d}
 \end{aligned}$$

Result (type 3, 636 leaves):

$$\begin{aligned}
 & \frac{\operatorname{Cos}[2(c+d x)](a+a \operatorname{Sin}[c+d x])^4}{2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} + \frac{\operatorname{Cos}[4(c+d x)](a+a \operatorname{Sin}[c+d x])^4}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \\
 & \frac{25 \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right](a+a \operatorname{Sin}[c+d x])^4}{12 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2(a+a \operatorname{Sin}[c+d x])^4}{2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \\
 & \frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2(a+a \operatorname{Sin}[c+d x])^4}{24 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \\
 & \frac{4 \operatorname{Log}[\operatorname{Sin}[c+d x]](a+a \operatorname{Sin}[c+d x])^4}{d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2(a+a \operatorname{Sin}[c+d x])^4}{2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \\
 & \frac{71 \operatorname{Sin}[c+d x](a+a \operatorname{Sin}[c+d x])^4}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \frac{19(a+a \operatorname{Sin}[c+d x])^4 \operatorname{Sin}[3(c+d x)]}{48 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} + \\
 & \frac{(a+a \operatorname{Sin}[c+d x])^4 \operatorname{Sin}[5(c+d x)]}{80 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \frac{25(a+a \operatorname{Sin}[c+d x])^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{12 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8} - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2(a+a \operatorname{Sin}[c+d x])^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^8}
 \end{aligned}$$

Problem 561: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+d x]^5}{(a+a \operatorname{Sin}[c+d x])^3} dx$$

Optimal (type 3, 96 leaves, 3 steps):

$$\begin{aligned}
 & \frac{4 \operatorname{Csc}[c+d x]}{a^3 d} - \frac{2 \operatorname{Csc}[c+d x]^2}{a^3 d} + \frac{\operatorname{Csc}[c+d x]^3}{a^3 d} - \\
 & \frac{\operatorname{Csc}[c+d x]^4}{4 a^3 d} + \frac{4 \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^3 d} - \frac{4 \operatorname{Log}[1+\operatorname{Sin}[c+d x]]}{a^3 d}
 \end{aligned}$$

Result (type 3, 558 leaves):

$$\begin{aligned}
 & \frac{9 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{4d(a+a\operatorname{Sin}[c+dx])^3} - \\
 & \frac{17 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32d(a+a\operatorname{Sin}[c+dx])^3} + \\
 & \left(\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) / \\
 & \left(8d(a+a\operatorname{Sin}[c+dx])^3\right) - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64d(a+a\operatorname{Sin}[c+dx])^3} - \\
 & \left(8 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) / \\
 & \left(d(a+a\operatorname{Sin}[c+dx])^3\right) + \frac{4 \operatorname{Log}[\operatorname{Sin}[c+dx]] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{d(a+a\operatorname{Sin}[c+dx])^3} - \\
 & \frac{17 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32d(a+a\operatorname{Sin}[c+dx])^3} - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64d(a+a\operatorname{Sin}[c+dx])^3} + \\
 & \frac{9 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{4d(a+a\operatorname{Sin}[c+dx])^3} + \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \\
 & \left(8d(a+a\operatorname{Sin}[c+dx])^3\right)
 \end{aligned}$$

Problem 563: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^5}{(a+a\operatorname{Sin}[c+dx])^4} dx$$

Optimal (type 3, 120 leaves, 3 steps):

$$\begin{aligned}
 & \frac{12 \operatorname{Csc}[c+dx]}{a^4 d} - \frac{4 \operatorname{Csc}[c+dx]^2}{a^4 d} + \frac{4 \operatorname{Csc}[c+dx]^3}{3 a^4 d} - \frac{\operatorname{Csc}[c+dx]^4}{4 a^4 d} + \\
 & \frac{16 \operatorname{Log}[\operatorname{Sin}[c+dx]]}{a^4 d} - \frac{16 \operatorname{Log}[1+\operatorname{Sin}[c+dx]]}{a^4 d} + \frac{4}{d(a^4+a^4\operatorname{Sin}[c+dx])}
 \end{aligned}$$

Result (type 3, 598 leaves):

$$\begin{aligned}
 & \frac{4 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^6}{d (a + a \sin[c+dx])^4} + \\
 & \frac{19 \cot\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{3 d (a + a \sin[c+dx])^4} - \\
 & \frac{33 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{32 d (a + a \sin[c+dx])^4} + \\
 & \left(\cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8 \right) / \\
 & \left(6 d (a + a \sin[c+dx])^4 \right) - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{64 d (a + a \sin[c+dx])^4} - \\
 & \left(32 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8 \right) / \\
 & \left(d (a + a \sin[c+dx])^4 \right) + \frac{16 \operatorname{Log}[\sin[c+dx]] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{d (a + a \sin[c+dx])^4} - \\
 & \frac{33 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{32 d (a + a \sin[c+dx])^4} - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8}{64 d (a + a \sin[c+dx])^4} + \\
 & \frac{19 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{3 d (a + a \sin[c+dx])^4} + \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left(6 d (a + a \sin[c+dx])^4 \right)
 \end{aligned}$$

Problem 564: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot[c+dx]^5 \operatorname{Csc}[c+dx]}{(a + a \sin[c+dx])^4} dx$$

Optimal (type 3, 135 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{16 \operatorname{Csc}[c+dx]}{a^4 d} + \frac{6 \operatorname{Csc}[c+dx]^2}{a^4 d} - \frac{8 \operatorname{Csc}[c+dx]^3}{3 a^4 d} + \frac{\operatorname{Csc}[c+dx]^4}{a^4 d} - \frac{\operatorname{Csc}[c+dx]^5}{5 a^4 d} - \\
 & \frac{20 \operatorname{Log}[\sin[c+dx]]}{a^4 d} + \frac{20 \operatorname{Log}[1 + \sin[c+dx]]}{a^4 d} - \frac{4}{d (a^4 + a^4 \sin[c+dx])}
 \end{aligned}$$

Result (type 3, 726 leaves):

$$\begin{aligned}
& - \frac{4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^6}{d (a + a \sin [c + dx])^4} - \\
& \frac{2089 \cot \left[\frac{1}{2} (c + dx) \right] \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{240 d (a + a \sin [c + dx])^4} + \\
& \frac{13 \operatorname{Csc} \left[\frac{1}{2} (c + dx) \right]^2 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{8 d (a + a \sin [c + dx])^4} - \\
& \left(169 \cot \left[\frac{1}{2} (c + dx) \right] \operatorname{Csc} \left[\frac{1}{2} (c + dx) \right]^2 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \right) / \\
& \left(480 d (a + a \sin [c + dx])^4 \right) + \frac{\operatorname{Csc} \left[\frac{1}{2} (c + dx) \right]^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{16 d (a + a \sin [c + dx])^4} - \\
& \left(\cot \left[\frac{1}{2} (c + dx) \right] \operatorname{Csc} \left[\frac{1}{2} (c + dx) \right]^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \right) / \\
& \left(160 d (a + a \sin [c + dx])^4 \right) + \\
& \left(40 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right] \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \right) / \\
& \left(d (a + a \sin [c + dx])^4 \right) - \frac{20 \operatorname{Log} [\sin [c + dx]] \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{d (a + a \sin [c + dx])^4} + \\
& \frac{13 \operatorname{Sec} \left[\frac{1}{2} (c + dx) \right]^2 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{8 d (a + a \sin [c + dx])^4} + \\
& \frac{\operatorname{Sec} \left[\frac{1}{2} (c + dx) \right]^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8}{16 d (a + a \sin [c + dx])^4} - \\
& \frac{2089 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \operatorname{Tan} \left[\frac{1}{2} (c + dx) \right]}{240 d (a + a \sin [c + dx])^4} - \\
& \left(169 \operatorname{Sec} \left[\frac{1}{2} (c + dx) \right]^2 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \operatorname{Tan} \left[\frac{1}{2} (c + dx) \right] \right) / \\
& \left(480 d (a + a \sin [c + dx])^4 \right) - \\
& \left(\operatorname{Sec} \left[\frac{1}{2} (c + dx) \right]^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^8 \operatorname{Tan} \left[\frac{1}{2} (c + dx) \right] \right) / \\
& \left(160 d (a + a \sin [c + dx])^4 \right)
\end{aligned}$$

Problem 565: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c + dx]^5 \sin [c + dx]^n (a + a \sin [c + dx])^3 dx$$

Optimal (type 3, 181 leaves, 3 steps):

$$\frac{a^3 \operatorname{Sin}[c + d x]^{1+n}}{d (1+n)} + \frac{3 a^3 \operatorname{Sin}[c + d x]^{2+n}}{d (2+n)} + \frac{a^3 \operatorname{Sin}[c + d x]^{3+n}}{d (3+n)} - \frac{5 a^3 \operatorname{Sin}[c + d x]^{4+n}}{d (4+n)} -$$

$$\frac{5 a^3 \operatorname{Sin}[c + d x]^{5+n}}{d (5+n)} + \frac{a^3 \operatorname{Sin}[c + d x]^{6+n}}{d (6+n)} + \frac{3 a^3 \operatorname{Sin}[c + d x]^{7+n}}{d (7+n)} + \frac{a^3 \operatorname{Sin}[c + d x]^{8+n}}{d (8+n)}$$

Result (type 3, 843 leaves):

$$\begin{aligned}
 & \frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} \\
 & \sin [c + d x]^n \left(a + a \sin [c + d x] \right)^3 \left(\frac{18064 + 5508 n + 596 n^2 + 27 n^3}{128 (2 + n) (4 + n) (6 + n) (8 + n)} + \right. \\
 & \left(\frac{5775 + 3015 n + 329 n^2 + 17 n^3}{(1 + n) (3 + n) (5 + n) (7 + n)} \left(-\frac{1}{128} \operatorname{Im} \cos [c + d x] + \frac{1}{128} \operatorname{Im} \sin [c + d x] \right) \right) / \\
 & \left(\frac{5775 + 3015 n + 329 n^2 + 17 n^3}{(1 + n) (3 + n) (5 + n) (7 + n)} \left(\frac{1}{128} \operatorname{Im} \cos [c + d x] + \frac{1}{128} \operatorname{Im} \sin [c + d x] \right) \right) / \\
 & \left(\frac{-3168 - 368 n + 38 n^2 + 3 n^3}{(2 + n) (4 + n) (6 + n) (8 + n)} \left(\frac{1}{64} \operatorname{Im} \cos [2 (c + d x)] - \frac{1}{64} \operatorname{Im} \sin [2 (c + d x)] \right) \right) / \\
 & \left(\frac{-3168 - 368 n + 38 n^2 + 3 n^3}{(2 + n) (4 + n) (6 + n) (8 + n)} \left(\frac{1}{64} \operatorname{Im} \cos [2 (c + d x)] + \frac{1}{64} \operatorname{Im} \sin [2 (c + d x)] \right) \right) / \\
 & \left(\frac{595 + 304 n + 21 n^2}{(3 + n) (5 + n) (7 + n)} \left(-\frac{1}{128} \operatorname{Im} \cos [3 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [3 (c + d x)] \right) \right) / \\
 & \left(\frac{595 + 304 n + 21 n^2}{(3 + n) (5 + n) (7 + n)} \left(\frac{1}{128} \operatorname{Im} \cos [3 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [3 (c + d x)] \right) \right) / \\
 & \left(\frac{-600 - 138 n - 7 n^2}{(3 + n) (5 + n) (7 + n)} + \frac{\left(\frac{1}{64} \operatorname{Im} \cos [4 (c + d x)] - \frac{1}{64} \operatorname{Im} \sin [4 (c + d x)] \right)}{(4 + n) (6 + n) (8 + n)} \right) + \\
 & \frac{\left(-600 - 138 n - 7 n^2 \right) \left(\frac{1}{64} \operatorname{Im} \cos [4 (c + d x)] + \frac{1}{64} \operatorname{Im} \sin [4 (c + d x)] \right)}{(4 + n) (6 + n) (8 + n)} + \\
 & \frac{\left(-35 + n \right) \left(-\frac{1}{128} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [5 (c + d x)] \right)}{(5 + n) (7 + n)} + \\
 & \frac{\left(-35 + n \right) \left(\frac{1}{128} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [5 (c + d x)] \right)}{(5 + n) (7 + n)} + \\
 & \frac{\left(-20 - 3 n \right) \left(\frac{1}{64} \operatorname{Im} \cos [6 (c + d x)] - \frac{1}{64} \operatorname{Im} \sin [6 (c + d x)] \right)}{(6 + n) (8 + n)} + \\
 & \frac{\left(-20 - 3 n \right) \left(\frac{1}{64} \operatorname{Im} \cos [6 (c + d x)] + \frac{1}{64} \operatorname{Im} \sin [6 (c + d x)] \right)}{(6 + n) (8 + n)} + \\
 & \frac{-\frac{3}{128} \operatorname{Im} \cos [7 (c + d x)] - \frac{3}{128} \operatorname{Im} \sin [7 (c + d x)]}{7 + n} + \frac{\frac{3}{128} \operatorname{Im} \cos [7 (c + d x)] - \frac{3}{128} \operatorname{Im} \sin [7 (c + d x)]}{7 + n} + \\
 & \left. \frac{\frac{1}{256} \operatorname{Im} \cos [8 (c + d x)] - \frac{1}{256} \operatorname{Im} \sin [8 (c + d x)]}{8 + n} + \frac{\frac{1}{256} \operatorname{Im} \cos [8 (c + d x)] + \frac{1}{256} \operatorname{Im} \sin [8 (c + d x)]}{8 + n} \right)
 \end{aligned}$$

Problem 566: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 \sin [c + d x]^n (a + a \sin [c + d x])^2 dx$$

Optimal (type 3, 160 leaves, 3 steps):

$$\frac{a^2 \sin [c + d x]^{1+n}}{d (1+n)} + \frac{2 a^2 \sin [c + d x]^{2+n}}{d (2+n)} - \frac{a^2 \sin [c + d x]^{3+n}}{d (3+n)} - \frac{4 a^2 \sin [c + d x]^{4+n}}{d (4+n)} - \frac{a^2 \sin [c + d x]^{5+n}}{d (5+n)} + \frac{2 a^2 \sin [c + d x]^{6+n}}{d (6+n)} + \frac{a^2 \sin [c + d x]^{7+n}}{d (7+n)}$$

Result (type 3, 705 leaves):

$$\begin{aligned}
 & \frac{1}{d \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^4} \\
 & \sin [c + dx]^n (a + a \sin [c + dx])^2 \left(\frac{88 + 14 n + n^2}{8 (2 + n) (4 + n) (6 + n)} + \left((4725 + 1853 n + 211 n^2 + 11 n^3) \right. \right. \\
 & \quad \left. \left. \left(-\frac{1}{128} i \cos [c + dx] + \frac{1}{128} \sin [c + dx] \right) \right) / \left((1 + n) (3 + n) (5 + n) (7 + n) \right) + \right. \\
 & \quad \left. \left((4725 + 1853 n + 211 n^2 + 11 n^3) \left(\frac{1}{128} i \cos [c + dx] + \frac{1}{128} \sin [c + dx] \right) \right) / \right. \\
 & \quad \left. \left((1 + n) (3 + n) (5 + n) (7 + n) \right) + \right. \\
 & \quad \left. \frac{(-120 + 6 n + n^2) \left(\frac{1}{32} \cos [2 (c + dx)] - \frac{1}{32} i \sin [2 (c + dx)] \right)}{(2 + n) (4 + n) (6 + n)} + \right. \\
 & \quad \left. \frac{(-120 + 6 n + n^2) \left(\frac{1}{32} \cos [2 (c + dx)] + \frac{1}{32} i \sin [2 (c + dx)] \right)}{(2 + n) (4 + n) (6 + n)} + \right. \\
 & \quad \left. \left((665 + 224 n + 15 n^2) \left(-\frac{1}{128} i \cos [3 (c + dx)] + \frac{1}{128} \sin [3 (c + dx)] \right) \right) / \right. \\
 & \quad \left. \left((3 + n) (5 + n) (7 + n) \right) + \right. \\
 & \quad \left. \left((665 + 224 n + 15 n^2) \left(\frac{1}{128} i \cos [3 (c + dx)] + \frac{1}{128} \sin [3 (c + dx)] \right) \right) / \right. \\
 & \quad \left. \left((3 + n) (5 + n) (7 + n) \right) + \frac{(-12 - n) \left(\frac{1}{16} \cos [4 (c + dx)] - \frac{1}{16} i \sin [4 (c + dx)] \right)}{(4 + n) (6 + n)} + \right. \\
 & \quad \left. \frac{(-12 - n) \left(\frac{1}{16} \cos [4 (c + dx)] + \frac{1}{16} i \sin [4 (c + dx)] \right)}{(4 + n) (6 + n)} + \right. \\
 & \quad \left. \frac{(7 + 3 n) \left(-\frac{1}{128} i \cos [5 (c + dx)] + \frac{1}{128} \sin [5 (c + dx)] \right)}{(5 + n) (7 + n)} + \right. \\
 & \quad \left. \frac{(7 + 3 n) \left(\frac{1}{128} i \cos [5 (c + dx)] + \frac{1}{128} \sin [5 (c + dx)] \right)}{(5 + n) (7 + n)} + \right. \\
 & \quad \left. \frac{-\frac{1}{32} \cos [6 (c + dx)] - \frac{1}{32} i \sin [6 (c + dx)]}{6 + n} + \frac{-\frac{1}{32} \cos [6 (c + dx)] + \frac{1}{32} i \sin [6 (c + dx)]}{6 + n} + \right. \\
 & \quad \left. \frac{-\frac{1}{128} i \cos [7 (c + dx)] - \frac{1}{128} \sin [7 (c + dx)]}{7 + n} + \frac{\frac{1}{128} i \cos [7 (c + dx)] - \frac{1}{128} \sin [7 (c + dx)]}{7 + n} \right)
 \end{aligned}$$

Problem 567: Result more than twice size of optimal antiderivative.

$$\int \cos [c + dx]^5 \sin [c + dx]^n (a + a \sin [c + dx]) dx$$

Optimal (type 3, 123 leaves, 3 steps):

$$\frac{a \sin[c+dx]^{1+n}}{d(1+n)} + \frac{a \sin[c+dx]^{2+n}}{d(2+n)} - \frac{2a \sin[c+dx]^{3+n}}{d(3+n)} - \frac{2a \sin[c+dx]^{4+n}}{d(4+n)} + \frac{a \sin[c+dx]^{5+n}}{d(5+n)} + \frac{a \sin[c+dx]^{6+n}}{d(6+n)}$$

Result (type 3, 345 leaves):

$$\frac{1}{16d(1+n)(2+n)(3+n)(4+n)(5+n)(6+n)} a \sin[c+dx]^{1+n} (8544 + 10520n + 4888n^2 + 1114n^3 + 128n^4 + 6n^5 + 8(336 + 692n + 484n^2 + 147n^3 + 20n^4 + n^5) \cos[2(c+dx)] + 2(144 + 324n + 260n^2 + 95n^3 + 16n^4 + n^5) \cos[4(c+dx)] + 2640 \sin[c+dx] + 4468n \sin[c+dx] + 2258n^2 \sin[c+dx] + 474n^3 \sin[c+dx] + 46n^4 \sin[c+dx] + 2n^5 \sin[c+dx] + 840 \sin[3(c+dx)] + 1798n \sin[3(c+dx)] + 1331n^2 \sin[3(c+dx)] + 431n^3 \sin[3(c+dx)] + 61n^4 \sin[3(c+dx)] + 3n^5 \sin[3(c+dx)] + 120 \sin[5(c+dx)] + 274n \sin[5(c+dx)] + 225n^2 \sin[5(c+dx)] + 85n^3 \sin[5(c+dx)] + 15n^4 \sin[5(c+dx)] + n^5 \sin[5(c+dx)])$$

Problem 570: Unable to integrate problem.

$$\int \frac{\cos[c+dx]^5 \sin[c+dx]^n}{(a+a \sin[c+dx])^3} dx$$

Optimal (type 5, 85 leaves, 4 steps):

$$-\frac{3 \sin[c+dx]^{1+n}}{a^3 d(1+n)} + \frac{4 \text{Hypergeometric2F1}[1, 1+n, 2+n, -\sin[c+dx]] \sin[c+dx]^{1+n}}{a^3 d(1+n)} + \frac{\sin[c+dx]^{2+n}}{a^3 d(2+n)}$$

Result (type 8, 31 leaves):

$$\int \frac{\cos[c+dx]^5 \sin[c+dx]^n}{(a+a \sin[c+dx])^3} dx$$

Problem 571: Unable to integrate problem.

$$\int \frac{\cos[c+dx]^5 \sin[c+dx]^n}{(a+a \sin[c+dx])^4} dx$$

Optimal (type 5, 88 leaves, 4 steps):

$$\frac{\sin[c+dx]^{1+n}}{a^4 d(1+n)} - \frac{4 \text{Hypergeometric2F1}[1, 1+n, 2+n, -\sin[c+dx]] \sin[c+dx]^{1+n}}{a^4 d} + \frac{4 \sin[c+dx]^{1+n}}{d(a^4 + a^4 \sin[c+dx])}$$

Result (type 8, 31 leaves):

$$\int \frac{\cos [c+d x]^5 \sin [c+d x]^n}{(a+a \sin [c+d x])^4} dx$$

Problem 585: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^6 \csc [c+d x]^4 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 138 leaves, 9 steps):

$$\frac{5 a \operatorname{ArcTanh}[\cos [c+d x]]}{128 d} - \frac{a \cot [c+d x]^7}{7 d} - \frac{a \cot [c+d x]^9}{9 d} + \frac{5 a \cot [c+d x] \csc [c+d x]}{128 d} - \frac{5 a \cot [c+d x] \csc [c+d x]^3}{64 d} + \frac{5 a \cot [c+d x]^3 \csc [c+d x]^3}{48 d} - \frac{a \cot [c+d x]^5 \csc [c+d x]^3}{8 d}$$

Result (type 3, 301 leaves):

$$\frac{2 a \cot [c+d x]}{63 d} + \frac{5 a \csc \left[\frac{1}{2}(c+d x)\right]^2}{512 d} - \frac{15 a \csc \left[\frac{1}{2}(c+d x)\right]^4}{1024 d} + \frac{7 a \csc \left[\frac{1}{2}(c+d x)\right]^6}{1536 d} - \frac{a \csc \left[\frac{1}{2}(c+d x)\right]^8}{2048 d} + \frac{a \cot [c+d x] \csc [c+d x]^2}{63 d} - \frac{5 a \cot [c+d x] \csc [c+d x]^4}{21 d} + \frac{19 a \cot [c+d x] \csc [c+d x]^6}{63 d} - \frac{a \cot [c+d x] \csc [c+d x]^8}{9 d} + \frac{5 a \log [\cos \left[\frac{1}{2}(c+d x)\right]]}{128 d} - \frac{5 a \log [\sin \left[\frac{1}{2}(c+d x)\right]]}{128 d} - \frac{5 a \sec \left[\frac{1}{2}(c+d x)\right]^2}{512 d} + \frac{15 a \sec \left[\frac{1}{2}(c+d x)\right]^4}{1024 d} - \frac{7 a \sec \left[\frac{1}{2}(c+d x)\right]^6}{1536 d} + \frac{a \sec \left[\frac{1}{2}(c+d x)\right]^8}{2048 d}$$

Problem 586: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^6 \csc [c+d x]^5 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 160 leaves, 10 steps):

$$\frac{3 a \operatorname{ArcTanh}[\cos [c+d x]]}{256 d} - \frac{a \cot [c+d x]^7}{7 d} - \frac{a \cot [c+d x]^9}{9 d} + \frac{3 a \cot [c+d x] \csc [c+d x]}{256 d} + \frac{a \cot [c+d x] \csc [c+d x]^3}{128 d} - \frac{a \cot [c+d x] \csc [c+d x]^5}{32 d} + \frac{a \cot [c+d x]^3 \csc [c+d x]^5}{16 d} - \frac{a \cot [c+d x]^5 \csc [c+d x]^5}{10 d}$$

Result (type 3, 341 leaves):

$$\begin{aligned}
 & \frac{2 a \cot [c+d x]}{63 d} + \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{1024 d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} - \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{2048 d} + \\
 & \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{4096 d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10}}{10240 d} + \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^2}{63 d} - \\
 & \frac{5 a \cot [c+d x] \operatorname{Csc}[c+d x]^4}{21 d} + \frac{19 a \cot [c+d x] \operatorname{Csc}[c+d x]^6}{63 d} - \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^8}{9 d} + \\
 & \frac{3 a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]\right]}{256 d} - \frac{3 a \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+d x)\right]\right]}{256 d} - \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{1024 d} + \\
 & \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} + \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6}{2048 d} - \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8}{4096 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{10}}{10240 d}
 \end{aligned}$$

Problem 587: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^6 \operatorname{Csc}[c+d x]^6 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 176 leaves, 10 steps):

$$\begin{aligned}
 & \frac{3 a \operatorname{ArcTanh}\left[\cos [c+d x]\right]}{256 d} - \frac{a \cot [c+d x]^7}{7 d} - \frac{2 a \cot [c+d x]^9}{9 d} - \\
 & \frac{a \cot [c+d x]^{11}}{11 d} + \frac{3 a \cot [c+d x] \operatorname{Csc}[c+d x]}{256 d} + \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^3}{128 d} - \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^5}{32 d} + \frac{a \cot [c+d x]^3 \operatorname{Csc}[c+d x]^5}{16 d} - \frac{a \cot [c+d x]^5 \operatorname{Csc}[c+d x]^5}{10 d}
 \end{aligned}$$

Result (type 3, 363 leaves):

$$\begin{aligned}
 & \frac{8 a \cot [c+d x]}{693 d} + \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{1024 d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} - \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{2048 d} + \\
 & \frac{3 a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{4096 d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10}}{10240 d} + \frac{4 a \cot [c+d x] \operatorname{Csc}[c+d x]^2}{693 d} + \\
 & \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^4}{231 d} - \frac{113 a \cot [c+d x] \operatorname{Csc}[c+d x]^6}{693 d} + \\
 & \frac{23 a \cot [c+d x] \operatorname{Csc}[c+d x]^8}{99 d} - \frac{a \cot [c+d x] \operatorname{Csc}[c+d x]^{10}}{11 d} + \frac{3 a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]\right]}{256 d} - \\
 & \frac{3 a \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+d x)\right]\right]}{256 d} - \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{1024 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{1024 d} + \\
 & \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6}{2048 d} - \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8}{4096 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{10}}{10240 d}
 \end{aligned}$$

Problem 594: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^3 \cot [c+d x]^3 (a+a \sin [c+d x])^2 d x$$

Optimal (type 3, 140 leaves, 16 steps):

$$\frac{-\frac{15 a^2 x}{4} + \frac{3 a^2 \operatorname{ArcTanh}[\cos [c+d x]]}{2 d}}{a^2 \cot [c+d x] \operatorname{Csc}[c+d x]} - \frac{\frac{a^2 \cos [c+d x]}{d}}{4 d} + \frac{\frac{a^2 \cos [c+d x]^5}{5 d}}{a^2 \cos [c+d x] \operatorname{Sin}[c+d x]} - \frac{\frac{2 a^2 \cot [c+d x]}{d}}{2 d} + \frac{\frac{9 a^2 \cos [c+d x] \operatorname{Sin}[c+d x]}{4 d}}{a^2 \cos [c+d x] \operatorname{Sin}[c+d x]^3}$$

Result (type 3, 607 leaves):

$$\frac{15 (c+d x) (a+a \sin [c+d x])^2}{4 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{7 \cos [c+d x] (a+a \sin [c+d x])^2}{8 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{\cos [3(c+d x)] (a+a \sin [c+d x])^2}{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{\cos [5(c+d x)] (a+a \sin [c+d x])^2}{80 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{\cot \left[\frac{1}{2}(c+d x)\right] (a+a \sin [c+d x])^2}{d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (a+a \sin [c+d x])^2}{8 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{3 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]\right] (a+a \sin [c+d x])^2}{2 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{3 \operatorname{Log}\left[\sin \left[\frac{1}{2}(c+d x)\right]\right] (a+a \sin [c+d x])^2}{2 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (a+a \sin [c+d x])^2}{8 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{(a+a \sin [c+d x])^2 \operatorname{Sin}[2(c+d x)]}{d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{(a+a \sin [c+d x])^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{(a+a \sin [c+d x])^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4}$$

Problem 600: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^6 \operatorname{Csc}[c+d x]^3 (a+a \sin [c+d x])^2 d x$$

Optimal (type 3, 182 leaves, 13 steps):

$$\frac{\frac{45 a^2 \operatorname{ArcTanh}[\cos [c+d x]]}{128 d}}{5 a^2 \cot [c+d x]^3 \operatorname{Csc}[c+d x]} - \frac{\frac{2 a^2 \cot [c+d x]^7}{7 d}}{24 d} - \frac{\frac{35 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]}{128 d}}{a^2 \cot [c+d x]^5 \operatorname{Csc}[c+d x]} + \frac{\frac{5 a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^3}{64 d}}{48 d} - \frac{\frac{a^2 \cot [c+d x]^5 \operatorname{Csc}[c+d x]^3}{6 d}}{8 d}$$

Result (type 3, 401 leaves):

$$\begin{aligned}
 a^2 & \left(\frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{7d} - \frac{83 \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{512d} - \frac{19 \text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{224d} + \right. \\
 & \frac{17 \text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} + \frac{5 \text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{224d} + \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{512d} - \\
 & \frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{448d} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{2048d} + \frac{45 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{128d} - \\
 & \frac{45 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{128d} + \frac{83 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{512d} - \frac{17 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} - \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{512d} + \\
 & \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^8}{2048d} - \frac{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}{7d} + \frac{19 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{224d} - \\
 & \left. \frac{5 \text{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{224d} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^6 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{448d} \right)
 \end{aligned}$$

Problem 601: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c+dx]^6 \text{Csc}[c+dx]^4 (a+a \text{Sin}[c+dx])^2 dx$$

Optimal (type 3, 152 leaves, 12 steps):

$$\begin{aligned}
 & \frac{5 a^2 \text{ArcTanh}\left[\text{Cos}[c+dx]\right]}{64 d} - \frac{2 a^2 \text{Cot}[c+dx]^7}{7 d} - \frac{a^2 \text{Cot}[c+dx]^9}{9 d} + \frac{5 a^2 \text{Cot}[c+dx] \text{Csc}[c+dx]}{64 d} - \\
 & \frac{5 a^2 \text{Cot}[c+dx] \text{Csc}[c+dx]^3}{32 d} + \frac{5 a^2 \text{Cot}[c+dx]^3 \text{Csc}[c+dx]^3}{24 d} - \frac{a^2 \text{Cot}[c+dx]^5 \text{Csc}[c+dx]^3}{4 d}
 \end{aligned}$$

Result (type 3, 313 leaves):

$$\begin{aligned}
 & - \frac{1}{1032192d} a^2 \operatorname{Csc}[c+dx]^9 \\
 & \left(72576 \operatorname{Cos}[c+dx] + 37632 \operatorname{Cos}[3(c+dx)] + 6912 \operatorname{Cos}[5(c+dx)] - 1728 \operatorname{Cos}[7(c+dx)] - \right. \\
 & \quad 704 \operatorname{Cos}[9(c+dx)] - 39690 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + 39690 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \\
 & \quad \operatorname{Sin}[c+dx] + 36540 \operatorname{Sin}[2(c+dx)] + 26460 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad 26460 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] + 20916 \operatorname{Sin}[4(c+dx)] - \\
 & \quad 11340 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] + 11340 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] + \\
 & \quad 16044 \operatorname{Sin}[6(c+dx)] + 2835 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] - \\
 & \quad 2835 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] + 630 \operatorname{Sin}[8(c+dx)] - \\
 & \quad \left. 315 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[9(c+dx)] + 315 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[9(c+dx)] \right)
 \end{aligned}$$

Problem 611: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^3 \operatorname{Cot}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^3 dx$$

Optimal (type 3, 181 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{85 a^3 x}{16} - \frac{a^3 \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{2d} + \frac{a^3 \operatorname{Cos}[c+dx]}{d} + \frac{2 a^3 \operatorname{Cos}[c+dx]^3}{3d} + \\
 & \frac{3 a^3 \operatorname{Cos}[c+dx]^5}{5d} - \frac{3 a^3 \operatorname{Cot}[c+dx]}{d} - \frac{a^3 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{2d} - \\
 & \frac{43 a^3 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{16d} + \frac{5 a^3 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]^3}{24d} + \frac{a^3 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]^5}{6d}
 \end{aligned}$$

Result (type 3, 664 leaves):

$$\begin{aligned}
 & - \frac{85 (c + d x) (a + a \sin [c + d x])^3}{16 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \frac{15 \cos [c + d x] (a + a \sin [c + d x])^3}{8 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{17 \cos [3 (c + d x)] (a + a \sin [c + d x])^3}{48 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \frac{3 \cos [5 (c + d x)] (a + a \sin [c + d x])^3}{80 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{3 \cot \left[\frac{1}{2} (c + d x) \right] (a + a \sin [c + d x])^3}{2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \\
 & \frac{\csc \left[\frac{1}{2} (c + d x) \right]^2 (a + a \sin [c + d x])^3}{8 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{\log [\cos \left[\frac{1}{2} (c + d x) \right]] (a + a \sin [c + d x])^3}{2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \frac{\log [\sin \left[\frac{1}{2} (c + d x) \right]] (a + a \sin [c + d x])^3}{2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{\sec \left[\frac{1}{2} (c + d x) \right]^2 (a + a \sin [c + d x])^3}{8 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \\
 & \frac{81 (a + a \sin [c + d x])^3 \sin [2 (c + d x)]}{64 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{3 (a + a \sin [c + d x])^3 \sin [4 (c + d x)]}{64 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \frac{(a + a \sin [c + d x])^3 \sin [6 (c + d x)]}{192 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{3 (a + a \sin [c + d x])^3 \tan \left[\frac{1}{2} (c + d x) \right]}{2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6}
 \end{aligned}$$

Problem 618: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^6 \csc [c + d x]^4 (a + a \sin [c + d x])^3 dx$$

Optimal (type 3, 200 leaves, 16 steps):

$$\begin{aligned}
 & \frac{55 a^3 \operatorname{ArcTanh} [\cos [c + d x]]}{128 d} - \frac{4 a^3 \cot [c + d x]^7}{7 d} - \frac{a^3 \cot [c + d x]^9}{9 d} - \\
 & \frac{25 a^3 \cot [c + d x] \csc [c + d x]}{128 d} + \frac{5 a^3 \cot [c + d x]^3 \csc [c + d x]}{24 d} - \frac{a^3 \cot [c + d x]^5 \csc [c + d x]}{6 d} - \\
 & \frac{15 a^3 \cot [c + d x] \csc [c + d x]^3}{64 d} + \frac{5 a^3 \cot [c + d x]^3 \csc [c + d x]^3}{16 d} - \frac{3 a^3 \cot [c + d x]^5 \csc [c + d x]^3}{8 d}
 \end{aligned}$$

Result (type 3, 459 leaves):

$$\begin{aligned}
 & a^3 \left(\frac{29 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{126d} - \frac{73 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{512d} - \frac{4163 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{32256d} - \right. \\
 & \frac{13 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} + \frac{319 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{10752d} + \frac{17 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{1536d} - \\
 & \frac{53 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{32256d} - \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{2048d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{4608d} + \\
 & \frac{55 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{128d} - \frac{55 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{128d} + \frac{73 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{512d} + \\
 & \frac{13 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} - \frac{17 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{1536d} + \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^8}{2048d} - \frac{29 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{126d} + \\
 & \frac{4163 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32256d} - \frac{319 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{10752d} + \\
 & \left. \frac{53 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32256d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{4608d} \right)
 \end{aligned}$$

Problem 624: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx]^6 \operatorname{Sin}[c+dx]^4}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 159 leaves, 9 steps):

$$\frac{3x}{128a} + \frac{\operatorname{Cos}[c+dx]^5}{5ad} - \frac{2 \operatorname{Cos}[c+dx]^7}{7ad} + \frac{\operatorname{Cos}[c+dx]^9}{9ad} + \frac{3 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{128ad} + \frac{\operatorname{Cos}[c+dx]^3 \operatorname{Sin}[c+dx]}{64ad} - \frac{\operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]}{16ad} - \frac{\operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]^3}{8ad}$$

Result (type 3, 429 leaves):

$$\begin{aligned}
 & \frac{1}{645120 a d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(2520 (5 c + 6 d x) \cos\left[\frac{c}{2}\right] + 7560 \cos\left[\frac{c}{2} + d x\right] + 7560 \cos\left[\frac{3 c}{2} + d x\right] + 1680 \cos\left[\frac{5 c}{2} + 3 d x\right] + \right. \\
 & 1680 \cos\left[\frac{7 c}{2} + 3 d x\right] - 2520 \cos\left[\frac{7 c}{2} + 4 d x\right] + 2520 \cos\left[\frac{9 c}{2} + 4 d x\right] - 1008 \cos\left[\frac{9 c}{2} + 5 d x\right] - \\
 & 1008 \cos\left[\frac{11 c}{2} + 5 d x\right] - 180 \cos\left[\frac{13 c}{2} + 7 d x\right] - 180 \cos\left[\frac{15 c}{2} + 7 d x\right] + 315 \cos\left[\frac{15 c}{2} + 8 d x\right] - \\
 & 315 \cos\left[\frac{17 c}{2} + 8 d x\right] + 140 \cos\left[\frac{17 c}{2} + 9 d x\right] + 140 \cos\left[\frac{19 c}{2} + 9 d x\right] + 12600 \sin\left[\frac{c}{2}\right] + \\
 & 12600 c \sin\left[\frac{c}{2}\right] + 15120 d x \sin\left[\frac{c}{2}\right] - 7560 \sin\left[\frac{c}{2} + d x\right] + 7560 \sin\left[\frac{3 c}{2} + d x\right] - \\
 & 1680 \sin\left[\frac{5 c}{2} + 3 d x\right] + 1680 \sin\left[\frac{7 c}{2} + 3 d x\right] - 2520 \sin\left[\frac{7 c}{2} + 4 d x\right] - 2520 \sin\left[\frac{9 c}{2} + 4 d x\right] + \\
 & 1008 \sin\left[\frac{9 c}{2} + 5 d x\right] - 1008 \sin\left[\frac{11 c}{2} + 5 d x\right] + 180 \sin\left[\frac{13 c}{2} + 7 d x\right] - 180 \sin\left[\frac{15 c}{2} + 7 d x\right] + \\
 & \left. 315 \sin\left[\frac{15 c}{2} + 8 d x\right] + 315 \sin\left[\frac{17 c}{2} + 8 d x\right] - 140 \sin\left[\frac{17 c}{2} + 9 d x\right] + 140 \sin\left[\frac{19 c}{2} + 9 d x\right] \right)
 \end{aligned}$$

Problem 625: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^3}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 141 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{3 x}{128 a} - \frac{\cos [c+d x]^5}{5 a d} + \frac{\cos [c+d x]^7}{7 a d} - \frac{3 \cos [c+d x] \sin [c+d x]}{128 a d} - \\
 & \frac{\cos [c+d x]^3 \sin [c+d x]}{64 a d} + \frac{\cos [c+d x]^5 \sin [c+d x]}{16 a d} + \frac{\cos [c+d x]^5 \sin [c+d x]^3}{8 a d}
 \end{aligned}$$

Result (type 3, 375 leaves):

$$\frac{1}{71680 a d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(1680 (c - d x) \cos\left[\frac{c}{2}\right] - 1680 \cos\left[\frac{c}{2} + d x\right] - 1680 \cos\left[\frac{3 c}{2} + d x\right] - 560 \cos\left[\frac{5 c}{2} + 3 d x\right] - 560 \cos\left[\frac{7 c}{2} + 3 d x\right] + 280 \cos\left[\frac{7 c}{2} + 4 d x\right] - 280 \cos\left[\frac{9 c}{2} + 4 d x\right] + 112 \cos\left[\frac{9 c}{2} + 5 d x\right] + 112 \cos\left[\frac{11 c}{2} + 5 d x\right] + 80 \cos\left[\frac{13 c}{2} + 7 d x\right] + 80 \cos\left[\frac{15 c}{2} + 7 d x\right] - 35 \cos\left[\frac{15 c}{2} + 8 d x\right] + 35 \cos\left[\frac{17 c}{2} + 8 d x\right] - 3360 \sin\left[\frac{c}{2}\right] + 1680 c \sin\left[\frac{c}{2}\right] - 1680 d x \sin\left[\frac{c}{2}\right] + 1680 \sin\left[\frac{c}{2} + d x\right] - 1680 \sin\left[\frac{3 c}{2} + d x\right] + 560 \sin\left[\frac{5 c}{2} + 3 d x\right] - 560 \sin\left[\frac{7 c}{2} + 3 d x\right] + 280 \sin\left[\frac{7 c}{2} + 4 d x\right] + 280 \sin\left[\frac{9 c}{2} + 4 d x\right] - 112 \sin\left[\frac{9 c}{2} + 5 d x\right] + 112 \sin\left[\frac{11 c}{2} + 5 d x\right] - 80 \sin\left[\frac{13 c}{2} + 7 d x\right] + 80 \sin\left[\frac{15 c}{2} + 7 d x\right] - 35 \sin\left[\frac{15 c}{2} + 8 d x\right] - 35 \sin\left[\frac{17 c}{2} + 8 d x\right] \right)$$

Problem 626: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^2}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 115 leaves, 8 steps):

$$\frac{x}{16 a} + \frac{\cos [c+d x]^5}{5 a d} - \frac{\cos [c+d x]^7}{7 a d} + \frac{\cos [c+d x] \sin [c+d x]}{16 a d} + \frac{\cos [c+d x]^3 \sin [c+d x]}{24 a d} - \frac{\cos [c+d x]^5 \sin [c+d x]}{6 a d}$$

Result (type 3, 414 leaves):

$$\begin{aligned}
 & \frac{1}{13440 a d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(840 d x \cos\left[\frac{c}{2}\right] + 315 \cos\left[\frac{c}{2} + d x\right] + 315 \cos\left[\frac{3 c}{2} + d x\right] + 105 \cos\left[\frac{3 c}{2} + 2 d x\right] - \right. \\
 & \quad 105 \cos\left[\frac{5 c}{2} + 2 d x\right] + 105 \cos\left[\frac{5 c}{2} + 3 d x\right] + 105 \cos\left[\frac{7 c}{2} + 3 d x\right] - 105 \cos\left[\frac{7 c}{2} + 4 d x\right] + \\
 & \quad 105 \cos\left[\frac{9 c}{2} + 4 d x\right] - 21 \cos\left[\frac{9 c}{2} + 5 d x\right] - 21 \cos\left[\frac{11 c}{2} + 5 d x\right] - 35 \cos\left[\frac{11 c}{2} + 6 d x\right] + \\
 & \quad 35 \cos\left[\frac{13 c}{2} + 6 d x\right] - 15 \cos\left[\frac{13 c}{2} + 7 d x\right] - 15 \cos\left[\frac{15 c}{2} + 7 d x\right] + 1050 \sin\left[\frac{c}{2}\right] + \\
 & \quad 840 d x \sin\left[\frac{c}{2}\right] - 315 \sin\left[\frac{c}{2} + d x\right] + 315 \sin\left[\frac{3 c}{2} + d x\right] + 105 \sin\left[\frac{3 c}{2} + 2 d x\right] + \\
 & \quad 105 \sin\left[\frac{5 c}{2} + 2 d x\right] - 105 \sin\left[\frac{5 c}{2} + 3 d x\right] + 105 \sin\left[\frac{7 c}{2} + 3 d x\right] - \\
 & \quad 105 \sin\left[\frac{7 c}{2} + 4 d x\right] - 105 \sin\left[\frac{9 c}{2} + 4 d x\right] + 21 \sin\left[\frac{9 c}{2} + 5 d x\right] - 21 \sin\left[\frac{11 c}{2} + 5 d x\right] - \\
 & \quad \left. 35 \sin\left[\frac{11 c}{2} + 6 d x\right] - 35 \sin\left[\frac{13 c}{2} + 6 d x\right] + 15 \sin\left[\frac{13 c}{2} + 7 d x\right] - 15 \sin\left[\frac{15 c}{2} + 7 d x\right] \right)
 \end{aligned}$$

Problem 627: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^6 \sin[c + d x]}{a + a \sin[c + d x]} dx$$

Optimal (type 3, 97 leaves, 7 steps):

$$\begin{aligned}
 & \frac{x}{16 a} - \frac{\cos[c + d x]^5}{5 a d} - \frac{\cos[c + d x] \sin[c + d x]}{16 a d} - \\
 & \frac{\cos[c + d x]^3 \sin[c + d x]}{24 a d} + \frac{\cos[c + d x]^5 \sin[c + d x]}{6 a d}
 \end{aligned}$$

Result (type 3, 377 leaves):

$$\begin{aligned}
 & - \frac{1}{1920 a d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(-30 (5 c - 4 d x) \cos\left[\frac{c}{2}\right] + 120 \cos\left[\frac{c}{2} + d x\right] + 120 \cos\left[\frac{3 c}{2} + d x\right] + 15 \cos\left[\frac{3 c}{2} + 2 d x\right] - \right. \\
 & 15 \cos\left[\frac{5 c}{2} + 2 d x\right] + 60 \cos\left[\frac{5 c}{2} + 3 d x\right] + 60 \cos\left[\frac{7 c}{2} + 3 d x\right] - 15 \cos\left[\frac{7 c}{2} + 4 d x\right] + \\
 & 15 \cos\left[\frac{9 c}{2} + 4 d x\right] + 12 \cos\left[\frac{9 c}{2} + 5 d x\right] + 12 \cos\left[\frac{11 c}{2} + 5 d x\right] - 5 \cos\left[\frac{11 c}{2} + 6 d x\right] + \\
 & 5 \cos\left[\frac{13 c}{2} + 6 d x\right] + 300 \sin\left[\frac{c}{2}\right] - 150 c \sin\left[\frac{c}{2}\right] + 120 d x \sin\left[\frac{c}{2}\right] - \\
 & 120 \sin\left[\frac{c}{2} + d x\right] + 120 \sin\left[\frac{3 c}{2} + d x\right] + 15 \sin\left[\frac{3 c}{2} + 2 d x\right] + 15 \sin\left[\frac{5 c}{2} + 2 d x\right] - \\
 & 60 \sin\left[\frac{5 c}{2} + 3 d x\right] + 60 \sin\left[\frac{7 c}{2} + 3 d x\right] - 15 \sin\left[\frac{7 c}{2} + 4 d x\right] - 15 \sin\left[\frac{9 c}{2} + 4 d x\right] - \\
 & \left. 12 \sin\left[\frac{9 c}{2} + 5 d x\right] + 12 \sin\left[\frac{11 c}{2} + 5 d x\right] - 5 \sin\left[\frac{11 c}{2} + 6 d x\right] - 5 \sin\left[\frac{13 c}{2} + 6 d x\right] \right)
 \end{aligned}$$

Problem 632: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \operatorname{Cot}[c+d x]^5}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 102 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{x}{a} - \frac{3 \operatorname{ArcTanh}[\cos [c+d x]]}{8 a d} - \frac{\operatorname{Cot}[c+d x]}{a d} + \\
 & \frac{\operatorname{Cot}[c+d x]^3}{3 a d} + \frac{3 \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{8 a d} - \frac{\operatorname{Cot}[c+d x]^3 \operatorname{Csc}[c+d x]}{4 a d}
 \end{aligned}$$

Result (type 3, 232 leaves):

$$\begin{aligned}
 & - \frac{1}{192 a d (1 + \sin [c+d x])} \\
 & \operatorname{Csc}[c+d x]^4 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \left(72 c + 72 d x + 18 \cos [c+d x] + \right. \\
 & 30 \cos [3 (c+d x)] + 24 c \cos [4 (c+d x)] + 24 d x \cos [4 (c+d x)] + \\
 & 27 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + 9 \cos [4 (c+d x)] \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] - 12 \cos [2 (c+d x)] \\
 & \left(8 c + 8 d x + 3 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] - 3 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \right) - 27 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] - \\
 & \left. 9 \cos [4 (c+d x)] \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] + 32 \sin [2 (c+d x)] - 32 \sin [4 (c+d x)] \right)
 \end{aligned}$$

Problem 633: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+d x]^6}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 82 leaves, 6 steps):

$$\frac{3 \operatorname{ArcTanh}[\cos[c+dx]]}{8ad} - \frac{\cot[c+dx]^5}{5ad} - \frac{3 \cot[c+dx] \operatorname{Csc}[c+dx]}{8ad} + \frac{\cot[c+dx]^3 \operatorname{Csc}[c+dx]}{4ad}$$

Result (type 3, 189 leaves):

$$\begin{aligned} & -\frac{1}{640ad} \operatorname{Csc}[c+dx]^5 \left(80 \cos[c+dx] + 40 \cos[3(c+dx)] + 8 \cos[5(c+dx)] \right) - \\ & 150 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] \sin[c+dx] + 150 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[c+dx] + \\ & 20 \sin[2(c+dx)] + 75 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] \sin[3(c+dx)] - \\ & 75 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[3(c+dx)] - 50 \sin[4(c+dx)] - \\ & 15 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] \sin[5(c+dx)] + 15 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] \sin[5(c+dx)] \end{aligned}$$

Problem 634: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^6 \sin[c+dx]^3}{(a+a \sin[c+dx])^2} dx$$

Optimal (type 3, 135 leaves, 13 steps):

$$\begin{aligned} & -\frac{x}{8a^2} - \frac{2 \cos[c+dx]^3}{3a^2d} + \frac{3 \cos[c+dx]^5}{5a^2d} - \frac{\cos[c+dx]^7}{7a^2d} - \\ & \frac{\cos[c+dx] \sin[c+dx]}{8a^2d} + \frac{\cos[c+dx]^3 \sin[c+dx]}{4a^2d} + \frac{\cos[c+dx]^3 \sin[c+dx]^3}{3a^2d} \end{aligned}$$

Result (type 3, 414 leaves):

$$\begin{aligned} & -\frac{1}{13440a^2d} \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \\ & \left(1680dx \cos\left[\frac{c}{2}\right] + 1365 \cos\left[\frac{c}{2}+dx\right] + 1365 \cos\left[\frac{3c}{2}+dx\right] - 210 \cos\left[\frac{3c}{2}+2dx\right] + \right. \\ & 210 \cos\left[\frac{5c}{2}+2dx\right] + 175 \cos\left[\frac{5c}{2}+3dx\right] + 175 \cos\left[\frac{7c}{2}+3dx\right] - 210 \cos\left[\frac{7c}{2}+4dx\right] + \\ & 210 \cos\left[\frac{9c}{2}+4dx\right] - 147 \cos\left[\frac{9c}{2}+5dx\right] - 147 \cos\left[\frac{11c}{2}+5dx\right] + 70 \cos\left[\frac{11c}{2}+6dx\right] - \\ & 70 \cos\left[\frac{13c}{2}+6dx\right] + 15 \cos\left[\frac{13c}{2}+7dx\right] + 15 \cos\left[\frac{15c}{2}+7dx\right] - 420 \sin\left[\frac{c}{2}\right] + \\ & 1680dx \sin\left[\frac{c}{2}\right] - 1365 \sin\left[\frac{c}{2}+dx\right] + 1365 \sin\left[\frac{3c}{2}+dx\right] - 210 \sin\left[\frac{3c}{2}+2dx\right] - \\ & 210 \sin\left[\frac{5c}{2}+2dx\right] - 175 \sin\left[\frac{5c}{2}+3dx\right] + 175 \sin\left[\frac{7c}{2}+3dx\right] - 210 \sin\left[\frac{7c}{2}+4dx\right] - \\ & 210 \sin\left[\frac{9c}{2}+4dx\right] + 147 \sin\left[\frac{9c}{2}+5dx\right] - 147 \sin\left[\frac{11c}{2}+5dx\right] + \\ & \left. 70 \sin\left[\frac{11c}{2}+6dx\right] + 70 \sin\left[\frac{13c}{2}+6dx\right] - 15 \sin\left[\frac{13c}{2}+7dx\right] + 15 \sin\left[\frac{15c}{2}+7dx\right] \right) \end{aligned}$$

Problem 635: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^2}{(a+a \sin [c+d x])^2} dx$$

Optimal (type 3, 104 leaves, 6 steps):

$$\frac{3 x}{16 a^2} + \frac{\cos [c+d x]^5}{10 a^2 d} + \frac{3 \cos [c+d x] \sin [c+d x]}{16 a^2 d} + \frac{\cos [c+d x]^3 \sin [c+d x]}{8 a^2 d} + \frac{\cos [c+d x]^3 (a-a \sin [c+d x])^3}{6 a^5 d}$$

Result (type 3, 362 leaves):

$$\frac{1}{1920 a^2 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right)} \left(360 d x \cos \left[\frac{c}{2} \right] + 240 \cos \left[\frac{c}{2} + d x \right] + 240 \cos \left[\frac{3 c}{2} + d x \right] - 15 \cos \left[\frac{3 c}{2} + 2 d x \right] + 15 \cos \left[\frac{5 c}{2} + 2 d x \right] + 40 \cos \left[\frac{5 c}{2} + 3 d x \right] + 40 \cos \left[\frac{7 c}{2} + 3 d x \right] - 45 \cos \left[\frac{7 c}{2} + 4 d x \right] + 45 \cos \left[\frac{9 c}{2} + 4 d x \right] - 24 \cos \left[\frac{9 c}{2} + 5 d x \right] - 24 \cos \left[\frac{11 c}{2} + 5 d x \right] + 5 \cos \left[\frac{11 c}{2} + 6 d x \right] - 5 \cos \left[\frac{13 c}{2} + 6 d x \right] + 50 \sin \left[\frac{c}{2} \right] + 360 d x \sin \left[\frac{c}{2} \right] - 240 \sin \left[\frac{c}{2} + d x \right] + 240 \sin \left[\frac{3 c}{2} + d x \right] - 15 \sin \left[\frac{3 c}{2} + 2 d x \right] - 15 \sin \left[\frac{5 c}{2} + 2 d x \right] - 40 \sin \left[\frac{5 c}{2} + 3 d x \right] + 40 \sin \left[\frac{7 c}{2} + 3 d x \right] - 45 \sin \left[\frac{7 c}{2} + 4 d x \right] - 45 \sin \left[\frac{9 c}{2} + 4 d x \right] + 24 \sin \left[\frac{9 c}{2} + 5 d x \right] - 24 \sin \left[\frac{11 c}{2} + 5 d x \right] + 5 \sin \left[\frac{11 c}{2} + 6 d x \right] + 5 \sin \left[\frac{13 c}{2} + 6 d x \right] \right)$$

Problem 636: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]}{(a+a \sin [c+d x])^2} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$-\frac{x}{4 a^2} - \frac{2 \cos [c+d x]^5}{15 a^2 d} - \frac{\cos [c+d x] \sin [c+d x]}{4 a^2 d} - \frac{\cos [c+d x]^3 \sin [c+d x]}{6 a^2 d} - \frac{\cos [c+d x]^7}{3 d (a+a \sin [c+d x])^2}$$

Result (type 3, 258 leaves):

$$\frac{1}{480 a^2 d} \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(-120 d x \cos \left[\frac{c}{2} \right] - 90 \cos \left[\frac{c}{2} + d x \right] - 90 \cos \left[\frac{3c}{2} + d x \right] - 25 \cos \left[\frac{5c}{2} + 3 d x \right] - 25 \cos \left[\frac{7c}{2} + 3 d x \right] + 15 \cos \left[\frac{7c}{2} + 4 d x \right] - 15 \cos \left[\frac{9c}{2} + 4 d x \right] + 3 \cos \left[\frac{9c}{2} + 5 d x \right] + 3 \cos \left[\frac{11c}{2} + 5 d x \right] + 50 \sin \left[\frac{c}{2} \right] - 120 d x \sin \left[\frac{c}{2} \right] + 90 \sin \left[\frac{c}{2} + d x \right] - 90 \sin \left[\frac{3c}{2} + d x \right] + 25 \sin \left[\frac{5c}{2} + 3 d x \right] - 25 \sin \left[\frac{7c}{2} + 3 d x \right] + 15 \sin \left[\frac{7c}{2} + 4 d x \right] + 15 \sin \left[\frac{9c}{2} + 4 d x \right] - 3 \sin \left[\frac{9c}{2} + 5 d x \right] + 3 \sin \left[\frac{11c}{2} + 5 d x \right] \right)$$

Problem 644: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^3}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 129 leaves, 14 steps):

$$\frac{23 x}{16 a^3} - \frac{4 \cos [c+d x]}{a^3 d} + \frac{7 \cos [c+d x]^3}{3 a^3 d} - \frac{3 \cos [c+d x]^5}{5 a^3 d} + \frac{23 \cos [c+d x] \sin [c+d x]}{16 a^3 d} + \frac{23 \cos [c+d x] \sin [c+d x]^3}{24 a^3 d} + \frac{\cos [c+d x] \sin [c+d x]^5}{6 a^3 d}$$

Result (type 3, 362 leaves):

$$\frac{1}{1920 a^3 d} \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(2760 d x \cos \left[\frac{c}{2} \right] + 2520 \cos \left[\frac{c}{2} + d x \right] + 2520 \cos \left[\frac{3c}{2} + d x \right] - 945 \cos \left[\frac{3c}{2} + 2 d x \right] + 945 \cos \left[\frac{5c}{2} + 2 d x \right] - 380 \cos \left[\frac{5c}{2} + 3 d x \right] - 380 \cos \left[\frac{7c}{2} + 3 d x \right] + 135 \cos \left[\frac{7c}{2} + 4 d x \right] - 135 \cos \left[\frac{9c}{2} + 4 d x \right] + 36 \cos \left[\frac{9c}{2} + 5 d x \right] + 36 \cos \left[\frac{11c}{2} + 5 d x \right] - 5 \cos \left[\frac{11c}{2} + 6 d x \right] + 5 \cos \left[\frac{13c}{2} + 6 d x \right] - 18 \sin \left[\frac{c}{2} \right] + 2760 d x \sin \left[\frac{c}{2} \right] - 2520 \sin \left[\frac{c}{2} + d x \right] + 2520 \sin \left[\frac{3c}{2} + d x \right] - 945 \sin \left[\frac{3c}{2} + 2 d x \right] - 945 \sin \left[\frac{5c}{2} + 2 d x \right] + 380 \sin \left[\frac{5c}{2} + 3 d x \right] - 380 \sin \left[\frac{7c}{2} + 3 d x \right] + 135 \sin \left[\frac{7c}{2} + 4 d x \right] + 135 \sin \left[\frac{9c}{2} + 4 d x \right] - 36 \sin \left[\frac{9c}{2} + 5 d x \right] + 36 \sin \left[\frac{11c}{2} + 5 d x \right] - 5 \sin \left[\frac{11c}{2} + 6 d x \right] - 5 \sin \left[\frac{13c}{2} + 6 d x \right] \right)$$

Problem 645: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^2}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 105 leaves, 12 steps):

$$\frac{13x}{8a^3} + \frac{4 \cos[c+dx]}{a^3 d} - \frac{5 \cos[c+dx]^3}{3a^3 d} + \frac{\cos[c+dx]^5}{5a^3 d} - \frac{13 \cos[c+dx] \sin[c+dx]}{8a^3 d} - \frac{3 \cos[c+dx] \sin[c+dx]^3}{4a^3 d}$$

Result (type 3, 310 leaves):

$$\frac{1}{960 a^3 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(1560 d x \cos\left[\frac{c}{2}\right] + 1380 \cos\left[\frac{c}{2} + dx\right] + 1380 \cos\left[\frac{3c}{2} + dx\right] - 480 \cos\left[\frac{3c}{2} + 2dx\right] + 480 \cos\left[\frac{5c}{2} + 2dx\right] - 170 \cos\left[\frac{5c}{2} + 3dx\right] - 170 \cos\left[\frac{7c}{2} + 3dx\right] + 45 \cos\left[\frac{7c}{2} + 4dx\right] - 45 \cos\left[\frac{9c}{2} + 4dx\right] + 6 \cos\left[\frac{9c}{2} + 5dx\right] + 6 \cos\left[\frac{11c}{2} + 5dx\right] + 10 \sin\left[\frac{c}{2}\right] + 1560 d x \sin\left[\frac{c}{2}\right] - 1380 \sin\left[\frac{c}{2} + dx\right] + 1380 \sin\left[\frac{3c}{2} + dx\right] - 480 \sin\left[\frac{3c}{2} + 2dx\right] - 480 \sin\left[\frac{5c}{2} + 2dx\right] + 170 \sin\left[\frac{5c}{2} + 3dx\right] - 170 \sin\left[\frac{7c}{2} + 3dx\right] + 45 \sin\left[\frac{7c}{2} + 4dx\right] + 45 \sin\left[\frac{9c}{2} + 4dx\right] - 6 \sin\left[\frac{9c}{2} + 5dx\right] + 6 \sin\left[\frac{11c}{2} + 5dx\right] \right)$$

Problem 646: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^6 \sin[c+dx]}{(a+a \sin[c+dx])^3} dx$$

Optimal (type 3, 84 leaves, 5 steps):

$$-\frac{15x}{8a^3} - \frac{4 \cos[c+dx]}{a^3 d} + \frac{\cos[c+dx]^3}{a^3 d} + \frac{15 \cos[c+dx] \sin[c+dx]}{8a^3 d} + \frac{\cos[c+dx] \sin[c+dx]^3}{4a^3 d}$$

Result (type 3, 252 leaves):

$$\frac{1}{64 a^3 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(120 d x \cos\left[\frac{c}{2}\right] + 104 \cos\left[\frac{c}{2} + dx\right] + 104 \cos\left[\frac{3c}{2} + dx\right] - 32 \cos\left[\frac{3c}{2} + 2dx\right] + 32 \cos\left[\frac{5c}{2} + 2dx\right] - 8 \cos\left[\frac{5c}{2} + 3dx\right] - 8 \cos\left[\frac{7c}{2} + 3dx\right] + \cos\left[\frac{7c}{2} + 4dx\right] - \cos\left[\frac{9c}{2} + 4dx\right] - 2 \sin\left[\frac{c}{2}\right] + 120 d x \sin\left[\frac{c}{2}\right] - 104 \sin\left[\frac{c}{2} + dx\right] + 104 \sin\left[\frac{3c}{2} + dx\right] - 32 \sin\left[\frac{3c}{2} + 2dx\right] - 32 \sin\left[\frac{5c}{2} + 2dx\right] + 8 \sin\left[\frac{5c}{2} + 3dx\right] - 8 \sin\left[\frac{7c}{2} + 3dx\right] + \sin\left[\frac{7c}{2} + 4dx\right] + \sin\left[\frac{9c}{2} + 4dx\right] \right)$$

Problem 648: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \cot [c+d x]^2}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 49 leaves, 7 steps):

$$\frac{3 x}{a^3} + \frac{3 \operatorname{ArcTanh}[\cos [c+d x]]}{a^3 d} + \frac{\cos [c+d x]}{a^3 d} - \frac{\cot [c+d x]}{a^3 d}$$

Result (type 3, 106 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \left(6 (c+d x) + 2 \cos [c+d x] - \cot \left[\frac{1}{2} (c+d x) \right] + 6 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] - 6 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] + \tan \left[\frac{1}{2} (c+d x) \right] \right) \right) / \left(2 d (a+a \sin [c+d x])^3 \right)$$

Problem 649: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]^3}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 60 leaves, 8 steps):

$$-\frac{x}{a^3} - \frac{7 \operatorname{ArcTanh}[\cos [c+d x]]}{2 a^3 d} + \frac{3 \cot [c+d x]}{a^3 d} - \frac{\cot [c+d x] \operatorname{Csc} [c+d x]}{2 a^3 d}$$

Result (type 3, 126 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \left(-8 (c+d x) + 12 \cot \left[\frac{1}{2} (c+d x) \right] - \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2 - 28 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] + 28 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] + \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 - 12 \tan \left[\frac{1}{2} (c+d x) \right] \right) \right) / \left(8 d (a+a \sin [c+d x])^3 \right)$$

Problem 651: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \cot [c+d x]^5}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 93 leaves, 12 steps):

$$-\frac{15 \operatorname{ArcTanh}[\cos [c+d x]]}{8 a^3 d} + \frac{4 \cot [c+d x]}{a^3 d} + \frac{\cot [c+d x]^3}{a^3 d} - \frac{15 \cot [c+d x] \operatorname{Csc} [c+d x]}{8 a^3 d} - \frac{\cot [c+d x] \operatorname{Csc} [c+d x]^3}{4 a^3 d}$$

Result (type 3, 555 leaves):

$$\begin{aligned}
& \frac{3 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2d(a+a\operatorname{Sin}[c+dx])^3} - \\
& \frac{15 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32d(a+a\operatorname{Sin}[c+dx])^3} + \\
& \left(\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) / \\
& \left(8d(a+a\operatorname{Sin}[c+dx])^3\right) - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64d(a+a\operatorname{Sin}[c+dx])^3} - \\
& \frac{15 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8d(a+a\operatorname{Sin}[c+dx])^3} + \\
& \frac{15 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{8d(a+a\operatorname{Sin}[c+dx])^3} + \\
& \frac{15 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{32d(a+a\operatorname{Sin}[c+dx])^3} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{64d(a+a\operatorname{Sin}[c+dx])^3} - \\
& \frac{3 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d(a+a\operatorname{Sin}[c+dx])^3} - \\
& \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \\
& \left(8d(a+a\operatorname{Sin}[c+dx])^3\right)
\end{aligned}$$

Problem 653: Unable to integrate problem.

$$\int \operatorname{Cos}[c+dx]^6 \operatorname{Sin}[c+dx]^n (a+a\operatorname{Sin}[c+dx])^3 dx$$

Optimal (type 5, 267 leaves, 6 steps):

$$\begin{aligned}
 & \left(a^3 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{1+n} \right) / \\
 & \left(d(1+n) \sqrt{\cos [c+d x]^2} \right) + \\
 & \left(3 a^3 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{2+n} \right) / \\
 & \left(d(2+n) \sqrt{\cos [c+d x]^2} \right) + \\
 & \left(3 a^3 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{3+n}{2}, \frac{5+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{3+n} \right) / \\
 & \left(d(3+n) \sqrt{\cos [c+d x]^2} \right) + \\
 & \left(a^3 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{4+n}{2}, \frac{6+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{4+n} \right) / \\
 & \left(d(4+n) \sqrt{\cos [c+d x]^2} \right)
 \end{aligned}$$

Result (type 8, 31 leaves):

$$\int \cos [c+d x]^6 \sin [c+d x]^n (a+a \sin [c+d x])^3 dx$$

Problem 654: Unable to integrate problem.

$$\int \cos [c+d x]^6 \sin [c+d x]^n (a+a \sin [c+d x])^2 dx$$

Optimal (type 5, 200 leaves, 5 steps):

$$\begin{aligned}
 & \left(a^2 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{1+n} \right) / \\
 & \left(d(1+n) \sqrt{\cos [c+d x]^2} \right) + \\
 & \left(2 a^2 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{2+n} \right) / \\
 & \left(d(2+n) \sqrt{\cos [c+d x]^2} \right) + \\
 & \left(a^2 \cos [c+d x] \operatorname{Hypergeometric2F1} \left[-\frac{5}{2}, \frac{3+n}{2}, \frac{5+n}{2}, \sin [c+d x]^2 \right] \sin [c+d x]^{3+n} \right) / \\
 & \left(d(3+n) \sqrt{\cos [c+d x]^2} \right)
 \end{aligned}$$

Result (type 8, 31 leaves):

$$\int \cos [c+d x]^6 \sin [c+d x]^n (a+a \sin [c+d x])^2 dx$$

Problem 655: Unable to integrate problem.

$$\int \cos [c+d x]^6 \sin [c+d x]^n (a+a \sin [c+d x]) dx$$

Optimal (type 5, 129 leaves, 3 steps):

$$\left(a \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \operatorname{Sin}[c + d x]^2\right] \operatorname{Sin}[c + d x]^{1+n} \right) /$$

$$\left(d (1+n) \sqrt{\operatorname{Cos}[c + d x]^2} \right) +$$

$$\left(a \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \operatorname{Sin}[c + d x]^2\right] \operatorname{Sin}[c + d x]^{2+n} \right) /$$

$$\left(d (2+n) \sqrt{\operatorname{Cos}[c + d x]^2} \right)$$

Result (type 8, 29 leaves):

$$\int \operatorname{Cos}[c + d x]^6 \operatorname{Sin}[c + d x]^n (a + a \operatorname{Sin}[c + d x]) dx$$

Problem 669: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c + d x]^7 \operatorname{Csc}[c + d x] (a + a \operatorname{Sin}[c + d x]) dx$$

Optimal (type 3, 119 leaves, 4 steps):

$$\frac{a \operatorname{Csc}[c + d x]}{d} - \frac{3 a \operatorname{Csc}[c + d x]^2}{2 d} - \frac{a \operatorname{Csc}[c + d x]^3}{d} + \frac{3 a \operatorname{Csc}[c + d x]^4}{4 d} +$$

$$\frac{3 a \operatorname{Csc}[c + d x]^5}{5 d} - \frac{a \operatorname{Csc}[c + d x]^6}{6 d} - \frac{a \operatorname{Csc}[c + d x]^7}{7 d} - \frac{a \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d}$$

Result (type 3, 278 leaves):

$$\frac{381 a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{1120 d} - \frac{179 a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{2240 d} +$$

$$\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^4}{70 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^6}{896 d} -$$

$$\frac{3 a \operatorname{Csc}[c + d x]^2}{2 d} + \frac{3 a \operatorname{Csc}[c + d x]^4}{4 d} - \frac{a \operatorname{Csc}[c + d x]^6}{6 d} - \frac{a \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} +$$

$$\frac{381 a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{1120 d} - \frac{179 a \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{2240 d} +$$

$$\frac{a \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{70 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{896 d}$$

Problem 670: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c + d x]^7 \operatorname{Csc}[c + d x]^2 (a + a \operatorname{Sin}[c + d x]) dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$-\frac{a \operatorname{Cot}[c + d x]^8}{8 d} + \frac{a \operatorname{Csc}[c + d x]}{d} - \frac{a \operatorname{Csc}[c + d x]^3}{d} + \frac{3 a \operatorname{Csc}[c + d x]^5}{5 d} - \frac{a \operatorname{Csc}[c + d x]^7}{7 d}$$

Result (type 3, 233 leaves):

$$\begin{aligned} & \frac{381 a \cot\left[\frac{1}{2}(c+dx)\right]}{1120 d} - \frac{a \cot[c+dx]^8}{8 d} - \frac{179 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{2240 d} + \\ & \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{70 d} - \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{896 d} + \\ & \frac{381 a \tan\left[\frac{1}{2}(c+dx)\right]}{1120 d} - \frac{179 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{2240 d} + \\ & \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{70 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{896 d} \end{aligned}$$

Problem 671: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^7 \operatorname{Csc}[c+dx]^3 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 81 leaves, 6 steps):

$$-\frac{a \cot[c+dx]^8}{8 d} + \frac{a \operatorname{Csc}[c+dx]^3}{3 d} - \frac{3 a \operatorname{Csc}[c+dx]^5}{5 d} + \frac{3 a \operatorname{Csc}[c+dx]^7}{7 d} - \frac{a \operatorname{Csc}[c+dx]^9}{9 d}$$

Result (type 3, 293 leaves):

$$\begin{aligned} & \frac{1823 a \cot\left[\frac{1}{2}(c+dx)\right]}{80640 d} - \frac{a \cot[c+dx]^8}{8 d} + \frac{1823 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{161280 d} - \\ & \frac{463 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{53760 d} + \frac{73 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{32256 d} - \\ & \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{4608 d} + \frac{1823 a \tan\left[\frac{1}{2}(c+dx)\right]}{80640 d} + \\ & \frac{1823 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{161280 d} - \frac{463 a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{53760 d} + \\ & \frac{73 a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{32256 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^8 \tan\left[\frac{1}{2}(c+dx)\right]}{4608 d} \end{aligned}$$

Problem 672: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^7 \operatorname{Csc}[c+dx]^4 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 97 leaves, 7 steps):

$$\begin{aligned} & -\frac{a \cot[c+dx]^8}{8 d} - \frac{a \cot[c+dx]^{10}}{10 d} + \frac{a \operatorname{Csc}[c+dx]^3}{3 d} - \\ & \frac{3 a \operatorname{Csc}[c+dx]^5}{5 d} + \frac{3 a \operatorname{Csc}[c+dx]^7}{7 d} - \frac{a \operatorname{Csc}[c+dx]^9}{9 d} \end{aligned}$$

Result (type 3, 341 leaves):

$$\frac{1823 a \cot \left[\frac{1}{2} (c+d x) \right]}{80640 d} + \frac{1823 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2}{161280 d} -$$

$$\frac{463 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^4}{53760 d} + \frac{73 a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^6}{32256 d} -$$

$$\frac{a \cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^8}{4608 d} + \frac{a \operatorname{Csc} [c+d x]^4}{4 d} - \frac{a \operatorname{Csc} [c+d x]^6}{2 d} +$$

$$\frac{3 a \operatorname{Csc} [c+d x]^8}{8 d} - \frac{a \operatorname{Csc} [c+d x]^{10}}{10 d} + \frac{1823 a \tan \left[\frac{1}{2} (c+d x) \right]}{80640 d} +$$

$$\frac{1823 a \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right]}{161280 d} - \frac{463 a \sec \left[\frac{1}{2} (c+d x) \right]^4 \tan \left[\frac{1}{2} (c+d x) \right]}{53760 d} +$$

$$\frac{73 a \sec \left[\frac{1}{2} (c+d x) \right]^6 \tan \left[\frac{1}{2} (c+d x) \right]}{32256 d} - \frac{a \sec \left[\frac{1}{2} (c+d x) \right]^8 \tan \left[\frac{1}{2} (c+d x) \right]}{4608 d}$$

Problem 673: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^7 \operatorname{Csc} [c+d x]^5 (a+a \sin [c+d x]) dx$$

Optimal (type 3, 97 leaves, 7 steps):

$$-\frac{a \cot [c+d x]^8}{8 d} - \frac{a \cot [c+d x]^{10}}{10 d} + \frac{a \operatorname{Csc} [c+d x]^5}{5 d} -$$

$$\frac{3 a \operatorname{Csc} [c+d x]^7}{7 d} + \frac{a \operatorname{Csc} [c+d x]^9}{3 d} - \frac{a \operatorname{Csc} [c+d x]^{11}}{11 d}$$

Result (type 3, 401 leaves):

$$\begin{aligned}
 & \frac{2911 a \cot\left[\frac{1}{2}(c+dx)\right]}{591360 d} + \frac{2911 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{1182720 d} + \\
 & \frac{27 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{197120 d} - \frac{485 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{473088 d} + \\
 & \frac{13 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{33792 d} - \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^{10}}{22528 d} + \\
 & \frac{a \operatorname{Csc}[c+dx]^4}{4 d} - \frac{a \operatorname{Csc}[c+dx]^6}{2 d} + \frac{3 a \operatorname{Csc}[c+dx]^8}{8 d} - \frac{a \operatorname{Csc}[c+dx]^{10}}{10 d} + \\
 & \frac{2911 a \tan\left[\frac{1}{2}(c+dx)\right]}{591360 d} + \frac{2911 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1182720 d} + \\
 & \frac{27 a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{197120 d} - \frac{485 a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{473088 d} + \\
 & \frac{13 a \sec\left[\frac{1}{2}(c+dx)\right]^8 \tan\left[\frac{1}{2}(c+dx)\right]}{33792 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^{10} \tan\left[\frac{1}{2}(c+dx)\right]}{22528 d}
 \end{aligned}$$

Problem 674: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^7 \operatorname{Csc}[c+dx]^6 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 113 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{a \cot[c+dx]^8}{8 d} - \frac{a \cot[c+dx]^{10}}{5 d} - \frac{a \cot[c+dx]^{12}}{12 d} + \\
 & \frac{a \operatorname{Csc}[c+dx]^5}{5 d} - \frac{3 a \operatorname{Csc}[c+dx]^7}{7 d} + \frac{a \operatorname{Csc}[c+dx]^9}{3 d} - \frac{a \operatorname{Csc}[c+dx]^{11}}{11 d}
 \end{aligned}$$

Result (type 3, 401 leaves):

$$\begin{aligned}
 & \frac{2911 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{591360 d} + \frac{2911 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{1182720 d} + \\
 & \frac{27 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{197120 d} - \frac{485 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{473088 d} + \\
 & \frac{13 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{33792 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10}}{22528 d} + \\
 & \frac{a \operatorname{Csc}[c+d x]^6}{6 d} - \frac{3 a \operatorname{Csc}[c+d x]^8}{8 d} + \frac{3 a \operatorname{Csc}[c+d x]^{10}}{10 d} - \frac{a \operatorname{Csc}[c+d x]^{12}}{12 d} + \\
 & \frac{2911 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{591360 d} + \frac{2911 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1182720 d} + \\
 & \frac{27 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{197120 d} - \frac{485 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{473088 d} + \\
 & \frac{13 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{33792 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{10} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{22528 d}
 \end{aligned}$$

Problem 675: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^7 \operatorname{Csc}[c+d x]^7 (a+a \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 113 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{a \operatorname{Cot}[c+d x]^8}{8 d} - \frac{a \operatorname{Cot}[c+d x]^{10}}{5 d} - \frac{a \operatorname{Cot}[c+d x]^{12}}{12 d} + \\
 & \frac{a \operatorname{Csc}[c+d x]^7}{7 d} - \frac{a \operatorname{Csc}[c+d x]^9}{3 d} + \frac{3 a \operatorname{Csc}[c+d x]^{11}}{11 d} - \frac{a \operatorname{Csc}[c+d x]^{13}}{13 d}
 \end{aligned}$$

Result (type 3, 461 leaves):

$$\begin{aligned}
 & \frac{10027 a \cot\left[\frac{1}{2}(c+dx)\right]}{6150144 d} + \frac{10027 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{12300288 d} + \\
 & \frac{755 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{4100096 d} - \frac{101 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{768768 d} - \\
 & \frac{101 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{878592 d} + \frac{79 a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^{10}}{1171456 d} - \\
 & \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^{12}}{106496 d} + \frac{a \operatorname{Csc}[c+dx]^6}{6 d} - \frac{3 a \operatorname{Csc}[c+dx]^8}{8 d} + \\
 & \frac{3 a \operatorname{Csc}[c+dx]^{10}}{10 d} - \frac{a \operatorname{Csc}[c+dx]^{12}}{12 d} + \frac{10027 a \tan\left[\frac{1}{2}(c+dx)\right]}{6150144 d} + \\
 & \frac{10027 a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{12300288 d} + \frac{755 a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{4100096 d} - \\
 & \frac{101 a \sec\left[\frac{1}{2}(c+dx)\right]^6 \tan\left[\frac{1}{2}(c+dx)\right]}{768768 d} - \frac{101 a \sec\left[\frac{1}{2}(c+dx)\right]^8 \tan\left[\frac{1}{2}(c+dx)\right]}{878592 d} + \\
 & \frac{79 a \sec\left[\frac{1}{2}(c+dx)\right]^{10} \tan\left[\frac{1}{2}(c+dx)\right]}{1171456 d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^{12} \tan\left[\frac{1}{2}(c+dx)\right]}{106496 d}
 \end{aligned}$$

Problem 676: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^7 \operatorname{Csc}[c+dx]^8 (a + a \sin[c+dx]) dx$$

Optimal (type 3, 129 leaves, 4 steps):

$$\begin{aligned}
 & \frac{a \operatorname{Csc}[c+dx]^7}{7 d} + \frac{a \operatorname{Csc}[c+dx]^8}{8 d} - \frac{a \operatorname{Csc}[c+dx]^9}{3 d} - \frac{3 a \operatorname{Csc}[c+dx]^{10}}{10 d} + \\
 & \frac{3 a \operatorname{Csc}[c+dx]^{11}}{11 d} + \frac{a \operatorname{Csc}[c+dx]^{12}}{4 d} - \frac{a \operatorname{Csc}[c+dx]^{13}}{13 d} - \frac{a \operatorname{Csc}[c+dx]^{14}}{14 d}
 \end{aligned}$$

Result (type 3, 461 leaves):

$$\begin{aligned}
 & \frac{10027 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{6150144 d} + \frac{10027 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{12300288 d} + \\
 & \frac{755 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{4100096 d} - \frac{101 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{768768 d} - \\
 & \frac{101 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{878592 d} + \frac{79 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10}}{1171456 d} - \\
 & \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{12}}{106496 d} + \frac{a \operatorname{Csc}[c+d x]^8}{8 d} - \frac{3 a \operatorname{Csc}[c+d x]^{10}}{10 d} + \\
 & \frac{a \operatorname{Csc}[c+d x]^{12}}{4 d} - \frac{a \operatorname{Csc}[c+d x]^{14}}{14 d} + \frac{10027 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{6150144 d} + \\
 & \frac{10027 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{12300288 d} + \frac{755 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{4100096 d} - \\
 & \frac{101 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{768768 d} - \frac{101 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{878592 d} + \\
 & \frac{79 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{10} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1171456 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{12} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{106496 d}
 \end{aligned}$$

Problem 697: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^7 \sin [c+d x]^n (a+a \sin [c+d x])^3 d x$$

Optimal (type 3, 184 leaves, 3 steps):

$$\begin{aligned}
 & \frac{a^3 \sin [c+d x]^{1+n}}{d(1+n)} + \frac{3 a^3 \sin [c+d x]^{2+n}}{d(2+n)} - \frac{8 a^3 \sin [c+d x]^{4+n}}{d(4+n)} - \frac{6 a^3 \sin [c+d x]^{5+n}}{d(5+n)} + \\
 & \frac{6 a^3 \sin [c+d x]^{6+n}}{d(6+n)} + \frac{8 a^3 \sin [c+d x]^{7+n}}{d(7+n)} - \frac{3 a^3 \sin [c+d x]^{9+n}}{d(9+n)} - \frac{a^3 \sin [c+d x]^{10+n}}{d(10+n)}
 \end{aligned}$$

Result (type 3, 1019 leaves):

$$\begin{aligned}
 & \frac{1}{d \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^6} \\
 & \sin [c+d x]^n (a+a \sin [c+d x])^3 \left(\frac{3(11792+2276 n+260 n^2+11 n^3)}{256(2+n)(4+n)(6+n)(10+n)} + \right. \\
 & \left. \frac{\left((28665+4541 n+471 n^2+19 n^3) \left(-\frac{1}{256} i \cos [c+d x] + \frac{1}{256} \sin [c+d x] \right) \right)}{\left((1+n)(5+n)(7+n)(9+n) \right)} + \right. \\
 & \left. \frac{\left((28665+4541 n+471 n^2+19 n^3) \left(\frac{1}{256} i \cos [c+d x] + \frac{1}{256} \sin [c+d x] \right) \right)}{\left((1+n)(5+n)(7+n)(9+n) \right)} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((-21840 + 2252n + 492n^2 + 25n^3) \left(\frac{1}{512} \cos[2(c+dx)] - \frac{1}{512} i \sin[2(c+dx)] \right) \right) / \\
 & \quad ((2+n)(4+n)(6+n)(10+n)) + \\
 & \left((-21840 + 2252n + 492n^2 + 25n^3) \left(\frac{1}{512} \cos[2(c+dx)] + \frac{1}{512} i \sin[2(c+dx)] \right) \right) / \\
 & \quad ((2+n)(4+n)(6+n)(10+n)) + \\
 & \left((735 + 108n + 5n^2) \left(-\frac{3}{128} i \cos[3(c+dx)] + \frac{3}{128} \sin[3(c+dx)] \right) \right) / \\
 & \quad ((5+n)(7+n)(9+n)) + \frac{(735 + 108n + 5n^2) \left(\frac{3}{128} i \cos[3(c+dx)] + \frac{3}{128} \sin[3(c+dx)] \right)}{(5+n)(7+n)(9+n)} + \\
 & \left((-1320 - 166n - 7n^2) \left(\frac{1}{128} \cos[4(c+dx)] - \frac{1}{128} i \sin[4(c+dx)] \right) \right) / \\
 & \quad ((4+n)(6+n)(10+n)) + \\
 & \left((-1320 - 166n - 7n^2) \left(\frac{1}{128} \cos[4(c+dx)] + \frac{1}{128} i \sin[4(c+dx)] \right) \right) / \\
 & \quad ((4+n)(6+n)(10+n)) + \frac{(63 + 76n + 5n^2) \left(-\frac{1}{128} i \cos[5(c+dx)] + \frac{1}{128} \sin[5(c+dx)] \right)}{(5+n)(7+n)(9+n)} + \\
 & \frac{(63 + 76n + 5n^2) \left(\frac{1}{128} i \cos[5(c+dx)] + \frac{1}{128} \sin[5(c+dx)] \right)}{(5+n)(7+n)(9+n)} + \\
 & \frac{(230 + 17n) \left(-\frac{3 \cos[6(c+dx)]}{1024} - \frac{3 i \sin[6(c+dx)]}{1024} \right)}{(6+n)(10+n)} + \frac{(230 + 17n) \left(-\frac{3 \cos[6(c+dx)]}{1024} + \frac{3 i \sin[6(c+dx)]}{1024} \right)}{(6+n)(10+n)} + \\
 & \frac{(99 + 5n) \left(-\frac{1}{512} i \cos[7(c+dx)] - \frac{1}{512} \sin[7(c+dx)] \right)}{(7+n)(9+n)} + \\
 & \frac{(99 + 5n) \left(\frac{1}{512} i \cos[7(c+dx)] - \frac{1}{512} \sin[7(c+dx)] \right)}{(7+n)(9+n)} + \\
 & \frac{-\frac{5}{512} \cos[8(c+dx)] - \frac{5}{512} i \sin[8(c+dx)]}{10+n} + \frac{-\frac{5}{512} \cos[8(c+dx)] + \frac{5}{512} i \sin[8(c+dx)]}{10+n} + \\
 & \frac{-\frac{3}{512} i \cos[9(c+dx)] - \frac{3}{512} \sin[9(c+dx)]}{9+n} + \frac{\frac{3}{512} i \cos[9(c+dx)] - \frac{3}{512} \sin[9(c+dx)]}{9+n} + \\
 & \left. \frac{\frac{\cos[10(c+dx)]}{1024} - \frac{i \sin[10(c+dx)]}{1024}}{10+n} + \frac{\frac{\cos[10(c+dx)]}{1024} + \frac{i \sin[10(c+dx)]}{1024}}{10+n} \right)
 \end{aligned}$$

Problem 698: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^7 \sin[c+dx]^n (a+a \sin[c+dx])^2 dx$$

Optimal (type 3, 184 leaves, 3 steps):

$$\frac{a^2 \operatorname{Sin}[c + d x]^{1+n}}{d (1+n)} + \frac{2 a^2 \operatorname{Sin}[c + d x]^{2+n}}{d (2+n)} - \frac{2 a^2 \operatorname{Sin}[c + d x]^{3+n}}{d (3+n)} - \frac{6 a^2 \operatorname{Sin}[c + d x]^{4+n}}{d (4+n)} +$$

$$\frac{6 a^2 \operatorname{Sin}[c + d x]^{6+n}}{d (6+n)} + \frac{2 a^2 \operatorname{Sin}[c + d x]^{7+n}}{d (7+n)} - \frac{2 a^2 \operatorname{Sin}[c + d x]^{8+n}}{d (8+n)} - \frac{a^2 \operatorname{Sin}[c + d x]^{9+n}}{d (9+n)}$$

Result (type 3, 925 leaves):

$$\frac{1}{d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4}$$

$$\operatorname{Sin}[c + d x]^n (a + a \operatorname{Sin}[c + d x])^2 \left(\frac{4464 + 892 n + 108 n^2 + 5 n^3}{64 (2+n) (4+n) (6+n) (8+n)} + \right.$$

$$\left. \left((14553 + 2547 n + 295 n^2 + 13 n^3) \left(-\frac{1}{256} \operatorname{Cos}[c + d x] + \frac{1}{256} \operatorname{Sin}[c + d x] \right) \right) / \right.$$

$$\left. \left((1+n) (3+n) (7+n) (9+n) \right) + \left((14553 + 2547 n + 295 n^2 + 13 n^3) \left(\frac{1}{256} \operatorname{Cos}[c + d x] + \frac{1}{256} \operatorname{Sin}[c + d x] \right) \right) / \right.$$

$$\left. \left((1+n) (3+n) (7+n) (9+n) \right) + \left((-672 + 80 n + 18 n^2 + n^3) \left(\frac{1}{32} \operatorname{Cos}[2(c + d x)] - \frac{1}{32} \operatorname{Sin}[2(c + d x)] \right) \right) / \right.$$

$$\left. \left((2+n) (4+n) (6+n) (8+n) \right) + \left((-672 + 80 n + 18 n^2 + n^3) \left(\frac{1}{32} \operatorname{Cos}[2(c + d x)] + \frac{1}{32} \operatorname{Sin}[2(c + d x)] \right) \right) / \right.$$

$$\left. \left((2+n) (4+n) (6+n) (8+n) \right) + \left((1323 + 218 n + 11 n^2) \left(-\frac{1}{128} \operatorname{Cos}[3(c + d x)] + \frac{1}{128} \operatorname{Sin}[3(c + d x)] \right) \right) / \right.$$

$$\left. \left((3+n) (7+n) (9+n) \right) + \left((1323 + 218 n + 11 n^2) \left(\frac{1}{128} \operatorname{Cos}[3(c + d x)] + \frac{1}{128} \operatorname{Sin}[3(c + d x)] \right) \right) / \right.$$

$$\left. \left((3+n) (7+n) (9+n) \right) + \frac{(-168 - 22 n - n^2) \left(\frac{1}{32} \operatorname{Cos}[4(c + d x)] - \frac{1}{32} \operatorname{Sin}[4(c + d x)] \right)}{(4+n) (6+n) (8+n)} + \right.$$

$$\left. \frac{(-168 - 22 n - n^2) \left(\frac{1}{32} \operatorname{Cos}[4(c + d x)] + \frac{1}{32} \operatorname{Sin}[4(c + d x)] \right)}{(4+n) (6+n) (8+n)} + \right.$$

$$\left. \frac{(63 + 5 n) \left(-\frac{1}{128} \operatorname{Cos}[5(c + d x)] + \frac{1}{128} \operatorname{Sin}[5(c + d x)] \right)}{(7+n) (9+n)} + \right.$$

$$\left. \frac{(63 + 5 n) \left(\frac{1}{128} \operatorname{Cos}[5(c + d x)] + \frac{1}{128} \operatorname{Sin}[5(c + d x)] \right)}{(7+n) (9+n)} + \right.$$

$$\left. \frac{(-12 - n) \left(\frac{1}{32} \operatorname{Cos}[6(c + d x)] - \frac{1}{32} \operatorname{Sin}[6(c + d x)] \right)}{(6+n) (8+n)} + \right.$$

$$\left. \frac{(-12 - n) \left(\frac{1}{32} \operatorname{Cos}[6(c + d x)] + \frac{1}{32} \operatorname{Sin}[6(c + d x)] \right)}{(6+n) (8+n)} + \right.$$

$$\begin{aligned}
 & \frac{(-9+n) \left(-\frac{1}{512} i \operatorname{Cos}[7(c+dx)] + \frac{1}{512} \operatorname{Sin}[7(c+dx)] \right)}{(7+n)(9+n)} + \\
 & \frac{(-9+n) \left(\frac{1}{512} i \operatorname{Cos}[7(c+dx)] + \frac{1}{512} \operatorname{Sin}[7(c+dx)] \right)}{(7+n)(9+n)} + \\
 & \frac{-\frac{1}{128} \operatorname{Cos}[8(c+dx)] - \frac{1}{128} i \operatorname{Sin}[8(c+dx)]}{8+n} + \frac{-\frac{1}{128} \operatorname{Cos}[8(c+dx)] + \frac{1}{128} i \operatorname{Sin}[8(c+dx)]}{8+n} + \\
 & \left. \frac{-\frac{1}{512} i \operatorname{Cos}[9(c+dx)] - \frac{1}{512} \operatorname{Sin}[9(c+dx)]}{9+n} + \frac{\frac{1}{512} i \operatorname{Cos}[9(c+dx)] - \frac{1}{512} \operatorname{Sin}[9(c+dx)]}{9+n} \right)
 \end{aligned}$$

Problem 699: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^7 \operatorname{Sin}[c+dx]^n (a+a \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 167 leaves, 3 steps):

$$\begin{aligned}
 & \frac{a \operatorname{Sin}[c+dx]^{1+n}}{d(1+n)} + \frac{a \operatorname{Sin}[c+dx]^{2+n}}{d(2+n)} - \frac{3a \operatorname{Sin}[c+dx]^{3+n}}{d(3+n)} - \frac{3a \operatorname{Sin}[c+dx]^{4+n}}{d(4+n)} + \\
 & \frac{3a \operatorname{Sin}[c+dx]^{5+n}}{d(5+n)} + \frac{3a \operatorname{Sin}[c+dx]^{6+n}}{d(6+n)} - \frac{a \operatorname{Sin}[c+dx]^{7+n}}{d(7+n)} - \frac{a \operatorname{Sin}[c+dx]^{8+n}}{d(8+n)}
 \end{aligned}$$

Result (type 3, 966 leaves):

$$\frac{1}{\left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2} a \sin[c + dx]^n (1 + \sin[c + dx])$$

$$\left(\frac{4464 + 892n + 108n^2 + 5n^3}{128d(2+n)(4+n)(6+n)(8+n)} + \frac{(3675 + 691n + 93n^2 + 5n^3) \left(-\frac{i \cos[c+dx]}{128d} + \frac{\sin[c+dx]}{128d}\right)}{(1+n)(3+n)(5+n)(7+n)} + \right.$$

$$\frac{(3675 + 691n + 93n^2 + 5n^3) \left(\frac{i \cos[c+dx]}{128d} + \frac{\sin[c+dx]}{128d}\right)}{(1+n)(3+n)(5+n)(7+n)} +$$

$$\frac{(-672 + 80n + 18n^2 + n^3) \left(\frac{\cos[2c+2dx]}{64d} - \frac{i \sin[2c+2dx]}{64d}\right)}{(2+n)(4+n)(6+n)(8+n)} +$$

$$\frac{(-672 + 80n + 18n^2 + n^3) \left(\frac{\cos[2c+2dx]}{64d} + \frac{i \sin[2c+2dx]}{64d}\right)}{(2+n)(4+n)(6+n)(8+n)} +$$

$$\frac{(245 + 48n + 3n^2) \left(-\frac{3i \cos[3c+3dx]}{128d} + \frac{3 \sin[3c+3dx]}{128d}\right)}{(3+n)(5+n)(7+n)} +$$

$$\frac{(245 + 48n + 3n^2) \left(\frac{3i \cos[3c+3dx]}{128d} + \frac{3 \sin[3c+3dx]}{128d}\right)}{(3+n)(5+n)(7+n)} +$$

$$\frac{(168 + 22n + n^2) \left(-\frac{\cos[4c+4dx]}{64d} - \frac{i \sin[4c+4dx]}{64d}\right)}{(4+n)(6+n)(8+n)} +$$

$$\frac{(-168 - 22n - n^2) \left(\frac{\cos[4c+4dx]}{64d} - \frac{i \sin[4c+4dx]}{64d}\right)}{(4+n)(6+n)(8+n)} + \frac{(49 + 5n) \left(-\frac{i \cos[5c+5dx]}{128d} + \frac{\sin[5c+5dx]}{128d}\right)}{(5+n)(7+n)} +$$

$$\frac{(49 + 5n) \left(\frac{i \cos[5c+5dx]}{128d} + \frac{\sin[5c+5dx]}{128d}\right)}{(5+n)(7+n)} + \frac{(12 + n) \left(-\frac{\cos[6c+6dx]}{64d} - \frac{i \sin[6c+6dx]}{64d}\right)}{(6+n)(8+n)} +$$

$$\frac{(-12 - n) \left(\frac{\cos[6c+6dx]}{64d} - \frac{i \sin[6c+6dx]}{64d}\right)}{(6+n)(8+n)} + \frac{-\frac{i \cos[7c+7dx]}{128d} + \frac{\sin[7c+7dx]}{128d}}{7+n} +$$

$$\left. \frac{\frac{i \cos[7c+7dx]}{128d} + \frac{\sin[7c+7dx]}{128d}}{7+n} + \frac{-\frac{\cos[8c+8dx]}{256d} - \frac{i \sin[8c+8dx]}{256d}}{8+n} + \frac{-\frac{\cos[8c+8dx]}{256d} + \frac{i \sin[8c+8dx]}{256d}}{8+n} \right)$$

Problem 700: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^7 \sin[c + dx]^n}{a + a \sin[c + dx]} dx$$

Optimal (type 3, 137 leaves, 3 steps):

$$\frac{\sin[c + dx]^{1+n}}{ad(1+n)} - \frac{\sin[c + dx]^{2+n}}{ad(2+n)} - \frac{2 \sin[c + dx]^{3+n}}{ad(3+n)} +$$

$$\frac{2 \sin[c + dx]^{4+n}}{ad(4+n)} + \frac{\sin[c + dx]^{5+n}}{ad(5+n)} - \frac{\sin[c + dx]^{6+n}}{ad(6+n)}$$

Result (type 3, 380 leaves):

$$\begin{aligned}
 & - \frac{1}{16 a d (1+n) (2+n) (3+n) (4+n) (5+n) (6+n) (1+\sin [c+d x])} \\
 & \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \sin [c+d x]^{1+n} \\
 & (-8544 - 10520 n - 4888 n^2 - 1114 n^3 - 128 n^4 - 6 n^5 - 8 (336 + 692 n + 484 n^2 + 147 n^3 + 20 n^4 + n^5) \\
 & \quad \cos [2 (c+d x)] - 2 (144 + 324 n + 260 n^2 + 95 n^3 + 16 n^4 + n^5) \cos [4 (c+d x)] + \\
 & \quad 2640 \sin [c+d x] + 4468 n \sin [c+d x] + 2258 n^2 \sin [c+d x] + 474 n^3 \sin [c+d x] + \\
 & \quad 46 n^4 \sin [c+d x] + 2 n^5 \sin [c+d x] + 840 \sin [3 (c+d x)] + 1798 n \sin [3 (c+d x)] + \\
 & \quad 1331 n^2 \sin [3 (c+d x)] + 431 n^3 \sin [3 (c+d x)] + 61 n^4 \sin [3 (c+d x)] + \\
 & \quad 3 n^5 \sin [3 (c+d x)] + 120 \sin [5 (c+d x)] + 274 n \sin [5 (c+d x)] + \\
 & \quad 225 n^2 \sin [5 (c+d x)] + 85 n^3 \sin [5 (c+d x)] + 15 n^4 \sin [5 (c+d x)] + n^5 \sin [5 (c+d x)])
 \end{aligned}$$

Problem 701: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^2} dx$$

Optimal (type 3, 92 leaves, 3 steps):

$$\frac{\sin [c+d x]^{1+n}}{a^2 d (1+n)} - \frac{2 \sin [c+d x]^{2+n}}{a^2 d (2+n)} + \frac{2 \sin [c+d x]^{4+n}}{a^2 d (4+n)} - \frac{\sin [c+d x]^{5+n}}{a^2 d (5+n)}$$

Result (type 3, 405 leaves):

$$\begin{aligned}
 & \frac{1}{d (a+a \sin [c+d x])^2} \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^4 \\
 & \sin [c+d x]^n \left(-\frac{10+n}{4 (2+n) (4+n)} + \frac{(35+3 n) \left(-\frac{1}{16} i \cos [c+d x] + \frac{1}{16} \sin [c+d x] \right)}{(1+n) (5+n)} + \right. \\
 & \quad \left. \frac{(35+3 n) \left(\frac{1}{16} i \cos [c+d x] + \frac{1}{16} \sin [c+d x] \right)}{(1+n) (5+n)} + \right. \\
 & \quad \frac{\cos [2 (c+d x)] - i \sin [2 (c+d x)]}{(2+n) (4+n)} + \frac{\cos [2 (c+d x)] + i \sin [2 (c+d x)]}{(2+n) (4+n)} + \\
 & \quad \left. -\frac{\frac{5}{32} i \cos [3 (c+d x)] + \frac{5}{32} \sin [3 (c+d x)]}{5+n} + \frac{\frac{5}{32} i \cos [3 (c+d x)] + \frac{5}{32} \sin [3 (c+d x)]}{5+n} + \right. \\
 & \quad \left. \frac{\frac{1}{8} \cos [4 (c+d x)] - \frac{1}{8} i \sin [4 (c+d x)]}{4+n} + \frac{\frac{1}{8} \cos [4 (c+d x)] + \frac{1}{8} i \sin [4 (c+d x)]}{4+n} + \right. \\
 & \quad \left. -\frac{\frac{1}{32} i \cos [5 (c+d x)] - \frac{1}{32} \sin [5 (c+d x)]}{5+n} + \frac{\frac{1}{32} i \cos [5 (c+d x)] - \frac{1}{32} \sin [5 (c+d x)]}{5+n} \right)
 \end{aligned}$$

Problem 702: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 92 leaves, 3 steps):

$$\frac{\sin [c+d x]^{1+n}}{a^3 d (1+n)} - \frac{3 \sin [c+d x]^{2+n}}{a^3 d (2+n)} + \frac{3 \sin [c+d x]^{3+n}}{a^3 d (3+n)} - \frac{\sin [c+d x]^{4+n}}{a^3 d (4+n)}$$

Result (type 3, 363 leaves):

$$\frac{1}{d (a+a \sin [c+d x])^3} \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6$$

$$\sin [c+d x]^n \left(-\frac{3 (18+5 n)}{8 (2+n) (4+n)} + \frac{(21+13 n) \left(-\frac{1}{8} i \cos [c+d x] + \frac{1}{8} \sin [c+d x] \right)}{(1+n) (3+n)} + \right.$$

$$\frac{(21+13 n) \left(\frac{1}{8} i \cos [c+d x] + \frac{1}{8} \sin [c+d x] \right)}{(1+n) (3+n)} +$$

$$\frac{(7+2 n) \left(\frac{1}{2} \cos [2 (c+d x)] - \frac{1}{2} i \sin [2 (c+d x)] \right)}{(2+n) (4+n)} +$$

$$\frac{(7+2 n) \left(\frac{1}{2} \cos [2 (c+d x)] + \frac{1}{2} i \sin [2 (c+d x)] \right)}{(2+n) (4+n)} +$$

$$\frac{-\frac{3}{8} i \cos [3 (c+d x)] - \frac{3}{8} \sin [3 (c+d x)]}{3+n} + \frac{\frac{3}{8} i \cos [3 (c+d x)] - \frac{3}{8} \sin [3 (c+d x)]}{3+n} +$$

$$\left. \frac{-\frac{1}{16} \cos [4 (c+d x)] - \frac{1}{16} i \sin [4 (c+d x)]}{4+n} + \frac{-\frac{1}{16} \cos [4 (c+d x)] + \frac{1}{16} i \sin [4 (c+d x)]}{4+n} \right)$$

Problem 703: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^4} dx$$

Optimal (type 5, 109 leaves, 8 steps):

$$-\frac{7 \sin [c+d x]^{1+n}}{a^4 d (1+n)} + \frac{8 \text{Hypergeometric2F1}[1, 1+n, 2+n, -\sin [c+d x]] \sin [c+d x]^{1+n}}{a^4 d (1+n)} +$$

$$\frac{4 \sin [c+d x]^{2+n}}{a^4 d (2+n)} - \frac{\sin [c+d x]^{3+n}}{a^4 d (3+n)}$$

Result (type 8, 31 leaves):

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^4} dx$$

Problem 704: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^5} d x$$

Optimal (type 5, 160 leaves, 4 steps):

$$-\frac{1}{a^5 d (1+n)} 4 (3+2 n) \operatorname{Hypergeometric2F1}[1, 1+n, 2+n, -\sin [c+d x]] \sin [c+d x]^{1+n} -$$

$$\frac{\sin [c+d x]^{1+n} (a-a \sin [c+d x])^2}{d (2+n) (a^7+a^7 \sin [c+d x])} + \frac{\sin [c+d x]^{1+n} (a (27+30 n+8 n^2)+a (7+2 n) \sin [c+d x])}{d (2+3 n+n^2) (a^6+a^6 \sin [c+d x])}$$

Result (type 8, 31 leaves):

$$\int \frac{\cos [c+d x]^7 \sin [c+d x]^n}{(a+a \sin [c+d x])^5} d x$$

Problem 705: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^8 \sin [c+d x]^5}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 209 leaves, 11 steps):

$$-\frac{5 x}{1024 a} - \frac{\cos [c+d x]^7}{7 a d} + \frac{2 \cos [c+d x]^9}{9 a d} - \frac{\cos [c+d x]^{11}}{11 a d} -$$

$$\frac{5 \cos [c+d x] \sin [c+d x]}{1024 a d} - \frac{5 \cos [c+d x]^3 \sin [c+d x]}{1536 a d} - \frac{\cos [c+d x]^5 \sin [c+d x]}{384 a d} +$$

$$\frac{\cos [c+d x]^7 \sin [c+d x]}{64 a d} + \frac{\cos [c+d x]^7 \sin [c+d x]^3}{24 a d} + \frac{\cos [c+d x]^7 \sin [c+d x]^5}{12 a d}$$

Result (type 3, 1247 leaves):

$$\frac{1}{2048} \left(-\frac{9 x}{a} - \frac{16 \cos [c] \cos [d x]}{a d} + \frac{4 \cos [3 c] \cos [3 d x]}{a d} - \frac{8 \cos [5 c] \cos [5 d x]}{5 a d} +$$

$$\frac{4 \cos [7 c] \cos [7 d x]}{7 a d} + \frac{7 \cos [2 d x] \sin [2 c]}{a d} - \frac{5 \cos [4 d x] \sin [4 c]}{2 a d} + \frac{\cos [6 d x] \sin [6 c]}{a d} -$$

$$\frac{\cos [8 d x] \sin [8 c]}{4 a d} + \frac{16 \sin [c] \sin [d x]}{a d} + \frac{7 \cos [2 c] \sin [2 d x]}{a d} - \frac{4 \sin [3 c] \sin [3 d x]}{a d} -$$

$$\frac{5 \cos [4 c] \sin [4 d x]}{2 a d} + \frac{8 \sin [5 c] \sin [5 d x]}{5 a d} + \frac{\cos [6 c] \sin [6 d x]}{a d} - \frac{4 \sin [7 c] \sin [7 d x]}{7 a d} -$$

$$\frac{\cos [8 c] \sin [8 d x]}{4 a d} + \frac{2 \sin \left[\frac{d x}{2} \right]}{a d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2} \right] + \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} \right) -$$

$$\frac{1}{24576 a} 5 \left(30 x + \frac{48 \cos [c] \cos [d x]}{d} - \frac{8 \cos [3 c] \cos [3 d x]}{d} - \frac{18 \cos [2 d x] \sin [2 c]}{d} +$$

$$\begin{aligned}
& \left. \begin{aligned}
& \frac{3 \cos [4 d x] \sin [4 c]}{d} - \frac{48 \sin [c] \sin [d x]}{d} - \frac{18 \cos [2 c] \sin [2 d x]}{d} + \frac{8 \sin [3 c] \sin [3 d x]}{d} + \\
& \frac{3 \cos [4 c] \sin [4 d x]}{d} - \frac{12 \sin \left[\frac{d x}{2}\right]}{d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)} \right\} + \\
& \frac{1}{4096 a} 25 \left(-3 x - \frac{4 \cos [c] \cos [d x]}{d} + \frac{\cos [2 d x] \sin [2 c]}{d} + \frac{4 \sin [c] \sin [d x]}{d} + \right. \\
& \left. \frac{\cos [2 c] \sin [2 d x]}{d} + \frac{2 \sin \left[\frac{d x}{2}\right]}{d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)} \right) - \\
& \frac{1}{61440 a} 7 \left(-210 x - \frac{360 \cos [c] \cos [d x]}{d} + \frac{80 \cos [3 c] \cos [3 d x]}{d} - \frac{24 \cos [5 c] \cos [5 d x]}{d} + \right. \\
& \frac{150 \cos [2 d x] \sin [2 c]}{d} - \frac{45 \cos [4 d x] \sin [4 c]}{d} + \frac{10 \cos [6 d x] \sin [6 c]}{d} + \\
& \frac{360 \sin [c] \sin [d x]}{d} + \frac{150 \cos [2 c] \sin [2 d x]}{d} - \frac{80 \sin [3 c] \sin [3 d x]}{d} - \\
& \frac{45 \cos [4 c] \sin [4 d x]}{d} + \frac{24 \sin [5 c] \sin [5 d x]}{d} + \frac{10 \cos [6 c] \sin [6 d x]}{d} + \\
& \left. \frac{60 \sin \left[\frac{d x}{2}\right]}{d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)} \right) + \\
& \left(5 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right] \right) \right. \\
& \left. \left((c+d x) \cos \left[\frac{1}{2}(c+d x)\right] + (-2+c+d x) \sin \left[\frac{1}{2}(c+d x)\right] \right) \right) / (1024 a d (1 + \sin [c+d x])) + \\
& \frac{1}{1720320 a d} \left(-13860 (c+d x) - 25200 \cos [c+d x] + 6720 \cos [3(c+d x)] - \right. \\
& 3024 \cos [5(c+d x)] + 1440 \cos [7(c+d x)] - 560 \cos [9(c+d x)] + \\
& \frac{2520 \sin \left[\frac{1}{2}(c+d x)\right]}{\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]} + 11340 \sin [2(c+d x)] - 4410 \sin [4(c+d x)] + \\
& \left. 2100 \sin [6(c+d x)] - 945 \sin [8(c+d x)] + 252 \sin [10(c+d x)] \right) + \frac{1}{56770560 a d} \\
& \left(180180 (c+d x) + 332640 \cos [c+d x] - 92400 \cos [3(c+d x)] + 44352 \cos [5(c+d x)] - \right. \\
& 23760 \cos [7(c+d x)] + 12320 \cos [9(c+d x)] - 5040 \cos [11(c+d x)] - \\
& \frac{27720 \sin \left[\frac{1}{2}(c+d x)\right]}{\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]} - 152460 \sin [2(c+d x)] + 62370 \sin [4(c+d x)] -
\end{aligned}
\right.
\end{aligned}$$

$$32340 \sin[6(c+dx)] + 17325 \sin[8(c+dx)] - 8316 \sin[10(c+dx)] + 2310 \sin[12(c+dx)] \Bigg)$$

Problem 706: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^8 \sin[c+dx]^4}{a+a \sin[c+dx]} dx$$

Optimal (type 3, 183 leaves, 10 steps):

$$\begin{aligned} & \frac{3x}{256a} + \frac{\cos[c+dx]^7}{7ad} - \frac{2\cos[c+dx]^9}{9ad} + \frac{\cos[c+dx]^{11}}{11ad} + \\ & \frac{3\cos[c+dx]\sin[c+dx]}{256ad} + \frac{\cos[c+dx]^3\sin[c+dx]}{128ad} + \\ & \frac{\cos[c+dx]^5\sin[c+dx]}{160ad} - \frac{3\cos[c+dx]^7\sin[c+dx]}{80ad} - \frac{\cos[c+dx]^7\sin[c+dx]^3}{10ad} \end{aligned}$$

Result (type 3, 1084 leaves):

$$\begin{aligned} & \frac{1}{1024} \left(-\frac{8x}{a} - \frac{14\cos[c]\cos[dx]}{ad} + \frac{10\cos[3c]\cos[3dx]}{3ad} - \frac{6\cos[5c]\cos[5dx]}{5ad} + \right. \\ & \frac{2\cos[7c]\cos[7dx]}{7ad} + \frac{6\cos[2dx]\sin[2c]}{ad} - \frac{2\cos[4dx]\sin[4c]}{ad} + \\ & \frac{2\cos[6dx]\sin[6c]}{3ad} + \frac{14\sin[c]\sin[dx]}{ad} + \frac{6\cos[2c]\sin[2dx]}{ad} - \frac{10\sin[3c]\sin[3dx]}{3ad} - \\ & \frac{2\cos[4c]\sin[4dx]}{ad} + \frac{6\sin[5c]\sin[5dx]}{5ad} + \frac{2\cos[6c]\sin[6dx]}{3ad} - \\ & \left. \frac{2\sin[7c]\sin[7dx]}{7ad} + \frac{2\sin\left[\frac{dx}{2}\right]}{ad \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)} \right) - \\ & \frac{1}{2560a} \left(30x + \frac{50\cos[c]\cos[dx]}{d} - \frac{10\cos[3c]\cos[3dx]}{d} + \frac{2\cos[5c]\cos[5dx]}{d} - \right. \\ & \frac{20\cos[2dx]\sin[2c]}{d} + \frac{5\cos[4dx]\sin[4c]}{d} - \frac{50\sin[c]\sin[dx]}{d} - \\ & \frac{20\cos[2c]\sin[2dx]}{d} + \frac{10\sin[3c]\sin[3dx]}{d} + \frac{5\cos[4c]\sin[4dx]}{d} - \\ & \left. \frac{2\sin[5c]\sin[5dx]}{d} - \frac{10\sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) + \\ & \frac{1}{128a} \left(x + \frac{\cos[c]\cos[dx]}{d} - \frac{\sin[c]\sin[dx]}{d} - \right. \\ & \left. \frac{\sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) - \frac{1}{3072a} \end{aligned}$$

$$\begin{aligned}
 & 17 \left(-6x - \frac{9 \cos[c] \cos[dx]}{d} + \frac{\cos[3c] \cos[3dx]}{d} + \frac{3 \cos[2dx] \sin[2c]}{d} + \right. \\
 & \quad \left. \frac{9 \sin[c] \sin[dx]}{d} + \frac{3 \cos[2c] \sin[2dx]}{d} - \frac{\sin[3c] \sin[3dx]}{d} + \frac{3 \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) + \\
 & \quad \frac{7 \sin\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)}{512 d (a + a \sin[c+dx])} + \frac{1}{64 512 a d} \\
 & \quad \left(1260 (c+dx) + 2268 \cos[c+dx] - 588 \cos[3(c+dx)] + 252 \cos[5(c+dx)] - \right. \\
 & \quad \left. 108 \cos[7(c+dx)] + 28 \cos[9(c+dx)] - \frac{252 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} - \right. \\
 & \quad \left. 1008 \sin[2(c+dx)] + 378 \sin[4(c+dx)] - 168 \sin[6(c+dx)] + 63 \sin[8(c+dx)] \right) + \\
 & \quad \frac{1}{2 365 440 a d} \left(-13 860 (c+dx) - 25 410 \cos[c+dx] + 6930 \cos[3(c+dx)] - \right. \\
 & \quad \left. 3234 \cos[5(c+dx)] + 1650 \cos[7(c+dx)] - 770 \cos[9(c+dx)] + 210 \cos[11(c+dx)] + \right. \\
 & \quad \left. \frac{2310 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 11 550 \sin[2(c+dx)] - 4620 \sin[4(c+dx)] + \right. \\
 & \quad \left. 2310 \sin[6(c+dx)] - 1155 \sin[8(c+dx)] + 462 \sin[10(c+dx)] \right)
 \end{aligned}$$

Problem 707: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^8 \sin[c+dx]^3}{a+a \sin[c+dx]} dx$$

Optimal (type 3, 165 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{3x}{256a} - \frac{\cos[c+dx]^7}{7ad} + \frac{\cos[c+dx]^9}{9ad} - \frac{3 \cos[c+dx] \sin[c+dx]}{256ad} - \frac{\cos[c+dx]^3 \sin[c+dx]}{128ad} \\
 & \frac{\cos[c+dx]^5 \sin[c+dx]}{160ad} + \frac{3 \cos[c+dx]^7 \sin[c+dx]}{80ad} + \frac{\cos[c+dx]^7 \sin[c+dx]^3}{10ad}
 \end{aligned}$$

Result (type 3, 1078 leaves):

$$-\frac{1}{1024} 5 \left(\frac{9x}{a} + \frac{16 \cos[c] \cos[dx]}{ad} - \frac{4 \cos[3c] \cos[3dx]}{ad} + \frac{8 \cos[5c] \cos[5dx]}{5ad} - \right.$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \frac{4 \cos[7c] \cos[7dx]}{7ad} - \frac{7 \cos[2dx] \sin[2c]}{ad} + \frac{5 \cos[4dx] \sin[4c]}{2ad} - \frac{\cos[6dx] \sin[6c]}{ad} + \\
 & \frac{\cos[8dx] \sin[8c]}{4ad} - \frac{16 \sin[c] \sin[dx]}{ad} - \frac{7 \cos[2c] \sin[2dx]}{ad} + \frac{4 \sin[3c] \sin[3dx]}{ad} + \\
 & \frac{5 \cos[4c] \sin[4dx]}{2ad} - \frac{8 \sin[5c] \sin[5dx]}{5ad} - \frac{\cos[6c] \sin[6dx]}{ad} + \frac{4 \sin[7c] \sin[7dx]}{7ad} + \\
 & \frac{\cos[8c] \sin[8dx]}{4ad} - \frac{2 \sin\left[\frac{dx}{2}\right]}{ad \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)} \right) + \\
 & \frac{1}{6144a} 5 \left(30x + \frac{48 \cos[c] \cos[dx]}{d} - \frac{8 \cos[3c] \cos[3dx]}{d} - \frac{18 \cos[2dx] \sin[2c]}{d} + \right. \\
 & \left. \frac{3 \cos[4dx] \sin[4c]}{d} - \frac{48 \sin[c] \sin[dx]}{d} - \frac{18 \cos[2c] \sin[2dx]}{d} + \frac{8 \sin[3c] \sin[3dx]}{d} + \right. \\
 & \left. \frac{3 \cos[4c] \sin[4dx]}{d} - \frac{12 \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) + \\
 & \frac{1}{512a} 11 \left(-3x - \frac{4 \cos[c] \cos[dx]}{d} + \frac{\cos[2dx] \sin[2c]}{d} + \frac{4 \sin[c] \sin[dx]}{d} + \right. \\
 & \left. \frac{\cos[2c] \sin[2dx]}{d} + \frac{2 \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) - \\
 & \frac{1}{30720a} 7 \left(-210x - \frac{360 \cos[c] \cos[dx]}{d} + \frac{80 \cos[3c] \cos[3dx]}{d} - \frac{24 \cos[5c] \cos[5dx]}{d} + \right. \\
 & \left. \frac{150 \cos[2dx] \sin[2c]}{d} - \frac{45 \cos[4dx] \sin[4c]}{d} + \frac{10 \cos[6dx] \sin[6c]}{d} + \right. \\
 & \left. \frac{360 \sin[c] \sin[dx]}{d} + \frac{150 \cos[2c] \sin[2dx]}{d} - \frac{80 \sin[3c] \sin[3dx]}{d} - \right. \\
 & \left. \frac{45 \cos[4c] \sin[4dx]}{d} + \frac{24 \sin[5c] \sin[5dx]}{d} + \frac{10 \cos[6c] \sin[6dx]}{d} + \right. \\
 & \left. \frac{60 \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) + \\
 & \left(7 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \left. \left((c+dx) \cos\left[\frac{1}{2}(c+dx)\right] + (-2+c+dx) \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / (512ad(1+\sin[c+dx])) - \\
 & \frac{1}{1290240ad} \left(-13860(c+dx) - 25200 \cos[c+dx] + 6720 \cos[3(c+dx)] - \right. \\
 & \left. 3024 \cos[5(c+dx)] + 1440 \cos[7(c+dx)] - 560 \cos[9(c+dx)] + \right. \\
 & \left. \frac{2520 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 11340 \sin[2(c+dx)] - 4410 \sin[4(c+dx)] + \right.
 \end{aligned}
 \end{aligned}$$

$$2100 \operatorname{Sin}[6(c+dx)] - 945 \operatorname{Sin}[8(c+dx)] + 252 \operatorname{Sin}[10(c+dx)] \Bigg)$$

Problem 708: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx]^8 \operatorname{Sin}[c+dx]^2}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 139 leaves, 9 steps):

$$\frac{5x}{128a} + \frac{\operatorname{Cos}[c+dx]^7}{7ad} - \frac{\operatorname{Cos}[c+dx]^9}{9ad} + \frac{5 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{128ad} + \frac{5 \operatorname{Cos}[c+dx]^3 \operatorname{Sin}[c+dx]}{192ad} + \frac{\operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]}{48ad} - \frac{\operatorname{Cos}[c+dx]^7 \operatorname{Sin}[c+dx]}{8ad}$$

Result (type 3, 923 leaves):

$$\begin{aligned} &-\frac{3}{256} \left(-\frac{8x}{a} - \frac{14 \operatorname{Cos}[c] \operatorname{Cos}[dx]}{ad} + \frac{10 \operatorname{Cos}[3c] \operatorname{Cos}[3dx]}{3ad} - \frac{6 \operatorname{Cos}[5c] \operatorname{Cos}[5dx]}{5ad} + \frac{2 \operatorname{Cos}[7c] \operatorname{Cos}[7dx]}{7ad} + \frac{6 \operatorname{Cos}[2dx] \operatorname{Sin}[2c]}{ad} - \frac{2 \operatorname{Cos}[4dx] \operatorname{Sin}[4c]}{ad} + \frac{2 \operatorname{Cos}[6dx] \operatorname{Sin}[6c]}{3ad} + \frac{14 \operatorname{Sin}[c] \operatorname{Sin}[dx]}{ad} + \frac{6 \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{ad} - \frac{10 \operatorname{Sin}[3c] \operatorname{Sin}[3dx]}{3ad} + \frac{2 \operatorname{Cos}[4c] \operatorname{Sin}[4dx]}{ad} + \frac{6 \operatorname{Sin}[5c] \operatorname{Sin}[5dx]}{5ad} + \frac{2 \operatorname{Cos}[6c] \operatorname{Sin}[6dx]}{3ad} - \frac{2 \operatorname{Sin}[7c] \operatorname{Sin}[7dx]}{7ad} + \frac{2 \operatorname{Sin}\left[\frac{dx}{2}\right]}{ad \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)} \right) - \\ &\frac{1}{2560a} \left(13 \left(30x + \frac{50 \operatorname{Cos}[c] \operatorname{Cos}[dx]}{d} - \frac{10 \operatorname{Cos}[3c] \operatorname{Cos}[3dx]}{d} + \frac{2 \operatorname{Cos}[5c] \operatorname{Cos}[5dx]}{d} - \frac{20 \operatorname{Cos}[2dx] \operatorname{Sin}[2c]}{d} + \frac{5 \operatorname{Cos}[4dx] \operatorname{Sin}[4c]}{d} - \frac{50 \operatorname{Sin}[c] \operatorname{Sin}[dx]}{d} - \frac{20 \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{d} + \frac{10 \operatorname{Sin}[3c] \operatorname{Sin}[3dx]}{d} + \frac{5 \operatorname{Cos}[4c] \operatorname{Sin}[4dx]}{d} - \frac{2 \operatorname{Sin}[5c] \operatorname{Sin}[5dx]}{d} - \frac{10 \operatorname{Sin}\left[\frac{dx}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)} \right) + \right. \\ &\left. \frac{1}{128a} \left(7 \left(x + \frac{\operatorname{Cos}[c] \operatorname{Cos}[dx]}{d} - \frac{\operatorname{Sin}[c] \operatorname{Sin}[dx]}{d} - \frac{\operatorname{Sin}\left[\frac{dx}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)} \right) - \frac{1}{96a} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(-6x - \frac{9 \cos[c] \cos[dx]}{d} + \frac{\cos[3c] \cos[3dx]}{d} + \frac{3 \cos[2dx] \sin[2c]}{d} + \right. \\
 & \quad \left. \frac{9 \sin[c] \sin[dx]}{d} + \frac{3 \cos[2c] \sin[2dx]}{d} - \frac{\sin[3c] \sin[3dx]}{d} + \right. \\
 & \quad \left. \frac{3 \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \right. \\
 & \quad \left. \frac{7 \sin\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)}{128 d (a + a \sin[c+dx])} - \right. \\
 & \quad \left. \frac{1}{64512 a d} \right. \\
 & \quad \left(1260 (c+dx) + 2268 \cos[c+dx] - 588 \cos[3(c+dx)] + 252 \cos[5(c+dx)] - \right. \\
 & \quad 108 \cos[7(c+dx)] + 28 \cos[9(c+dx)] - \frac{252 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} - \\
 & \quad \left. \left. 1008 \sin[2(c+dx)] + 378 \sin[4(c+dx)] - 168 \sin[6(c+dx)] + 63 \sin[8(c+dx)] \right) \right)
 \end{aligned}$$

Problem 709: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^8 \sin[c+dx]}{a + a \sin[c+dx]} dx$$

Optimal (type 3, 121 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{5x}{128a} - \frac{\cos[c+dx]^7}{7ad} - \frac{5 \cos[c+dx] \sin[c+dx]}{128ad} - \\
 & \frac{5 \cos[c+dx]^3 \sin[c+dx]}{192ad} - \frac{\cos[c+dx]^5 \sin[c+dx]}{48ad} + \frac{\cos[c+dx]^7 \sin[c+dx]}{8ad}
 \end{aligned}$$

Result (type 3, 481 leaves):

$$\begin{aligned}
 & - \frac{1}{43008 a d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(-336 (7 c - 5 d x) \cos\left[\frac{c}{2}\right] + 1680 \cos\left[\frac{c}{2} + d x\right] + 1680 \cos\left[\frac{3 c}{2} + d x\right] + 336 \cos\left[\frac{3 c}{2} + 2 d x\right] - \right. \\
 & 336 \cos\left[\frac{5 c}{2} + 2 d x\right] + 1008 \cos\left[\frac{5 c}{2} + 3 d x\right] + 1008 \cos\left[\frac{7 c}{2} + 3 d x\right] - 168 \cos\left[\frac{7 c}{2} + 4 d x\right] + \\
 & 168 \cos\left[\frac{9 c}{2} + 4 d x\right] + 336 \cos\left[\frac{9 c}{2} + 5 d x\right] + 336 \cos\left[\frac{11 c}{2} + 5 d x\right] - 112 \cos\left[\frac{11 c}{2} + 6 d x\right] + \\
 & 112 \cos\left[\frac{13 c}{2} + 6 d x\right] + 48 \cos\left[\frac{13 c}{2} + 7 d x\right] + 48 \cos\left[\frac{15 c}{2} + 7 d x\right] - 21 \cos\left[\frac{15 c}{2} + 8 d x\right] + \\
 & 21 \cos\left[\frac{17 c}{2} + 8 d x\right] + 4704 \sin\left[\frac{c}{2}\right] - 2352 c \sin\left[\frac{c}{2}\right] + 1680 d x \sin\left[\frac{c}{2}\right] - \\
 & 1680 \sin\left[\frac{c}{2} + d x\right] + 1680 \sin\left[\frac{3 c}{2} + d x\right] + 336 \sin\left[\frac{3 c}{2} + 2 d x\right] + 336 \sin\left[\frac{5 c}{2} + 2 d x\right] - \\
 & 1008 \sin\left[\frac{5 c}{2} + 3 d x\right] + 1008 \sin\left[\frac{7 c}{2} + 3 d x\right] - 168 \sin\left[\frac{7 c}{2} + 4 d x\right] - 168 \sin\left[\frac{9 c}{2} + 4 d x\right] - \\
 & 336 \sin\left[\frac{9 c}{2} + 5 d x\right] + 336 \sin\left[\frac{11 c}{2} + 5 d x\right] - 112 \sin\left[\frac{11 c}{2} + 6 d x\right] - 112 \sin\left[\frac{13 c}{2} + 6 d x\right] - \\
 & \left. 48 \sin\left[\frac{13 c}{2} + 7 d x\right] + 48 \sin\left[\frac{15 c}{2} + 7 d x\right] - 21 \sin\left[\frac{15 c}{2} + 8 d x\right] - 21 \sin\left[\frac{17 c}{2} + 8 d x\right] \right)
 \end{aligned}$$

Problem 716: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \operatorname{Cot}[c+d x]^7}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 142 leaves, 9 steps):

$$\begin{aligned}
 & \frac{x}{a} + \frac{5 \operatorname{ArcTanh}[\cos [c+d x]]}{16 a d} + \frac{\operatorname{Cot}[c+d x]}{a d} - \frac{\operatorname{Cot}[c+d x]^3}{3 a d} + \frac{\operatorname{Cot}[c+d x]^5}{5 a d} - \\
 & \frac{5 \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{16 a d} + \frac{5 \operatorname{Cot}[c+d x]^3 \operatorname{Csc}[c+d x]}{24 a d} - \frac{\operatorname{Cot}[c+d x]^5 \operatorname{Csc}[c+d x]}{6 a d}
 \end{aligned}$$

Result (type 3, 317 leaves):

$$\begin{aligned}
 & - \frac{1}{7680 a d (1 + \sin [c + d x])} \\
 & \operatorname{Csc}[c + d x]^6 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(-2400 c - 2400 d x + 900 \cos [c + d x] + \right. \\
 & \quad 50 \cos [3 (c + d x)] - 1440 c \cos [4 (c + d x)] - 1440 d x \cos [4 (c + d x)] + 330 \cos [5 (c + d x)] + \\
 & \quad 240 c \cos [6 (c + d x)] + 240 d x \cos [6 (c + d x)] - 750 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - \\
 & \quad 450 \cos [4 (c + d x)] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] + 75 \cos [6 (c + d x)] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 225 \cos [2 (c + d x)] \left(16 (c + d x) + 5 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - 5 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \right) + \\
 & \quad 750 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] + 450 \cos [4 (c + d x)] \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] - 75 \cos [6 (c + d x)] \\
 & \quad \left. \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] - 1200 \sin [2 (c + d x)] + 768 \sin [4 (c + d x)] - 368 \sin [6 (c + d x)] \right)
 \end{aligned}$$

Problem 717: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x]^8}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 106 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{5 \operatorname{ArcTanh}[\cos [c + d x]]}{16 a d} - \frac{\operatorname{Cot}[c + d x]^7}{7 a d} + \frac{5 \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]}{16 a d} - \\
 & \frac{5 \operatorname{Cot}[c + d x]^3 \operatorname{Csc}[c + d x]}{24 a d} + \frac{\operatorname{Cot}[c + d x]^5 \operatorname{Csc}[c + d x]}{6 a d}
 \end{aligned}$$

Result (type 3, 284 leaves):

$$\begin{aligned}
 & - \frac{1}{86016 a d (1 + \sin [c + d x])} \\
 & \operatorname{Csc}[c + d x]^5 \left(\operatorname{Csc} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(1680 \cos [c + d x] + 1008 \cos [3 (c + d x)] + \right. \\
 & \quad 336 \cos [5 (c + d x)] + 48 \cos [7 (c + d x)] + 3675 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [c + d x] - \\
 & \quad 3675 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [c + d x] - 1190 \sin [2 (c + d x)] - \\
 & \quad 2205 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [3 (c + d x)] + 2205 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [3 (c + d x)] + \\
 & \quad 392 \sin [4 (c + d x)] + 735 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [5 (c + d x)] - \\
 & \quad 735 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [5 (c + d x)] - 462 \sin [6 (c + d x)] - \\
 & \quad \left. 105 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [7 (c + d x)] + 105 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [7 (c + d x)] \right)
 \end{aligned}$$

Problem 718: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + dx]^8 \text{Csc}[c + dx]}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 134 leaves, 8 steps):

$$\frac{5 \text{ArcTanh}[\text{Cos}[c + dx]]}{128 a d} + \frac{\text{Cot}[c + dx]^7}{7 a d} + \frac{5 \text{Cot}[c + dx] \text{Csc}[c + dx]}{128 a d} - \frac{5 \text{Cot}[c + dx] \text{Csc}[c + dx]^3}{64 a d} + \frac{5 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]^3}{48 a d} - \frac{\text{Cot}[c + dx]^5 \text{Csc}[c + dx]^3}{8 a d}$$

Result (type 3, 291 leaves):

$$\frac{1}{344064 a d} \text{Csc}[c + dx]^8 \left(-24710 \text{Cos}[c + dx] - 12530 \text{Cos}[3(c + dx)] - 5558 \text{Cos}[5(c + dx)] - 210 \text{Cos}[7(c + dx)] + 3675 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right] - 5880 \text{Cos}[2(c + dx)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right] + 2940 \text{Cos}[4(c + dx)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right] - 840 \text{Cos}[6(c + dx)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right] + 105 \text{Cos}[8(c + dx)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right] - 3675 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 5880 \text{Cos}[2(c + dx)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - 2940 \text{Cos}[4(c + dx)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 840 \text{Cos}[6(c + dx)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - 105 \text{Cos}[8(c + dx)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 5376 \text{Sin}[2(c + dx)] + 5376 \text{Sin}[4(c + dx)] + 2304 \text{Sin}[6(c + dx)] + 384 \text{Sin}[8(c + dx)] \right)$$

Problem 719: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + dx]^8 \text{Csc}[c + dx]^2}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 152 leaves, 9 steps):

$$\frac{5 \text{ArcTanh}[\text{Cos}[c + dx]]}{128 a d} - \frac{\text{Cot}[c + dx]^7}{7 a d} - \frac{\text{Cot}[c + dx]^9}{9 a d} - \frac{5 \text{Cot}[c + dx] \text{Csc}[c + dx]}{128 a d} + \frac{5 \text{Cot}[c + dx] \text{Csc}[c + dx]^3}{64 a d} - \frac{5 \text{Cot}[c + dx]^3 \text{Csc}[c + dx]^3}{48 a d} + \frac{\text{Cot}[c + dx]^5 \text{Csc}[c + dx]^3}{8 a d}$$

Result (type 3, 313 leaves):

$$\begin{aligned}
 & - \frac{1}{2064384 a d} \operatorname{Csc}[c + d x]^9 \\
 & \left(129024 \operatorname{Cos}[c + d x] + 75264 \operatorname{Cos}[3(c + d x)] + 23040 \operatorname{Cos}[5(c + d x)] + 2304 \operatorname{Cos}[7(c + d x)] - \right. \\
 & \quad 256 \operatorname{Cos}[9(c + d x)] + 39690 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[c + d x] - 39690 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \\
 & \quad \operatorname{Sin}[c + d x] - 36540 \operatorname{Sin}[2(c + d x)] - 26460 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[3(c + d x)] + \\
 & \quad 26460 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[3(c + d x)] - 20916 \operatorname{Sin}[4(c + d x)] + \\
 & \quad 11340 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[5(c + d x)] - 11340 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[5(c + d x)] - \\
 & \quad 16044 \operatorname{Sin}[6(c + d x)] - 2835 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[7(c + d x)] + \\
 & \quad 2835 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[7(c + d x)] - 630 \operatorname{Sin}[8(c + d x)] + \\
 & \quad \left. 315 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[9(c + d x)] - 315 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[9(c + d x)] \right)
 \end{aligned}$$

Problem 720: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x]^8 \operatorname{Csc}[c + d x]^3}{a + a \operatorname{Sin}[c + d x]} dx$$

Optimal (type 3, 176 leaves, 10 steps):

$$\begin{aligned}
 & \frac{3 \operatorname{ArcTanh}[\operatorname{Cos}[c + d x]]}{256 a d} + \frac{\operatorname{Cot}[c + d x]^7}{7 a d} + \frac{\operatorname{Cot}[c + d x]^9}{9 a d} + \\
 & \frac{3 \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]}{256 a d} + \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3}{128 a d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^5}{32 a d} + \frac{\operatorname{Cot}[c + d x]^3 \operatorname{Csc}[c + d x]^5}{16 a d} - \frac{\operatorname{Cot}[c + d x]^5 \operatorname{Csc}[c + d x]^5}{10 a d}
 \end{aligned}$$

Result (type 3, 386 leaves):

$$\begin{aligned}
 & - \frac{1}{165150720 a d (1 + \text{Csc}[c + d x])} \text{Csc}[c + d x]^9 \left(\text{Csc}\left[\frac{1}{2}(c + d x)\right] + \text{Sec}\left[\frac{1}{2}(c + d x)\right] \right)^2 \\
 & \left(2367540 \text{Cos}[c + d x] + 1307880 \text{Cos}[3(c + d x)] + 436968 \text{Cos}[5(c + d x)] + \right. \\
 & 18270 \text{Cos}[7(c + d x)] - 1890 \text{Cos}[9(c + d x)] - 119070 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + \\
 & 198450 \text{Cos}[2(c + d x)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - 113400 \text{Cos}[4(c + d x)] \\
 & \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 42525 \text{Cos}[6(c + d x)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - \\
 & 9450 \text{Cos}[8(c + d x)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 945 \text{Cos}[10(c + d x)] \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + \\
 & 119070 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 198450 \text{Cos}[2(c + d x)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 113400 \\
 & \text{Cos}[4(c + d x)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 42525 \text{Cos}[6(c + d x)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\
 & 9450 \text{Cos}[8(c + d x)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 945 \text{Cos}[10(c + d x)] \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\
 & 537600 \text{Sin}[2(c + d x)] - 522240 \text{Sin}[4(c + d x)] - \\
 & \left. 207360 \text{Sin}[6(c + d x)] - 25600 \text{Sin}[8(c + d x)] + 2560 \text{Sin}[10(c + d x)] \right)
 \end{aligned}$$

Problem 722: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cos}[c + d x]^8 \text{Sin}[c + d x]^5}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 203 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{3x}{128 a^2} - \frac{2 \text{Cos}[c + d x]^5}{5 a^2 d} + \frac{5 \text{Cos}[c + d x]^7}{7 a^2 d} - \frac{4 \text{Cos}[c + d x]^9}{9 a^2 d} + \\
 & \frac{\text{Cos}[c + d x]^{11}}{11 a^2 d} - \frac{3 \text{Cos}[c + d x] \text{Sin}[c + d x]}{128 a^2 d} - \frac{\text{Cos}[c + d x]^3 \text{Sin}[c + d x]}{64 a^2 d} + \\
 & \frac{\text{Cos}[c + d x]^5 \text{Sin}[c + d x]}{16 a^2 d} + \frac{\text{Cos}[c + d x]^5 \text{Sin}[c + d x]^3}{8 a^2 d} + \frac{\text{Cos}[c + d x]^5 \text{Sin}[c + d x]^5}{5 a^2 d}
 \end{aligned}$$

Result (type 3, 1469 leaves):

$$\begin{aligned}
 & - \left((5(-3 + \text{Cos}[c + d x] + \text{Cos}[2(c + d x)] - 4 \text{Sin}[c + d x] + \text{Sin}[2(c + d x)])) / \right. \\
 & \left. (3072 a^2 d (1 + \text{Sin}[c + d x])^2) \right) + \\
 & \frac{1}{86016 a^2 d} \left(27720 (c + d x) + 41580 \text{Cos}[c + d x] - 7056 \text{Cos}[3(c + d x)] + 1764 \text{Cos}[5(c + d x)] - \right. \\
 & \left. 360 \text{Cos}[7(c + d x)] + 28 \text{Cos}[9(c + d x)] + \frac{42 \text{Sin}\left[\frac{1}{2}(c + d x)\right]}{\left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{21}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{15204 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} - \\
 & \left. 15120 \sin[2(c+dx)] + 3528 \sin[4(c+dx)] - 840 \sin[6(c+dx)] + 126 \sin[8(c+dx)] \right) + \\
 & \frac{1}{2027520 a^2 d} \left(-360360(c+dx) - 566280 \cos[c+dx] + 108900 \cos[3(c+dx)] - \right. \\
 & 33264 \cos[5(c+dx)] + 9900 \cos[7(c+dx)] - 2200 \cos[9(c+dx)] + 180 \cos[11(c+dx)] - \\
 & \frac{330 \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{165}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
 & \frac{166980 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 217800 \sin[2(c+dx)] - 59400 \sin[4(c+dx)] + \\
 & \left. 18480 \sin[6(c+dx)] - 4950 \sin[8(c+dx)] + 792 \sin[10(c+dx)] \right) + \\
 & \left(25 \left(36 dx \cos\left[\frac{dx}{2}\right] - 21 \cos\left[c + \frac{dx}{2}\right] + 35 \cos\left[c + \frac{3dx}{2}\right] - 12 dx \cos\left[2c + \frac{3dx}{2}\right] - \right. \right. \\
 & \quad 3 \cos\left[3c + \frac{5dx}{2}\right] - 57 \sin\left[\frac{dx}{2}\right] + 36 dx \sin\left[c + \frac{dx}{2}\right] + \\
 & \quad \left. \left. 12 dx \sin\left[c + \frac{3dx}{2}\right] + 9 \sin\left[2c + \frac{3dx}{2}\right] + 3 \sin\left[2c + \frac{5dx}{2}\right] \right) \right) / \\
 & \left(12288 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) + \\
 & \left(5 \left(180 dx \cos\left[\frac{dx}{2}\right] - 21 \cos\left[c + \frac{dx}{2}\right] + 147 \cos\left[c + \frac{3dx}{2}\right] - 60 dx \cos\left[2c + \frac{3dx}{2}\right] - \right. \right. \\
 & \quad 15 \cos\left[3c + \frac{5dx}{2}\right] + 3 \cos\left[3c + \frac{7dx}{2}\right] + \cos\left[5c + \frac{9dx}{2}\right] - 201 \sin\left[\frac{dx}{2}\right] + \\
 & \quad 180 dx \sin\left[c + \frac{dx}{2}\right] + 60 dx \sin\left[c + \frac{3dx}{2}\right] + 73 \sin\left[2c + \frac{3dx}{2}\right] + \\
 & \quad \left. \left. 15 \sin\left[2c + \frac{5dx}{2}\right] + 3 \sin\left[4c + \frac{7dx}{2}\right] - \sin\left[4c + \frac{9dx}{2}\right] \right) \right) / \\
 & \left(12288 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) - \\
 & \frac{1}{30720 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} \\
 & 7 \left(2520 dx \cos\left[\frac{dx}{2}\right] + 165 \cos\left[c + \frac{dx}{2}\right] + 1905 \cos\left[c + \frac{3dx}{2}\right] - 840 dx \cos\left[2c + \frac{3dx}{2}\right] - \right. \\
 & \quad \left. 210 \cos\left[3c + \frac{5dx}{2}\right] + 42 \cos\left[3c + \frac{7dx}{2}\right] + 14 \cos\left[5c + \frac{9dx}{2}\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Cos}\left[5c + \frac{11dx}{2}\right] - 3 \operatorname{Cos}\left[7c + \frac{13dx}{2}\right] - 2355 \operatorname{Sin}\left[\frac{dx}{2}\right] + 2520 dx \operatorname{Sin}\left[c + \frac{dx}{2}\right] + \\
 & 840 dx \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 1175 \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 210 \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + \\
 & 42 \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - 14 \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] - 6 \operatorname{Sin}\left[6c + \frac{11dx}{2}\right] + 3 \operatorname{Sin}\left[6c + \frac{13dx}{2}\right] \Big) + \\
 & \frac{1}{43008 a^2 d \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & \left(7560 dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 1239 \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 5467 \operatorname{Cos}\left[c + \frac{3dx}{2}\right] - 2520 dx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] - \right. \\
 & 630 \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] + 126 \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 42 \operatorname{Cos}\left[5c + \frac{9dx}{2}\right] - 18 \operatorname{Cos}\left[5c + \frac{11dx}{2}\right] - \\
 & 9 \operatorname{Cos}\left[7c + \frac{13dx}{2}\right] + 5 \operatorname{Cos}\left[7c + \frac{15dx}{2}\right] + 3 \operatorname{Cos}\left[9c + \frac{17dx}{2}\right] - 6321 \operatorname{Sin}\left[\frac{dx}{2}\right] + \\
 & 7560 dx \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 2520 dx \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 3773 \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + \\
 & 630 \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 126 \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - 42 \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] - \\
 & \left. 18 \operatorname{Sin}\left[6c + \frac{11dx}{2}\right] + 9 \operatorname{Sin}\left[6c + \frac{13dx}{2}\right] + 5 \operatorname{Sin}\left[8c + \frac{15dx}{2}\right] - 3 \operatorname{Sin}\left[8c + \frac{17dx}{2}\right] \right)
 \end{aligned}$$

Problem 723: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx]^8 \operatorname{Sin}[c+dx]^4}{(a+a \operatorname{Sin}[c+dx])^2} dx$$

Optimal (type 3, 185 leaves, 17 steps):

$$\begin{aligned}
 & \frac{9x}{256 a^2} + \frac{2 \operatorname{Cos}[c+dx]^5}{5 a^2 d} - \frac{4 \operatorname{Cos}[c+dx]^7}{7 a^2 d} + \frac{2 \operatorname{Cos}[c+dx]^9}{9 a^2 d} + \\
 & \frac{9 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{256 a^2 d} + \frac{3 \operatorname{Cos}[c+dx]^3 \operatorname{Sin}[c+dx]}{128 a^2 d} - \\
 & \frac{3 \operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]}{32 a^2 d} - \frac{3 \operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]^3}{16 a^2 d} - \frac{\operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]^5}{10 a^2 d}
 \end{aligned}$$

Result (type 3, 585 leaves):

$$\begin{aligned}
 & \frac{1}{1290240 a^2 d} \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \\
 & \left(-2520 (187 c - 18 d x) \cos\left[\frac{c}{2}\right] + 30240 \cos\left[\frac{c}{2} + d x\right] + 30240 \cos\left[\frac{3c}{2} + d x\right] - 1260 \cos\left[\frac{3c}{2} + 2 d x\right] + \right. \\
 & 1260 \cos\left[\frac{5c}{2} + 2 d x\right] + 6720 \cos\left[\frac{5c}{2} + 3 d x\right] + 6720 \cos\left[\frac{7c}{2} + 3 d x\right] - 7560 \cos\left[\frac{7c}{2} + 4 d x\right] + \\
 & 7560 \cos\left[\frac{9c}{2} + 4 d x\right] - 4032 \cos\left[\frac{9c}{2} + 5 d x\right] - 4032 \cos\left[\frac{11c}{2} + 5 d x\right] + 630 \cos\left[\frac{11c}{2} + 6 d x\right] - \\
 & 630 \cos\left[\frac{13c}{2} + 6 d x\right] - 720 \cos\left[\frac{13c}{2} + 7 d x\right] - 720 \cos\left[\frac{15c}{2} + 7 d x\right] + 945 \cos\left[\frac{15c}{2} + 8 d x\right] - \\
 & 945 \cos\left[\frac{17c}{2} + 8 d x\right] + 560 \cos\left[\frac{17c}{2} + 9 d x\right] + 560 \cos\left[\frac{19c}{2} + 9 d x\right] - 126 \cos\left[\frac{19c}{2} + 10 d x\right] + \\
 & 126 \cos\left[\frac{21c}{2} + 10 d x\right] + 327180 \sin\left[\frac{c}{2}\right] - 471240 c \sin\left[\frac{c}{2}\right] + 45360 d x \sin\left[\frac{c}{2}\right] - \\
 & 30240 \sin\left[\frac{c}{2} + d x\right] + 30240 \sin\left[\frac{3c}{2} + d x\right] - 1260 \sin\left[\frac{3c}{2} + 2 d x\right] - 1260 \sin\left[\frac{5c}{2} + 2 d x\right] - \\
 & 6720 \sin\left[\frac{5c}{2} + 3 d x\right] + 6720 \sin\left[\frac{7c}{2} + 3 d x\right] - 7560 \sin\left[\frac{7c}{2} + 4 d x\right] - 7560 \sin\left[\frac{9c}{2} + 4 d x\right] + \\
 & 4032 \sin\left[\frac{9c}{2} + 5 d x\right] - 4032 \sin\left[\frac{11c}{2} + 5 d x\right] + 630 \sin\left[\frac{11c}{2} + 6 d x\right] + 630 \sin\left[\frac{13c}{2} + 6 d x\right] + \\
 & 720 \sin\left[\frac{13c}{2} + 7 d x\right] - 720 \sin\left[\frac{15c}{2} + 7 d x\right] + 945 \sin\left[\frac{15c}{2} + 8 d x\right] + 945 \sin\left[\frac{17c}{2} + 8 d x\right] - \\
 & \left. 560 \sin\left[\frac{17c}{2} + 9 d x\right] + 560 \sin\left[\frac{19c}{2} + 9 d x\right] - 126 \sin\left[\frac{19c}{2} + 10 d x\right] - 126 \sin\left[\frac{21c}{2} + 10 d x\right] \right)
 \end{aligned}$$

Problem 724: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^8 \sin[c + d x]^3}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 159 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{3x}{64a^2} - \frac{2\cos[c + dx]^5}{5a^2d} + \frac{3\cos[c + dx]^7}{7a^2d} - \frac{\cos[c + dx]^9}{9a^2d} - \frac{3\cos[c + dx]\sin[c + dx]}{64a^2d} \\
 & \frac{\cos[c + dx]^3\sin[c + dx]}{32a^2d} + \frac{\cos[c + dx]^5\sin[c + dx]}{8a^2d} + \frac{\cos[c + dx]^5\sin[c + dx]^3}{4a^2d}
 \end{aligned}$$

Result (type 3, 429 leaves):

$$\begin{aligned}
 & - \frac{1}{322560 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(2520 (55 c + 6 d x) \cos\left[\frac{c}{2}\right] + 11340 \cos\left[\frac{c}{2} + d x\right] + 11340 \cos\left[\frac{3 c}{2} + d x\right] + 3360 \cos\left[\frac{5 c}{2} + 3 d x\right] + \right. \\
 & 3360 \cos\left[\frac{7 c}{2} + 3 d x\right] - 2520 \cos\left[\frac{7 c}{2} + 4 d x\right] + 2520 \cos\left[\frac{9 c}{2} + 4 d x\right] - 1008 \cos\left[\frac{9 c}{2} + 5 d x\right] - \\
 & 1008 \cos\left[\frac{11 c}{2} + 5 d x\right] - 450 \cos\left[\frac{13 c}{2} + 7 d x\right] - 450 \cos\left[\frac{15 c}{2} + 7 d x\right] + 315 \cos\left[\frac{15 c}{2} + 8 d x\right] - \\
 & 315 \cos\left[\frac{17 c}{2} + 8 d x\right] + 70 \cos\left[\frac{17 c}{2} + 9 d x\right] + 70 \cos\left[\frac{19 c}{2} + 9 d x\right] - 81900 \sin\left[\frac{c}{2}\right] + \\
 & 138600 c \sin\left[\frac{c}{2}\right] + 15120 d x \sin\left[\frac{c}{2}\right] - 11340 \sin\left[\frac{c}{2} + d x\right] + 11340 \sin\left[\frac{3 c}{2} + d x\right] - \\
 & 3360 \sin\left[\frac{5 c}{2} + 3 d x\right] + 3360 \sin\left[\frac{7 c}{2} + 3 d x\right] - 2520 \sin\left[\frac{7 c}{2} + 4 d x\right] - 2520 \sin\left[\frac{9 c}{2} + 4 d x\right] + \\
 & 1008 \sin\left[\frac{9 c}{2} + 5 d x\right] - 1008 \sin\left[\frac{11 c}{2} + 5 d x\right] + 450 \sin\left[\frac{13 c}{2} + 7 d x\right] - 450 \sin\left[\frac{15 c}{2} + 7 d x\right] + \\
 & \left. 315 \sin\left[\frac{15 c}{2} + 8 d x\right] + 315 \sin\left[\frac{17 c}{2} + 8 d x\right] - 70 \sin\left[\frac{17 c}{2} + 9 d x\right] + 70 \sin\left[\frac{19 c}{2} + 9 d x\right] \right)
 \end{aligned}$$

Problem 725: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^8 \sin [c+d x]^2}{(a+a \sin [c+d x])^2} d x$$

Optimal (type 3, 141 leaves, 15 steps):

$$\begin{aligned}
 & \frac{11 x}{128 a^2} + \frac{2 \cos [c+d x]^5}{5 a^2 d} - \frac{2 \cos [c+d x]^7}{7 a^2 d} + \frac{11 \cos [c+d x] \sin [c+d x]}{128 a^2 d} + \\
 & \frac{11 \cos [c+d x]^3 \sin [c+d x]}{192 a^2 d} - \frac{11 \cos [c+d x]^5 \sin [c+d x]}{48 a^2 d} - \frac{\cos [c+d x]^5 \sin [c+d x]^3}{8 a^2 d}
 \end{aligned}$$

Result (type 3, 481 leaves):

$$\begin{aligned}
 & \frac{1}{215040 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
 & \left(9240 (15 c + 2 d x) \cos\left[\frac{c}{2}\right] + 10080 \cos\left[\frac{c}{2} + d x\right] + 10080 \cos\left[\frac{3 c}{2} + d x\right] + 1680 \cos\left[\frac{3 c}{2} + 2 d x\right] - \right. \\
 & \quad 1680 \cos\left[\frac{5 c}{2} + 2 d x\right] + 3360 \cos\left[\frac{5 c}{2} + 3 d x\right] + 3360 \cos\left[\frac{7 c}{2} + 3 d x\right] - 2520 \cos\left[\frac{7 c}{2} + 4 d x\right] + \\
 & \quad 2520 \cos\left[\frac{9 c}{2} + 4 d x\right] - 672 \cos\left[\frac{9 c}{2} + 5 d x\right] - 672 \cos\left[\frac{11 c}{2} + 5 d x\right] - 560 \cos\left[\frac{11 c}{2} + 6 d x\right] + \\
 & \quad 560 \cos\left[\frac{13 c}{2} + 6 d x\right] - 480 \cos\left[\frac{13 c}{2} + 7 d x\right] - 480 \cos\left[\frac{15 c}{2} + 7 d x\right] + 105 \cos\left[\frac{15 c}{2} + 8 d x\right] - \\
 & \quad 105 \cos\left[\frac{17 c}{2} + 8 d x\right] - 79800 \sin\left[\frac{c}{2}\right] + 138600 c \sin\left[\frac{c}{2}\right] + 18480 d x \sin\left[\frac{c}{2}\right] - \\
 & \quad 10080 \sin\left[\frac{c}{2} + d x\right] + 10080 \sin\left[\frac{3 c}{2} + d x\right] + 1680 \sin\left[\frac{3 c}{2} + 2 d x\right] + 1680 \sin\left[\frac{5 c}{2} + 2 d x\right] - \\
 & \quad 3360 \sin\left[\frac{5 c}{2} + 3 d x\right] + 3360 \sin\left[\frac{7 c}{2} + 3 d x\right] - 2520 \sin\left[\frac{7 c}{2} + 4 d x\right] - 2520 \sin\left[\frac{9 c}{2} + 4 d x\right] + \\
 & \quad 672 \sin\left[\frac{9 c}{2} + 5 d x\right] - 672 \sin\left[\frac{11 c}{2} + 5 d x\right] - 560 \sin\left[\frac{11 c}{2} + 6 d x\right] - 560 \sin\left[\frac{13 c}{2} + 6 d x\right] + \\
 & \quad \left. 480 \sin\left[\frac{13 c}{2} + 7 d x\right] - 480 \sin\left[\frac{15 c}{2} + 7 d x\right] + 105 \sin\left[\frac{15 c}{2} + 8 d x\right] + 105 \sin\left[\frac{17 c}{2} + 8 d x\right] \right)
 \end{aligned}$$

Problem 726: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^8 \sin[c + d x]}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 124 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{x}{8 a^2} - \frac{2 \cos[c + d x]^7}{35 a^2 d} - \frac{\cos[c + d x] \sin[c + d x]}{8 a^2 d} - \\
 & \frac{\cos[c + d x]^3 \sin[c + d x]}{12 a^2 d} - \frac{\cos[c + d x]^5 \sin[c + d x]}{15 a^2 d} - \frac{\cos[c + d x]^9}{5 d (a + a \sin[c + d x])^2}
 \end{aligned}$$

Result (type 3, 414 leaves):

$$\begin{aligned}
& - \frac{1}{13440 a^2 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \\
& \left(1680 d x \cos\left[\frac{c}{2}\right] + 1155 \cos\left[\frac{c}{2} + d x\right] + 1155 \cos\left[\frac{3c}{2} + d x\right] + 210 \cos\left[\frac{3c}{2} + 2 d x\right] - \right. \\
& 210 \cos\left[\frac{5c}{2} + 2 d x\right] + 525 \cos\left[\frac{5c}{2} + 3 d x\right] + 525 \cos\left[\frac{7c}{2} + 3 d x\right] - 210 \cos\left[\frac{7c}{2} + 4 d x\right] + \\
& 210 \cos\left[\frac{9c}{2} + 4 d x\right] + 63 \cos\left[\frac{9c}{2} + 5 d x\right] + 63 \cos\left[\frac{11c}{2} + 5 d x\right] - 70 \cos\left[\frac{11c}{2} + 6 d x\right] + \\
& 70 \cos\left[\frac{13c}{2} + 6 d x\right] - 15 \cos\left[\frac{13c}{2} + 7 d x\right] - 15 \cos\left[\frac{15c}{2} + 7 d x\right] - 980 \sin\left[\frac{c}{2}\right] + \\
& 1680 d x \sin\left[\frac{c}{2}\right] - 1155 \sin\left[\frac{c}{2} + d x\right] + 1155 \sin\left[\frac{3c}{2} + d x\right] + 210 \sin\left[\frac{3c}{2} + 2 d x\right] + \\
& 210 \sin\left[\frac{5c}{2} + 2 d x\right] - 525 \sin\left[\frac{5c}{2} + 3 d x\right] + 525 \sin\left[\frac{7c}{2} + 3 d x\right] - \\
& 210 \sin\left[\frac{7c}{2} + 4 d x\right] - 210 \sin\left[\frac{9c}{2} + 4 d x\right] - 63 \sin\left[\frac{9c}{2} + 5 d x\right] + 63 \sin\left[\frac{11c}{2} + 5 d x\right] - \\
& \left. 70 \sin\left[\frac{11c}{2} + 6 d x\right] - 70 \sin\left[\frac{13c}{2} + 6 d x\right] + 15 \sin\left[\frac{13c}{2} + 7 d x\right] - 15 \sin\left[\frac{15c}{2} + 7 d x\right] \right)
\end{aligned}$$

Problem 732: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^2 \cot[c + d x]^6}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 118 leaves, 11 steps):

$$\begin{aligned}
& \frac{x}{a^2} + \frac{3 \operatorname{ArcTanh}[\cos[c + d x]]}{4 a^2 d} + \frac{\cot[c + d x]}{a^2 d} - \frac{\cot[c + d x]^3}{3 a^2 d} - \\
& \frac{\cot[c + d x]^5}{5 a^2 d} - \frac{3 \cot[c + d x] \operatorname{Csc}[c + d x]}{4 a^2 d} + \frac{\cot[c + d x]^3 \operatorname{Csc}[c + d x]}{2 a^2 d}
\end{aligned}$$

Result (type 3, 254 leaves):

$$\begin{aligned}
& \frac{1}{960 a^2 d} \\
& \operatorname{Csc}[c + d x]^5 \left(-40 \cos[c + d x] - 220 \cos[3(c + d x)] + 68 \cos[5(c + d x)] + 600 c \sin[c + d x] + \right. \\
& 600 d x \sin[c + d x] + 450 \log\left[\cos\left[\frac{1}{2}(c + d x)\right]\right] \sin[c + d x] - 450 \log\left[\sin\left[\frac{1}{2}(c + d x)\right]\right] \\
& \sin[c + d x] - 60 \sin[2(c + d x)] - 300 c \sin[3(c + d x)] - 300 d x \sin[3(c + d x)] - \\
& 225 \log\left[\cos\left[\frac{1}{2}(c + d x)\right]\right] \sin[3(c + d x)] + 225 \log\left[\sin\left[\frac{1}{2}(c + d x)\right]\right] \sin[3(c + d x)] + \\
& 150 \sin[4(c + d x)] + 60 c \sin[5(c + d x)] + 60 d x \sin[5(c + d x)] + \\
& \left. 45 \log\left[\cos\left[\frac{1}{2}(c + d x)\right]\right] \sin[5(c + d x)] - 45 \log\left[\sin\left[\frac{1}{2}(c + d x)\right]\right] \sin[5(c + d x)] \right)
\end{aligned}$$

Problem 734: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^8}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 124 leaves, 19 steps):

$$\frac{\text{ArcTanh}[\text{Cos}[c + d x]]}{8 a^2 d} - \frac{2 \text{Cot}[c + d x]^5}{5 a^2 d} - \frac{\text{Cot}[c + d x]^7}{7 a^2 d} + \frac{\text{Cot}[c + d x] \text{Csc}[c + d x]}{8 a^2 d} - \frac{7 \text{Cot}[c + d x] \text{Csc}[c + d x]^3}{12 a^2 d} + \frac{\text{Cot}[c + d x] \text{Csc}[c + d x]^5}{3 a^2 d}$$

Result (type 3, 251 leaves):

$$-\frac{1}{53760 a^2 d} \text{Csc}[c + d x]^7 \left(5880 \text{Cos}[c + d x] + 2184 \text{Cos}[3(c + d x)] - 168 \text{Cos}[5(c + d x)] - 216 \text{Cos}[7(c + d x)] - 3675 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[c + d x] + 3675 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[c + d x] - 2170 \text{Sin}[2(c + d x)] + 2205 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[3(c + d x)] - 2205 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[3(c + d x)] - 3080 \text{Sin}[4(c + d x)] - 735 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[5(c + d x)] + 735 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[5(c + d x)] - 210 \text{Sin}[6(c + d x)] + 105 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[7(c + d x)] - 105 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \text{Sin}[7(c + d x)] \right)$$

Problem 739: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cos}[c + d x]^8 \text{Sin}[c + d x]^3}{(a + a \text{Sin}[c + d x])^3} dx$$

Optimal (type 3, 161 leaves, 18 steps):

$$-\frac{29 x}{128 a^3} - \frac{4 \text{Cos}[c + d x]^3}{3 a^3 d} + \frac{7 \text{Cos}[c + d x]^5}{5 a^3 d} - \frac{3 \text{Cos}[c + d x]^7}{7 a^3 d} - \frac{29 \text{Cos}[c + d x] \text{Sin}[c + d x]}{128 a^3 d} + \frac{29 \text{Cos}[c + d x]^3 \text{Sin}[c + d x]}{64 a^3 d} + \frac{29 \text{Cos}[c + d x]^3 \text{Sin}[c + d x]^3}{48 a^3 d} + \frac{\text{Cos}[c + d x]^3 \text{Sin}[c + d x]^5}{8 a^3 d}$$

Result (type 3, 481 leaves):

$$\begin{aligned}
 & \frac{1}{215\,040\,a^3\,d} \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \\
 & \left(840\,(1287\,c - 58\,d\,x)\,\cos\left[\frac{c}{2}\right] - 38\,640\,\cos\left[\frac{c}{2} + d\,x\right] - 38\,640\,\cos\left[\frac{3\,c}{2} + d\,x\right] + 6720\,\cos\left[\frac{3\,c}{2} + 2\,d\,x\right] - \right. \\
 & 6720\,\cos\left[\frac{5\,c}{2} + 2\,d\,x\right] - 3920\,\cos\left[\frac{5\,c}{2} + 3\,d\,x\right] - 3920\,\cos\left[\frac{7\,c}{2} + 3\,d\,x\right] + 5880\,\cos\left[\frac{7\,c}{2} + 4\,d\,x\right] - \\
 & 5880\,\cos\left[\frac{9\,c}{2} + 4\,d\,x\right] + 4368\,\cos\left[\frac{9\,c}{2} + 5\,d\,x\right] + 4368\,\cos\left[\frac{11\,c}{2} + 5\,d\,x\right] - 2240\,\cos\left[\frac{11\,c}{2} + 6\,d\,x\right] + \\
 & 2240\,\cos\left[\frac{13\,c}{2} + 6\,d\,x\right] - 720\,\cos\left[\frac{13\,c}{2} + 7\,d\,x\right] - 720\,\cos\left[\frac{15\,c}{2} + 7\,d\,x\right] + 105\,\cos\left[\frac{15\,c}{2} + 8\,d\,x\right] - \\
 & 105\,\cos\left[\frac{17\,c}{2} + 8\,d\,x\right] - 998\,340\,\sin\left[\frac{c}{2}\right] + 1\,081\,080\,c\,\sin\left[\frac{c}{2}\right] - 48\,720\,d\,x\,\sin\left[\frac{c}{2}\right] + \\
 & 38\,640\,\sin\left[\frac{c}{2} + d\,x\right] - 38\,640\,\sin\left[\frac{3\,c}{2} + d\,x\right] + 6720\,\sin\left[\frac{3\,c}{2} + 2\,d\,x\right] + 6720\,\sin\left[\frac{5\,c}{2} + 2\,d\,x\right] + \\
 & 3920\,\sin\left[\frac{5\,c}{2} + 3\,d\,x\right] - 3920\,\sin\left[\frac{7\,c}{2} + 3\,d\,x\right] + 5880\,\sin\left[\frac{7\,c}{2} + 4\,d\,x\right] + 5880\,\sin\left[\frac{9\,c}{2} + 4\,d\,x\right] - \\
 & 4368\,\sin\left[\frac{9\,c}{2} + 5\,d\,x\right] + 4368\,\sin\left[\frac{11\,c}{2} + 5\,d\,x\right] - 2240\,\sin\left[\frac{11\,c}{2} + 6\,d\,x\right] - 2240\,\sin\left[\frac{13\,c}{2} + 6\,d\,x\right] + \\
 & \left. 720\,\sin\left[\frac{13\,c}{2} + 7\,d\,x\right] - 720\,\sin\left[\frac{15\,c}{2} + 7\,d\,x\right] + 105\,\sin\left[\frac{15\,c}{2} + 8\,d\,x\right] + 105\,\sin\left[\frac{17\,c}{2} + 8\,d\,x\right] \right)
 \end{aligned}$$

Problem 740: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^8 \sin[c + d x]^2}{(a + a \sin[c + d x])^3} dx$$

Optimal (type 3, 133 leaves, 16 steps):

$$\begin{aligned}
 & \frac{5x}{16a^3} + \frac{4\cos[c + dx]^3}{3a^3d} - \frac{\cos[c + dx]^5}{a^3d} + \frac{\cos[c + dx]^7}{7a^3d} + \\
 & \frac{5\cos[c + dx]\sin[c + dx]}{16a^3d} - \frac{5\cos[c + dx]^3\sin[c + dx]}{8a^3d} - \frac{\cos[c + dx]^3\sin[c + dx]^3}{2a^3d}
 \end{aligned}$$

Result (type 3, 429 leaves):

$$\frac{1}{2688 a^3 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(-168 (99 c - 5 d x) \cos\left[\frac{c}{2}\right] + 609 \cos\left[\frac{c}{2} + d x\right] + 609 \cos\left[\frac{3 c}{2} + d x\right] - 63 \cos\left[\frac{3 c}{2} + 2 d x\right] + 63 \cos\left[\frac{5 c}{2} + 2 d x\right] + 91 \cos\left[\frac{5 c}{2} + 3 d x\right] + 91 \cos\left[\frac{7 c}{2} + 3 d x\right] - 105 \cos\left[\frac{7 c}{2} + 4 d x\right] + 105 \cos\left[\frac{9 c}{2} + 4 d x\right] - 63 \cos\left[\frac{9 c}{2} + 5 d x\right] - 63 \cos\left[\frac{11 c}{2} + 5 d x\right] + 21 \cos\left[\frac{11 c}{2} + 6 d x\right] - 21 \cos\left[\frac{13 c}{2} + 6 d x\right] + 3 \cos\left[\frac{13 c}{2} + 7 d x\right] + 3 \cos\left[\frac{15 c}{2} + 7 d x\right] + 16996 \sin\left[\frac{c}{2}\right] - 16632 c \sin\left[\frac{c}{2}\right] + 840 d x \sin\left[\frac{c}{2}\right] - 609 \sin\left[\frac{c}{2} + d x\right] + 609 \sin\left[\frac{3 c}{2} + d x\right] - 63 \sin\left[\frac{3 c}{2} + 2 d x\right] - 63 \sin\left[\frac{5 c}{2} + 2 d x\right] - 91 \sin\left[\frac{5 c}{2} + 3 d x\right] + 91 \sin\left[\frac{7 c}{2} + 3 d x\right] - 105 \sin\left[\frac{7 c}{2} + 4 d x\right] - 105 \sin\left[\frac{9 c}{2} + 4 d x\right] + 63 \sin\left[\frac{9 c}{2} + 5 d x\right] - 63 \sin\left[\frac{11 c}{2} + 5 d x\right] + 21 \sin\left[\frac{11 c}{2} + 6 d x\right] + 21 \sin\left[\frac{13 c}{2} + 6 d x\right] - 3 \sin\left[\frac{13 c}{2} + 7 d x\right] + 3 \sin\left[\frac{15 c}{2} + 7 d x\right] \right)$$

Problem 741: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^8 \sin[c + d x]}{(a + a \sin[c + d x])^3} dx$$

Optimal (type 3, 131 leaves, 6 steps):

$$\frac{7 x}{16 a^3} - \frac{7 \cos[c + d x]^5}{30 a^3 d} - \frac{7 \cos[c + d x] \sin[c + d x]}{16 a^3 d} - \frac{7 \cos[c + d x]^3 \sin[c + d x]}{24 a^3 d} - \frac{\cos[c + d x]^9}{3 d (a + a \sin[c + d x])^3} - \frac{\cos[c + d x]^7}{6 d (a^3 + a^3 \sin[c + d x])}$$

Result (type 3, 362 leaves):

$$\frac{1}{1920 a^3 d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right)} \left(-840 d x \cos\left[\frac{c}{2}\right] - 600 \cos\left[\frac{c}{2} + d x\right] - 600 \cos\left[\frac{3 c}{2} + d x\right] + 15 \cos\left[\frac{3 c}{2} + 2 d x\right] - 15 \cos\left[\frac{5 c}{2} + 2 d x\right] - 140 \cos\left[\frac{5 c}{2} + 3 d x\right] - 140 \cos\left[\frac{7 c}{2} + 3 d x\right] + 105 \cos\left[\frac{7 c}{2} + 4 d x\right] - 105 \cos\left[\frac{9 c}{2} + 4 d x\right] + 36 \cos\left[\frac{9 c}{2} + 5 d x\right] + 36 \cos\left[\frac{11 c}{2} + 5 d x\right] - 5 \cos\left[\frac{11 c}{2} + 6 d x\right] + 5 \cos\left[\frac{13 c}{2} + 6 d x\right] + 42 \sin\left[\frac{c}{2}\right] - 840 d x \sin\left[\frac{c}{2}\right] + 600 \sin\left[\frac{c}{2} + d x\right] - 600 \sin\left[\frac{3 c}{2} + d x\right] + 15 \sin\left[\frac{3 c}{2} + 2 d x\right] + 15 \sin\left[\frac{5 c}{2} + 2 d x\right] + 140 \sin\left[\frac{5 c}{2} + 3 d x\right] - 140 \sin\left[\frac{7 c}{2} + 3 d x\right] + 105 \sin\left[\frac{7 c}{2} + 4 d x\right] + 105 \sin\left[\frac{9 c}{2} + 4 d x\right] - 36 \sin\left[\frac{9 c}{2} + 5 d x\right] + 36 \sin\left[\frac{11 c}{2} + 5 d x\right] - 5 \sin\left[\frac{11 c}{2} + 6 d x\right] - 5 \sin\left[\frac{13 c}{2} + 6 d x\right] \right)$$

Problem 745: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4 \cot [c+d x]^4}{(a+a \sin [c+d x])^3} d x$$

Optimal (type 3, 92 leaves, 11 steps):

$$\frac{3 x}{a^3} - \frac{\operatorname{ArcTanh}[\cos [c+d x]]}{2 a^3 d} - \frac{\cos [c+d x]}{a^3 d} - \frac{3 \cot [c+d x]}{a^3 d} - \frac{\cot [c+d x]^3}{3 a^3 d} + \frac{3 \cot [c+d x] \operatorname{Csc}[c+d x]}{2 a^3 d}$$

Result (type 3, 538 leaves):

$$\begin{aligned} & - \frac{3 (c+d x) \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{d (a+a \sin [c+d x])^3} - \\ & \frac{\cos [c+d x] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{d (a+a \sin [c+d x])^3} - \\ & \frac{4 \cot \left[\frac{1}{2} (c+d x) \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{3 d (a+a \sin [c+d x])^3} + \\ & \frac{3 \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{8 d (a+a \sin [c+d x])^3} - \\ & \left(\cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \right) / \\ & \left(24 d (a+a \sin [c+d x])^3 \right) - \frac{\operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{2 d (a+a \sin [c+d x])^3} + \\ & \frac{\operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{2 d (a+a \sin [c+d x])^3} - \\ & \frac{3 \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{8 d (a+a \sin [c+d x])^3} + \\ & \frac{4 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]}{3 d (a+a \sin [c+d x])^3} + \\ & \left(\operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] \right) / \\ & \left(24 d (a+a \sin [c+d x])^3 \right) \end{aligned}$$

Problem 746: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]^5}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 97 leaves, 12 steps):

$$\frac{x}{a^3} + \frac{13 \operatorname{ArcTanh}[\cos [c+d x]]}{8 a^3 d} + \frac{\cot [c+d x]}{a^3 d} + \frac{\cot [c+d x]^3}{a^3 d} - \frac{11 \cot [c+d x] \operatorname{Csc}[c+d x]}{8 a^3 d} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^3}{4 a^3 d}$$

Result (type 3, 495 leaves):

$$\begin{aligned} & \frac{(c+d x) \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{d (a+a \sin [c+d x])^3} - \\ & \frac{11 \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{32 d (a+a \sin [c+d x])^3} + \\ & \frac{\left(\cot \left[\frac{1}{2} (c+d x) \right] \operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \right)}{\left(8 d (a+a \sin [c+d x])^3 \right)} - \frac{\operatorname{Csc} \left[\frac{1}{2} (c+d x) \right]^4 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{64 d (a+a \sin [c+d x])^3} + \\ & \frac{13 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{8 d (a+a \sin [c+d x])^3} - \\ & \frac{13 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{8 d (a+a \sin [c+d x])^3} + \\ & \frac{11 \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{32 d (a+a \sin [c+d x])^3} + \\ & \frac{\operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^4 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6}{64 d (a+a \sin [c+d x])^3} - \\ & \frac{\left(\operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^6 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] \right)}{\left(8 d (a+a \sin [c+d x])^3 \right)} \end{aligned}$$

Problem 750: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c+d x]^8 \operatorname{Csc}[c+d x]}{(a+a \sin [c+d x])^3} dx$$

Optimal (type 3, 166 leaves, 18 steps):

$$\frac{29 \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{128 a^3 d} + \frac{4 \operatorname{Cot}[c+dx]^3}{3 a^3 d} + \frac{7 \operatorname{Cot}[c+dx]^5}{5 a^3 d} +$$

$$\frac{3 \operatorname{Cot}[c+dx]^7}{7 a^3 d} + \frac{29 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{128 a^3 d} + \frac{29 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{192 a^3 d} -$$

$$\frac{23 \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^5}{48 a^3 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^7}{8 a^3 d}$$

Result (type 3, 1027 leaves):

$$\frac{19 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{105 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\frac{29 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{512 d (a+a \operatorname{Sin}[c+dx])^3} -$$

$$\left(83 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) /$$

$$\left(6720 d (a+a \operatorname{Sin}[c+dx])^3\right) + \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{1024 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\left(23 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) /$$

$$\left(2240 d (a+a \operatorname{Sin}[c+dx])^3\right) - \frac{13 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{1536 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\left(3 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6\right) /$$

$$\left(896 d (a+a \operatorname{Sin}[c+dx])^3\right) - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{2048 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\frac{29 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{128 d (a+a \operatorname{Sin}[c+dx])^3} -$$

$$\frac{29 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{128 d (a+a \operatorname{Sin}[c+dx])^3} -$$

$$\frac{29 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{512 d (a+a \operatorname{Sin}[c+dx])^3} -$$

$$\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{1024 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\frac{13 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6}{1536 d (a+a \operatorname{Sin}[c+dx])^3} +$$

$$\frac{\sec\left[\frac{1}{2}(c+dx)\right]^8 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^6}{2048 d (a+a \sin[c+dx])^3} +$$

$$\frac{19 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^6 \tan\left[\frac{1}{2}(c+dx)\right]}{105 d (a+a \sin[c+dx])^3} +$$

$$\left(83 \sec\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^6 \tan\left[\frac{1}{2}(c+dx)\right]\right) /$$

$$(6720 d (a+a \sin[c+dx])^3) -$$

$$\left(23 \sec\left[\frac{1}{2}(c+dx)\right]^4 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^6 \tan\left[\frac{1}{2}(c+dx)\right]\right) /$$

$$(2240 d (a+a \sin[c+dx])^3) -$$

$$\left(3 \sec\left[\frac{1}{2}(c+dx)\right]^6 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^6 \tan\left[\frac{1}{2}(c+dx)\right]\right) /$$

$$(896 d (a+a \sin[c+dx])^3)$$

Problem 757: Result more than twice size of optimal antiderivative.

$$\int \csc[c+dx]^3 \sec[c+dx]^2 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 75 leaves, 8 steps):

$$-\frac{3 a \operatorname{ArcTanh}[\cos[c+dx]]}{2 d} - \frac{a \operatorname{Cot}[c+dx]}{d} +$$

$$\frac{3 a \sec[c+dx]}{2 d} - \frac{a \csc[c+dx]^2 \sec[c+dx]}{2 d} + \frac{a \tan[c+dx]}{d}$$

Result (type 3, 172 leaves):

$$-\frac{2 a \operatorname{Cot}\left[2\left(\frac{1}{2}(c+dx)\right)\right]}{d} - \frac{a \csc\left[\frac{1}{2}(c+dx)\right]^2}{8 d} -$$

$$\frac{3 a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \frac{3 a \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2}{8 d} +$$

$$\frac{a \sin\left[\frac{1}{2}(c+dx)\right]}{d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)} - \frac{a \sin\left[\frac{1}{2}(c+dx)\right]}{d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}$$

Problem 758: Result more than twice size of optimal antiderivative.

$$\int \csc[c+dx]^4 \sec[c+dx]^2 (a+a \sin[c+dx]) dx$$

Optimal (type 3, 91 leaves, 8 steps):

$$-\frac{3 a \operatorname{ArcTanh}[\cos [c+d x]]}{2 d}-\frac{2 a \cot [c+d x]}{d}-\frac{a \cot [c+d x]^3}{3 d}+\frac{3 a \sec [c+d x]}{2 d}-\frac{a \csc [c+d x]^2 \sec [c+d x]}{2 d}+\frac{a \tan [c+d x]}{d}$$

Result (type 3, 205 leaves):

$$-\frac{5 a \cot [c+d x]}{3 d}-\frac{a \csc \left[\frac{1}{2}(c+d x)\right]^2}{8 d}-\frac{a \cot [c+d x] \csc [c+d x]^2}{3 d}-\frac{3 a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]\right]}{2 d}+\frac{3 a \operatorname{Log}\left[\sin \left[\frac{1}{2}(c+d x)\right]\right]}{2 d}+\frac{a \sec \left[\frac{1}{2}(c+d x)\right]^2}{8 d}+\frac{a \sin \left[\frac{1}{2}(c+d x)\right]}{d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)}-\frac{a \sin \left[\frac{1}{2}(c+d x)\right]}{d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)}+\frac{a \tan [c+d x]}{d}$$

Problem 760: Result more than twice size of optimal antiderivative.

$$\int(a+a \sin [c+d x])^2 \tan [c+d x]^2 dx$$

Optimal (type 3, 71 leaves, 6 steps):

$$-\frac{5 a^2 x}{2}+\frac{2 a^2 \cos [c+d x]}{d}+\frac{2 a^2 \cos [c+d x]}{d(1-\sin [c+d x])}+\frac{a^2 \cos [c+d x] \sin [c+d x]}{2 d}$$

Result (type 3, 145 leaves):

$$-\left(\left(a^2(1+\sin [c+d x])^2\left(\cos \left[\frac{1}{2}(c+d x)\right]\left(10(c+d x)-8 \cos [c+d x]-\sin [2(c+d x)]\right)\right)+\sin \left[\frac{1}{2}(c+d x)\right]\left(-2(8+5 c+5 d x)+8 \cos [c+d x]+\sin [2(c+d x)]\right)\right)\right) / \left(4 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4\right)$$

Problem 761: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x](a+a \sin [c+d x])^2 \tan [c+d x] dx$$

Optimal (type 3, 43 leaves, 3 steps):

$$-2 a^2 x+\frac{2 a^2 \cos [c+d x]}{d}+\frac{\sec [c+d x](a+a \sin [c+d x])^2}{d}$$

Result (type 3, 90 leaves):

$$\left(\left(-2(c+dx) + \cos[c+dx] + \frac{4 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} \right) (a + a \sin[c+dx])^2 \right) / \left(d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)$$

Problem 767: Result more than twice size of optimal antiderivative.

$$\int \sec[c+dx] (a + a \sin[c+dx])^3 \tan[c+dx] dx$$

Optimal (type 3, 67 leaves, 2 steps):

$$-\frac{9a^3x}{2} + \frac{6a^3 \cos[c+dx]}{d} + \frac{3a^3 \cos[c+dx] \sin[c+dx]}{2d} + \frac{\sec[c+dx] (a + a \sin[c+dx])^3}{d}$$

Result (type 3, 145 leaves):

$$-\left(\left(a^3 (1 + \sin[c+dx])^3 \left(\cos\left[\frac{1}{2}(c+dx)\right] (18(c+dx) - 12 \cos[c+dx] - \sin[2(c+dx)]) + \sin\left[\frac{1}{2}(c+dx)\right] (-2(16+9c+9dx) + 12 \cos[c+dx] + \sin[2(c+dx)]) \right) \right) \right) / \left(4d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^6 \right)$$

Problem 771: Result more than twice size of optimal antiderivative.

$$\int \csc[c+dx]^4 \sec[c+dx]^2 (a + a \sin[c+dx])^3 dx$$

Optimal (type 3, 98 leaves, 10 steps):

$$-\frac{11a^3 \operatorname{ArcTanh}[\cos[c+dx]]}{2d} - \frac{5a^3 \cot[c+dx]}{d} - \frac{a^3 \cot[c+dx]^3}{3d} - \frac{3a^3 \cot[c+dx] \csc[c+dx]}{2d} + \frac{4a^3 \cos[c+dx]}{d(1 - \sin[c+dx])}$$

Result (type 3, 211 leaves):

$$a^3 \left(-\frac{7 \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{3d} - \frac{3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24d} - \frac{11 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{11 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8d} + \frac{8 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)} + \frac{7 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{3d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24d} \right)$$

Problem 774: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tan}[c+dx]^2}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 50 leaves, 5 steps):

$$\frac{\operatorname{Sec}[c+dx]}{ad} - \frac{\operatorname{Sec}[c+dx]^3}{3ad} + \frac{\operatorname{Tan}[c+dx]^3}{3ad}$$

Result (type 3, 106 leaves):

$$\left(6 - 10 \operatorname{Cos}[c+dx] + 2 \operatorname{Cos}[2(c+dx)] + 8 \operatorname{Sin}[c+dx] - 5 \operatorname{Sin}[2(c+dx)]\right) / \left(12ad \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right) (1 + \operatorname{Sin}[c+dx])\right)$$

Problem 775: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 37 leaves, 5 steps):

$$\frac{\operatorname{Sec}[c+dx]^3}{3ad} - \frac{\operatorname{Tan}[c+dx]^3}{3ad}$$

Result (type 3, 104 leaves):

$$\left(-3 + \operatorname{Cos}[c+dx] + \operatorname{Cos}[2(c+dx)] - 2 \operatorname{Sin}[c+dx] + \frac{1}{2} \operatorname{Sin}[2(c+dx)]\right) / \left(6ad \left(-\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right) (1 + \operatorname{Sin}[c+dx])\right)$$

Problem 777: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + dx]^2 \text{Sec}[c + dx]^2}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 93 leaves, 8 steps):

$$\frac{\text{ArcTanh}[\text{Cos}[c + dx]]}{ad} - \frac{\text{Cot}[c + dx]}{ad} - \frac{\text{Sec}[c + dx]}{ad} - \frac{\text{Sec}[c + dx]^3}{3ad} + \frac{2 \text{Tan}[c + dx]}{ad} + \frac{\text{Tan}[c + dx]^3}{3ad}$$

Result (type 3, 245 leaves):

$$\begin{aligned} & - \left(\left(\text{Csc}[c + dx]^3 \left(2 + 10 \text{Cos}[2(c + dx)] + 8 \text{Cos}[3(c + dx)] + \right. \right. \right. \\ & \quad \left. \left. \left. 3 \text{Cos}[3(c + dx)] \text{Log}[\text{Cos}[\frac{1}{2}(c + dx)]] - 3 \text{Cos}[3(c + dx)] \text{Log}[\text{Sin}[\frac{1}{2}(c + dx)]] \right] + \right. \right. \\ & \quad \left. \left. \text{Cos}[c + dx] \left(-8 - 3 \text{Log}[\text{Cos}[\frac{1}{2}(c + dx)]] + 3 \text{Log}[\text{Sin}[\frac{1}{2}(c + dx)]] \right) + \right. \right. \\ & \quad \left. \left. 4 \text{Sin}[c + dx] - 16 \text{Sin}[2(c + dx)] - 6 \text{Log}[\text{Cos}[\frac{1}{2}(c + dx)]] \text{Sin}[2(c + dx)] + \right. \right. \\ & \quad \left. \left. 6 \text{Log}[\text{Sin}[\frac{1}{2}(c + dx)]] \text{Sin}[2(c + dx)] + 8 \text{Sin}[3(c + dx)] \right) \right) / \\ & \left(3ad \left(\text{Csc}[\frac{1}{2}(c + dx)] - \text{Sec}[\frac{1}{2}(c + dx)] \right) \left(\text{Csc}[\frac{1}{2}(c + dx)] + \text{Sec}[\frac{1}{2}(c + dx)] \right) \right) \\ & \left. (1 + \text{Sin}[c + dx]) \right) \end{aligned}$$

Problem 785: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + dx]^2 \text{Sec}[c + dx]^2}{(a + a \text{Sin}[c + dx])^2} dx$$

Optimal (type 3, 130 leaves, 12 steps):

$$\frac{2 \text{ArcTanh}[\text{Cos}[c + dx]]}{a^2 d} - \frac{\text{Cot}[c + dx]}{a^2 d} - \frac{2 \text{Sec}[c + dx]}{a^2 d} - \frac{2 \text{Sec}[c + dx]^3}{3 a^2 d} - \frac{2 \text{Sec}[c + dx]^5}{5 a^2 d} + \frac{4 \text{Tan}[c + dx]}{a^2 d} + \frac{5 \text{Tan}[c + dx]^3}{3 a^2 d} + \frac{2 \text{Tan}[c + dx]^5}{5 a^2 d}$$

Result (type 3, 289 leaves):

$$\begin{aligned}
 & - \frac{1}{15 a^2 d \left(\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 - \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) \left(1 + \operatorname{Sin}[c+d x]\right)^2} \\
 & \operatorname{Csc}[c+d x]^3 \left(40 + 48 \operatorname{Cos}[2(c+d x)] + 112 \operatorname{Cos}[3(c+d x)] - \right. \\
 & \quad \left. 28 \operatorname{Cos}[4(c+d x)] + 60 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] - \right. \\
 & \quad \left. 4 \operatorname{Cos}[c+d x] \left(28 + 15 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] - 15 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right) - \right. \\
 & \quad \left. 60 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + 58 \operatorname{Sin}[c+d x] - \right. \\
 & \quad \left. 168 \operatorname{Sin}[2(c+d x)] - 90 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[2(c+d x)] + \right. \\
 & \quad \left. 90 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[2(c+d x)] + 82 \operatorname{Sin}[3(c+d x)] + 28 \operatorname{Sin}[4(c+d x)] + \right. \\
 & \quad \left. 15 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[4(c+d x)] - 15 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[4(c+d x)] \right)
 \end{aligned}$$

Problem 786: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x]^2}{(a+a \operatorname{Sin}[c+d x])^2} dx$$

Optimal (type 3, 158 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{9 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{2 a^2 d} + \frac{2 \operatorname{Cot}[c+d x]}{a^2 d} + \frac{9 \operatorname{Sec}[c+d x]}{2 a^2 d} + \frac{3 \operatorname{Sec}[c+d x]^3}{2 a^2 d} + \frac{9 \operatorname{Sec}[c+d x]^5}{10 a^2 d} - \\
 & \frac{\operatorname{Csc}[c+d x]^2 \operatorname{Sec}[c+d x]^5}{2 a^2 d} - \frac{6 \operatorname{Tan}[c+d x]}{a^2 d} - \frac{2 \operatorname{Tan}[c+d x]^3}{a^2 d} - \frac{2 \operatorname{Tan}[c+d x]^5}{5 a^2 d}
 \end{aligned}$$

Result (type 3, 328 leaves):

$$\begin{aligned}
 & - \frac{1}{320 a^2 d (1 + \sin [c + d x])^2} \operatorname{Csc}[c + d x]^2 \operatorname{Sec}[c + d x] \\
 & \left(-348 + 176 \operatorname{Cos}[2(c + d x)] - 651 \operatorname{Cos}[3(c + d x)] + 332 \operatorname{Cos}[4(c + d x)] + 93 \operatorname{Cos}[5(c + d x)] - \right. \\
 & 630 \operatorname{Cos}[3(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 90 \operatorname{Cos}[5(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + \\
 & 18 \operatorname{Cos}[c + d x] \left(31 + 30 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - 30 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \\
 & 630 \operatorname{Cos}[3(c + d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 90 \operatorname{Cos}[5(c + d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\
 & 432 \operatorname{Sin}[c + d x] + 744 \operatorname{Sin}[2(c + d x)] + 720 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[2(c + d x)] - \\
 & 720 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[2(c + d x)] - 176 \operatorname{Sin}[3(c + d x)] - \\
 & 372 \operatorname{Sin}[4(c + d x)] - 360 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4(c + d x)] + \\
 & \left. 360 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4(c + d x)] + 128 \operatorname{Sin}[5(c + d x)] \right)
 \end{aligned}$$

Problem 793: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c + d x] \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 151 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{\operatorname{ArcTanh}[\operatorname{Cos}[c + d x]]}{a^3 d} + \frac{\operatorname{Sec}[c + d x]}{a^3 d} + \frac{\operatorname{Sec}[c + d x]^3}{3 a^3 d} + \frac{\operatorname{Sec}[c + d x]^5}{5 a^3 d} + \\
 & \frac{4 \operatorname{Sec}[c + d x]^7}{7 a^3 d} - \frac{3 \operatorname{Tan}[c + d x]}{a^3 d} - \frac{10 \operatorname{Tan}[c + d x]^3}{3 a^3 d} - \frac{11 \operatorname{Tan}[c + d x]^5}{5 a^3 d} - \frac{4 \operatorname{Tan}[c + d x]^7}{7 a^3 d}
 \end{aligned}$$

Result (type 3, 341 leaves):

$$\frac{1}{840 d (a + a \sin [c + d x])^3} \left(60 - \frac{120 \sin \left[\frac{1}{2} (c + d x) \right]}{\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right]} - \right. \\
324 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) + \\
162 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - 706 \sin \left[\frac{1}{2} (c + d x) \right] \\
\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + 353 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \\
2281 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 - \\
840 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 + \\
840 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 + \\
\left. \frac{105 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6}{\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right]} \right)$$

Problem 794: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c + d x]^2 \sec [c + d x]^2}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 162 leaves, 14 steps):

$$\frac{3 \operatorname{ArcTanh}[\cos [c + d x]]}{a^3 d} - \frac{\operatorname{Cot}[c + d x]}{a^3 d} - \frac{3 \sec [c + d x]}{a^3 d} - \frac{\sec [c + d x]^3}{a^3 d} - \frac{3 \sec [c + d x]^5}{5 a^3 d} - \\
\frac{4 \sec [c + d x]^7}{7 a^3 d} + \frac{7 \tan [c + d x]}{a^3 d} + \frac{5 \tan [c + d x]^3}{a^3 d} + \frac{13 \tan [c + d x]^5}{5 a^3 d} + \frac{4 \tan [c + d x]^7}{7 a^3 d}$$

Result (type 3, 351 leaves):

$$\frac{1}{140 a^3 d \left(\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) (1 + \operatorname{Sin}[c+dx])^3} \operatorname{Csc}[c+dx]^3$$

$$\begin{aligned} & \left(-966 - 440 \operatorname{Cos}[2(c+dx)] - 2640 \operatorname{Cos}[3(c+dx)] + 846 \operatorname{Cos}[4(c+dx)] + 176 \operatorname{Cos}[5(c+dx)] \right) - \\ & 1575 \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] + 105 \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 14 \operatorname{Cos}[c+dx] \left(176 + 105 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] - 105 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\ & 1575 \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 105 \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 1316 \operatorname{Sin}[c+dx] + 3520 \operatorname{Sin}[2(c+dx)] + 2100 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[2(c+dx)] - \\ & 2100 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[2(c+dx)] - 1380 \operatorname{Sin}[3(c+dx)] - \\ & 1056 \operatorname{Sin}[4(c+dx)] - 630 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[4(c+dx)] + \\ & 630 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[4(c+dx)] + 176 \operatorname{Sin}[5(c+dx)] \end{aligned}$$

Problem 803: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^3 \operatorname{Sec}[c+dx]^4 (a + a \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 110 leaves, 9 steps):

$$\begin{aligned} & -\frac{5 a \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{2 d} - \frac{a \operatorname{Cot}[c+dx]}{d} + \frac{5 a \operatorname{Sec}[c+dx]}{2 d} + \\ & \frac{5 a \operatorname{Sec}[c+dx]^3}{6 d} - \frac{a \operatorname{Csc}[c+dx]^2 \operatorname{Sec}[c+dx]^3}{2 d} + \frac{2 a \operatorname{Tan}[c+dx]}{d} + \frac{a \operatorname{Tan}[c+dx]^3}{3 d} \end{aligned}$$

Result (type 3, 359 leaves):

$$\begin{aligned} & -\frac{a \operatorname{Cot}[c+dx]}{d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8 d} - \frac{5 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \\ & \frac{5 a \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8 d} + \frac{a}{12 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2} + \\ & \frac{a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3} + \frac{13 a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)} - \\ & \frac{a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3} + \frac{a}{12 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2} - \\ & \frac{13 a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)} + \frac{5 a \operatorname{Tan}[c+dx]}{3 d} + \frac{a \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} \end{aligned}$$

Problem 818: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^4 \text{Sec}[c + dx]^4 (a + a \text{Sin}[c + dx])^3 dx$$

Optimal (type 3, 128 leaves, 12 steps):

$$\begin{aligned} & -\frac{17 a^3 \text{ArcTanh}[\text{Cos}[c + dx]]}{2 d} - \frac{6 a^3 \text{Cot}[c + dx]}{d} - \frac{a^3 \text{Cot}[c + dx]^3}{3 d} - \\ & \frac{3 a^3 \text{Cot}[c + dx] \text{Csc}[c + dx]}{2 d} + \frac{2 a^3 \text{Cos}[c + dx]}{3 d (1 - \text{Sin}[c + dx])^2} + \frac{23 a^3 \text{Cos}[c + dx]}{3 d (1 - \text{Sin}[c + dx])} \end{aligned}$$

Result (type 3, 287 leaves):

$$\begin{aligned} & a^3 \left(-\frac{17 \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{6 d} - \frac{3 \text{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{8 d} - \right. \\ & \frac{\text{Cot}\left[\frac{1}{2}(c + dx)\right] \text{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{24 d} - \frac{17 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right]\right]}{2 d} + \frac{17 \text{Log}\left[\text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{2 d} + \\ & \frac{3 \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2}{8 d} + \frac{2}{3 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\ & \frac{4 \text{Sin}\left[\frac{1}{2}(c + dx)\right]}{3 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^3} + \frac{46 \text{Sin}\left[\frac{1}{2}(c + dx)\right]}{3 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)} + \\ & \left. \frac{17 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{6 d} + \frac{\text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{24 d} \right) \end{aligned}$$

Problem 827: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + dx] \text{Sec}[c + dx]^4}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 115 leaves, 7 steps):

$$\begin{aligned} & -\frac{\text{ArcTanh}[\text{Cos}[c + dx]]}{a d} + \frac{\text{Sec}[c + dx]}{a d} + \frac{\text{Sec}[c + dx]^3}{3 a d} + \\ & \frac{\text{Sec}[c + dx]^5}{5 a d} - \frac{\text{Tan}[c + dx]}{a d} - \frac{2 \text{Tan}[c + dx]^3}{3 a d} - \frac{\text{Tan}[c + dx]^5}{5 a d} \end{aligned}$$

Result (type 3, 267 leaves):

$$\begin{aligned}
 & - \frac{1}{120 a d (1 + \sin [c + d x])} \\
 & \sec [c + d x]^3 \left(-100 - 76 \cos [2 (c + d x)] + \frac{149}{4} \cos [3 (c + d x)] - 8 \cos [4 (c + d x)] + \right. \\
 & \quad 30 \cos [3 (c + d x)] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] + \\
 & \quad \left. \cos [c + d x] \left(\frac{447}{4} + 90 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - 90 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \right) - \right. \\
 & \quad 30 \cos [3 (c + d x)] \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] - 22 \sin [c + d x] + \\
 & \quad \frac{149}{4} \sin [2 (c + d x)] + 30 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [2 (c + d x)] - \\
 & \quad 30 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [2 (c + d x)] - 14 \sin [3 (c + d x)] + \frac{149}{8} \sin [4 (c + d x)] + \\
 & \quad \left. 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [4 (c + d x)] - 15 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [4 (c + d x)] \right)
 \end{aligned}$$

Problem 828: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c + d x]^2 \sec [c + d x]^4}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 126 leaves, 8 steps):

$$\frac{\operatorname{ArcTanh}[\cos [c + d x]]}{a d} - \frac{\operatorname{Cot}[c + d x]}{a d} - \frac{\sec [c + d x]}{a d} - \frac{\sec [c + d x]^3}{3 a d} - \frac{\sec [c + d x]^5}{5 a d} + \frac{3 \tan [c + d x]}{a d} + \frac{\tan [c + d x]^3}{a d} + \frac{\tan [c + d x]^5}{5 a d}$$

Result (type 3, 341 leaves):

$$\begin{aligned}
 & - \frac{1}{3840 a d (1 + \sin[c + d x])} \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^3 \\
 & \left(176 + 1216 \operatorname{Cos}[2(c + d x)] + 149 \operatorname{Cos}[3(c + d x)] + 528 \operatorname{Cos}[4(c + d x)] + 149 \operatorname{Cos}[5(c + d x)] + \right. \\
 & 120 \operatorname{Cos}[3(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 120 \operatorname{Cos}[5(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] - \\
 & 120 \operatorname{Cos}[3(c + d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 120 \operatorname{Cos}[5(c + d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\
 & \operatorname{Cos}[c + d x] \left(-298 - 240 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] + 240 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \\
 & 352 \operatorname{Sin}[c + d x] - 596 \operatorname{Sin}[2(c + d x)] - 480 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[2(c + d x)] + \\
 & 480 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[2(c + d x)] + 864 \operatorname{Sin}[3(c + d x)] - \\
 & 298 \operatorname{Sin}[4(c + d x)] - 240 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4(c + d x)] + \\
 & \left. 240 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4(c + d x)] + 384 \operatorname{Sin}[5(c + d x)] \right)
 \end{aligned}$$

Problem 836: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c + d x] \operatorname{Sec}[c + d x]^4}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 149 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{\operatorname{ArcTanh}[\operatorname{Cos}[c + d x]]}{a^2 d} + \frac{\operatorname{Sec}[c + d x]}{a^2 d} + \frac{\operatorname{Sec}[c + d x]^3}{3 a^2 d} + \frac{\operatorname{Sec}[c + d x]^5}{5 a^2 d} + \\
 & \frac{2 \operatorname{Sec}[c + d x]^7}{7 a^2 d} - \frac{2 \operatorname{Tan}[c + d x]}{a^2 d} - \frac{2 \operatorname{Tan}[c + d x]^3}{a^2 d} - \frac{6 \operatorname{Tan}[c + d x]^5}{5 a^2 d} - \frac{2 \operatorname{Tan}[c + d x]^7}{7 a^2 d}
 \end{aligned}$$

Result (type 3, 352 leaves):

$$\begin{aligned}
 & \left(6216 + 5312 \cos [2 (c + d x)] - 1677 \cos [3 (c + d x)] + 696 \cos [4 (c + d x)] + 559 \cos [5 (c + d x)] - \right. \\
 & \quad 1260 \cos [3 (c + d x)] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] + 420 \cos [5 (c + d x)] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - \\
 & \quad 14 \cos [c + d x] \left(559 + 420 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - 420 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \right) + \\
 & \quad 1260 \cos [3 (c + d x)] \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] - 420 \cos [5 (c + d x)] \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 2464 \sin [c + d x] - 4472 \sin [2 (c + d x)] - 3360 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [2 (c + d x)] + \\
 & \quad 3360 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [2 (c + d x)] + 2208 \sin [3 (c + d x)] - \\
 & \quad 2236 \sin [4 (c + d x)] - 1680 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] \sin [4 (c + d x)] + \\
 & \quad \left. 1680 \log \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [4 (c + d x)] + 384 \sin [5 (c + d x)] \right) / \\
 & \left(6720 a^2 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^7 \right)
 \end{aligned}$$

Problem 837: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c + d x]^2 \sec [c + d x]^4}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 164 leaves, 12 steps):

$$\begin{aligned}
 & \frac{2 \operatorname{ArcTanh}[\cos [c + d x]]}{a^2 d} - \frac{\operatorname{Cot}[c + d x]}{a^2 d} - \frac{2 \sec [c + d x]}{a^2 d} - \frac{2 \sec [c + d x]^3}{3 a^2 d} - \frac{2 \sec [c + d x]^5}{5 a^2 d} - \\
 & \frac{2 \sec [c + d x]^7}{7 a^2 d} + \frac{5 \tan [c + d x]}{a^2 d} + \frac{3 \tan [c + d x]^3}{a^2 d} + \frac{7 \tan [c + d x]^5}{5 a^2 d} + \frac{2 \tan [c + d x]^7}{7 a^2 d}
 \end{aligned}$$

Result (type 3, 442 leaves):

$$\frac{1}{a^2} 16 \left(-\frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{32d} + \frac{\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} - \frac{\operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \right.$$

$$\frac{1}{768d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{384d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} +$$

$$\frac{13 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{384d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)} + \frac{\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{224d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} -$$

$$\frac{1}{448d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^6} + \frac{3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{140d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} -$$

$$\frac{3}{280d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{997 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{13440d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} -$$

$$\frac{997}{26880d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} +$$

$$\frac{4777 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{13440d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)} + \frac{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32d} \Bigg)$$

Problem 852: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sin}[c + dx]) \operatorname{Tan}[c + dx]^5 dx$$

Optimal (type 3, 115 leaves, 3 steps):

$$-\frac{23 a \operatorname{Log}[1 - \operatorname{Sin}[c + dx]]}{16 d a^3} + \frac{7 a \operatorname{Log}[1 + \operatorname{Sin}[c + dx]]}{16 d a^2} - \frac{a \operatorname{Sin}[c + dx]}{d a^2} + \frac{1}{8 d (a - a \operatorname{Sin}[c + dx])^2} - \frac{1}{d (a - a \operatorname{Sin}[c + dx])} + \frac{1}{8 d (a + a \operatorname{Sin}[c + dx])}$$

Result (type 3, 246 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{15 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \\
 & \frac{15 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} - \frac{a \operatorname{Sec}[c + d x]^2}{d} + \\
 & \frac{a \operatorname{Sec}[c + d x]^4}{4 d} + \frac{a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \\
 & \frac{a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \\
 & \frac{9 a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{a \operatorname{Sin}[c + d x]}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2}
 \end{aligned}$$

Problem 853: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x] (a + a \operatorname{Sin}[c + d x]) \operatorname{Tan}[c + d x]^4 dx$$

Optimal (type 3, 105 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{11 a \operatorname{Log}[1 - \operatorname{Sin}[c + d x]]}{16 d} - \frac{5 a \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{16 d} + \\
 & \frac{a^3}{8 d (a - a \operatorname{Sin}[c + d x])^2} - \frac{3 a^2}{4 d (a - a \operatorname{Sin}[c + d x])} - \frac{a^2}{8 d (a + a \operatorname{Sin}[c + d x])}
 \end{aligned}$$

Result (type 3, 234 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \\
 & \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} - \frac{a \operatorname{Sec}[c + d x]^2}{d} + \frac{a \operatorname{Sec}[c + d x]^4}{4 d} + \\
 & \frac{5 a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{5 a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \\
 & \frac{5 a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{5 a}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2}
 \end{aligned}$$

Problem 854: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^2 (a + a \operatorname{Sin}[c + d x]) \operatorname{Tan}[c + d x]^3 dx$$

Optimal (type 3, 84 leaves, 5 steps):

$$\frac{3 a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{a^3}{8 d (a-a \operatorname{Sin}[c+d x])^2} - \frac{a^2}{2 d (a-a \operatorname{Sin}[c+d x])} + \frac{a^2}{8 d (a+a \operatorname{Sin}[c+d x])}$$

Result (type 3, 207 leaves):

$$\begin{aligned} & - \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\ & \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} - \\ & \frac{5 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\ & \frac{5 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{a \operatorname{Tan}[c+d x]^4}{4 d} \end{aligned}$$

Problem 855: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sin}[c+d x]) \operatorname{Tan}[c+d x]^2 dx$$

Optimal (type 3, 84 leaves, 5 steps):

$$\frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{a^3}{8 d (a-a \operatorname{Sin}[c+d x])^2} - \frac{a^2}{4 d (a-a \operatorname{Sin}[c+d x])} - \frac{a^2}{8 d (a+a \operatorname{Sin}[c+d x])}$$

Result (type 3, 207 leaves):

$$\begin{aligned} & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} - \\ & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} - \\ & \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\ & \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{a \operatorname{Tan}[c+d x]^4}{4 d} \end{aligned}$$

Problem 856: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^4 (a+a \sin [c+d x]) \tan [c+d x] d x$$

Optimal (type 3, 61 leaves, 5 steps):

$$-\frac{a \operatorname{ArcTanh}[\sin [c+d x]]}{8 d} + \frac{a^3}{8 d (a-a \sin [c+d x])^2} + \frac{a^2}{8 d (a+a \sin [c+d x])}$$

Result (type 3, 207 leaves):

$$\frac{a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} - \frac{a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a \sec [c+d x]^4}{4 d} + \frac{a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}$$

Problem 857: Result more than twice size of optimal antiderivative.

$$\int \csc [c+d x] \sec [c+d x]^5 (a+a \sin [c+d x]) d x$$

Optimal (type 3, 117 leaves, 4 steps):

$$-\frac{11 a \operatorname{Log}[1-\sin [c+d x]]}{16 d} + \frac{a \operatorname{Log}[\sin [c+d x]]}{d} - \frac{5 a \operatorname{Log}[1+\sin [c+d x]]}{16 d} + \frac{a^3}{8 d (a-a \sin [c+d x])^2} + \frac{a^2}{2 d (a-a \sin [c+d x])} + \frac{a^2}{8 d (a+a \sin [c+d x])}$$

Result (type 3, 248 leaves):

$$-\frac{a \operatorname{Log}[\cos [c+d x]]}{d} - \frac{3 a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{3 a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a \operatorname{Log}[\sin [c+d x]]}{d} + \frac{a \sec [c+d x]^2}{2 d} + \frac{a \sec [c+d x]^4}{4 d} + \frac{a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{3 a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{3 a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{3 a}{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}$$

Problem 858: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^2 \text{Sec}[c + dx]^5 (a + a \text{Sin}[c + dx]) dx$$

Optimal (type 3, 129 leaves, 4 steps):

$$\begin{aligned} & -\frac{a \text{Csc}[c + dx]}{d} - \frac{23 a \text{Log}[1 - \text{Sin}[c + dx]]}{16 d} + \frac{a \text{Log}[\text{Sin}[c + dx]]}{d} + \frac{7 a \text{Log}[1 + \text{Sin}[c + dx]]}{16 d} + \\ & \frac{a^3}{8 d (a - a \text{Sin}[c + dx])^2} + \frac{3 a^2}{4 d (a - a \text{Sin}[c + dx])} - \frac{a^2}{8 d (a + a \text{Sin}[c + dx])} \end{aligned}$$

Result (type 3, 284 leaves):

$$\begin{aligned} & -\frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{2 d} - \frac{a \text{Log}[\text{Cos}[c + dx]]}{d} - \frac{15 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} + \\ & \frac{15 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} + \frac{a \text{Log}[\text{Sin}[c + dx]]}{d} + \\ & \frac{a \text{Sec}[c + dx]^2}{2 d} + \frac{a \text{Sec}[c + dx]^4}{4 d} + \frac{a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\ & \frac{7 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} - \\ & \frac{7 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{a \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{2 d} \end{aligned}$$

Problem 859: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^3 \text{Sec}[c + dx]^5 (a + a \text{Sin}[c + dx]) dx$$

Optimal (type 3, 143 leaves, 4 steps):

$$\begin{aligned} & -\frac{a \text{Csc}[c + dx]}{d} - \frac{a \text{Csc}[c + dx]^2}{2 d} - \frac{39 a \text{Log}[1 - \text{Sin}[c + dx]]}{16 d} + \frac{3 a \text{Log}[\text{Sin}[c + dx]]}{d} - \\ & \frac{9 a \text{Log}[1 + \text{Sin}[c + dx]]}{16 d} + \frac{a^3}{8 d (a - a \text{Sin}[c + dx])^2} + \frac{a^2}{d (a - a \text{Sin}[c + dx])} + \frac{a^2}{8 d (a + a \text{Sin}[c + dx])} \end{aligned}$$

Result (type 3, 298 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{2d} - \frac{a \operatorname{Csc}[c+dx]^2}{2d} - \\
 & \frac{3a \operatorname{Log}[\operatorname{Cos}[c+dx]]}{d} - \frac{15a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{15a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{3a \operatorname{Log}[\operatorname{Sin}[c+dx]]}{d} + \\
 & \frac{a \operatorname{Sec}[c+dx]^2}{d} + \frac{a \operatorname{Sec}[c+dx]^4}{4d} + \frac{a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \\
 & \frac{7a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\
 & \frac{7a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d}
 \end{aligned}$$

Problem 860: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^4 \operatorname{Sec}[c+dx]^5 (a+a \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 162 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{3a \operatorname{Csc}[c+dx]}{d} - \frac{a \operatorname{Csc}[c+dx]^2}{2d} - \frac{a \operatorname{Csc}[c+dx]^3}{3d} - \\
 & \frac{59a \operatorname{Log}[1 - \operatorname{Sin}[c+dx]]}{16d} + \frac{3a \operatorname{Log}[\operatorname{Sin}[c+dx]]}{d} + \frac{11a \operatorname{Log}[1 + \operatorname{Sin}[c+dx]]}{16d} + \\
 & \frac{8d(a - a \operatorname{Sin}[c+dx])^2}{a^3} + \frac{4d(a - a \operatorname{Sin}[c+dx])}{5a^2} - \frac{8d(a + a \operatorname{Sin}[c+dx])}{a^2}
 \end{aligned}$$

Result (type 3, 358 leaves):

$$\begin{aligned}
 & - \frac{19 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{12 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 d} - \frac{a \operatorname{Csc}[c+d x]^2}{2 d} - \\
 & \frac{3 a \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d} - \frac{35 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\
 & \frac{35 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{3 a \operatorname{Log}[\operatorname{Sin}[c+d x]]}{d} + \\
 & \frac{a \operatorname{Sec}[c+d x]^2}{d} + \frac{a \operatorname{Sec}[c+d x]^4}{4 d} + \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\
 & \frac{11 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
 & \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{11 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
 & \frac{19 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{12 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 d}
 \end{aligned}$$

Problem 863: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^2 (a+a \operatorname{Sin}[c+d x])^2 \operatorname{Tan}[c+d x]^3 dx$$

Optimal (type 3, 87 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{7 a^2 \operatorname{Log}[1-\operatorname{Sin}[c+d x]]}{8 d} - \frac{a^2 \operatorname{Log}[1+\operatorname{Sin}[c+d x]]}{8 d} + \\
 & \frac{4 d(a-a \operatorname{Sin}[c+d x])^2}{a^4} - \frac{5 a^3}{4 d(a-a \operatorname{Sin}[c+d x])}
 \end{aligned}$$

Result (type 3, 270 leaves):

$$\begin{aligned}
 & - \frac{a^2 \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d} - \frac{3 a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{4 d} + \\
 & \frac{3 a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{4 d} - \frac{a^2 \operatorname{Sec}[c+d x]^2}{d} + \\
 & \frac{a^2 \operatorname{Sec}[c+d x]^4}{4 d} + \frac{a^2}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} - \\
 & \frac{a^2}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a^2}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\
 & \frac{5 a^2}{8 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{a^2 \operatorname{Tan}[c+d x]^4}{4 d}
 \end{aligned}$$

Problem 869: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c+dx]^4 \text{Sec}[c+dx]^5 (a+a \sin[c+dx])^2 dx$$

Optimal (type 3, 150 leaves, 4 steps):

$$\begin{aligned} & -\frac{4 a^2 \text{Csc}[c+dx]}{d} - \frac{a^2 \text{Csc}[c+dx]^2}{d} - \frac{a^2 \text{Csc}[c+dx]^3}{3 d} - \frac{49 a^2 \text{Log}[1-\text{Sin}[c+dx]]}{8 d} + \\ & \frac{6 a^2 \text{Log}[\text{Sin}[c+dx]]}{d} + \frac{a^2 \text{Log}[1+\text{Sin}[c+dx]]}{8 d} + \frac{a^4}{4 d (a-a \text{Sin}[c+dx])^2} + \frac{9 a^3}{4 d (a-a \text{Sin}[c+dx])} \end{aligned}$$

Result (type 3, 652 leaves):

$$\begin{aligned} & \frac{25 \text{Cot}\left[\frac{1}{2}(c+dx)\right] (a+a \text{Sin}[c+dx])^2}{12 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \frac{\text{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \text{Sin}[c+dx])^2}{4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} \\ & \frac{\text{Cot}\left[\frac{1}{2}(c+dx)\right] \text{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \text{Sin}[c+dx])^2}{24 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\ & \frac{49 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right] - \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+a \text{Sin}[c+dx])^2}{4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \\ & \frac{\text{Log}\left[\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+a \text{Sin}[c+dx])^2}{4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \\ & \frac{6 \text{Log}[\text{Sin}[c+dx]] (a+a \text{Sin}[c+dx])^2}{d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\ & \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \text{Sin}[c+dx])^2}{4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + (a+a \text{Sin}[c+dx])^2 / \\ & \left(4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] - \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4 \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4\right) + \\ & \left(9 (a+a \text{Sin}[c+dx])^2\right) / \\ & \left(4 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] - \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2 \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4\right) - \\ & \frac{25 (a+a \text{Sin}[c+dx])^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{12 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\ & \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a+a \text{Sin}[c+dx])^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{24 d \left(\text{Cos}\left[\frac{1}{2}(c+dx)\right] + \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} \end{aligned}$$

Problem 882: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^7}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 130 leaves, 8 steps):

$$\begin{aligned} & -\frac{35 \operatorname{ArcTanh}[\sin [c+d x]]}{128 a d} + \frac{35 \sec [c+d x] \tan [c+d x]}{128 a d} - \frac{35 \sec [c+d x] \tan [c+d x]^3}{192 a d} + \\ & \frac{7 \sec [c+d x] \tan [c+d x]^5}{48 a d} - \frac{\sec [c+d x] \tan [c+d x]^7}{8 a d} + \frac{\tan [c+d x]^8}{8 a d} \end{aligned}$$

Result (type 3, 342 leaves):

$$\begin{aligned} & \frac{1}{384 d (a+a \sin [c+d x])} \left(-192 + \frac{6}{\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^6} - \right. \\ & \frac{40}{\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{114}{\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} + \\ & 105 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2 - \\ & 105 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2 + \\ & \frac{4\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^6} - \frac{27\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} + \\ & \left. \frac{87\left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} \right) \end{aligned}$$

Problem 883: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x] \tan [c+d x]^6}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 134 leaves, 8 steps):

$$\begin{aligned} & -\frac{5 \operatorname{ArcTanh}[\sin [c+d x]]}{128 a d} - \frac{5 \sec [c+d x] \tan [c+d x]}{128 a d} + \frac{5 \sec [c+d x]^3 \tan [c+d x]}{64 a d} - \\ & \frac{5 \sec [c+d x]^3 \tan [c+d x]^3}{48 a d} + \frac{\sec [c+d x]^3 \tan [c+d x]^5}{8 a d} - \frac{\tan [c+d x]^8}{8 a d} \end{aligned}$$

Result (type 3, 342 leaves):

$$\frac{1}{384 d (a + a \sin [c + d x])} \left(60 - \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \right. \\ \left. \frac{32}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{66}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} + \right. \\ 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \\ 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \\ 4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \frac{21 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{21 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\ \left. \frac{45 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 884: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^2 \tan [c + d x]^5}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 152 leaves, 9 steps):

$$\frac{5 \operatorname{ArcTanh}[\sin [c + d x]]}{128 a d} + \frac{5 \sec [c + d x] \tan [c + d x]}{128 a d} - \frac{5 \sec [c + d x]^3 \tan [c + d x]}{64 a d} + \\ \frac{5 \sec [c + d x]^3 \tan [c + d x]^3}{48 a d} - \frac{\sec [c + d x]^3 \tan [c + d x]^5}{8 a d} + \frac{\tan [c + d x]^6}{6 a d} + \frac{\tan [c + d x]^8}{8 a d}$$

Result (type 3, 340 leaves):

$$\begin{aligned}
 & \frac{1}{384 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} \\
 & \left(6 - 24 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \right. \\
 & 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 + \\
 & 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 + \\
 & \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\
 & \left. \frac{15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)
 \end{aligned}$$

Problem 885: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^3 \tan [c + d x]^4}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 150 leaves, 9 steps):

$$\frac{3 \operatorname{ArcTanh}[\sin [c + d x]]}{128 a d} + \frac{3 \sec [c + d x] \tan [c + d x]}{128 a d} + \frac{\sec [c + d x]^3 \tan [c + d x]}{64 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]}{16 a d} + \frac{\sec [c + d x]^5 \tan [c + d x]^3}{8 a d} - \frac{\tan [c + d x]^6}{6 a d} - \frac{\tan [c + d x]^8}{8 a d}$$

Result (type 3, 342 leaves):

$$\begin{aligned}
 & - \frac{1}{384 d (a + a \sin [c + d x])} \left(12 + \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \right. \\
 & \quad \frac{16}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} + \\
 & \quad 9 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \\
 & \quad 9 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - \\
 & \quad \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \quad \left. \frac{9 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)
 \end{aligned}$$

Problem 886: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^4 \tan [c + d x]^3}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 150 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{3 \operatorname{ArcTanh}[\sin [c + d x]]}{128 a d} - \frac{\sec [c + d x]^6}{6 a d} + \frac{\sec [c + d x]^8}{8 a d} - \frac{3 \sec [c + d x] \tan [c + d x]}{128 a d} - \\
 & \frac{\sec [c + d x]^3 \tan [c + d x]}{64 a d} + \frac{\sec [c + d x]^5 \tan [c + d x]}{16 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]^3}{8 a d}
 \end{aligned}$$

Result (type 3, 340 leaves):

$$\frac{1}{384 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} \left(-6 + 8 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 6 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - 9 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 + 9 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 - \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{9 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 887: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^5 \tan [c + d x]^2}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 148 leaves, 9 steps):

$$\frac{5 \operatorname{ArcTanh}[\sin [c + d x]]}{128 a d} + \frac{\sec [c + d x]^6}{6 a d} - \frac{\sec [c + d x]^8}{8 a d} - \frac{5 \sec [c + d x] \tan [c + d x]}{128 a d} - \frac{5 \sec [c + d x]^3 \tan [c + d x]}{192 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]}{48 a d} + \frac{\sec [c + d x]^7 \tan [c + d x]}{8 a d}$$

Result (type 3, 317 leaves):

$$\frac{1}{384 d (a + a \sin [c + d x])} \left(12 - \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} + 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - 15 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 888: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^6 \text{Tan}[c + dx]}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 130 leaves, 8 steps):

$$\frac{5 \text{ArcTanh}[\text{Sin}[c + dx]]}{128 a d} + \frac{\text{Sec}[c + dx]^8}{8 a d} + \frac{5 \text{Sec}[c + dx] \text{Tan}[c + dx]}{128 a d} +$$

$$\frac{5 \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{192 a d} + \frac{\text{Sec}[c + dx]^5 \text{Tan}[c + dx]}{48 a d} - \frac{\text{Sec}[c + dx]^7 \text{Tan}[c + dx]}{8 a d}$$

Result (type 3, 340 leaves):

$$\frac{1}{384 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6 (a + a \text{Sin}[c + dx])}$$

$$\left(6 + 8 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 + 6 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 - \right.$$

$$15 \text{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 +$$

$$15 \text{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 +$$

$$\frac{4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8}{\left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^6} + \frac{9 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8}{\left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^4} +$$

$$\left. \frac{15 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8}{\left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^2} \right)$$

Problem 889: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^7}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 165 leaves, 4 steps):

$$\frac{35 \text{ArcTanh}[\text{Sin}[c + dx]]}{128 a d} + \frac{a^2}{96 d (a - a \text{Sin}[c + dx])^3} +$$

$$\frac{5 a}{128 d (a - a \text{Sin}[c + dx])^2} + \frac{15}{128 d (a - a \text{Sin}[c + dx])} - \frac{a^3}{64 d (a + a \text{Sin}[c + dx])^4} -$$

$$\frac{a^2}{24 d (a + a \text{Sin}[c + dx])^3} - \frac{5 a}{64 d (a + a \text{Sin}[c + dx])^2} - \frac{5}{32 d (a + a \text{Sin}[c + dx])}$$

Result (type 3, 342 leaves):

$$\frac{1}{384 d (a + a \sin [c + d x])} \left(-60 - \frac{6}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{16}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{30}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} - 105 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 105 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{45 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 891: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c + d x]^2 \sec [c + d x]^7}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 217 leaves, 4 steps):

$$\frac{\csc [c + d x]}{a d} - \frac{187 \log [1 - \sin [c + d x]]}{256 a d} - \frac{\log [\sin [c + d x]]}{a d} + \frac{443 \log [1 + \sin [c + d x]]}{256 a d} + \frac{a^2}{96 d (a - a \sin [c + d x])^3} + \frac{9 a}{128 d (a - a \sin [c + d x])^2} + \frac{47}{128 d (a - a \sin [c + d x])} - \frac{a^3}{64 d (a + a \sin [c + d x])^4} - \frac{a^2}{12 d (a + a \sin [c + d x])^3} - \frac{19 a}{64 d (a + a \sin [c + d x])^2} - \frac{35}{32 d (a + a \sin [c + d x])}$$

Result (type 3, 628 leaves):

$$\begin{aligned}
 & \frac{35}{32 d (a + a \sin [c + d x])} - \frac{1}{64 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} \\
 & \frac{1}{12 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 (a + a \sin [c + d x])} \\
 & \frac{19}{64 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 (a + a \sin [c + d x])} \\
 & \frac{\cot \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{2 d (a + a \sin [c + d x])} \\
 & \left(187 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) / \\
 & (128 d (a + a \sin [c + d x])) + \\
 & \left(443 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) / \\
 & (128 d (a + a \sin [c + d x])) - \frac{\log [\sin [c + d x]] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{d (a + a \sin [c + d x])} + \\
 & \frac{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{96 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} + \\
 & \frac{9 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{128 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 (a + a \sin [c + d x])} + \\
 & \frac{47 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{128 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 (a + a \sin [c + d x])} \\
 & \frac{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \tan \left[\frac{1}{2} (c + d x) \right]}{2 d (a + a \sin [c + d x])}
 \end{aligned}$$

Problem 892: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c + d x]^3 \sec [c + d x]^7}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 232 leaves, 4 steps):

$$\begin{aligned} & \frac{\text{Csc}[c + d x]}{a d} - \frac{\text{Csc}[c + d x]^2}{2 a d} - \frac{325 \text{Log}[1 - \text{Sin}[c + d x]]}{256 a d} + \\ & \frac{5 \text{Log}[\text{Sin}[c + d x]]}{a d} - \frac{955 \text{Log}[1 + \text{Sin}[c + d x]]}{256 a d} + \frac{a^2}{96 d (a - a \text{Sin}[c + d x])^3} + \\ & \frac{11 a}{128 d (a - a \text{Sin}[c + d x])^2} + \frac{69}{128 d (a - a \text{Sin}[c + d x])} + \frac{a^3}{64 d (a + a \text{Sin}[c + d x])^4} + \\ & \frac{5 a^2}{48 d (a + a \text{Sin}[c + d x])^3} + \frac{29 a}{64 d (a + a \text{Sin}[c + d x])^2} + \frac{2}{d (a + a \text{Sin}[c + d x])} \end{aligned}$$

Result(type 3, 734 leaves):

$$\begin{aligned}
 & \frac{2}{d (a + a \sin[c + d x])} + \frac{1}{64 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} + \\
 & \frac{48 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])}{5} + \\
 & \frac{64 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])}{29} + \\
 & \frac{\cot\left[\frac{1}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{2 d (a + a \sin[c + d x])} - \\
 & \frac{\csc\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{8 d (a + a \sin[c + d x])} - \\
 & \left(325 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (128 d (a + a \sin[c + d x])) - \\
 & \left(955 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (128 d (a + a \sin[c + d x])) + \frac{5 \log[\sin[c + d x]] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{d (a + a \sin[c + d x])} - \\
 & \frac{\sec\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{8 d (a + a \sin[c + d x])} + \\
 & \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{96 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} + \\
 & \frac{11 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])} + \\
 & \frac{69 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])} + \\
 & \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \tan\left[\frac{1}{2}(c + d x)\right]}{2 d (a + a \sin[c + d x])}
 \end{aligned}$$

Problem 893: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc[c + d x]^4 \sec[c + d x]^7}{a + a \sin[c + d x]} dx$$

Optimal (type 3, 253 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{5 \operatorname{Csc}[c + d x]}{a d} + \frac{\operatorname{Csc}[c + d x]^2}{2 a d} - \frac{\operatorname{Csc}[c + d x]^3}{3 a d} - \frac{515 \operatorname{Log}[1 - \operatorname{Sin}[c + d x]]}{256 a d} - \\
 & \frac{5 \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a d} + \frac{1795 \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{256 a d} + \frac{a^2}{96 d (a - a \operatorname{Sin}[c + d x])^3} + \\
 & \frac{13 a}{128 d (a - a \operatorname{Sin}[c + d x])^2} + \frac{95}{128 d (a - a \operatorname{Sin}[c + d x])} - \frac{a^3}{64 d (a + a \operatorname{Sin}[c + d x])^4} - \\
 & \frac{a^2}{8 d (a + a \operatorname{Sin}[c + d x])^3} - \frac{41 a}{64 d (a + a \operatorname{Sin}[c + d x])^2} - \frac{105}{32 d (a + a \operatorname{Sin}[c + d x])}
 \end{aligned}$$

Result(type 3, 864 leaves):

105

1

$$\begin{aligned}
 & \frac{32 d (a + a \sin[c + d x])}{1} - \frac{64 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])}{1} \\
 & \frac{8 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])}{41} - \\
 & \frac{64 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])}{1} - \\
 & \frac{31 \cot\left[\frac{1}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{12 d (a + a \sin[c + d x])} + \\
 & \frac{\csc\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{8 d (a + a \sin[c + d x])} - \\
 & \left(\cot\left[\frac{1}{2}(c + d x)\right] \csc\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (24 d (a + a \sin[c + d x])) - \\
 & \left(515 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (128 d (a + a \sin[c + d x])) + \\
 & \left(1795 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (128 d (a + a \sin[c + d x])) - \frac{5 \log[\sin[c + d x]] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{d (a + a \sin[c + d x])} + \\
 & \frac{\sec\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{8 d (a + a \sin[c + d x])} + \\
 & \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{1} + \\
 & \frac{96 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])}{13 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2} + \\
 & \frac{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])}{95 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2} - \\
 & \frac{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])}{1} - \\
 & \frac{31 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \tan\left[\frac{1}{2}(c + d x)\right]}{12 d (a + a \sin[c + d x])} - \\
 & \left(\sec\left[\frac{1}{2}(c + d x)\right]^2 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \tan\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & (24 d (a + a \sin[c + d x]))
 \end{aligned}$$

Problem 897: Result more than twice size of optimal antiderivative.

$$\int \frac{\sin [c+d x] \tan [c+d x]^9}{a+a \sin [c+d x]} d x$$

Optimal (type 3, 233 leaves, 4 steps):

$$\begin{aligned} & - \frac{193 \operatorname{Log}[1-\sin [c+d x]]}{512 a d} - \frac{319 \operatorname{Log}[1+\sin [c+d x]]}{512 a d} + \\ & \frac{81 a}{256 d (a-a \sin [c+d x])^4} - \frac{192 d (a-a \sin [c+d x])^3}{61 a^4} + \frac{512 d (a-a \sin [c+d x])^2}{128 d (a-a \sin [c+d x])} - \frac{15 a^3}{160 d (a+a \sin [c+d x])^5} + \frac{384 d (a+a \sin [c+d x])^3}{95 a^2} + \frac{325 a}{512 d (a+a \sin [c+d x])^2} - \frac{315}{256 d (a+a \sin [c+d x])} \end{aligned}$$

Result (type 3, 586 leaves):

$$\begin{aligned}
 & - \frac{315}{256 d (a + a \sin[c + d x])} - \frac{1}{160 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^8 (a + a \sin[c + d x])} + \\
 & \frac{15}{256 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} - \\
 & \frac{95}{384 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])} + \\
 & \frac{325}{512 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])} - \\
 & \left(193 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (256 d (a + a \sin[c + d x])) - \\
 & \left(319 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
 & (256 d (a + a \sin[c + d x])) + \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{256 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^8 (a + a \sin[c + d x])} - \\
 & \frac{7 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{192 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} + \\
 & \frac{81 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{512 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])} - \\
 & \frac{61 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])}
 \end{aligned}$$

Problem 898: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan[c + d x]^9}{a + a \sin[c + d x]} dx$$

Optimal (type 3, 154 leaves, 9 steps):

$$\begin{aligned}
 & \frac{63 \operatorname{ArcTanh}[\sin[c + d x]]}{256 a d} - \frac{63 \operatorname{Sec}[c + d x] \tan[c + d x]}{256 a d} + \\
 & \frac{21 \operatorname{Sec}[c + d x] \tan[c + d x]^3}{128 a d} - \frac{21 \operatorname{Sec}[c + d x] \tan[c + d x]^5}{160 a d} + \\
 & \frac{9 \operatorname{Sec}[c + d x] \tan[c + d x]^7}{80 a d} - \frac{\operatorname{Sec}[c + d x] \tan[c + d x]^9}{10 a d} + \frac{\tan[c + d x]^{10}}{10 a d}
 \end{aligned}$$

Result (type 3, 417 leaves):

$$\frac{1}{2560 d (a + a \sin [c + d x])} \left(\frac{1280 + \frac{16}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^8} - \frac{130}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^6} + \frac{460}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{935}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} - 630 \log \left[\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right] \right] \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2 + 630 \log \left[\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right] \right] \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2 + \frac{10 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^8} - \frac{80 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^6} + \frac{285 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{650 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} \right)$$

Problem 899: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x] \tan [c + d x]^8}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 160 leaves, 9 steps):

$$\frac{7 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} + \frac{7 \sec [c + d x] \tan [c + d x]}{256 a d} - \frac{7 \sec [c + d x]^3 \tan [c + d x]}{128 a d} + \frac{7 \sec [c + d x]^3 \tan [c + d x]^3}{96 a d} - \frac{7 \sec [c + d x]^3 \tan [c + d x]^5}{80 a d} + \frac{\sec [c + d x]^3 \tan [c + d x]^7}{10 a d} - \frac{\tan [c + d x]^{10}}{10 a d}$$

Result (type 3, 417 leaves):

$$\frac{1}{7680 d (a + a \sin [c + d x])} \left(-1050 - \frac{48}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} + \frac{330}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{940}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{1395}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} - 210 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 210 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} - \frac{200 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{555 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{840 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 900: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^2 \tan [c + d x]^7}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 178 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{7 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} - \frac{7 \sec [c + d x] \tan [c + d x]}{256 a d} + \\
 & \frac{7 \sec [c + d x]^3 \tan [c + d x]}{128 a d} - \frac{7 \sec [c + d x]^3 \tan [c + d x]^3}{96 a d} + \\
 & \frac{7 \sec [c + d x]^3 \tan [c + d x]^5}{80 a d} - \frac{\sec [c + d x]^3 \tan [c + d x]^7}{10 a d} + \frac{\tan [c + d x]^8}{8 a d} + \frac{\tan [c + d x]^{10}}{10 a d}
 \end{aligned}$$

Result (type 3, 415 leaves):

$$\frac{1}{7680 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x]) \left(48 - 270 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 580 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - 525 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 + 210 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} - 210 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \frac{30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} - \frac{160 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{315 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{210 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 901: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^3 \tan [c + d x]^6}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 176 leaves, 10 steps):

$$\frac{3 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} - \frac{3 \sec [c + d x] \tan [c + d x]}{256 a d} - \frac{\sec [c + d x]^3 \tan [c + d x]}{128 a d} + \frac{\sec [c + d x]^5 \tan [c + d x]}{32 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]^3}{16 a d} + \frac{\sec [c + d x]^5 \tan [c + d x]^5}{10 a d} - \frac{\tan [c + d x]^8}{8 a d} - \frac{\tan [c + d x]^{10}}{10 a d}$$

Result (type 3, 417 leaves):

$$\frac{1}{2560 d (a + a \sin [c + d x])} \left(50 - \frac{16}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} + \frac{70}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} - \frac{100}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{25}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} + 30 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - 30 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{10 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} - \frac{40 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{45 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{20 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 902: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^4 \tan [c + d x]^5}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 194 leaves, 11 steps):

$$\frac{3 \operatorname{ArcTanh} [\sin [c + d x]]}{256 a d} + \frac{\sec [c + d x]^6}{6 a d} - \frac{\sec [c + d x]^8}{4 a d} + \frac{\sec [c + d x]^{10}}{10 a d} + \frac{3 \sec [c + d x] \tan [c + d x]}{256 a d} + \frac{\sec [c + d x]^3 \tan [c + d x]}{128 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]}{32 a d} + \frac{\sec [c + d x]^5 \tan [c + d x]^3}{16 a d} - \frac{\sec [c + d x]^5 \tan [c + d x]^5}{10 a d}$$

Result (type 3, 415 leaves):

$$\begin{aligned}
 & \frac{1}{7680 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x])} \\
 & \left(48 - 150 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \\
 & 100 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 + 75 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 - \\
 & 90 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \\
 & 90 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \\
 & \frac{30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} - \frac{80 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \left. \frac{15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{90 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)
 \end{aligned}$$

Problem 904: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^6 \tan [c + d x]^3}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 174 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{3 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} - \frac{\sec [c + d x]^8}{8 a d} + \frac{\sec [c + d x]^{10}}{10 a d} - \\
 & \frac{3 \sec [c + d x] \tan [c + d x]}{256 a d} - \frac{\sec [c + d x]^3 \tan [c + d x]}{128 a d} - \\
 & \frac{\sec [c + d x]^5 \tan [c + d x]}{160 a d} + \frac{3 \sec [c + d x]^7 \tan [c + d x]}{80 a d} - \frac{\sec [c + d x]^7 \tan [c + d x]^3}{10 a d}
 \end{aligned}$$

Result (type 3, 365 leaves):

$$\begin{aligned}
 & \frac{1}{2560 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x])} \\
 & \left(-16 + 10 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \\
 & 20 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 + 15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 - \\
 & 30 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \\
 & 30 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} - \\
 & \frac{10 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} + \\
 & \left. \frac{15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)
 \end{aligned}$$

Problem 905: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^7 \tan [c + d x]^2}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 172 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{7 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} + \frac{\sec [c + d x]^8}{8 a d} - \frac{\sec [c + d x]^{10}}{10 a d} - \\
 & \frac{7 \sec [c + d x] \tan [c + d x]}{256 a d} - \frac{7 \sec [c + d x]^3 \tan [c + d x]}{384 a d} - \\
 & \frac{7 \sec [c + d x]^5 \tan [c + d x]}{480 a d} - \frac{\sec [c + d x]^7 \tan [c + d x]}{80 a d} + \frac{\sec [c + d x]^9 \tan [c + d x]}{10 a d}
 \end{aligned}$$

Result (type 3, 417 leaves):

$$\frac{1}{7680 d (a + a \sin [c + d x])} \left(\frac{150 - \frac{48}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^8} - \frac{30}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^6} + \frac{20}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{75}{\left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} + 210 \log \left[\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right] \right] \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2 - 210 \log \left[\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right] \right] \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2 + \frac{30 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^8} + \frac{40 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^6} - \frac{15 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{60 \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} \right)$$

Problem 906: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^8 \tan [c + d x]}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 154 leaves, 9 steps):

$$\frac{7 \operatorname{ArcTanh}[\sin [c + d x]]}{256 a d} + \frac{\sec [c + d x]^{10}}{10 a d} + \frac{7 \sec [c + d x] \tan [c + d x]}{256 a d} + \frac{7 \sec [c + d x]^3 \tan [c + d x]}{384 a d} + \frac{7 \sec [c + d x]^5 \tan [c + d x]}{480 a d} + \frac{\sec [c + d x]^7 \tan [c + d x]}{80 a d} - \frac{\sec [c + d x]^9 \tan [c + d x]}{10 a d}$$

Result (type 3, 415 leaves):

$$\begin{aligned}
 & \frac{1}{7680 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x])} \\
 & \left(48 + 90 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \\
 & 100 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 + 75 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 - \\
 & 210 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \\
 & 210 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10} + \\
 & \frac{30 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} + \frac{80 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
 & \left. \frac{135 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{210 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^{10}}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)
 \end{aligned}$$

Problem 909: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c + d x]^2 \operatorname{Sec}[c + d x]^9}{a + a \sin [c + d x]} dx$$

Optimal (type 3, 262 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{\operatorname{Csc}[c + d x]}{a d} - \frac{437 \operatorname{Log}[1 - \sin [c + d x]]}{512 a d} - \frac{\operatorname{Log}[\sin [c + d x]]}{a d} + \frac{949 \operatorname{Log}[1 + \sin [c + d x]]}{512 a d} + \\
 & \frac{256 d (a - a \sin [c + d x])^4}{61} + \frac{5 a^2}{192 d (a - a \sin [c + d x])^3} + \frac{57 a}{512 d (a - a \sin [c + d x])^2} + \\
 & \frac{128 d (a - a \sin [c + d x])}{47 a^2} - \frac{160 d (a + a \sin [c + d x])^5}{187 a} - \frac{256 d (a + a \sin [c + d x])^4}{315} - \\
 & \frac{384 d (a + a \sin [c + d x])^3}{512 d (a + a \sin [c + d x])^2} - \frac{256 d (a + a \sin [c + d x])}{256 d (a + a \sin [c + d x])}
 \end{aligned}$$

Result (type 3, 737 leaves):

$$\begin{aligned}
& - \frac{315}{256 d (a + a \sin[c + d x])} - \frac{1}{160 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^8 (a + a \sin[c + d x])} - \\
& \frac{9}{256 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} - \\
& \frac{47}{384 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])} - \\
& \frac{187}{512 d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])} - \\
& \frac{\cot\left[\frac{1}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{2 d (a + a \sin[c + d x])} - \\
& \left(437 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
& (256 d (a + a \sin[c + d x])) + \\
& \left(949 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) / \\
& (256 d (a + a \sin[c + d x])) - \frac{\log[\sin[c + d x]] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{d (a + a \sin[c + d x])} + \\
& \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{256 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^8 (a + a \sin[c + d x])} + \\
& \frac{5 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{192 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^6 (a + a \sin[c + d x])} + \\
& \frac{57 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{512 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 (a + a \sin[c + d x])} + \\
& \frac{61 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2}{128 d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 (a + a \sin[c + d x])} - \\
& \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \tan\left[\frac{1}{2}(c + d x)\right]}{2 d (a + a \sin[c + d x])}
\end{aligned}$$

Problem 910: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc[c + d x]^3 \sec[c + d x]^9}{a + a \sin[c + d x]} dx$$

Optimal (type 3, 279 leaves, 4 steps):

$$\begin{aligned}
 & \frac{\text{Csc}[c + d x]}{a d} - \frac{\text{Csc}[c + d x]^2}{2 a d} - \frac{843 \text{Log}[1 - \text{Sin}[c + d x]]}{512 a d} + \\
 & \frac{6 \text{Log}[\text{Sin}[c + d x]]}{a d} - \frac{2229 \text{Log}[1 + \text{Sin}[c + d x]]}{512 a d} + \frac{a^3}{256 d (a - a \text{Sin}[c + d x])^4} + \\
 & \frac{a^2}{32 d (a - a \text{Sin}[c + d x])^3} + \frac{81 a}{512 d (a - a \text{Sin}[c + d x])^2} + \frac{203}{256 d (a - a \text{Sin}[c + d x])} + \\
 & \frac{a^4}{160 d (a + a \text{Sin}[c + d x])^5} + \frac{11 a^3}{256 d (a + a \text{Sin}[c + d x])^4} + \\
 & \frac{23 a^2}{128 d (a + a \text{Sin}[c + d x])^3} + \frac{325 a}{512 d (a + a \text{Sin}[c + d x])^2} + \frac{5}{2 d (a + a \text{Sin}[c + d x])}
 \end{aligned}$$

Result (type 3, 845 leaves):

$$\begin{aligned}
& \frac{5}{2 d (a + a \sin [c + d x])} + \frac{1}{160 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x])} + \\
& \frac{11}{256 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} + \\
& \frac{23}{128 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 (a + a \sin [c + d x])} + \\
& \frac{325}{512 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 (a + a \sin [c + d x])} + \\
& \frac{\cot \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{2 d (a + a \sin [c + d x])} - \\
& \frac{\csc \left[\frac{1}{2} (c + d x) \right]^2 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{8 d (a + a \sin [c + d x])} - \\
& \left(843 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) / \\
& (256 d (a + a \sin [c + d x])) - \\
& \left(2229 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) / \\
& (256 d (a + a \sin [c + d x])) + \frac{6 \log [\sin [c + d x]] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{d (a + a \sin [c + d x])} - \\
& \frac{\sec \left[\frac{1}{2} (c + d x) \right]^2 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{8 d (a + a \sin [c + d x])} + \\
& \frac{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{256 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 (a + a \sin [c + d x])} + \\
& \frac{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{32 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 (a + a \sin [c + d x])} + \\
& \frac{81 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{512 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 (a + a \sin [c + d x])} + \\
& \frac{203 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{256 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 (a + a \sin [c + d x])} + \\
& \frac{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \tan \left[\frac{1}{2} (c + d x) \right]}{2 d (a + a \sin [c + d x])}
\end{aligned}$$

Problem 911: Result more than twice size of optimal antiderivative.

$$\int (g \operatorname{Sec}[e + f x])^p (d \operatorname{Sin}[e + f x])^n (a + a \operatorname{Sin}[e + f x])^m dx$$

Optimal (type 6, 127 leaves, 5 steps):

$$\frac{1}{d f (1+n)} \operatorname{AppellF1}\left[1+n, \frac{1+p}{2}, \frac{1}{2}(1-2m+p), 2+n, \operatorname{Sin}[e+fx], -\operatorname{Sin}[e+fx]\right]$$

$$\operatorname{Sec}[e+fx] (g \operatorname{Sec}[e+fx])^p (1-\operatorname{Sin}[e+fx])^{\frac{1+p}{2}}$$

$$(d \operatorname{Sin}[e+fx])^{1+n} (1+\operatorname{Sin}[e+fx])^{\frac{1}{2}(1-2m+p)} (a+a \operatorname{Sin}[e+fx])^m$$

Result (type 6, 3577 leaves):

$$\left((-3+p) \operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2}, -n, 1+m+n-p, \frac{3}{2}-\frac{p}{2}, \right.\right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-m}$$

$$\operatorname{Sec}[e+fx]^{-1+p} (g \operatorname{Sec}[e+fx])^p \operatorname{Sin}[e+fx]^n (d \operatorname{Sin}[e+fx])^n (a+a \operatorname{Sin}[e+fx])^m \Big/$$

$$\left(f(-1+p) \left((-3+p) \operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2}, -n, 1+m+n-p, \frac{3}{2}-\frac{p}{2}, \right.\right.\right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] +$$

$$2 \left(n \operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2}, 1-n, 1+m+n-p, \frac{5}{2}-\frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.$$

$$\left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (1+m+n-p) \operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2}, -n, 2+m+n-p, \frac{5}{2}-\frac{p}{2}, \right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right)$$

$$\left(\left(n(-3+p) \operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2}, -n, 1+m+n-p, \frac{3}{2}-\frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.\right.$$

$$\left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-m} \operatorname{Sec}[e+fx]^{-2+p} \operatorname{Sin}[e+fx]^{-1+n} \Big/$$

$$\left((-1+p) \left((-3+p) \operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2}, -n, 1+m+n-p, \frac{3}{2}-\frac{p}{2}, \right.\right.\right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] +$$

$$2 \left(n \operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2}, 1-n, 1+m+n-p, \frac{5}{2}-\frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] +$$

$$\left. (1+m+n-p) \operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2}, -n, 2+m+n-p, \frac{5}{2}-\frac{p}{2}, \right.\right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) +$$

$$\left((-3+p) \operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2}, -n, 1+m+n-p, \frac{3}{2}-\frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right.$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\left(\sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-m}\sec[efx]^p\sin[efx]^{1+n}\Big/ \\
& \left((-3+p)\operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2},-n,1+m+n-p,\frac{3}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+2\left(n\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},1-n,1+m+n-p,\frac{5}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(1+m+n-p)\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},-n,2+m+n-p,\frac{5}{2}-\frac{p}{2},\right.\right. \\
& \quad \left.\left.\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+ \\
& \left(m(-3+p)\operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2},-n,1+m+n-p,\frac{3}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\left(\sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-m}\right. \\
& \quad \left.\sec[efx]^{-1+p}\sin[efx]^n\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\Big/ \\
& \left((-1+p)\left((-3+p)\operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2},-n,1+m+n-p,\frac{3}{2}-\frac{p}{2},\right.\right.\right. \\
& \quad \left.\left.\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+2\left(n\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},1-n,1+m+n-p,\frac{5}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(1+m+n-p)\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},-n,2+m+n-p,\frac{5}{2}-\frac{p}{2},\right.\right. \\
& \quad \left.\left.\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)\right)- \\
& \left((-3+p)\left(\sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{-m}\sec[efx]^{-1+p}\sin[efx]^n\right. \\
& \quad \left(-\frac{1}{\frac{3}{2}-\frac{p}{2}}n\left(\frac{1}{2}-\frac{p}{2}\right)\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},1-n,1+m+n-p,\frac{5}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]-\frac{1}{\frac{3}{2}-\frac{p}{2}}\right. \\
& \quad \left.(1+m+n-p)\left(\frac{1}{2}-\frac{p}{2}\right)\operatorname{AppellF1}\left[\frac{3}{2}-\frac{p}{2},-n,2+m+n-p,\frac{5}{2}-\frac{p}{2},\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\sec\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\Big/ \\
& \left((-1+p)\left((-3+p)\operatorname{AppellF1}\left[\frac{1}{2}-\frac{p}{2},-n,1+m+n-p,\frac{3}{2}-\frac{p}{2},\right.\right.\right. \\
& \quad \left.\left.\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2,-\tan\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)+\right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left(n \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, 1-n, 1+m+n-p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1+m+n-p) \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, -n, 2+m+n-p, \frac{5}{2} - \frac{p}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right) + \\
 & \left((-3+p) \operatorname{AppellF1} \left[\frac{1}{2} - \frac{p}{2}, -n, 1+m+n-p, \frac{3}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \left(\operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right)^{-m} \operatorname{Sec} [e + f x]^{-1+p} \operatorname{Sin} [e + f x]^n \right. \\
 & \quad \left. 2 \left(n \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, 1-n, 1+m+n-p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] + (1+m+n-p) \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, -n, 2+m+n-p, \frac{5}{2} - \frac{p}{2}, \right. \right. \\
 & \quad \left. \left. \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right) \operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \\
 & \quad \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] + (-3+p) \left(-\frac{1}{\frac{3}{2} - \frac{p}{2}} n \left(\frac{1}{2} - \frac{p}{2} \right) \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, 1-n, \right. \right. \\
 & \quad \left. \left. 1+m+n-p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] - \frac{1}{\frac{3}{2} - \frac{p}{2}} (1+m+n-p) \right. \\
 & \quad \left. \left(\frac{1}{2} - \frac{p}{2} \right) \operatorname{AppellF1} \left[\frac{3}{2} - \frac{p}{2}, -n, 2+m+n-p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + \\
 & 2 \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \left(n \left(-\frac{1}{\frac{5}{2} - \frac{p}{2}} (1+m+n-p) \left(\frac{3}{2} - \frac{p}{2} \right) \operatorname{AppellF1} \left[\frac{5}{2} - \frac{p}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1-n, 2+m+n-p, \frac{7}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] + \frac{1}{\frac{5}{2} - \frac{p}{2}} (1-n) \left(\frac{3}{2} - \frac{p}{2} \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5}{2} - \frac{p}{2}, 2-n, 1+m+n-p, \frac{7}{2} - \frac{p}{2}, \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \operatorname{Tan} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right] \right) + \\
 & (1+m+n-p) \left(-\frac{1}{\frac{5}{2} - \frac{p}{2}} n \left(\frac{3}{2} - \frac{p}{2} \right) \operatorname{AppellF1} \left[\frac{5}{2} - \frac{p}{2}, 1-n, 2+m+n-p, \right. \right.
 \end{aligned}$$

$$\left. \left(\frac{7}{2} - \frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{\frac{5}{2} - \frac{p}{2}} (2 + m + n - p) \left(\frac{3}{2} - \frac{p}{2}\right) \operatorname{AppellF1}\left[\frac{5}{2} - \frac{p}{2}, -n, 3 + m + n - p, \frac{7}{2} - \frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) \left((-1 + p) \left((-3 + p) \operatorname{AppellF1}\left[\frac{1}{2} - \frac{p}{2}, -n, 1 + m + n - p, \frac{3}{2} - \frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + 2 \left(n \operatorname{AppellF1}\left[\frac{3}{2} - \frac{p}{2}, 1 - n, 1 + m + n - p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (1 + m + n - p) \operatorname{AppellF1}\left[\frac{3}{2} - \frac{p}{2}, -n, 2 + m + n - p, \frac{5}{2} - \frac{p}{2}, \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) \right)$$

Problem 913: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[e + fx] (a + a \sin[e + fx])^4 (c + d \sin[e + fx])^n dx$$

Optimal (type 3, 175 leaves, 3 steps):

$$\frac{a^4 (c - d)^4 (c + d \sin[e + fx])^{1+n}}{d^5 f (1 + n)} - \frac{4 a^4 (c - d)^3 (c + d \sin[e + fx])^{2+n}}{d^5 f (2 + n)} + \frac{6 a^4 (c - d)^2 (c + d \sin[e + fx])^{3+n}}{d^5 f (3 + n)} - \frac{4 a^4 (c - d) (c + d \sin[e + fx])^{4+n}}{d^5 f (4 + n)} + \frac{a^4 (c + d \sin[e + fx])^{5+n}}{d^5 f (5 + n)}$$

Result (type 3, 1209 leaves):

$$\frac{1}{f \left(\cos\left[\frac{1}{2}(e + fx)\right] + \sin\left[\frac{1}{2}(e + fx)\right] \right)^8} (a + a \sin[e + fx])^4 (c + d \sin[e + fx])^n \left((192 c^5 - 960 c^4 d + 1920 c^3 d^2 - 1920 c^2 d^3 + 960 c d^4 + 1320 d^5 - 192 c^4 d n + 912 c^3 d^2 n - 1744 c^2 d^3 n + 1730 c d^4 n + 2444 d^5 n + 144 c^3 d^2 n^2 - 672 c^2 d^3 n^2 + 1297 c d^4 n^2 + 1436 d^5 n^2 - 80 c^2 d^3 n^3 + 370 c d^4 n^3 + 340 d^5 n^3 + 35 c d^4 n^4 + 28 d^5 n^4) / (8 d^5 (1 + n) (2 + n) (3 + n) (4 + n) (5 + n)) + (2520 d^4 - 192 c^4 n + 960 c^3 d n - 1968 c^2 d^2 n + 2160 c d^3 n + 4290 d^4 n + 192 c^3 d n^2 - 936 c^2 d^2 n^2 + 1912 c d^3 n^2 + 2507 d^4 n^2 - 120 c^2 d^2 n^3 + 576 c d^3 n^3 + 594 d^4 n^3 + 56 c d^3 n^4 + 49 d^4 n^4) \right)$$

$$\begin{aligned}
 & \left(-\frac{i \operatorname{Cos}[e+fx]}{16d^4} + \frac{\operatorname{Sin}[e+fx]}{16d^4} \right) \Big/ \left((1+n)(2+n)(3+n)(4+n)(5+n) \right) + \\
 & \left((2520d^4 - 192c^4n + 960c^3dn - 1968c^2d^2n + 2160cd^3n + 4290d^4n + 192c^3d^2n^2 - 936c^2d^2n^2 + \right. \\
 & \quad \left. 1912cd^3n^2 + 2507d^4n^2 - 120c^2d^2n^3 + 576cd^3n^3 + 594d^4n^3 + 56cd^3n^4 + 49d^4n^4) \right. \\
 & \quad \left. \left(\frac{i \operatorname{Cos}[e+fx]}{16d^4} + \frac{\operatorname{Sin}[e+fx]}{16d^4} \right) \right) \Big/ \left((1+n)(2+n)(3+n)(4+n)(5+n) \right) + \\
 & \left((-360d^3 - 12c^3n + 60c^2dn - 126cd^2n - 312d^3n + 12c^2d^2n^2 - 59cd^2n^2 - 88d^3n^2 - 7cd^2n^3 - \right. \\
 & \quad \left. 8d^3n^3) \left(\frac{\operatorname{Cos}[2(e+fx)]}{4d^3} - \frac{i \operatorname{Sin}[2(e+fx)]}{4d^3} \right) \right) \Big/ \left((2+n)(3+n)(4+n)(5+n) \right) + \\
 & \left((-360d^3 - 12c^3n + 60c^2dn - 126cd^2n - 312d^3n + 12c^2d^2n^2 - 59cd^2n^2 - 88d^3n^2 - \right. \\
 & \quad \left. 7cd^2n^3 - 8d^3n^3) \left(\frac{\operatorname{Cos}[2(e+fx)]}{4d^3} + \frac{i \operatorname{Sin}[2(e+fx)]}{4d^3} \right) \right) \Big/ \\
 & \left((2+n)(3+n)(4+n)(5+n) \right) + \left((540d^2 - 16c^2n + 80cdn + 251d^2n + 16cdn^2 + 29d^2n^2) \right. \\
 & \quad \left. \left(-\frac{i \operatorname{Cos}[3(e+fx)]}{32d^2} - \frac{\operatorname{Sin}[3(e+fx)]}{32d^2} \right) \right) \Big/ \left((3+n)(4+n)(5+n) \right) + \\
 & \left((540d^2 - 16c^2n + 80cdn + 251d^2n + 16cdn^2 + 29d^2n^2) \right. \\
 & \quad \left. \left(\frac{i \operatorname{Cos}[3(e+fx)]}{32d^2} - \frac{\operatorname{Sin}[3(e+fx)]}{32d^2} \right) \right) \Big/ \left((3+n)(4+n)(5+n) \right) + \\
 & \frac{(20d + cn + 4dn) \left(\frac{\operatorname{Cos}[4(e+fx)]}{16d} - \frac{i \operatorname{Sin}[4(e+fx)]}{16d} \right)}{(4+n)(5+n)} + \\
 & \frac{(20d + cn + 4dn) \left(\frac{\operatorname{Cos}[4(e+fx)]}{16d} + \frac{i \operatorname{Sin}[4(e+fx)]}{16d} \right)}{(4+n)(5+n)} + \\
 & -\frac{\frac{1}{32} i \operatorname{Cos}[5(e+fx)] + \frac{1}{32} \operatorname{Sin}[5(e+fx)]}{5+n} + \\
 & \left. \frac{\frac{1}{32} i \operatorname{Cos}[5(e+fx)] + \frac{1}{32} \operatorname{Sin}[5(e+fx)]}{5+n} \right)
 \end{aligned}$$

Problem 914: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[e+fx] (a + a \operatorname{Sin}[e+fx])^3 (c + d \operatorname{Sin}[e+fx])^n dx$$

Optimal (type 3, 139 leaves, 3 steps):

$$-\frac{a^3 (c-d)^3 (c+d \operatorname{Sin}[e+fx])^{1+n}}{d^4 f (1+n)} + \frac{3 a^3 (c-d)^2 (c+d \operatorname{Sin}[e+fx])^{2+n}}{d^4 f (2+n)} -$$

$$\frac{3 a^3 (c-d) (c+d \operatorname{Sin}[e+fx])^{3+n}}{d^4 f (3+n)} + \frac{a^3 (c+d \operatorname{Sin}[e+fx])^{4+n}}{d^4 f (4+n)}$$

Result (type 3, 784 leaves):

$$\frac{1}{f \left(\operatorname{Cos} \left[\frac{1}{2} (e+fx) \right] + \operatorname{Sin} \left[\frac{1}{2} (e+fx) \right] \right)^6} (a+a \operatorname{Sin}[e+fx])^3 (c+d \operatorname{Sin}[e+fx])^n$$

$$\left((-48 c^4 + 192 c^3 d - 288 c^2 d^2 + 192 c d^3 + 162 d^4 + 48 c^3 d n - 180 c^2 d^2 n + 256 c d^3 n + 261 d^4 n - 36 c^2 d^2 n^2 + 132 c d^3 n^2 + 114 d^4 n^2 + 20 c d^3 n^3 + 15 d^4 n^3) / (8 d^4 (1+n) (2+n) (3+n) (4+n)) + \right.$$

$$\left((168 d^3 + 24 c^3 n - 96 c^2 d n + 150 c d^2 n + 230 d^3 n - 24 c^2 d n^2 + 93 c d^2 n^2 + 99 d^3 n^2 + 15 c d^2 n^3 + 13 d^3 n^3) \left(-\frac{i \operatorname{Cos}[e+fx]}{8 d^3} + \frac{\operatorname{Sin}[e+fx]}{8 d^3} \right) \right) / ((1+n) (2+n) (3+n) (4+n)) +$$

$$\left((168 d^3 + 24 c^3 n - 96 c^2 d n + 150 c d^2 n + 230 d^3 n - 24 c^2 d n^2 + 93 c d^2 n^2 + 99 d^3 n^2 + 15 c d^2 n^3 + 13 d^3 n^3) \left(\frac{i \operatorname{Cos}[e+fx]}{8 d^3} + \frac{\operatorname{Sin}[e+fx]}{8 d^3} \right) \right) / ((1+n) (2+n) (3+n) (4+n)) +$$

$$\left((-42 d^2 + 3 c^2 n - 12 c d n - 26 d^2 n - 3 c d n^2 - 4 d^2 n^2) \left(\frac{\operatorname{Cos}[2(e+fx)]}{4 d^2} - \frac{i \operatorname{Sin}[2(e+fx)]}{4 d^2} \right) \right) /$$

$$\left((2+n) (3+n) (4+n) \right) +$$

$$\left((-42 d^2 + 3 c^2 n - 12 c d n - 26 d^2 n - 3 c d n^2 - 4 d^2 n^2) \left(\frac{\operatorname{Cos}[2(e+fx)]}{4 d^2} + \frac{i \operatorname{Sin}[2(e+fx)]}{4 d^2} \right) \right) /$$

$$\left((2+n) (3+n) (4+n) \right) + \frac{(12 d + c n + 3 d n) \left(-\frac{i \operatorname{Cos}[3(e+fx)]}{8 d} - \frac{\operatorname{Sin}[3(e+fx)]}{8 d} \right)}{(3+n) (4+n)} +$$

$$\frac{(12 d + c n + 3 d n) \left(\frac{i \operatorname{Cos}[3(e+fx)]}{8 d} - \frac{\operatorname{Sin}[3(e+fx)]}{8 d} \right)}{(3+n) (4+n)} + \frac{\frac{1}{16} \operatorname{Cos}[4(e+fx)] - \frac{1}{16} i \operatorname{Sin}[4(e+fx)]}{4+n} +$$

$$\frac{\frac{1}{16} \operatorname{Cos}[4(e+fx)] + \frac{1}{16} i \operatorname{Sin}[4(e+fx)]}{4+n} \Bigg)$$

Problem 917: Unable to integrate problem.

$$\int \frac{\operatorname{Cos}[e+fx] (c+d \operatorname{Sin}[e+fx])^n}{a+a \operatorname{Sin}[e+fx]} dx$$

Optimal (type 5, 60 leaves, 2 steps):

$$- \left(\left(\text{Hypergeometric2F1} \left[1, 1+n, 2+n, \frac{c+d \sin[e+fx]}{c-d} \right] (c+d \sin[e+fx])^{1+n} \right) / \right. \\ \left. (a(c-d) f (1+n)) \right)$$

Result (type 8, 33 leaves):

$$\int \frac{\cos[e+fx] (c+d \sin[e+fx])^n}{a+a \sin[e+fx]} dx$$

Problem 918: Unable to integrate problem.

$$\int \frac{\cos[e+fx] (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^2} dx$$

Optimal (type 5, 60 leaves, 2 steps):

$$\left(d \text{Hypergeometric2F1} \left[2, 1+n, 2+n, \frac{c+d \sin[e+fx]}{c-d} \right] (c+d \sin[e+fx])^{1+n} \right) / \\ (a^2 (c-d)^2 f (1+n))$$

Result (type 8, 33 leaves):

$$\int \frac{\cos[e+fx] (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^2} dx$$

Problem 919: Unable to integrate problem.

$$\int \frac{\cos[e+fx] (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^3} dx$$

Optimal (type 5, 63 leaves, 2 steps):

$$- \left(\left(d^2 \text{Hypergeometric2F1} \left[3, 1+n, 2+n, \frac{c+d \sin[e+fx]}{c-d} \right] (c+d \sin[e+fx])^{1+n} \right) / \right. \\ \left. (a^3 (c-d)^3 f (1+n)) \right)$$

Result (type 8, 33 leaves):

$$\int \frac{\cos[e+fx] (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^3} dx$$

Problem 920: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[e+fx] (a+a \sin[e+fx])^m (c+d \sin[e+fx])^4 dx$$

Optimal (type 3, 170 leaves, 3 steps):

$$\frac{(c-d)^4 (a+a \operatorname{Sin}[e+f x])^{1+m}}{a f (1+m)} + \frac{4 (c-d)^3 d (a+a \operatorname{Sin}[e+f x])^{2+m}}{a^2 f (2+m)} +$$

$$\frac{6 (c-d)^2 d^2 (a+a \operatorname{Sin}[e+f x])^{3+m}}{a^3 f (3+m)} + \frac{4 (c-d) d^3 (a+a \operatorname{Sin}[e+f x])^{4+m}}{a^4 f (4+m)} + \frac{d^4 (a+a \operatorname{Sin}[e+f x])^{5+m}}{a^5 f (5+m)}$$

Result (type 3, 1457 leaves):

$$\frac{1}{f} (a (1 + \operatorname{Sin}[e + f x]))^m$$

$$\left((960 c^4 - 960 c^3 d + 1920 c^2 d^2 - 600 c d^3 + 192 d^4 + 1232 c^4 m + 208 c^3 d m + 1344 c^2 d^2 m + 300 c d^3 m +$$

$$66 d^4 m + 568 c^4 m^2 + 560 c^3 d m^2 + 792 c^2 d^2 m^2 + 204 c d^3 m^2 + 81 d^4 m^2 + 112 c^4 m^3 + 176 c^3 d m^3 +$$

$$240 c^2 d^2 m^3 + 84 c d^3 m^3 + 18 d^4 m^3 + 8 c^4 m^4 + 16 c^3 d m^4 + 24 c^2 d^2 m^4 + 12 c d^3 m^4 + 3 d^4 m^4) /$$

$$(8 (1+m) (2+m) (3+m) (4+m) (5+m)) + \frac{1}{(1+m) (2+m) (3+m) (4+m) (5+m)}$$

$$(960 c^4 + 1440 c^2 d^2 + 120 d^4 + 1232 c^4 m + 1920 c^3 d m + 888 c^2 d^2 m + 1200 c d^3 m + 10 d^4 m +$$

$$568 c^4 m^2 + 1504 c^3 d m^2 + 900 c^2 d^2 m^2 + 600 c d^3 m^2 + 103 d^4 m^2 + 112 c^4 m^3 + 384 c^3 d m^3 +$$

$$336 c^2 d^2 m^3 + 192 c d^3 m^3 + 26 d^4 m^3 + 8 c^4 m^4 + 32 c^3 d m^4 + 36 c^2 d^2 m^4 + 24 c d^3 m^4 + 5 d^4 m^4)$$

$$\left(-\frac{1}{16} \operatorname{Cos}[e + f x] + \frac{1}{16} \operatorname{Sin}[e + f x] \right) + \frac{1}{(1+m) (2+m) (3+m) (4+m) (5+m)}$$

$$(960 c^4 + 1440 c^2 d^2 + 120 d^4 + 1232 c^4 m + 1920 c^3 d m + 888 c^2 d^2 m + 1200 c d^3 m +$$

$$10 d^4 m + 568 c^4 m^2 + 1504 c^3 d m^2 + 900 c^2 d^2 m^2 + 600 c d^3 m^2 + 103 d^4 m^2 +$$

$$112 c^4 m^3 + 384 c^3 d m^3 + 336 c^2 d^2 m^3 + 192 c d^3 m^3 + 26 d^4 m^3 + 8 c^4 m^4 + 32 c^3 d m^4 +$$

$$36 c^2 d^2 m^4 + 24 c d^3 m^4 + 5 d^4 m^4) \left(\frac{1}{16} \operatorname{Cos}[e + f x] + \frac{1}{16} \operatorname{Sin}[e + f x] \right) +$$

$$\left((-240 c^3 d - 120 c d^3 - 188 c^3 d m - 120 c^2 d^2 m - 64 c d^3 m - 18 d^4 m - 48 c^3 d m^2 -$$

$$54 c^2 d^2 m^2 - 28 c d^3 m^2 - 5 d^4 m^2 - 4 c^3 d m^3 - 6 c^2 d^2 m^3 - 4 c d^3 m^3 - d^4 m^3)$$

$$\left(\frac{1}{4} \operatorname{Cos}[2(e + f x)] - \frac{1}{4} \operatorname{Sin}[2(e + f x)] \right) \right) / ((2+m) (3+m) (4+m) (5+m)) +$$

$$\left((-240 c^3 d - 120 c d^3 - 188 c^3 d m - 120 c^2 d^2 m - 64 c d^3 m - 18 d^4 m - 48 c^3 d m^2 -$$

$$54 c^2 d^2 m^2 - 28 c d^3 m^2 - 5 d^4 m^2 - 4 c^3 d m^3 - 6 c^2 d^2 m^3 - 4 c d^3 m^3 - d^4 m^3)$$

$$\left(\frac{1}{4} \operatorname{Cos}[2(e + f x)] + \frac{1}{4} \operatorname{Sin}[2(e + f x)] \right) \right) / ((2+m) (3+m) (4+m) (5+m)) +$$

$$\left((480 c^2 d^2 + 60 d^4 + 216 c^2 d^2 m + 80 c d^3 m + 19 d^4 m + 24 c^2 d^2 m^2 + 16 c d^3 m^2 + 5 d^4 m^2)$$

$$\left(-\frac{1}{32} \operatorname{Cos}[3(e + f x)] - \frac{1}{32} \operatorname{Sin}[3(e + f x)] \right) \right) / ((3+m) (4+m) (5+m)) +$$

$$\left((480 c^2 d^2 + 60 d^4 + 216 c^2 d^2 m + 80 c d^3 m + 19 d^4 m + 24 c^2 d^2 m^2 + 16 c d^3 m^2 + 5 d^4 m^2)$$

$$\left(\frac{1}{32} \operatorname{Cos}[3(e + f x)] - \frac{1}{32} \operatorname{Sin}[3(e + f x)] \right) \right) / ((3+m) (4+m) (5+m)) +$$

$$\frac{1}{(4+m) (5+m)} (20 c d^3 + 4 c d^3 m + d^4 m) \left(\frac{1}{16} \operatorname{Cos}[4(e + f x)] - \frac{1}{16} \operatorname{Sin}[4(e + f x)] \right) \right) +$$

$$\frac{1}{(4+m)(5+m)} \left((20cd^3 + 4cd^3m + d^4m) \left(\frac{1}{16} \cos[4(e+fx)] + \frac{1}{16} \sin[4(e+fx)] \right) + \frac{-\frac{1}{32}d^4 \cos[5(e+fx)] + \frac{1}{32}d^4 \sin[5(e+fx)]}{5+m} + \frac{\frac{1}{32}d^4 \cos[5(e+fx)] + \frac{1}{32}d^4 \sin[5(e+fx)]}{5+m} \right)$$

Problem 921: Result more than twice size of optimal antiderivative.

$$\int \cos[e+fx] (a+a \sin[e+fx])^m (c+d \sin[e+fx])^3 dx$$

Optimal (type 3, 133 leaves, 3 steps):

$$\frac{(c-d)^3 (a+a \sin[e+fx])^{1+m}}{af(1+m)} + \frac{3(c-d)^2 d (a+a \sin[e+fx])^{2+m}}{a^2 f(2+m)} + \frac{3(c-d)d^2 (a+a \sin[e+fx])^{3+m}}{a^3 f(3+m)} + \frac{d^3 (a+a \sin[e+fx])^{4+m}}{a^4 f(4+m)}$$

Result (type 3, 295 leaves):

$$\frac{1}{4f(1+m)(2+m)(3+m)(4+m)} \left(\cos\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{1}{2}(e+fx)\right] \right)^2 (a(1+\sin[e+fx]))^m \left(96c^3 - 144c^2d + 144cd^2 - 36d^3 + 104c^3m - 84c^2dm + 108cd^2m - 18d^3m + 36c^3m^2 - 12c^2dm^2 + 42cd^2m^2 - 6d^3m^2 + 4c^3m^3 + 6cd^2m^3 + 6d^2(2+3m+m^2)(d-c(4+m)) \cos[2(e+fx)] + 3d(1+m)(-8cd(4+m) + d^2(14+5m+m^2) + 4c^2(12+7m+m^2)) \sin[e+fx] - 6d^3 \sin[3(e+fx)] - 11d^3m \sin[3(e+fx)] - 6d^3m^2 \sin[3(e+fx)] - d^3m^3 \sin[3(e+fx)] \right)$$

Problem 926: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[e+fx] (a+a \sin[e+fx])^m}{(c+d \sin[e+fx])^3} dx$$

Optimal (type 5, 59 leaves, 2 steps):

$$\left(\text{Hypergeometric2F1}\left[3, 1+m, 2+m, -\frac{d(1+\sin[e+fx])}{c-d}\right] (a+a \sin[e+fx])^{1+m} \right) / (a(c-d)^3 f(1+m))$$

Result (type 5, 203 leaves):

$$\left(2 \left(a \left(1 + \sin[e + f x] \right) \right)^m \left(\frac{c - d}{c + d \sin[e + f x]} \right)^m \left(-2 d (1 + m) \cos \left[\frac{1}{4} (2 e - \pi + 2 f x) \right] \right)^2 \right. \\ \left. \text{Hypergeometric2F1} \left[m, 2 + m, 3 + m, \frac{2 d \cos \left[\frac{1}{4} (2 e - \pi + 2 f x) \right]^2}{c + d \sin[e + f x]} \right] + \right. \\ \left. (2 + m) \text{Hypergeometric2F1} \left[m, 1 + m, 2 + m, \frac{2 d \cos \left[\frac{1}{4} (2 e - \pi + 2 f x) \right]^2}{c + d \sin[e + f x]} \right] (c + d \sin[e + f x]) \right) \\ \left. \sin \left[\frac{1}{4} (2 e + \pi + 2 f x) \right]^2 \right) / \left((c - d)^2 f (1 + m) (2 + m) (c + d \sin[e + f x])^2 \right)$$

Problem 932: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cot[c + d x] (a + a \sin[c + d x])^m dx$$

Optimal (type 5, 43 leaves, 2 steps):

$$-\frac{1}{a d (1 + m)} \text{Hypergeometric2F1} [1, 1 + m, 2 + m, 1 + \sin[c + d x]] (a + a \sin[c + d x])^{1+m}$$

Result (type 6, 12204 leaves):

$$-\frac{1}{d} \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^{-2m} \\ (a + a \sin[c + d x])^m \left(\frac{1}{2^m} \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^{2m} \left(-1 + (-\text{Csc}[c + d x])^m \right. \right. \\ \left. \left. \text{Hypergeometric2F1} \left[m, m, 1 + m, 2 \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Csc}[c + d x] \right] \right) + \right. \\ \left. \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^{2+2m} \text{Csc}[c + d x] \left(\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-m} \right. \\ \left. \left(4 m \text{Hypergeometric2F1} \left[\frac{1}{2}, 1 + m, \frac{3}{2}, -\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \\ \left. \left(\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right] + \text{AppellF1} [2 m, m, m, \right. \\ \left. 1 + 2 m, -\frac{1 + i}{-1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}, -\frac{1 - i}{-1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right] \\ \left. \left. \left(\frac{-i + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \left(\frac{i + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \right) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right] \\
 & \left(\frac{-i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m \left(\frac{i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m \Bigg) / \\
 & \left(16m \left(-\frac{1}{8} \left(\sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^2\right)^{-m} \tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right] \right. \\
 & \left. \left(4m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \right. \\
 & \left. \left(\sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^m \tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right] + \text{AppellF1}\left[2m, m, m, \right. \right. \\
 & \left. \left. 1+2m, -\frac{1+i}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right] \right. \\
 & \left. \left(\frac{-i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m \left(\frac{i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m - \right. \\
 & \left. \text{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right] \right. \\
 & \left. \left(\frac{-i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m \left(\frac{i+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right)^m \right) + \\
 & \frac{1}{8m} \left(\sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^2\right)^{-m} \left(2m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \left. \left.-\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \left(\sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^{1+m} + 4 \right. \\
 & \left. m^2 \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \left. \left(\sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^m \tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 + \right. \\
 & \left. \left(\left((1-i)m^2 \text{AppellF1}\left[1+2m, m, 1+m, 2+2m, -\frac{1+i}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right], \right. \right. \right. \\
 & \left. \left. -\frac{1-i}{-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]}\right] \sec\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) / \left((1+2m) \right. \\
 & \left. \left(-1+\tan\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)^2\right) + \left((1+i)m^2 \text{AppellF1}\left[1+2m, 1+m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left((1-i) m^2 \operatorname{AppellF1} \left[1+2m, 1+m, m, 2+2m, \frac{1-i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right. \right. \\
 & \quad \left. \left. \frac{1+i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \quad \left((1+2m) \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) - m \operatorname{AppellF1} [2m, m, \\
 & \quad m, 1+2m, \frac{1-i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, \frac{1+i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \\
 & \quad \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \\
 & \quad \left(- \left(\left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \left(-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \left(2 \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) + \frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} - m \operatorname{AppellF1} [\\
 & \quad 2m, m, m, 1+2m, \frac{1-i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, \frac{1+i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \\
 & \quad \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \\
 & \quad \left(- \left(\left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \left(i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \right. \\
 & \quad \left. \left(2 \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) + \frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} + 2 \\
 & \quad m \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^{1+m} \left(-\operatorname{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right]^2 + \left(1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right)^{-1+m} \right) \right) - \\
 & \quad \left(\operatorname{Cos} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^{2m} \operatorname{Csc} [c+dx] \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^{-m} \\
 & \quad \operatorname{Sin} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \left(4 m \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, -\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
 & \quad \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right] - \\
 & \quad \operatorname{AppellF1} \left[2 m, m, m, 1+2 m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}, \right. \\
 & \quad \left. -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right] \\
 & \quad \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m + \\
 & \quad \operatorname{AppellF1} \left[2 m, m, m, 1+2 m, \frac{1-i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}, \frac{1+i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right] \\
 & \quad \left. \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \right) \Bigg/ \\
 & \left(16 m \left(\frac{1}{8} \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-m} \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right] \right. \right. \\
 & \quad \left(4 m \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, -\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
 & \quad \left. \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right] - \operatorname{AppellF1} \left[2 m, m, m, \right. \right. \\
 & \quad \left. \left. 1+2 m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}, -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right] \right. \\
 & \quad \left. \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[2 m, m, m, 1+2 m, \frac{1-i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}, \frac{1+i}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right] \right) \\
 & \quad \left. \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]} \right)^m \right) - \\
 & \quad \frac{1}{8 m} \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-m} \left(2 m \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{1+m} + 4 \right. \\
 & \quad \left. m^2 \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, -\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \\
 & \left(\left((1-i) m^2 \operatorname{AppellF1} \left[1+2m, m, 1+m, 2+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right], \right. \right. \\
 & \quad \left. \left. -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \left((1+2m) \right. \\
 & \quad \left. \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) + \left((1+i) m^2 \operatorname{AppellF1} \left[1+2m, 1+m, \right. \right. \\
 & \quad \left. \left. m, 2+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right], -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \left((1+2m) \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) \\
 & \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m - m \\
 & \operatorname{AppellF1} \left[2m, m, m, 1+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right], \\
 & \quad \left. -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \\
 & \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} - \right. \\
 & \quad \left. \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \left(-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \\
 & \quad \left(2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) - m \operatorname{AppellF1} \left[2m, m, m, \right. \\
 & \quad \left. 1+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right], -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \\
 & \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \\
 & \left(\frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} - \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right) / \left(2 \left(-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \Bigg) + \\
& \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \\
& \left(- \left(\left((1+i) m^2 \operatorname{AppellF1}\left[1+2m, m, 1+m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right], \right. \right. \right. \\
& \left. \left. \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \right. \\
& \left. \left((1+2m) \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \right) - \left((1-i) m^2 \operatorname{AppellF1}\left[1+2m, \right. \right. \\
& \left. \left. 1+m, m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right], \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \left((1+2m) \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \Bigg) + m \\
& \operatorname{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right], \\
& \left. \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \\
& \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(- \left(\left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right. \right. \\
& \left. \left. \left(-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) \right) / \left(2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \Bigg) + \\
& \left. \frac{\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)} \right) + m \operatorname{AppellF1}\left[2m, m, m, 1+2m, \right. \\
& \left. \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right], \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
& \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \\
& \left(- \left(\left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \left(i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left(2 \left(1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) + \frac{\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} + 2 \\
 & m \left(\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{1+m} \left(-\text{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(1 + \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1-m} \right) \right) \right) + \\
 & \frac{1}{d} \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{-2m} (a + a \sin [c + dx])^m \\
 & \left(-\frac{1}{2m} \right. \\
 & \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \\
 & \left(-1 + \right. \\
 & \left. (-\csc [c + dx])^m \right. \\
 & \left. \text{Hypergeometric2F1} [m, m, 1+m, \right. \\
 & \left. 2 \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \csc [c + dx] \right] \right) + \\
 & \left(\cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2+2m} \left(\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-m} \right. \\
 & \left(4m \text{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \left. \left(\sec \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] + \right. \\
 & \left. \text{AppellF1} \left[2m, m, m, 1+2m, -\frac{1+i}{-1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, -\frac{1-i}{-1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right. \\
 & \left. \left(\frac{-i+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{-1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m - \right. \\
 & \left. \text{AppellF1} \left[2m, m, m, 1+2m, \frac{1-i}{1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, \frac{1+i}{1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right. \\
 & \left. \left(\frac{-i+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1+\tan \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \right) \right) / \\
 & \left(16m \left(\cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] - \sin \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right. \\
 & \left. \left(\cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \\
& \left(-\frac{1}{8}\left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-m} \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right. \\
& \left(4m \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^m \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] + \operatorname{AppellF1}\left[2m, m, m, 1+\right.\right. \\
& \left.\left.2m, -\frac{1+i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right]\right. \\
& \left.\left(\frac{-i+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right)^m \left(\frac{i+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right)^m - \right. \\
& \left.\operatorname{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right]\right. \\
& \left.\left(\frac{-i+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right)^m \left(\frac{i+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right)^m\right) + \\
& \frac{1}{8m}\left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-m} \left(2m \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2},\right.\right. \\
& \left.\left.-\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{1+m} + \right. \\
& \left.4m^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^m \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 + \right. \\
& \left.\left(\left((1-i)m^2 \operatorname{AppellF1}\left[1+2m, m, 1+m, 2+2m, -\frac{1+i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]},\right.\right.\right.\right. \\
& \left.\left.\left.-\frac{1-i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right] \sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \right. \\
& \left.\left(\left((1+2m)\left(-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2\right) + \left((1+i)m^2 \operatorname{AppellF1}\left[1+2m, 1+m,\right.\right.\right.\right. \\
& \left.\left.\left.2m, 2+2m, -\frac{1+i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right]\right) / \right. \\
& \left.\left.\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(\left((1+2m)\left(-1+\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2\right)\right)
\end{aligned}$$

$$\begin{aligned}
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m + \\
 & m \operatorname{AppellF1}\left[2m, m, m, 1+2m, -\frac{1+i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, \right. \\
 & \left. -\frac{1-i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \\
 & \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{2\left(-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)} - \right. \\
 & \left. \left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \right) / \right. \\
 & \left. \left(2\left(-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \right) \right) + m \operatorname{AppellF1}\left[2m, m, m, \right. \\
 & \left. 1+2m, -\frac{1+i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, -\frac{1-i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \\
 & \left(\frac{\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{2\left(-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)} - \left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
 & \left. \left. \left(i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \right) / \left(2\left(-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \right) \right) - \\
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \\
 & \left(- \left(\left((1+i) m^2 \operatorname{AppellF1}\left[1+2m, m, 1+m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right], \right. \right. \right. \\
 & \left. \left. \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \right. \\
 & \left. \left((1+2m) \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \right) \right) - \left((1-i) m^2 \operatorname{AppellF1}\left[1+2m, \right. \right. \\
 & \left. \left. 1+m, m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \left((1+2m) \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) - m \right. \\
 & \left. \text{AppellF1} \left[2m, m, m, 1+2m, \frac{1-i}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, \frac{1+i}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right. \\
 & \left. \left(\frac{-i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \left(\frac{i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \right. \\
 & \left. \left(- \left(\left(\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \left(-i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \right. \right. \\
 & \left. \left. \left(2 \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) + \frac{\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} \right) - m \\
 & \left. \text{AppellF1} \left[2m, m, m, 1+2m, \frac{1-i}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, \frac{1+i}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right. \\
 & \left. \left(\frac{-i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^m \left(\frac{i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}{1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right)^{-1+m} \right. \\
 & \left. \left(- \left(\left(\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \left(i + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \right. \right. \\
 & \left. \left. \left(2 \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^2 \right) \right) + \frac{\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{2 \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)} \right) + \\
 & 2m \left(\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{1+m} \left(-\text{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \left. \left. -\text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+m} \right) \right) \right) - \\
 & \left(\text{Cos} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \left(\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-m} \text{Sin} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
 & \left. \left(4m \text{Hypergeometric2F1} \left[\frac{1}{2}, 1+m, \frac{3}{2}, -\text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
 & \left. \left. \left(\text{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right] - \right. \right. \\
 & \left. \left. \text{AppellF1} \left[2m, m, m, 1+2m, -\frac{1+i}{-1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]}, -\frac{1-i}{-1 + \text{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m + \\
 & \text{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \Big/ \\
 & \left(16m \left(\cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] - \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right. \\
 & \quad \left(\cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
 & \quad \quad \left. \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \\
 & \quad \left. \left(\frac{1}{8} \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right)^{-m} \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right. \\
 & \quad \left(4m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2 \right) \\
 & \quad \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] - \text{AppellF1}\left[2m, m, m, 1+ \right. \\
 & \quad \quad \left. 2m, -\frac{1+i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, -\frac{1-i}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \quad \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{-1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m + \\
 & \quad \text{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \quad \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m - \\
 & \quad \frac{1}{8m} \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \left(2m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2 \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^{1+m} + \right. \\
 & \quad \quad \left. 4m^2 \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, -\tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2 \right) \\
 & \quad \left(\sec\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 -
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left((1-i) m^2 \operatorname{AppellF1} \left[1+2m, m, 1+m, 2+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right] \operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]^2 \right) / \right. \\
 & \quad \left((1+2m) \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \right) + \left((1+i) m^2 \operatorname{AppellF1} \left[1+2m, 1+m, \right. \right. \\
 & \quad \left. \left. m, 2+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}, -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]^2 \right) / \left((1+2m) \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \right) \right) \\
 & \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^m - \\
 & m \operatorname{AppellF1} \left[2m, m, m, 1+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}, \right. \\
 & \quad \left. -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right] \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^{-1+m} \\
 & \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^m \left(\frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]^2}{2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)} - \right. \\
 & \quad \left. \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \left(-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right) \right) / \\
 & \quad \left(2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \right) - m \operatorname{AppellF1} \left[2m, m, m, \right. \\
 & \quad \left. 1+2m, -\frac{1+i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}, -\frac{1-i}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right] \\
 & \left(\frac{-i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^m \left(\frac{i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]}{-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]} \right)^{-1+m} \\
 & \left(\frac{\operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right]^2}{2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)} - \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \right. \\
 & \quad \left. \left(i+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right) \right) / \left(2 \left(-1+\operatorname{Tan} \left[\frac{1}{2} \left(-c+\frac{\pi}{2}-dx \right) \right] \right)^2 \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \\
 & \left(- \left(\left((1+i) m^2 \operatorname{AppellF1}\left[1+2m, m, 1+m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right], \right. \right. \right. \\
 & \quad \left. \left. \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \right. \\
 & \quad \left. \left((1+2m) \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \right) - \left((1-i) m^2 \operatorname{AppellF1}\left[1+2m, \right. \right. \\
 & \quad \left. \left. 1+m, m, 2+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right], \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \left((1+2m) \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \right) + m \\
 & \operatorname{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right], \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \\
 & \left(- \left(\left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \left(-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) \right) / \\
 & \quad \left(2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \right) + \frac{\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)} \right) + m \\
 & \operatorname{AppellF1}\left[2m, m, m, 1+2m, \frac{1-i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}\right], \frac{1+i}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right] \\
 & \left(\frac{-i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^m \left(\frac{i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]}{1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]} \right)^{-1+m} \\
 & \left(- \left(\left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \left(i + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) \right) / \\
 & \quad \left(2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right) \right) + \frac{\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{2 \left(1 + \tan\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)} \right) + \\
 & 2m \left(\operatorname{Sec}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right)^2 \right)^{1+m} \left(-\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \right. \right.
 \end{aligned}$$

$$-\operatorname{Tan}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2+\left(1+\operatorname{Tan}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{-1-m}\right)\right)\right)\right)\right)$$

Problem 933: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cot [c+dx] \operatorname{Csc}[c+dx] (a+a \sin [c+dx])^m dx$$

Optimal (type 5, 42 leaves, 3 steps):

$$\frac{1}{ad(1+m)} \operatorname{Hypergeometric2F1}[2, 1+m, 2+m, 1+\sin [c+dx]] (a+a \sin [c+dx])^{1+m}$$

Result (type 6, 20340 leaves): Display of huge result suppressed!

Problem 934: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cot [c+dx] \operatorname{Csc}[c+dx]^2 (a+a \sin [c+dx])^m dx$$

Optimal (type 5, 43 leaves, 3 steps):

$$-\frac{1}{ad(1+m)} \operatorname{Hypergeometric2F1}[3, 1+m, 2+m, 1+\sin [c+dx]] (a+a \sin [c+dx])^{1+m}$$

Result (type 6, 35073 leaves): Display of huge result suppressed!

Problem 936: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [e+fx]^2}{(a+a \sin [e+fx])^{3/2} (c+d \sin [e+fx])} dx$$

Optimal (type 3, 123 leaves, 6 steps):

$$-\frac{2\sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [e+fx]}{\sqrt{2} \sqrt{a+a \sin [e+fx]}}\right]}{a^{3/2} (c-d) f} + \frac{2\sqrt{c+d} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{d} \cos [e+fx]}{\sqrt{c+d} \sqrt{a+a \sin [e+fx]}}\right]}{a^{3/2} (c-d) \sqrt{d} f}$$

Result (type 3, 220 leaves):

$$\frac{1}{\sqrt{d} (-c+d) f (a (1 + \sin[e+fx]))^{3/2}}$$

$$(-1)^{3/4} \left((-4-4i) \sqrt{d} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (e+fx) \right] \right) \right] \right) + (-1)^{1/4} \sqrt{c+d}$$

$$\left(\operatorname{Log} \left[\operatorname{Sec} \left[\frac{1}{4} (e+fx) \right] \right]^2 \left(\sqrt{c+d} + \sqrt{d} \cos \left[\frac{1}{2} (e+fx) \right] - \sqrt{d} \sin \left[\frac{1}{2} (e+fx) \right] \right) \right) -$$

$$\operatorname{Log} \left[\operatorname{Sec} \left[\frac{1}{4} (e+fx) \right] \right]^2 \left(\sqrt{c+d} - \sqrt{d} \cos \left[\frac{1}{2} (e+fx) \right] + \sqrt{d} \sin \left[\frac{1}{2} (e+fx) \right] \right) \right) \right)$$

$$\left(\cos \left[\frac{1}{2} (e+fx) \right] + \sin \left[\frac{1}{2} (e+fx) \right] \right)^3$$

Problem 937: Humongous result has more than 200000 leaves.

$$\int \frac{\cos[e+fx]^2}{(a+a \sin[e+fx])^{3/2} \sqrt{c+d \sin[e+fx]}} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$\frac{2 \operatorname{ArcTan} \left[\frac{\sqrt{a} \sqrt{d} \cos[e+fx]}{\sqrt{a+a \sin[e+fx]} \sqrt{c+d \sin[e+fx]}} \right]}{a^{3/2} \sqrt{d} f} - \frac{2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \sqrt{c-d} \cos[e+fx]}{\sqrt{2} \sqrt{a+a \sin[e+fx]} \sqrt{c+d \sin[e+fx]}} \right]}{a^{3/2} \sqrt{c-d} f}$$

Result (type ?, 208404 leaves): Display of huge result suppressed!

Problem 938: Result more than twice size of optimal antiderivative.

$$\int \cos[e+fx]^2 (a+a \sin[e+fx])^m (c+d \sin[e+fx])^n dx$$

Optimal (type 6, 135 leaves, 4 steps):

$$\left(2 \sqrt{2} \operatorname{AppellF1} \left[\frac{3}{2} + m, -\frac{1}{2}, -n, \frac{5}{2} + m, \frac{1}{2} (1 + \sin[e+fx]), -\frac{d (1 + \sin[e+fx])}{c-d} \right] \right.$$

$$\left. \cos[e+fx] (a+a \sin[e+fx])^{1+m} (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c-d} \right)^{-n} \right) /$$

$$(a f (3+2m) \sqrt{1-\sin[e+fx]})$$

Result (type 6, 391 leaves):

$$\left(10 (c+d) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-m, -n, \frac{5}{2}, \cos\left[\frac{1}{4}(2e+\pi+2fx)\right]^2, \frac{2d \sin\left[\frac{1}{4}(2e-\pi+2fx)\right]^2}{c+d}\right] \right. \\ \left. \left(\cos\left[\frac{1}{4}(2e-\pi+2fx)\right]^2 \right)^{\frac{1}{2}+m} \cos\left[\frac{1}{4}(2e+\pi+2fx)\right]^2 \operatorname{Csc}[e+fx] (a(1+\sin[e+fx]))^m \right. \right. \\ \left. \left. (c+d \sin[e+fx])^n \sin[2(e+fx)] \left(\sin\left[\frac{1}{4}(2e+\pi+2fx)\right]^2 \right)^{-\frac{1}{2}-m} \right) / \left(3f \left(-5(c+d) \right. \right. \right. \\ \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-m, -n, \frac{5}{2}, \cos\left[\frac{1}{4}(2e+\pi+2fx)\right]^2, \frac{2d \sin\left[\frac{1}{4}(2e-\pi+2fx)\right]^2}{c+d}\right] \right) + \right. \right. \\ \left. \left. \left(4dn \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}-m, 1-n, \frac{7}{2}, \cos\left[\frac{1}{4}(2e+\pi+2fx)\right]^2, \frac{2d \sin\left[\frac{1}{4}(2e-\pi+2fx)\right]^2}{c+d}\right] \right) + \right. \right. \\ \left. \left. (c+d)(1+2m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}-m, -n, \frac{7}{2}, \cos\left[\frac{1}{4}(2e+\pi+2fx)\right]^2, \right. \right. \right. \\ \left. \left. \left. \frac{2d \sin\left[\frac{1}{4}(2e-\pi+2fx)\right]^2}{c+d} \right] \right) \sin\left[\frac{1}{4}(2e-\pi+2fx)\right]^2 \right) \right) \right)$$

Problem 939: Attempted integration timed out after 120 seconds.

$$\int \cos[e+fx]^2 (a+a \sin[e+fx])^3 (c+d \sin[e+fx])^n dx$$

Optimal (type 6, 119 leaves, 3 steps):

$$- \left(\left(16\sqrt{2} a^3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{7}{2}, -n, \frac{5}{2}, \frac{1}{2}(1-\sin[e+fx]), \frac{d(1-\sin[e+fx])}{c+d}\right] \cos[e+fx] \right. \right. \\ \left. \left. (1-\sin[e+fx]) (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n} \right) / \left(3f \sqrt{1+\sin[e+fx]} \right) \right)$$

Result (type 1, 1 leaves):

???

Problem 940: Unable to integrate problem.

$$\int \cos[e+fx]^2 (a+a \sin[e+fx])^2 (c+d \sin[e+fx])^n dx$$

Optimal (type 6, 119 leaves, 3 steps):

$$- \left(\left(8\sqrt{2} a^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{5}{2}, -n, \frac{5}{2}, \frac{1}{2}(1-\sin[e+fx]), \frac{d(1-\sin[e+fx])}{c+d}\right] \cos[e+fx] \right. \right. \\ \left. \left. (1-\sin[e+fx]) (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n} \right) / \left(3f \sqrt{1+\sin[e+fx]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \cos[e+fx]^2 (a+a \sin[e+fx])^2 (c+d \sin[e+fx])^n dx$$

Problem 941: Unable to integrate problem.

$$\int \cos[e+fx]^2 (a+a \sin[e+fx]) (c+d \sin[e+fx])^n dx$$

Optimal (type 6, 117 leaves, 3 steps):

$$-\left(\left(4\sqrt{2} a \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}, -n, \frac{5}{2}, \frac{1}{2} (1 - \sin[e+fx]), \frac{d(1 - \sin[e+fx])}{c+d}\right] \cos[e+fx] \right. \right. \\ \left. \left. (1 - \sin[e+fx]) (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n} \right) / \left(3f\sqrt{1+\sin[e+fx]} \right) \right)$$

Result (type 8, 33 leaves):

$$\int \cos[e+fx]^2 (a+a \sin[e+fx]) (c+d \sin[e+fx])^n dx$$

Problem 943: Unable to integrate problem.

$$\int \frac{\cos[e+fx]^2 (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^2} dx$$

Optimal (type 6, 119 leaves, 3 steps):

$$-\left(\left(\operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}, -n, \frac{5}{2}, \frac{1}{2} (1 - \sin[e+fx]), \frac{d(1 - \sin[e+fx])}{c+d}\right] \right. \right. \\ \left. \left. \cos[e+fx] (1 - \sin[e+fx]) (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n} \right) / \left(3\sqrt{2} a^2 f \sqrt{1+\sin[e+fx]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e+fx]^2 (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^2} dx$$

Problem 944: Unable to integrate problem.

$$\int \frac{\cos[e+fx]^2 (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^3} dx$$

Optimal (type 6, 119 leaves, 3 steps):

$$-\left(\left(\operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}, -n, \frac{5}{2}, \frac{1}{2} (1 - \sin[e+fx]), \frac{d(1 - \sin[e+fx])}{c+d}\right] \right. \right. \\ \left. \left. \cos[e+fx] (1 - \sin[e+fx]) (c+d \sin[e+fx])^n \left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n} \right) / \left(6\sqrt{2} a^3 f \sqrt{1+\sin[e+fx]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos [e+f x]^2 (c+d \sin [e+f x])^n}{(a+a \sin [e+f x])^3} dx$$

Problem 945: Result more than twice size of optimal antiderivative.

$$\int \cos [e+f x]^4 (a+a \sin [e+f x])^m (c+d \sin [e+f x])^n dx$$

Optimal (type 6, 135 leaves, 4 steps):

$$\left(4 \sqrt{2} \operatorname{AppellF1}\left[\frac{5}{2}+m, -\frac{3}{2}, -n, \frac{7}{2}+m, \frac{1}{2}(1+\sin [e+f x]), -\frac{d(1+\sin [e+f x])}{c-d}\right] \right. \\ \left. \cos [e+f x] (a+a \sin [e+f x])^{2+m} (c+d \sin [e+f x])^n \left(\frac{c+d \sin [e+f x]}{c-d}\right)^{-n}\right) / \\ \left(a^2 f(5+2 m) \sqrt{1-\sin [e+f x]}\right)$$

Result (type 6, 455 leaves):

$$\left(224 (c+d) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}-m, -n, \frac{7}{2}, \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \\ \left. \cos \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^3 \left(\cos \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{\frac{1}{2}(-3-2 m)} \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^5 \right. \\ \left. \left(1-\sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{\frac{3}{2}+m} (c+d-2 d \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2)^n (a+a \sin [e+f x])^m\right) / \\ \left(5 f \left(-7 (c+d) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}-m, -n, \frac{7}{2}, \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \right. \\ \left. \left. \left(4 d n \operatorname{AppellF1}\left[\frac{7}{2}, -\frac{3}{2}-m, 1-n, \frac{9}{2}, \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \frac{2 d \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \right. \right. \\ \left. \left. \left. (c+d)(3+2 m) \operatorname{AppellF1}\left[\frac{7}{2}, -\frac{1}{2}-m, -n, \frac{9}{2}, \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \\ \left. \left. \left. \left. \frac{2 d \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \sin \left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) \right) \right)$$

Problem 946: Unable to integrate problem.

$$\int \cos [e+f x]^4 (a+a \sin [e+f x])^2 (c+d \sin [e+f x])^n dx$$

Optimal (type 6, 121 leaves, 3 steps):

$$- \left(\left[16 \sqrt{2} a^2 \text{AppellF1} \left[\frac{5}{2}, -\frac{7}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \right. \\ \left. \left. (1 - \sin[e + f x])^2 (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left(5 f \sqrt{1 + \sin[e + f x]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \cos[e + f x]^4 (a + a \sin[e + f x])^2 (c + d \sin[e + f x])^n dx$$

Problem 947: Unable to integrate problem.

$$\int \cos[e + f x]^4 (a + a \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

Optimal (type 6, 119 leaves, 3 steps):

$$- \left(\left[8 \sqrt{2} a \text{AppellF1} \left[\frac{5}{2}, -\frac{5}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x]^3 \right. \right. \\ \left. \left. (1 - \sin[e + f x]) (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left(5 f (1 + \sin[e + f x])^{3/2} \right) \right)$$

Result (type 8, 33 leaves):

$$\int \cos[e + f x]^4 (a + a \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

Problem 948: Unable to integrate problem.

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

Optimal (type 6, 121 leaves, 3 steps):

$$- \left(\left[2 \sqrt{2} \text{AppellF1} \left[\frac{5}{2}, -\frac{1}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \right. \\ \left. \left. (1 - \sin[e + f x])^2 (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right] / \left(5 a f \sqrt{1 + \sin[e + f x]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

Problem 949: Unable to integrate problem.

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 6, 121 leaves, 4 steps):

$$- \left(\left(\sqrt{2} \operatorname{AppellF1} \left[\frac{5}{2}, \frac{1}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \cos[e + f x] \right. \right. \\ \left. \left. (1 - \sin[e + f x])^2 (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left(5 a^2 f \sqrt{1 + \sin[e + f x]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^2} dx$$

Problem 950: Unable to integrate problem.

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^3} dx$$

Optimal (type 6, 121 leaves, 3 steps):

$$- \left(\left(\operatorname{AppellF1} \left[\frac{5}{2}, \frac{3}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \right. \right. \\ \left. \left. \cos[e + f x] (1 - \sin[e + f x])^2 (c + d \sin[e + f x])^n \right. \right. \\ \left. \left. \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left(5 \sqrt{2} a^3 f \sqrt{1 + \sin[e + f x]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^3} dx$$

Problem 951: Unable to integrate problem.

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^4} dx$$

Optimal (type 6, 121 leaves, 3 steps):

$$- \left(\left(\operatorname{AppellF1} \left[\frac{5}{2}, \frac{5}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x]), \frac{d (1 - \sin[e + f x])}{c + d} \right] \right. \right. \\ \left. \left. \cos[e + f x] (1 - \sin[e + f x])^2 (c + d \sin[e + f x])^n \right. \right. \\ \left. \left. \left(\frac{c + d \sin[e + f x]}{c + d} \right)^{-n} \right) / \left(10 \sqrt{2} a^4 f \sqrt{1 + \sin[e + f x]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e + f x]^4 (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^4} dx$$

Problem 952: Unable to integrate problem.

$$\int \frac{\cos[e+fx]^4 (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^5} dx$$

Optimal (type 6, 121 leaves, 3 steps):

$$-\left(\left(\text{AppellF1} \left[\frac{5}{2}, \frac{7}{2}, -n, \frac{7}{2}, \frac{1}{2} (1 - \sin[e+fx]), \frac{d(1 - \sin[e+fx])}{c+d} \right] \right. \right. \\ \left. \left. \frac{\cos[e+fx] (1 - \sin[e+fx])^2 (c+d \sin[e+fx])^n}{\left(\frac{c+d \sin[e+fx]}{c+d} \right)^{-n}} \right) / \left(20 \sqrt{2} a^5 f \sqrt{1 + \sin[e+fx]} \right) \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\cos[e+fx]^4 (c+d \sin[e+fx])^n}{(a+a \sin[e+fx])^5} dx$$

Problem 957: Result more than twice size of optimal antiderivative.

$$\int \sec[c+dx] (a+a \sin[c+dx]) (A+B \sin[c+dx]) dx$$

Optimal (type 3, 34 leaves, 3 steps):

$$\frac{a(A+B) \log[1 - \sin[c+dx]]}{d} - \frac{aB \sin[c+dx]}{d}$$

Result (type 3, 172 leaves):

$$\frac{aA \log[\cos[c+dx]]}{d} - \frac{aB \log[\cos[c+dx]]}{d} - \frac{aA \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\ \frac{aA \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} - \frac{aB \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \\ \frac{aB \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \frac{aB \sin[c+dx]}{d}$$

Problem 958: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c+dx]^3 (a+a \sin[c+dx]) (A+B \sin[c+dx]) dx$$

Optimal (type 3, 47 leaves, 4 steps):

$$\frac{a(A-B) \text{ArcTanh}[\sin[c+dx]]}{2d} + \frac{a^2(A+B)}{2d(a-a \sin[c+dx])}$$

Result (type 3, 260 leaves):

$$\frac{1}{4 d \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2}$$

$$a \left(2 A + 2 B + i A d x - i B d x - 2 A \log \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] + \right.$$

$$2 B \log \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] + A \log \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right] -$$

$$B \log \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right] + 2 i (A - B) \operatorname{ArcTan} \left[\tan \left[\frac{1}{2} (c+d x) \right] \right]$$

$$\left. (-1 + \sin [c+d x]) + (A - B) \left(-i d x + 2 \log \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] - \right.$$

$$\left. \log \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right] \right) \sin [c+d x]$$

Problem 959: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^5 (a+a \sin [c+d x]) (A+B \sin [c+d x]) dx$$

Optimal (type 3, 100 leaves, 4 steps):

$$\frac{a (3 A - B) \operatorname{ArcTanh} [\sin [c+d x]]}{8 d} +$$

$$\frac{a^3 (A+B)}{8 d (a-a \sin [c+d x])^2} + \frac{a^2 A}{4 d (a-a \sin [c+d x])} - \frac{a^2 (A-B)}{8 d (a+a \sin [c+d x])}$$

Result (type 3, 357 leaves):

$$\frac{1}{16 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^4}$$

$$a \left(\frac{2 (-A+B)}{d} + i (3 A - B) x \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 - \frac{1}{d} \right.$$

$$2 i (3 A - B) \operatorname{ArcTan} \left[\tan \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 - \frac{1}{d}$$

$$2 (3 A - B) \log \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 +$$

$$\frac{1}{d} (3 A - B) \log \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right] \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 +$$

$$\frac{2 (A+B) \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2}{d \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^4} +$$

$$\left. \frac{4 A \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2}{d \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2} \right) (1 + \sin [c+d x])$$

Problem 960: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^7 (a + a \sin[c + dx]) (A + B \sin[c + dx]) dx$$

Optimal (type 3, 157 leaves, 4 steps):

$$\frac{a(5A - B) \operatorname{ArcTanh}[\sin[c + dx]]}{16d} + \frac{a^4(A + B)}{24d(a - a \sin[c + dx])^3} + \frac{a^3(3A + B)}{32d(a - a \sin[c + dx])^2} + \frac{3a^2A}{16d(a - a \sin[c + dx])} - \frac{a^3(A - B)}{32d(a + a \sin[c + dx])^2} - \frac{a^2(2A - B)}{16d(a + a \sin[c + dx])}$$

Result (type 3, 451 leaves):

$$\frac{1}{96 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6} a \left(\frac{3(-A + B)}{d} - \frac{6(2A - B) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2}{d} + 3i(5A - B) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 - \frac{1}{d} 6i(5A - B) \operatorname{ArcTan}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 - \frac{1}{d} 6(5A - B) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 + \frac{1}{d} 3(5A - B) \operatorname{Log}\left[\left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 + \frac{4(A + B) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4}{d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^6} + \frac{3(3A + B) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4}{d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^4} + \frac{18A \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4}{d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^2} \right) (1 + \sin[c + dx])$$

Problem 964: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^2 (a + a \sin[c + dx]) (A + B \sin[c + dx]) dx$$

Optimal (type 3, 29 leaves, 2 steps):

$$-a B x + \frac{(A+B) \operatorname{Sec}[c+d x] (a+a \operatorname{Sin}[c+d x])}{d}$$

Result (type 3, 85 leaves):

$$\frac{a \left(-B d x \operatorname{Cos}\left[\frac{d x}{2}\right] + 2 (A+B) \operatorname{Sin}\left[\frac{d x}{2}\right] + B d x \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right)}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)}$$

Problem 966: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^6 (a+a \operatorname{Sin}[c+d x]) (A+B \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 73 leaves, 3 steps):

$$\frac{(A+B) \operatorname{Sec}[c+d x]^5 (a+a \operatorname{Sin}[c+d x])}{5 d} + \frac{a (4 A-B) \operatorname{Tan}[c+d x]}{5 d} + \frac{a (4 A-B) \operatorname{Tan}[c+d x]^3}{15 d}$$

Result (type 3, 223 leaves):

$$\begin{aligned} & (a \operatorname{Sec}[c] (240 B \operatorname{Cos}[c] - 54 (A+B) \operatorname{Cos}[c+d x] - 18 A \operatorname{Cos}[3(c+d x)] - 18 B \operatorname{Cos}[3(c+d x)] + \\ & 128 A \operatorname{Cos}[c+2 d x] - 32 B \operatorname{Cos}[c+2 d x] + 64 A \operatorname{Cos}[3 c+4 d x] - 16 B \operatorname{Cos}[3 c+4 d x] + \\ & 384 A \operatorname{Sin}[d x] - 96 B \operatorname{Sin}[d x] + 18 A \operatorname{Sin}[2(c+d x)] + 18 B \operatorname{Sin}[2(c+d x)] + \\ & 9 A \operatorname{Sin}[4(c+d x)] + 9 B \operatorname{Sin}[4(c+d x)] + 128 A \operatorname{Sin}[2 c+3 d x] - 32 B \operatorname{Sin}[2 c+3 d x])) / \\ & \left(960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3 \right) \end{aligned}$$

Problem 967: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^8 (a+a \operatorname{Sin}[c+d x]) (A+B \operatorname{Sin}[c+d x]) dx$$

Optimal (type 3, 96 leaves, 3 steps):

$$\frac{(A+B) \operatorname{Sec}[c+d x]^7 (a+a \operatorname{Sin}[c+d x])}{7 d} + \frac{a (6 A-B) \operatorname{Tan}[c+d x]}{7 d} + \frac{2 a (6 A-B) \operatorname{Tan}[c+d x]^3}{21 d} + \frac{a (6 A-B) \operatorname{Tan}[c+d x]^5}{35 d}$$

Result (type 3, 315 leaves):

$$\begin{aligned} & (a \operatorname{Sec}[c] (8960 B \operatorname{Cos}[c] - 1500 (A+B) \operatorname{Cos}[c+d x] - 750 A \operatorname{Cos}[3(c+d x)] - \\ & 750 B \operatorname{Cos}[3(c+d x)] - 150 A \operatorname{Cos}[5(c+d x)] - 150 B \operatorname{Cos}[5(c+d x)] + \\ & 3840 A \operatorname{Cos}[c+2 d x] - 640 B \operatorname{Cos}[c+2 d x] + 3072 A \operatorname{Cos}[3 c+4 d x] - 512 B \operatorname{Cos}[3 c+4 d x] + \\ & 768 A \operatorname{Cos}[5 c+6 d x] - 128 B \operatorname{Cos}[5 c+6 d x] + 15360 A \operatorname{Sin}[d x] - 2560 B \operatorname{Sin}[d x] + \\ & 375 A \operatorname{Sin}[2(c+d x)] + 375 B \operatorname{Sin}[2(c+d x)] + 300 A \operatorname{Sin}[4(c+d x)] + \\ & 300 B \operatorname{Sin}[4(c+d x)] + 75 A \operatorname{Sin}[6(c+d x)] + 75 B \operatorname{Sin}[6(c+d x)] + 7680 A \operatorname{Sin}[2 c+3 d x] - \\ & 1280 B \operatorname{Sin}[2 c+3 d x] + 1536 A \operatorname{Sin}[4 c+5 d x] - 256 B \operatorname{Sin}[4 c+5 d x])) / \\ & \left(53760 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^7 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^5 \right) \end{aligned}$$

Problem 968: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^{10} (a+a \sin [c+d x]) (A+B \sin [c+d x]) d x$$

Optimal (type 3, 119 leaves, 3 steps):

$$\frac{(A+B) \sec [c+d x]^9 (a+a \sin [c+d x])}{9 d} + \frac{a(8 A-B) \tan [c+d x]}{9 d} + \frac{a(8 A-B) \tan [c+d x]^3}{9 d} + \frac{a(8 A-B) \tan [c+d x]^5}{15 d} + \frac{a(8 A-B) \tan [c+d x]^7}{63 d}$$

Result (type 3, 1683 leaves):

$$\begin{aligned} & a \left(\frac{(A \sin [\frac{d x}{2}] - B \sin [\frac{d x}{2}]) (1 + \sin [c+d x])}{112 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^9} + \right. \\ & \frac{(-A \cos [\frac{c}{2}] + B \cos [\frac{c}{2}] + A \sin [\frac{c}{2}] - B \sin [\frac{c}{2}]) (1 + \sin [c+d x])}{224 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^8} + \\ & \frac{(41 A \sin [\frac{d x}{2}] - 27 B \sin [\frac{d x}{2}]) (1 + \sin [c+d x])}{1120 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^7} + \\ & \left. \frac{\left((-41 A \cos [\frac{c}{2}] + 27 B \cos [\frac{c}{2}] + 41 A \sin [\frac{c}{2}] - 27 B \sin [\frac{c}{2}]) (1 + \sin [c+d x]) \right)}{\left(2240 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^6 \right)} + \right. \\ & \frac{(689 A \sin [\frac{d x}{2}] - 283 B \sin [\frac{d x}{2}]) (1 + \sin [c+d x])}{6720 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^5} + \\ & \left. \frac{\left((-689 A \cos [\frac{c}{2}] + 283 B \cos [\frac{c}{2}] + 689 A \sin [\frac{c}{2}] - 283 B \sin [\frac{c}{2}]) (1 + \sin [c+d x]) \right)}{\left(13440 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^4 \right)} + \right. \\ & \frac{(5053 A \sin [\frac{d x}{2}] - 1091 B \sin [\frac{d x}{2}]) (1 + \sin [c+d x])}{13440 d \left(\cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^3} + \\ & \left. \frac{\left((A \sin [\frac{d x}{2}] + B \sin [\frac{d x}{2}]) (1 + \sin [c+d x]) \right)}{\left(72 d \left(\cos [\frac{c}{2}] - \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] - \sin [\frac{c}{2} + \frac{d x}{2}] \right)^9 \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^2 \right)} + \right. \\ & \left. \frac{\left((A \cos [\frac{c}{2}] + B \cos [\frac{c}{2}] + A \sin [\frac{c}{2}] + B \sin [\frac{c}{2}]) (1 + \sin [c+d x]) \right)}{\left(144 d \left(\cos [\frac{c}{2}] - \sin [\frac{c}{2}] \right) \left(\cos [\frac{c}{2} + \frac{d x}{2}] - \sin [\frac{c}{2} + \frac{d x}{2}] \right)^8 \left(\cos [\frac{c}{2} + \frac{d x}{2}] + \sin [\frac{c}{2} + \frac{d x}{2}] \right)^2 \right)} + \end{aligned}$$

$$\begin{aligned}
& \left(\left(22 A \sin\left[\frac{dx}{2}\right] + 13 B \sin\left[\frac{dx}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(504 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^7 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(22 A \cos\left[\frac{c}{2}\right] + 13 B \cos\left[\frac{c}{2}\right] + 22 A \sin\left[\frac{c}{2}\right] + 13 B \sin\left[\frac{c}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(1008 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^6 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(149 A \sin\left[\frac{dx}{2}\right] + 47 B \sin\left[\frac{dx}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(1680 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^5 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(149 A \cos\left[\frac{c}{2}\right] + 47 B \cos\left[\frac{c}{2}\right] + 149 A \sin\left[\frac{c}{2}\right] + 47 B \sin\left[\frac{c}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(3360 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^4 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(823 A \sin\left[\frac{dx}{2}\right] + 94 B \sin\left[\frac{dx}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(5040 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(823 A \cos\left[\frac{c}{2}\right] + 94 B \cos\left[\frac{c}{2}\right] + 823 A \sin\left[\frac{c}{2}\right] + 94 B \sin\left[\frac{c}{2}\right] \right) (1 + \sin[c + dx]) \right) / \left(10080 \right. \\
& \quad \left. d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
& \left(\left(17609 A \sin\left[\frac{dx}{2}\right] - 823 B \sin\left[\frac{dx}{2}\right] \right) (1 + \sin[c + dx]) \right) / \\
& \left(40320 d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right)
\end{aligned}$$

Problem 974: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 (a + a \sin[c + dx])^2 (A + B \sin[c + dx]) dx$$

Optimal (type 3, 43 leaves, 3 steps):

$$\frac{a^2 B \operatorname{Log}[1 - \sin[c + dx]]}{d} + \frac{a^3 (A + B)}{d (a - a \sin[c + dx])}$$

Result (type 3, 95 leaves):

$$\left(a^2 \left(A + B + 2 B \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] - \right. \right. \\ \left. \left. 2 B \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \sin [c + d x] \right) \right) / \\ \left(d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right)$$

Problem 976: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^7 (a + a \sin [c + d x])^2 (A + B \sin [c + d x]) dx$$

Optimal (type 3, 132 leaves, 4 steps):

$$\frac{a^2 (2 A - B) \operatorname{ArcTanh}[\sin [c + d x]]}{8 d} + \frac{a^5 (A + B)}{12 d (a - a \sin [c + d x])^3} + \\ \frac{a^4 A}{8 d (a - a \sin [c + d x])^2} + \frac{a^3 (3 A - B)}{16 d (a - a \sin [c + d x])} - \frac{a^3 (A - B)}{16 d (a + a \sin [c + d x])}$$

Result (type 3, 319 leaves):

$$\frac{1}{48 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} \left(3 (-A + B) + \right. \\ 6 (-2 A + B) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \\ 6 (2 A - B) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \\ \frac{4 (A + B) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{6 A \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\ \left. \frac{3 (3 A - B) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right) (a + a \sin [c + d x])^2$$

Problem 984: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^{10} (a + a \sin [c + d x])^2 (A + B \sin [c + d x]) dx$$

Optimal (type 3, 154 leaves, 4 steps):

$$\frac{a^2 (7 A - 2 B) \sec [c + d x]^7}{63 d} + \frac{(A + B) \sec [c + d x]^9 (a + a \sin [c + d x])^2}{9 d} + \frac{a^2 (7 A - 2 B) \tan [c + d x]}{9 d} + \\ \frac{a^2 (7 A - 2 B) \tan [c + d x]^3}{9 d} + \frac{a^2 (7 A - 2 B) \tan [c + d x]^5}{15 d} + \frac{a^2 (7 A - 2 B) \tan [c + d x]^7}{63 d}$$

Result (type 3, 324 leaves):

$$\begin{aligned}
 & - \frac{1}{1290240 d} a^2 \operatorname{Sec}[c+dx]^9 (1+\operatorname{Sin}[c+dx])^2 \\
 & \quad (-184320 B + 1125 (49 A + 13 B) \operatorname{Cos}[c+dx] - 20480 (7 A - 2 B) \operatorname{Cos}[2(c+dx)] + \\
 & \quad 23275 A \operatorname{Cos}[3(c+dx)] + 6175 B \operatorname{Cos}[3(c+dx)] - 114688 A \operatorname{Cos}[4(c+dx)] + \\
 & \quad 32768 B \operatorname{Cos}[4(c+dx)] + 1225 A \operatorname{Cos}[5(c+dx)] + 325 B \operatorname{Cos}[5(c+dx)] - \\
 & \quad 28672 A \operatorname{Cos}[6(c+dx)] + 8192 B \operatorname{Cos}[6(c+dx)] - 1225 A \operatorname{Cos}[7(c+dx)] - \\
 & \quad 325 B \operatorname{Cos}[7(c+dx)] - 322560 A \operatorname{Sin}[c+dx] + 92160 B \operatorname{Sin}[c+dx] - \\
 & \quad 24500 A \operatorname{Sin}[2(c+dx)] - 6500 B \operatorname{Sin}[2(c+dx)] - 136192 A \operatorname{Sin}[3(c+dx)] + \\
 & \quad 38912 B \operatorname{Sin}[3(c+dx)] - 19600 A \operatorname{Sin}[4(c+dx)] - 5200 B \operatorname{Sin}[4(c+dx)] - \\
 & \quad 7168 A \operatorname{Sin}[5(c+dx)] + 2048 B \operatorname{Sin}[5(c+dx)] - 4900 A \operatorname{Sin}[6(c+dx)] - \\
 & \quad 1300 B \operatorname{Sin}[6(c+dx)] + 7168 A \operatorname{Sin}[7(c+dx)] - 2048 B \operatorname{Sin}[7(c+dx)])
 \end{aligned}$$

Problem 985: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^{12} (a+a \operatorname{Sin}[c+dx])^2 (A+B \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 179 leaves, 4 steps):

$$\begin{aligned}
 & \frac{a^2 (9 A - 2 B) \operatorname{Sec}[c+dx]^9}{99 d} + \frac{(A+B) \operatorname{Sec}[c+dx]^{11} (a+a \operatorname{Sin}[c+dx])^2}{11 d} + \\
 & \frac{a^2 (9 A - 2 B) \operatorname{Tan}[c+dx]}{11 d} + \frac{4 a^2 (9 A - 2 B) \operatorname{Tan}[c+dx]^3}{33 d} + \\
 & \frac{6 a^2 (9 A - 2 B) \operatorname{Tan}[c+dx]^5}{55 d} + \frac{4 a^2 (9 A - 2 B) \operatorname{Tan}[c+dx]^7}{77 d} + \frac{a^2 (9 A - 2 B) \operatorname{Tan}[c+dx]^9}{99 d}
 \end{aligned}$$

Result (type 3, 1349 leaves):

$$\begin{aligned}
 & \frac{(-A+B) (a+a \operatorname{Sin}[c+dx])^2}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^{10}} + \frac{(-24 A + 17 B) (a+a \operatorname{Sin}[c+dx])^2}{2240 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^8} + \\
 & \frac{(-927 A + 451 B) (a+a \operatorname{Sin}[c+dx])^2}{26880 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^6} + \frac{(A+B) (a+a \operatorname{Sin}[c+dx])^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4} + \\
 & \frac{\left(176 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^{10} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)}{\left((27 A + 16 B) (a+a \operatorname{Sin}[c+dx])^2 \right)} + \\
 & \frac{\left(1584 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^8 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)}{\left((711 A + 227 B) (a+a \operatorname{Sin}[c+dx])^2 \right)} + \\
 & \frac{\left(22176 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^6 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)}{\left((1866 A + 227 B) (a+a \operatorname{Sin}[c+dx])^2 \right)} + \\
 & \frac{\left(36960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)}{\left((1866 A + 227 B) (a+a \operatorname{Sin}[c+dx])^2 \right)}
 \end{aligned}$$

$$\begin{aligned}
 & \left((70281A - 2143B) (a + a \sin[c + dx])^2 \right) / \\
 & \left(887040d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((167301A \sin\left[\frac{1}{2}(c + dx)\right] - 26398B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(443520d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((70281A \sin\left[\frac{1}{2}(c + dx)\right] - 2143B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(443520d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((3867A \sin\left[\frac{1}{2}(c + dx)\right] - 1186B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(13440d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \right) + \\
 & \left((927A \sin\left[\frac{1}{2}(c + dx)\right] - 451B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(13440d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
 & \frac{\left(24A \sin\left[\frac{1}{2}(c + dx)\right] - 17B \sin\left[\frac{1}{2}(c + dx)\right] \right) (a + a \sin[c + dx])^2}{1120d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^9} + \\
 & \frac{\left(A \sin\left[\frac{1}{2}(c + dx)\right] - B \sin\left[\frac{1}{2}(c + dx)\right] \right) (a + a \sin[c + dx])^2}{224d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^{11}} + \\
 & \left(\left(A \sin\left[\frac{1}{2}(c + dx)\right] + B \sin\left[\frac{1}{2}(c + dx)\right] \right) (a + a \sin[c + dx])^2 \right) / \\
 & \left(88d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^{11} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((27A \sin\left[\frac{1}{2}(c + dx)\right] + 16B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(792d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^9 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((711A \sin\left[\frac{1}{2}(c + dx)\right] + 227B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(11088d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right) + \\
 & \left((1866A \sin\left[\frac{1}{2}(c + dx)\right] + 227B \sin\left[\frac{1}{2}(c + dx)\right]) (a + a \sin[c + dx])^2 \right) / \\
 & \left(18480d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right)
 \end{aligned}$$

Problem 989: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x] (a + a \sin [c + d x])^3 (A + B \sin [c + d x]) dx$$

Optimal (type 3, 51 leaves, 3 steps):

$$\frac{(A - B) (a + a \sin [c + d x])^4}{4 a d} + \frac{B (a + a \sin [c + d x])^5}{5 a^2 d}$$

Result (type 3, 116 leaves):

$$\left((a + a \sin [c + d x])^3 (-20 (7 A + 5 B) \cos [2 (c + d x)] + 5 (A + 3 B) \cos [4 (c + d x)] + 140 (2 A + B) \sin [c + d x] - 10 (4 A + 5 B) \sin [3 (c + d x)] + 2 B \sin [5 (c + d x)]) \right) / \left(160 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 \right)$$

Problem 994: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^9 (a + a \sin [c + d x])^3 (A + B \sin [c + d x]) dx$$

Optimal (type 3, 162 leaves, 4 steps):

$$\frac{a^3 (5 A - 3 B) \operatorname{ArcTanh}[\sin [c + d x]]}{32 d} + \frac{a^7 (A + B)}{16 d (a - a \sin [c + d x])^4} + \frac{a^6 A}{12 d (a - a \sin [c + d x])^3} + \frac{a^5 (3 A - B)}{32 d (a - a \sin [c + d x])^2} + \frac{a^4 (2 A - B)}{16 d (a - a \sin [c + d x])} - \frac{a^4 (A - B)}{32 d (a + a \sin [c + d x])}$$

Result (type 3, 378 leaves):

$$\frac{1}{96 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} \left(3 (-A + B) + 3 (-5 A + 3 B) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \right. \\ \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 3 (5 A - 3 B) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \\ \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{6 (A + B) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^8} + \\ \frac{8 A \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{3 (3 A - B) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\ \left. \frac{6 (2 A - B) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right) (a + a \sin [c + d x])^3$$

Problem 1007: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx] (A + B \text{Sin}[c + dx])}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 45 leaves, 4 steps):

$$\frac{(A + B) \text{ArcTanh}[\text{Sin}[c + dx]]}{2ad} - \frac{A - B}{2d(a + a \text{Sin}[c + dx])}$$

Result (type 3, 126 leaves):

$$\left(-A + B - (A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2 + \right. \\ \left. (A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2 \right) / (2ad(1 + \text{Sin}[c + dx]))$$

Problem 1008: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^3 (A + B \text{Sin}[c + dx])}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 91 leaves, 4 steps):

$$\frac{(3A + B) \text{ArcTanh}[\text{Sin}[c + dx]]}{8ad} + \frac{A + B}{8d(a - a \text{Sin}[c + dx])} - \frac{a(A - B)}{8d(a + a \text{Sin}[c + dx])^2} - \frac{A}{4d(a + a \text{Sin}[c + dx])}$$

Result (type 3, 210 leaves):

$$\left(-2A + \frac{-A + B}{\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \right. \\ \left. (3A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2 + \right. \\ \left. (3A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2 + \right. \\ \left. \frac{(A + B) \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2}{\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} \right) / (8ad(1 + \text{Sin}[c + dx]))$$

Problem 1009: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^5 (A + B \text{Sin}[c + dx])}{a + a \text{Sin}[c + dx]} dx$$

Optimal (type 3, 146 leaves, 4 steps):

$$\frac{(5A+B) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{16ad} + \frac{a(A+B)}{32d(a-a\operatorname{Sin}[c+dx])^2} + \frac{2A+B}{16d(a-a\operatorname{Sin}[c+dx])} - \frac{a^2(A-B)}{24d(a+a\operatorname{Sin}[c+dx])^3} - \frac{a(3A-B)}{32d(a+a\operatorname{Sin}[c+dx])^2} - \frac{3A}{16d(a+a\operatorname{Sin}[c+dx])}$$

Result (type 3, 298 leaves):

$$\frac{1}{96ad(1+\operatorname{Sin}[c+dx])} \left(-18A + \frac{4(-A+B)}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{3(-3A+B)}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - 6(5A+B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2 + 6(5A+B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2 + \frac{3(A+B) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{6(2A+B) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} \right)$$

Problem 1014: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx] (A+B\operatorname{Sin}[c+dx])}{(a+a\operatorname{Sin}[c+dx])^2} dx$$

Optimal (type 3, 44 leaves, 3 steps):

$$\frac{B \operatorname{Log}[1+\operatorname{Sin}[c+dx]]}{a^2d} - \frac{A-B}{d(a^2+a^2\operatorname{Sin}[c+dx])}$$

Result (type 3, 92 leaves):

$$\left(\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \left(-A+B+2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) \right) / \left(d(a+a\operatorname{Sin}[c+dx])^2 \right)$$

Problem 1015: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x] (A + B \text{Sin}[c + d x])}{(a + a \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 71 leaves, 4 steps):

$$\frac{(A + B) \text{ArcTanh}[\text{Sin}[c + d x]]}{4 a^2 d} - \frac{A - B}{4 d (a + a \text{Sin}[c + d x])^2} - \frac{A + B}{4 d (a^2 + a^2 \text{Sin}[c + d x])}$$

Result (type 3, 153 leaves):

$$\begin{aligned} & - \left(\left(A - B + (A + B) \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right)^2 + \right. \\ & \quad (A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 - \\ & \quad \left. (A + B) \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) / \left(4 \right. \\ & \quad \left. a^2 d (1 + \text{Sin}[c + d x])^2 \right) \end{aligned}$$

Problem 1020: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \text{Cos}[e + f x]^7 (a + a \text{Sin}[e + f x])^m (A + B \text{Sin}[e + f x]) dx$$

Optimal (type 3, 159 leaves, 3 steps):

$$\begin{aligned} & \frac{8(A - B)(a + a \text{Sin}[e + f x])^{4+m}}{a^4 f (4 + m)} - \frac{4(3A - 5B)(a + a \text{Sin}[e + f x])^{5+m}}{a^5 f (5 + m)} + \\ & \frac{6(A - 3B)(a + a \text{Sin}[e + f x])^{6+m}}{a^6 f (6 + m)} - \frac{(A - 7B)(a + a \text{Sin}[e + f x])^{7+m}}{a^7 f (7 + m)} - \frac{B(a + a \text{Sin}[e + f x])^{8+m}}{a^8 f (8 + m)} \end{aligned}$$

Result (type 3, 1361 leaves):

$$\begin{aligned} & \frac{1}{f} (a (1 + \text{Sin}[e + f x]))^m \\ & \left((393216A - 29400B + 118528Am + 26822Bm + 16160Am^2 + 2407Bm^2 + 1256Am^3 + \right. \\ & \quad \left. 166Bm^3 + 40Am^4 + 5Bm^4) / (128(4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \right. \\ & \quad \left((235200A + 50024Am + 29400Bm + 3946Am^2 + 2578Bm^2 + 211Am^3 + 171Bm^3 + 5Am^4 + 5Bm^4) \right. \\ & \quad \left. \left(-\frac{1}{128} \text{Cos}[e + f x] + \frac{1}{128} \text{Sin}[e + f x] \right) \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\ & \quad \left((235200A + 50024Am + 29400Bm + 3946Am^2 + 2578Bm^2 + 211Am^3 + 171Bm^3 + 5Am^4 + 5Bm^4) \right. \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{128} \operatorname{Im} \left[\cos [e + f x] + \frac{1}{128} \sin [e + f x] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(-11760 B + 19296 A m - 8932 B m + 5028 A m^2 - 94 B m^2 + 447 A m^3 + 19 B m^3 + 15 A m^4 + B m^4 \right) \\
 & \left(\frac{1}{64} \operatorname{Im} \left[\cos [2(e + f x)] - \frac{1}{64} \sin [2(e + f x)] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(-11760 B + 19296 A m - 8932 B m + 5028 A m^2 - 94 B m^2 + 447 A m^3 + 19 B m^3 + 15 A m^4 + B m^4 \right) \\
 & \left(\frac{1}{64} \operatorname{Im} \left[\cos [2(e + f x)] + \frac{1}{64} \sin [2(e + f x)] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(15680 A + 10520 A m + 1960 B m + 1814 A m^2 + 1070 B m^2 + 117 A m^3 + 93 B m^3 + 3 A m^4 + 3 B m^4 \right) \\
 & \left(-\frac{3}{128} \operatorname{Im} \left[\cos [3(e + f x)] + \frac{3}{128} \sin [3(e + f x)] \right] \right) / \\
 & ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(15680 A + 10520 A m + 1960 B m + 1814 A m^2 + 1070 B m^2 + 117 A m^3 + 93 B m^3 + 3 A m^4 + 3 B m^4 \right) \\
 & \left(\frac{3}{128} \operatorname{Im} \left[\cos [3(e + f x)] + \frac{3}{128} \sin [3(e + f x)] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(-5880 B + 2112 A m - 4466 B m + 1080 A m^2 - 989 B m^2 + 150 A m^3 - 52 B m^3 + 6 A m^4 - B m^4 \right) \\
 & \left(\frac{1}{64} \operatorname{Im} \left[\cos [4(e + f x)] - \frac{1}{64} \sin [4(e + f x)] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(-5880 B + 2112 A m - 4466 B m + 1080 A m^2 - 989 B m^2 + 150 A m^3 - 52 B m^3 + 6 A m^4 - B m^4 \right) \\
 & \left(\frac{1}{64} \operatorname{Im} \left[\cos [4(e + f x)] + \frac{1}{64} \sin [4(e + f x)] \right] \right) / ((4 + m)(5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(2352 A + 1118 A m + 294 B m + 143 A m^2 + 103 B m^2 + 5 A m^3 + 5 B m^3 \right) \\
 & \left(-\frac{1}{128} \operatorname{Im} \left[\cos [5(e + f x)] + \frac{1}{128} \sin [5(e + f x)] \right] \right) / ((5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(2352 A + 1118 A m + 294 B m + 143 A m^2 + 103 B m^2 + 5 A m^3 + 5 B m^3 \right) \\
 & \left(\frac{1}{128} \operatorname{Im} \left[\cos [5(e + f x)] + \frac{1}{128} \sin [5(e + f x)] \right] \right) / ((5 + m)(6 + m)(7 + m)(8 + m)) + \\
 & \left(-84 B + 8 A m - 26 B m + A m^2 - B m^2 \right) \left(\frac{1}{64} \operatorname{Im} \left[\cos [6(e + f x)] - \frac{1}{64} \sin [6(e + f x)] \right] \right) / \\
 & ((6 + m)(7 + m)(8 + m)) + \\
 & \left(-84 B + 8 A m - 26 B m + A m^2 - B m^2 \right) \left(\frac{1}{64} \operatorname{Im} \left[\cos [6(e + f x)] + \frac{1}{64} \sin [6(e + f x)] \right] \right) / \\
 & ((6 + m)(7 + m)(8 + m)) + \frac{(8 A + A m + B m) \left(-\frac{1}{128} \operatorname{Im} \left[\cos [7(e + f x)] + \frac{1}{128} \sin [7(e + f x)] \right] \right)}{(7 + m)(8 + m)} + \\
 & \frac{(8 A + A m + B m) \left(\frac{1}{128} \operatorname{Im} \left[\cos [7(e + f x)] + \frac{1}{128} \sin [7(e + f x)] \right] \right)}{(7 + m)(8 + m)} +
 \end{aligned}$$

$$\left. \begin{aligned} & \frac{-\frac{1}{256} B \cos [8 (e + f x)] - \frac{1}{256} i B \sin [8 (e + f x)]}{8 + m} + \\ & \frac{-\frac{1}{256} B \cos [8 (e + f x)] + \frac{1}{256} i B \sin [8 (e + f x)]}{8 + m} \end{aligned} \right)$$

Problem 1021: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [e + f x]^5 (a + a \sin [e + f x])^m (A + B \sin [e + f x]) dx$$

Optimal (type 3, 123 leaves, 3 steps):

$$\begin{aligned} & \frac{4 (A - B) (a + a \sin [e + f x])^{3+m}}{a^3 f (3 + m)} - \frac{4 (A - 2 B) (a + a \sin [e + f x])^{4+m}}{a^4 f (4 + m)} + \\ & \frac{(A - 5 B) (a + a \sin [e + f x])^{5+m}}{a^5 f (5 + m)} + \frac{B (a + a \sin [e + f x])^{6+m}}{a^6 f (6 + m)} \end{aligned}$$

Result (type 3, 869 leaves):

$$\begin{aligned}
 & \frac{1}{f} \left(a \left(1 + \text{Sin}[e + f x] \right) \right)^m \left(\frac{3072 A - 300 B + 1004 A m + 277 B m + 118 A m^2 + 22 B m^2 + 6 A m^3 + B m^3}{16 (3 + m) (4 + m) (5 + m) (6 + m)} + \right. \\
 & \left(\frac{1800 A + 438 A m + 300 B m + 29 A m^2 + 23 B m^2 + A m^3 + B m^3}{\left(-\frac{1}{16} \text{Cos}[e + f x] + \frac{1}{16} \text{Sin}[e + f x] \right)} \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(\frac{1800 A + 438 A m + 300 B m + 29 A m^2 + 23 B m^2 + A m^3 + B m^3}{\left(\frac{1}{16} \text{Cos}[e + f x] + \frac{1}{16} \text{Sin}[e + f x] \right)} \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(-900 B + 1056 A m - 705 B m + 272 A m^2 - 4 B m^2 + 16 A m^3 + B m^3 \right) \\
 & \left(\frac{1}{64} \text{Cos}[2 (e + f x)] - \frac{1}{64} \text{Sin}[2 (e + f x)] \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(-900 B + 1056 A m - 705 B m + 272 A m^2 - 4 B m^2 + 16 A m^3 + B m^3 \right) \\
 & \left(\frac{1}{64} \text{Cos}[2 (e + f x)] + \frac{1}{64} \text{Sin}[2 (e + f x)] \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(600 A + 418 A m + 100 B m + 71 A m^2 + 53 B m^2 + 3 A m^3 + 3 B m^3 \right) \\
 & \left(-\frac{1}{32} \text{Cos}[3 (e + f x)] + \frac{1}{32} \text{Sin}[3 (e + f x)] \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(600 A + 418 A m + 100 B m + 71 A m^2 + 53 B m^2 + 3 A m^3 + 3 B m^3 \right) \\
 & \left(\frac{1}{32} \text{Cos}[3 (e + f x)] + \frac{1}{32} \text{Sin}[3 (e + f x)] \right) / \left((3 + m) (4 + m) (5 + m) (6 + m) \right) + \\
 & \left(-60 B + 12 A m - 27 B m + 2 A m^2 - B m^2 \right) \left(\frac{1}{32} \text{Cos}[4 (e + f x)] - \frac{1}{32} \text{Sin}[4 (e + f x)] \right) / \\
 & \left((4 + m) (5 + m) (6 + m) \right) + \\
 & \left(-60 B + 12 A m - 27 B m + 2 A m^2 - B m^2 \right) \left(\frac{1}{32} \text{Cos}[4 (e + f x)] + \frac{1}{32} \text{Sin}[4 (e + f x)] \right) / \\
 & \left((4 + m) (5 + m) (6 + m) \right) + \frac{(6 A + A m + B m) \left(-\frac{1}{32} \text{Cos}[5 (e + f x)] + \frac{1}{32} \text{Sin}[5 (e + f x)] \right)}{(5 + m) (6 + m)} + \\
 & \frac{(6 A + A m + B m) \left(\frac{1}{32} \text{Cos}[5 (e + f x)] + \frac{1}{32} \text{Sin}[5 (e + f x)] \right)}{(5 + m) (6 + m)} + \\
 & \frac{-\frac{1}{64} B \text{Cos}[6 (e + f x)] - \frac{1}{64} B \text{Sin}[6 (e + f x)]}{6 + m} + \\
 & \left. \frac{-\frac{1}{64} B \text{Cos}[6 (e + f x)] + \frac{1}{64} B \text{Sin}[6 (e + f x)]}{6 + m} \right)
 \end{aligned}$$

Problem 1024: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec[e + f x] (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 80 leaves, 3 steps):

$$\frac{(A - B) (a + a \sin[e + f x])^m}{2 f m} + \frac{1}{4 a f (1 + m)}$$

$$(A + B) \operatorname{Hypergeometric2F1}\left[1, 1 + m, 2 + m, \frac{1}{2} (1 + \sin[e + f x])\right] (a + a \sin[e + f x])^{1+m}$$

Result (type 6, 16323 leaves):

$$\begin{aligned} & - \left(\left(\cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right] \right)^{-2m} \cot\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 (a + a \sin[e + f x])^m \right. \\ & \quad \left(\left(A \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \right) / \left(\left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right) \right. \right. \\ & \quad \left. \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] + \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right) \right) + \left(B \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^{2m} \right. \\ & \quad \left. \sin[e + f x] \right) / \left(\left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right) \right. \\ & \quad \left. \left(\cos\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] + \sin\left[\frac{\pi}{4} + \frac{1}{2} \left(e - \frac{\pi}{2} + f x\right)\right] \right) \right) \left(\frac{1 - \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2} \right)^{2m} \\ & \quad \left(2 A \operatorname{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\ & \quad \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^4 \right) / \left(\left(-1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right. \\ & \quad \left(-2 \operatorname{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\ & \quad \left(2 m \operatorname{AppellF1}\left[2, 1 - 2 m, 1 + 2 m, 3, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1 + 2 m) \operatorname{AppellF1}\left[2, 2 - 2 m, 2 m, 3, \right. \right. \\ & \quad \left. \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right) \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) - \\ & \quad \left(2 B \operatorname{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\ & \quad \left. \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^4 \right) / \left(\left(-1 + \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \right) \right. \\ & \quad \left(-2 \operatorname{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \right. \\ & \quad \left. \left(2 m \operatorname{AppellF1}\left[2, 1 - 2 m, 1 + 2 m, 3, \tan\left[\frac{1}{4} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(-1+2 m) \operatorname{AppellF1}\left[2,2-2 m, 2 m, 3,\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)+ \\
 & \left(4 B \operatorname{AppellF1}\left[1,-2 m, 1+2 m, 2, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^4\right) / \left(\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right. \\
 & \left(-2 \operatorname{AppellF1}\left[1,-2 m, 1+2 m, 2, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left.\left(2 m \operatorname{AppellF1}\left[2,1-2 m, 1+2 m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(1+2 m) \operatorname{AppellF1}\left[2,-2 m, 2+2 m, 3,\right.\right.\right. \\
 & \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)+ \\
 & \left(A(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
 & \left(\left(1+2 m\right)\left(2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right.\right. \\
 & \left.\left.\left.\frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+m\right.\right.\right. \\
 & \left.\left.\left.\operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right)+ \\
 & \left(B(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right) / \\
 & \left(\left(1+2 m\right)\left(2(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]-\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right.\right. \\
 & \left.\left.\left.\frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+m\right.\right.\right. \\
 & \left.\left.\left.\operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.\left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 - \left(\text{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. m\text{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) + \\
 & \left(B(1+m)\text{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \\
 & \left((1+2m)\left(2(1+m)\text{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\text{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. m\text{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\right)\right) + \\
 & 2m\cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(\frac{1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}\right)^{-1+2m} \\
 & \left(-\left(\left(\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)\right)\right) \Big/ \\
 & \left(2\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^2\right) - \frac{\sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]}{2\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)} \Big) \\
 & \left(\left(2A\text{AppellF1}\left[1, 1 - 2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4\right) \Big/ \left(\left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-2\text{AppellF1}\left[1, 1 - 2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(2m\text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2m, 1 + 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \left(-1 + 2m\right)\text{AppellF1}\left[2, 2 - 2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & \left(2B\text{AppellF1}\left[1, 1 - 2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \Big/ \left(\left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-2 \operatorname{AppellF1}\left[1, 1 - 2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, 1 - 2m, 1 + 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. (-1 + 2m) \operatorname{AppellF1}\left[2, 2 - 2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(4B \operatorname{AppellF1}\left[1, -2m, 1 + 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \Big/ \left(\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-2 \operatorname{AppellF1}\left[1, -2m, 1 + 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, 1 - 2m, 1 + 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. (1 + 2m) \operatorname{AppellF1}\left[2, -2m, 2 + 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) + \\
 & \left(A(1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \right. \\
 & \left. \left((1 + 2m) \left(2(1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. m \operatorname{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \right) + \\
 & \left(B(1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \right. \\
 & \left. \left((1 + 2m) \left(2(1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \Big) - \\
 & \left(2B \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^3\right] \Big) / \\
 & \left(\left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \left(-2 \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) + \\
 & \left(2A \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \left(-\frac{1}{2}m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{4}(1-2m) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \right) / \\
 & \left(\left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \left(-2 \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) - \\
 & \left(2B \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \left(-\frac{1}{2}m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{4}(1-2m) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[2, -2m, 2+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \Big/ \\
 & \left(\left(1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \left(-2 \text{AppellF1}\left[1, -2m, 1+2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \left(2m \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+2m) \text{AppellF1}\left[2, -2m, 2+2m, 3, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right) + \\
 & \left(A(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Big/ \\
 & \left(2(1+2m) \left(2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) \right) + \\
 & \left(B(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] \right) \Big/ \\
 & \left(2(1+2m) \left(2(1+m) \text{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \left(\text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. m \text{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2}-\frac{1}{2}\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \left(-1+\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) \right) \right) + \\
 & \left(A(1+m) \left(-\frac{1}{2(2+2m)} (1+2m) \text{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2}-\frac{1}{2} \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, 1-\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)}m(1+2m) \operatorname{AppellF1}\left[2+2m, 1+2m, \right. \\
 & \left. 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big/ \\
 & \left((1+2m)\left(2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\right)\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big) + \\
 & \left(B(1+m)\left(-\frac{1}{2(2+2m)}(1+2m) \operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2+2m)}m(1+2m) \operatorname{AppellF1}\left[2+2m, 1+2m, \right. \right. \right. \\
 & \left. \left. 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \right) \Big/ \right. \\
 & \left. \left((1+2m)\left(2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \left. \left. \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2}\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right)\right)\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \Big) - \\
 & \left(2A \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \left(\frac{1}{2}\left(2m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \right. \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + (-1+2m) \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. 2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - 2\left(-\frac{1}{2} m \text{AppellF1}\left[2, \right.\right. \\
 & \quad \left.1 - 2 m, 1 + 2 m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{1}{4}(1 - 2 m) \text{AppellF1}\left[\right. \\
 & \quad \left.2, 2 - 2 m, 2 m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left(2 m\left(-\frac{1}{3}(1 + 2 m) \text{AppellF1}\left[3, 1 - 2 m, 2 + 2 m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\right. \\
 & \quad \left.\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{1}{3}(1 - 2 m) \text{AppellF1}\left[3, 2 - 2 m, 1 + 2 m, 4, \text{Tan}\left[\frac{1}{4}\right. \right. \\
 & \quad \left.\left. \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \quad \left.\left.\left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right] + (-1 + 2 m)\left(-\frac{2}{3} m \text{AppellF1}\left[3, 2 - 2 m, \right.\right.\right. \\
 & \quad \left.1 + 2 m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \quad \left.\left.\left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{1}{3}(2 - 2 m) \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left.3, 3 - 2 m, 2 m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \left.\left.\left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right]\right)\right) / \\
 & \left(\left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\left(-2 \text{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \right.\right.\right. \\
 & \quad \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \left(2 m \text{AppellF1}\left[2, \right.\right. \right. \\
 & \quad \left.1 - 2 m, 1 + 2 m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + \\
 & \quad \left(-1 + 2 m\right) \text{AppellF1}\left[2, 2 - 2 m, 2 m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left.\left.\right)\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \\
 & \left(2 B \text{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right. \\
 & \quad \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^4\left(\frac{1}{2}\left(2 m \text{AppellF1}\left[2, 1 - 2 m, 1 + 2 m, 3, \right.\right.\right. \right. \\
 & \quad \left.\left.\left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1 + 2 m) \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left.2, 2 - 2 m, 2 m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2\left(-\frac{1}{2}m \text{AppellF1}\left[2, \right. \right. \\
 & \quad \left. \left. 1 - 2m, 1 + 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{4}(1 - 2m) \text{AppellF1}\left[\right. \\
 & \quad \left. 2, 2 - 2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \left(2m\left(-\frac{1}{3}(1 + 2m) \text{AppellF1}\left[3, 1 - 2m, 2 + 2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\right. \right. \\
 & \quad \left. \left. \frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{3}(1 - 2m) \text{AppellF1}\left[3, 2 - 2m, 1 + 2m, 4, \text{Tan}\left[\frac{1}{4} \right. \right. \right. \\
 & \quad \left. \left. \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + (-1 + 2m)\left(-\frac{2}{3}m \text{AppellF1}\left[3, 2 - 2m, \right. \right. \\
 & \quad \left. \left. 1 + 2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{3}(2 - 2m) \text{AppellF1}\left[\right. \\
 & \quad \left. 3, 3 - 2m, 2m, 4, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right)\right) / \\
 & \left(\left(-1 + \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-2 \text{AppellF1}\left[1, 1 - 2m, 2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(2m \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2m, 1 + 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. \left(-1 + 2m\right) \text{AppellF1}\left[2, 2 - 2m, 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) - \\
 & \left(4B \text{AppellF1}\left[1, -2m, 1 + 2m, 2, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \left(\frac{1}{2}\left(2m \text{AppellF1}\left[2, 1 - 2m, 1 + 2m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \left(1 + 2m\right) \text{AppellF1}\left[2, -2m, 2 + 2m, 3, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 2 \\
 & \left(-\frac{1}{2}m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \right. \\
 & \quad \left. \frac{1}{4}(1+2m) \operatorname{AppellF1}\left[2, -2m, 2+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \left(2m\left(-\frac{1}{3}(1+2m) \operatorname{AppellF1}\left[3, 1-2m, 2+2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{1}{3}(1-2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. 3, 2-2m, 1+2m, 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + \\
 & (1+2m)\left(-\frac{2}{3}m \operatorname{AppellF1}\left[3, 1-2m, 2+2m, 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{3}(2+2m) \operatorname{AppellF1}\left[3, -2m, 3+2m, \right. \\
 & \quad \left. 4, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) \Big/ \\
 & \left(\left(1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)^2\right) \left(-2 \operatorname{AppellF1}\left[1, -2m, 1+2m, 2, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. (1+2m) \operatorname{AppellF1}\left[2, -2m, 2+2m, 3, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) - \\
 & \left(A(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \\
 & \quad \left. 1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \\
 & \left(-\frac{1}{2}\left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + m \operatorname{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \right. \\
& \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 2(1 + m) \\
& \left(-\frac{1}{2(2 + 2m)}(1 + 2m) \operatorname{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \\
& \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(2 + 2m)} \right. \\
& \left. m(1 + 2m) \operatorname{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) - \\
& \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right) \left(-\frac{1}{3 + 2m}(2 + 2m) \operatorname{AppellF1}\left[3 + 2m, 2m, \right. \right. \\
& \left. \left. 3, 4 + 2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{2(3 + 2m)} \right. \\
& \left. m(2 + 2m) \operatorname{AppellF1}\left[3 + 2m, 1 + 2m, 2, 4 + 2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
& \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \right. \\
& \left. m\left(-\frac{1}{2(3 + 2m)}(2 + 2m) \operatorname{AppellF1}\left[3 + 2m, 1 + 2m, 2, 4 + 2m, \right. \right. \right. \\
& \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - \frac{1}{4(3 + 2m)} \right. \\
& \left. (1 + 2m)(2 + 2m) \operatorname{AppellF1}\left[3 + 2m, 2 + 2m, 1, 4 + 2m, \right. \right. \\
& \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right) \Bigg/ \\
& \left((1 + 2m)\left(2(1 + m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \\
& \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^2\right)- \\
 & \left(B(1+m) \operatorname{AppellF1}\left[1+2 m, 2 m, 1, 2+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right. \\
 & \left(-\frac{1}{2}\left(\operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+m \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m,\right. \\
 & \quad \left.\frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+2(1+m) \\
 & \left(-\frac{1}{2(2+2 m)}(1+2 m) \operatorname{AppellF1}\left[2+2 m, 2 m, 2, 3+2 m,\right.\right. \\
 & \quad \left.\frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2(2+2 m)}\right. \\
 & \quad \left.m(1+2 m) \operatorname{AppellF1}\left[2+2 m, 1+2 m, 1, 3+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)- \\
 & \left(-1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(-\frac{1}{3+2 m}(2+2 m) \operatorname{AppellF1}\left[3+2 m, 2 m,\right.\right. \\
 & \quad \left.3, 4+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{2(3+2 m)}\right. \\
 & \quad \left.m(2+2 m) \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m, \frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \quad \left.1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \\
 & \quad \left.m\left(-\frac{1}{2(3+2 m)}(2+2 m) \operatorname{AppellF1}\left[3+2 m, 1+2 m, 2, 4+2 m,\right.\right.\right. \\
 & \quad \left.\frac{1}{2}-\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, 1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-\frac{1}{4(3+2 m)}\right. \\
 & \quad \left.(1+2 m)(2+2 m) \operatorname{AppellF1}\left[3+2 m, 2+2 m, 1, 4+2 m,\right.\right.
 \end{aligned}$$

$$\frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\right) /$$

$$\left((1 + 2 m) \left(2 (1 + m) \operatorname{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \left(\operatorname{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + m \operatorname{AppellF1}\left[2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right], 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2\right)\right)\right)\right)\right)$$

Problem 1025: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[e + f x]^3 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Optimal (type 5, 100 leaves, 3 steps):

$$-\frac{1}{4 f (1 - m)} a (A (2 - m) - B m) \operatorname{Hypergeometric2F1}\left[1, -1 + m, m, \frac{1}{2} (1 + \operatorname{Sin}[e + f x])\right] (a + a \operatorname{Sin}[e + f x])^{-1+m} + \frac{a^2 (A + B) (a + a \operatorname{Sin}[e + f x])^{-1+m}}{2 f (a - a \operatorname{Sin}[e + f x])}$$

Result (type 6, 46238 leaves): Display of huge result suppressed!

Problem 1026: Unable to integrate problem.

$$\int \operatorname{Sec}[e + f x]^5 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Optimal (type 5, 104 leaves, 3 steps):

$$-\frac{1}{16 f (2 - m)} a^2 (A (4 - m) - B m) \operatorname{Hypergeometric2F1}\left[2, -2 + m, -1 + m, \frac{1}{2} (1 + \operatorname{Sin}[e + f x])\right] (a + a \operatorname{Sin}[e + f x])^{-2+m} + \frac{a^4 (A + B) (a + a \operatorname{Sin}[e + f x])^{-2+m}}{4 f (a - a \operatorname{Sin}[e + f x])^2}$$

Result (type 8, 33 leaves):

$$\int \operatorname{Sec}[e + f x]^5 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Problem 1027: Unable to integrate problem.

$$\int \cos[e + f x]^6 (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 129 leaves, 4 steps):

$$-\frac{1}{7 f (7+m)} 2^{\frac{7}{2}+m} a^3 (B m + A (7+m)) \cos[e + f x]^7 \text{Hypergeometric2F1}\left[\frac{7}{2}, -\frac{5}{2}-m, \frac{9}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \\ (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^{-3+m} - \frac{B \cos[e + f x]^7 (a + a \sin[e + f x])^m}{f (7+m)}$$

Result (type 8, 33 leaves):

$$\int \cos[e + f x]^6 (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Problem 1028: Unable to integrate problem.

$$\int \cos[e + f x]^4 (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 129 leaves, 4 steps):

$$-\frac{1}{5 f (5+m)} 2^{\frac{5}{2}+m} a^2 (B m + A (5+m)) \cos[e + f x]^5 \text{Hypergeometric2F1}\left[\frac{5}{2}, -\frac{3}{2}-m, \frac{7}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \\ (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^{-2+m} - \frac{B \cos[e + f x]^5 (a + a \sin[e + f x])^m}{f (5+m)}$$

Result (type 8, 33 leaves):

$$\int \cos[e + f x]^4 (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Problem 1029: Attempted integration timed out after 120 seconds.

$$\int \cos[e + f x]^2 (a + a \sin[e + f x])^m (A + B \sin[e + f x]) dx$$

Optimal (type 5, 127 leaves, 4 steps):

$$-\frac{1}{3 f (3+m)} 2^{\frac{3}{2}+m} a (B m + A (3+m)) \cos[e + f x]^3 \text{Hypergeometric2F1}\left[\frac{3}{2}, -\frac{1}{2}-m, \frac{5}{2}, \frac{1}{2} (1 - \sin[e + f x])\right] \\ (1 + \sin[e + f x])^{-\frac{1}{2}-m} (a + a \sin[e + f x])^{-1+m} - \frac{B \cos[e + f x]^3 (a + a \sin[e + f x])^m}{f (3+m)}$$

Result (type 1, 1 leaves):

???

Problem 1030: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Sec}[e + f x]^2 (a + a \text{Sin}[e + f x])^m (A + B \text{Sin}[e + f x]) dx$$

Optimal (type 5, 123 leaves, 4 steps):

$$\frac{B \text{Sec}[e + f x] (a + a \text{Sin}[e + f x])^m}{f (1 - m)} + \frac{1}{f (1 - m)}$$

$$2^{-\frac{1}{2}+m} (A (1 - m) - B m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{3}{2} - m, \frac{1}{2}, \frac{1}{2} (1 - \text{Sin}[e + f x])\right]$$

$$\text{Sec}[e + f x] (1 + \text{Sin}[e + f x])^{\frac{1}{2}-m} (a + a \text{Sin}[e + f x])^m$$

Result (type 6, 12366 leaves):

$$-\left(\left(\cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{-2m} \cot\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] (a + a \text{Sin}[e + f x])^m\right.$$

$$\left.\left(\left(A \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{2m}\right) / \left(\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \text{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)^2\right.$$

$$\left.\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] + \text{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)^2\right) + \left(B \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{2m}$$

$$\text{Sin}[e + f x] / \left(\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] - \text{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)^2\right.$$

$$\left.\left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right] + \text{Sin}\left[\frac{\pi}{4} + \frac{1}{2}\left(e - \frac{\pi}{2} + f x\right)\right]\right)^2\right)$$

$$\left(1 - \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^2 \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{2m}$$

$$\left(-\left(\left(15 (A + B) \text{AppellF1}\left[-\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2},\right.\right.\right.\right.$$

$$\left.\left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \right.$$

$$\left(\text{AppellF1}\left[-\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right.$$

$$4 \left(m \text{AppellF1}\left[\frac{1}{2}, 2 - 2m, 1 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.$$

$$\left.\left.-\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\frac{1}{2}, 3 - 2m, 2m, \frac{3}{2},\right.\right.$$

$$\left.\left.\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) +$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)^2\right]\Bigg/\left(\operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2},\right.\right. \\
& \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2-4\left(m\operatorname{AppellF1}\left[\frac{1}{2},\right.\right. \\
& \quad 2-2m, 1+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]^2 + \\
& \quad (-1+m)\operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\Bigg) + \\
(45 & (3A-5B)\operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\Bigg/\right. \\
& \left.(3\operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]^2 - \right. \\
& \quad 4\left(m\operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(-1+m)\operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right.\right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + \\
(25 & (3A-5B)\operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^4\Bigg/\right. \\
& \left.(5\operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]^2 - \right. \\
& \quad 4\left(m\operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(-1+m)\operatorname{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right.\right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) - \\
(21 & (A+B)\operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^6\Bigg/\right. \\
& \left.(-7\operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]^2 + \right. \\
& \quad 4\left(m\operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]+(-1+m)\operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right.\right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) -
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{240} \operatorname{Csc}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\left(15(A+B) \operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - 4\left(m \operatorname{AppellF1}\left[\frac{1}{2}, \right.\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left.\left.2-2m, 1+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right)^2 + \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.\left(-1+m\right) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)\right) + \right. \\
 & \left(45(3A-5B) \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) / \right. \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad 4\left(m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) + \right. \\
 & \left(25(3A-5B) \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^4\right) / \right. \\
 & \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] - \right. \\
 & \quad 4\left(m \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right) - \right. \\
 & \left(21(A+B) \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^6\right) / \right.
 \end{aligned}$$

$$\begin{aligned}
& \left(-7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \\
& 4 \left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) - \\
& \frac{1}{60} m \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \left(1 - \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right)^{2(-1+m)} \\
& \left(\frac{1}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right)^{1+2m} \\
& \left(- \left(\left(15(A+B) \operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - 4 \left(m \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. 2-2m, 1+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \right. \\
& \left(45(3A-5B) \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& 4 \left(m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right) + \\
& \left(25(3A-5B) \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \right) / \\
& \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& 4 \left(m \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(-1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3-2 m, 2 m, \frac{7}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)- \\
 & \left(21(A+B) \operatorname{AppellF1}\left[\frac{5}{2}, 2-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^6\right) / \\
 & \left(-7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left.4\left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2 m, 1+2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+(-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2 m, 2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)+ \\
 & \frac{1}{60} \operatorname{Cot}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{2(-1+m)} \\
 & \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}\right)^{2 m} \\
 & \left(-\left(\left(15(A+B)\left(m \operatorname{AppellF1}\left[\frac{1}{2}, 2-2 m, 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]- \right.\right.\right. \\
 & \left.\left.\left.\frac{1}{2}(2-2 m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right) / \\
 & \left(\operatorname{AppellF1}\left[-\frac{1}{2}, 2-2 m, 2 m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]- \right. \\
 & \left.4\left(m \operatorname{AppellF1}\left[\frac{1}{2}, 2-2 m, 1+2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right.\right. \\
 & \left.\left.(-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\right)+ \\
 & \left(45(3 A-5 B) \operatorname{AppellF1}\left[\frac{1}{2}, 2-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right) / \\
 & \left(2\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2 m, 2 m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]- \right.\right. \\
 & \left.\left.4\left(m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2 m, 1+2 m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \\
& \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - 2\left(m \text{AppellF1}\left[\frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (-1+m) \text{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \\
& \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \\
& \left(m\left(-\frac{1}{6}(1+2m) \text{AppellF1}\left[\frac{3}{2}, 2-2m, 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. + \frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{6}(2-2m) \text{AppellF1}\left[\frac{3}{2}, 3-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right) + (-1+m) \left(-\frac{1}{3}m \text{AppellF1}\left[\frac{3}{2}, 3-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right] + \frac{1}{6}(3-2m) \text{AppellF1}\left[\frac{3}{2}, 4-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]\right)\right) \Big/ \\
& \left(\text{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] - \right. \\
& \quad \left. 4\left(m \text{AppellF1}\left[\frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] + (-1+m) \text{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 - \right. \\
& \quad \left. (45(3A-5B) \text{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \right. \right. \\
& \quad \left. \left. - 2\left(m \text{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right) + (-1+m) \text{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-fx\right)\right]^2\right]\right) \Big/
\end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + 3\left(-\frac{1}{3} m \text{AppellF1}\left[\frac{3}{2},\right.\right. \\
 & \quad \left.2 - 2 m, 1 + 2 m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{1}{6}(2 - 2 m) \text{AppellF1}\left[\right. \\
 & \quad \left.\frac{3}{2}, 3 - 2 m, 2 m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] - 4 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left(m\left(-\frac{3}{10}(1 + 2 m) \text{AppellF1}\left[\frac{5}{2}, 2 - 2 m, 2 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\right. \\
 & \quad \left.\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{10}(2 - 2 m) \text{AppellF1}\left[\frac{5}{2}, 3 - 2 m, 1 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\right.\right. \\
 & \quad \left.\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \\
 & \left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right) + (-1 + m)\left(-\frac{3}{5} m \text{AppellF1}\left[\frac{5}{2}, 3 - 2 m,\right.\right. \\
 & \quad \left.1 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right] + \frac{3}{10}(3 - 2 m) \text{AppellF1}\left[\right. \\
 & \quad \left.\frac{5}{2}, 4 - 2 m, 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \\
 & \left.\text{Sec}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]\right)\right)\right) / \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, 2 - 2 m, 2 m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] -\right. \\
 & \quad \left.4\left(m \text{AppellF1}\left[\frac{3}{2}, 2 - 2 m, 1 + 2 m, \frac{5}{2},\right.\right.\right. \\
 & \quad \left.\left.\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] +\right. \\
 & \quad \left.(-1 + m) \text{AppellF1}\left[\frac{3}{2}, 3 - 2 m, 2 m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^2 - \\
 & \left(25(3 A - 5 B) \text{AppellF1}\left[\frac{3}{2}, 2 - 2 m, 2 m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^4\right. \\
 & \left.(-2\left(m \text{AppellF1}\left[\frac{5}{2}, 2 - 2 m, 1 + 2 m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2,\right.\right.\right. \\
 & \quad \left.-\text{Tan}\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - f x\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\frac{5}{2}, 3 - 2 m,\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \Big] \\
 & \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + 5\left(-\frac{3}{5}m \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. 2-2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{3}{10}(2-2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \\
 & \quad \left. \left(m\left(-\frac{5}{14}(1+2m) \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 2+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{5}{14}(2-2m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right) + (-1+m)\left(-\frac{5}{7}m \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, \right. \right. \right. \\
 & \quad \left. \left. 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right] + \frac{5}{14}(3-2m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{7}{2}, 4-2m, 2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]\right)\right)\right)\right) / \\
 & \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] - \right. \\
 & \quad \left. 4\left(m \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] + \right. \\
 & \quad \left. (-1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 + \right. \\
 & \left. (21(A+B) \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^6 \right. \\
 & \quad \left. \left(2\left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2]+(-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2 m,\right. \\
 & \left.2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]-7 \\
 & \left(-\frac{5}{7} m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2 m, 1+2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+ \right. \\
 & \left. \frac{5}{14}(2-2 m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2 m, 2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+4 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\left(m\left(-\frac{7}{18}(1+2 m) \operatorname{AppellF1}\left[\frac{9}{2}, 2-2 m, 2+2 m,\right.\right.\right. \\
 & \left.\left.\frac{11}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{7}{18}(2-2 m) \operatorname{AppellF1}\left[\frac{9}{2},\right.\right. \\
 & \left.\left.3-2 m, 1+2 m, \frac{11}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)+(-1+m) \\
 & \left(-\frac{7}{9} m \operatorname{AppellF1}\left[\frac{9}{2}, 3-2 m, 1+2 m, \frac{11}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]+\frac{7}{18}(3-2 m) \operatorname{AppellF1}\left[\frac{9}{2}, 4-2 m,\right.\right. \\
 & \left.\left.2 m, \frac{11}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right) / \\
 & \left(-7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2 m, 2 m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+4\left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2 m, 1+2 m,\right.\right.\right. \\
 & \left.\left.\frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]+ \right. \\
 & \left. (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2 m, 2 m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)
 \end{aligned}$$

Problem 1031: Unable to integrate problem.

$$\int \operatorname{Sec}[e + f x]^4 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Optimal (type 5, 135 leaves, 4 steps):

$$\frac{B \operatorname{Sec}[e + f x]^3 (a + a \operatorname{Sin}[e + f x])^m}{f (3 - m)} + \frac{1}{3 a f (3 - m)}$$

$$2^{-\frac{3}{2}+m} (A (3 - m) - B m) \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{5}{2} - m, -\frac{1}{2}, \frac{1}{2} (1 - \operatorname{Sin}[e + f x])\right]$$

$$\operatorname{Sec}[e + f x]^3 (1 + \operatorname{Sin}[e + f x])^{\frac{1}{2}-m} (a + a \operatorname{Sin}[e + f x])^{1+m}$$

Result (type 8, 33 leaves):

$$\int \operatorname{Sec}[e + f x]^4 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Problem 1032: Unable to integrate problem.

$$\int \operatorname{Sec}[e + f x]^6 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Optimal (type 5, 135 leaves, 4 steps):

$$\frac{B \operatorname{Sec}[e + f x]^5 (a + a \operatorname{Sin}[e + f x])^m}{f (5 - m)} + \frac{1}{5 a^2 f (5 - m)}$$

$$2^{-\frac{5}{2}+m} (A (5 - m) - B m) \operatorname{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{7}{2} - m, -\frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sin}[e + f x])\right]$$

$$\operatorname{Sec}[e + f x]^5 (1 + \operatorname{Sin}[e + f x])^{\frac{1}{2}-m} (a + a \operatorname{Sin}[e + f x])^{2+m}$$

Result (type 8, 33 leaves):

$$\int \operatorname{Sec}[e + f x]^6 (a + a \operatorname{Sin}[e + f x])^m (A + B \operatorname{Sin}[e + f x]) \, dx$$

Problem 1033: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (g \operatorname{Cos}[e + f x])^p (A + B \operatorname{Sin}[e + f x]) (c - c \operatorname{Sin}[e + f x])^{-4-p} \, dx$$

Optimal (type 3, 239 leaves, 4 steps):

$$\begin{aligned} & \frac{(A+B) (g \cos [e+f x])^{1+p} (c-c \sin [e+f x])^{-4-p}}{f g (7+p)} + \\ & \frac{(3 A-B(4+p)) (g \cos [e+f x])^{1+p} (c-c \sin [e+f x])^{-3-p}}{c f g (5+p)(7+p)} + \\ & \frac{2(3 A-B(4+p)) (g \cos [e+f x])^{1+p} (c-c \sin [e+f x])^{-2-p}}{c^2 f g (3+p)(5+p)(7+p)} + \\ & \frac{2(3 A-B(4+p)) (g \cos [e+f x])^{1+p} (c-c \sin [e+f x])^{-1-p}}{c^3 f g (1+p)(3+p)(5+p)(7+p)} \end{aligned}$$

Result (type 5, 1100 leaves):

$$\begin{aligned} & \frac{1}{f \left(-1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^7} \\ & \cos [e+f x]^{-p} (g \cos [e+f x])^p \left(\cos \left[\frac{1}{2}(e+f x)\right] - \sin \left[\frac{1}{2}(e+f x)\right]\right)^{-2(-4-p)-2p} \\ & (c-c \sin [e+f x])^{-4-p} \left(\frac{1 - \tan \left[\frac{1}{2}(e+f x)\right]}{\sqrt{\sec \left[\frac{1}{2}(e+f x)\right]^2}}\right)^{2p} \left(\frac{1 - \tan \left[\frac{1}{2}(e+f x)\right]^2}{1 + \tan \left[\frac{1}{2}(e+f x)\right]^2}\right)^p \\ & \left(\frac{1 - \tan \left[\frac{1}{2}(e+f x)\right]}{\sqrt{1 + \tan \left[\frac{1}{2}(e+f x)\right]^2}}\right)^{-2p} \left(-\frac{A \left(-1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^6 \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)}{1+p} - \frac{1}{7+p} 2^{4+p} A\right. \\ & \quad \text{Hypergeometric2F1}\left[-7-p, -p, -6-p, \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^{-p} - \\ & \quad \frac{1}{7+p} 2^{4+p} B \text{Hypergeometric2F1}\left[-7-p, -p, -6-p, \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \\ & \quad \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^{-p} - \frac{1}{6+p} 3 \times 2^{4+p} A \text{Hypergeometric2F1}\left[-6-p, -p, -5-p, \right. \\ & \quad \left. \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \left(-1 + \tan \left[\frac{1}{2}(e+f x)\right]\right) \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^{-p} - \\ & \quad \frac{1}{6+p} 3 \times 2^{4+p} B \text{Hypergeometric2F1}\left[-6-p, -p, -5-p, \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \\ & \quad \left(-1 + \tan \left[\frac{1}{2}(e+f x)\right]\right) \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^{-p} - \frac{1}{5+p} \\ & \quad 9 \times 2^{3+p} A \text{Hypergeometric2F1}\left[-5-p, -p, -4-p, \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \\ & \quad \left(-1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^2 \left(1 + \tan \left[\frac{1}{2}(e+f x)\right]\right)^{-p} - \frac{1}{5+p} \\ & \quad 2^{6+p} B \text{Hypergeometric2F1}\left[-5-p, -p, -4-p, \frac{1}{2}\left(1 - \tan \left[\frac{1}{2}(e+f x)\right]\right)\right] \end{aligned}$$

$$\begin{aligned} & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{4+p} \\ & 2^{6+p} A \operatorname{Hypergeometric2F1}\left[-4-p, -p, -3-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^3 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{4+p} \\ & 3 \times 2^{4+p} B \operatorname{Hypergeometric2F1}\left[-4-p, -p, -3-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^3 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{3+p} \\ & 9 \times 2^{2+p} A \operatorname{Hypergeometric2F1}\left[-3-p, -p, -2-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^4 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{3+p} \\ & 5 \times 2^{2+p} B \operatorname{Hypergeometric2F1}\left[-3-p, -p, -2-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^4 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{2+p} \\ & 3 \times 2^{2+p} A \operatorname{Hypergeometric2F1}\left[-2-p, -p, -1-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^5 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} - \frac{1}{2+p} \\ & 2^{2+p} B \operatorname{Hypergeometric2F1}\left[-2-p, -p, -1-p, \frac{1}{2}\left(1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right] \\ & \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^5 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^{-p} \end{aligned}$$

Problem 1036: Unable to integrate problem.

$$\int (g \operatorname{Cos}[e+fx])^p (A+B \operatorname{Sin}[e+fx]) (c-c \operatorname{Sin}[e+fx])^{-1-p} dx$$

Optimal (type 5, 151 leaves, 4 steps):

$$\begin{aligned} & \frac{(A+B) (g \operatorname{Cos}[e+fx])^{1+p} (c-c \operatorname{Sin}[e+fx])^{-1-p}}{fg(1+p)} - \frac{1}{fg(1+p)} \\ & 2^{\frac{1-p}{2}} B (g \operatorname{Cos}[e+fx])^{1+p} \operatorname{Hypergeometric2F1}\left[\frac{1+p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1+\operatorname{Sin}[e+fx])\right] \\ & (1-\operatorname{Sin}[e+fx])^{\frac{1+p}{2}} (c-c \operatorname{Sin}[e+fx])^{-1-p} \end{aligned}$$

Result (type 8, 40 leaves):

$$\int (g \operatorname{Cos}[e+fx])^p (A+B \operatorname{Sin}[e+fx]) (c-c \operatorname{Sin}[e+fx])^{-1-p} dx$$

Problem 1037: Unable to integrate problem.

$$\int (g \cos[e + f x])^p (A + B \sin[e + f x]) (c - c \sin[e + f x])^{-p} dx$$

Optimal (type 5, 147 leaves, 4 steps):

$$\frac{1}{f g (1+p)} 2^{\frac{1-p}{2}} c (A+Bp) (g \cos[e + f x])^{1+p} \text{Hypergeometric2F1}\left[\frac{1+p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 + \sin[e + f x])\right] \\ (1 - \sin[e + f x])^{\frac{1+p}{2}} (c - c \sin[e + f x])^{-1-p} - \frac{B (g \cos[e + f x])^{1+p} (c - c \sin[e + f x])^{-p}}{f g}$$

Result (type 8, 38 leaves):

$$\int (g \cos[e + f x])^p (A + B \sin[e + f x]) (c - c \sin[e + f x])^{-p} dx$$

Problem 1038: Unable to integrate problem.

$$\int (g \cos[e + f x])^p (A + B \sin[e + f x]) (c - c \sin[e + f x])^{1-p} dx$$

Optimal (type 5, 160 leaves, 4 steps):

$$\frac{1}{f g (1+p)} 2^{\frac{1-p}{2}} c^2 (2A - B(1-p)) (g \cos[e + f x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{1}{2} (-1+p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 + \sin[e + f x])\right] \\ (1 - \sin[e + f x])^{\frac{1+p}{2}} (c - c \sin[e + f x])^{-1-p} - \frac{B (g \cos[e + f x])^{1+p} (c - c \sin[e + f x])^{1-p}}{2 f g}$$

Result (type 8, 40 leaves):

$$\int (g \cos[e + f x])^p (A + B \sin[e + f x]) (c - c \sin[e + f x])^{1-p} dx$$

Problem 1039: Attempted integration timed out after 120 seconds.

$$\int (g \cos[e + f x])^p (A + B \sin[e + f x]) (c - c \sin[e + f x])^{2-p} dx$$

Optimal (type 5, 163 leaves, 4 steps):

$$\frac{1}{3 f g (1+p)} 2^{\frac{5-p}{2}} c^3 (3A - B(2-p)) (g \cos[e + f x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{1}{2} (-3+p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 + \sin[e + f x])\right] \\ (1 - \sin[e + f x])^{\frac{1+p}{2}} (c - c \sin[e + f x])^{-1-p} - \frac{B (g \cos[e + f x])^{1+p} (c - c \sin[e + f x])^{2-p}}{3 f g}$$

Result (type 1, 1 leaves):

???

Problem 1042: Result more than twice size of optimal antiderivative.

$$\int (g \cos [e + f x])^p (a + a \sin [e + f x])^m (c + d \sin [e + f x])^n dx$$

Optimal (type 6, 168 leaves, 4 steps):

$$\frac{1}{a f (1 + 2 m + p)} 2^{\frac{1+p}{2}} g \operatorname{AppellF1}\left[\frac{1}{2} (1 + 2 m + p), \frac{1-p}{2}, -n, \frac{1}{2} (3 + 2 m + p), \frac{1}{2} (1 + \sin [e + f x]), -\frac{d (1 + \sin [e + f x])}{c-d}\right] (g \cos [e + f x])^{-1+p} (1 - \sin [e + f x])^{\frac{1-p}{2}} (a + a \sin [e + f x])^{1+m} (c + d \sin [e + f x])^n \left(\frac{c + d \sin [e + f x]}{c-d}\right)^{-n}$$

Result (type 6, 4377 leaves):

$$\begin{aligned} & - \left(\left(2 (c + d) (3 + p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1 + m + n + p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \\ & \quad \left. \left. \left. - \frac{(c-d) \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \cos [e + f x]^p (g \cos [e + f x])^p \left(\sec\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2\right)^{-1-m} \right. \right. \\ & \quad \left. \left. (a + a \sin [e + f x])^m (c + d \sin [e + f x])^{2n} \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right] \right) \right) / \\ & \left(f (1 + p) \left((c + d) (3 + p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1 + m + n + p, -n, \frac{3+p}{2}, \right. \right. \right. \\ & \quad \left. \left. \left. -\tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\frac{(c-d) \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] - \right. \right. \\ & \quad \left. \left. 2 \left((-c + d) n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1 + m + n + p, 1 - n, \frac{5+p}{2}, -\tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, \right. \right. \right. \right. \\ & \quad \left. \left. \left. - \frac{(c-d) \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] + (c + d) (1 + m + n + p) \operatorname{AppellF1}\left[\frac{3+p}{2}, \right. \right. \right. \\ & \quad \left. \left. \left. 2 + m + n + p, -n, \frac{5+p}{2}, -\tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2, -\frac{(c-d) \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{c+d}\right] \right) \right) \right) \\ & \tan\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 \left((c + d) (3 + p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1 + m + n + p, -n, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d} \\
 & \cos[ex+fx]^p \left(\sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-m} (c+d \sin[ex+fx])^n \Big/ \\
 & \left((1+p) \left((c+d)(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] - 2 \left((-c+d)n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + (c+d) \right. \right. \right. \\
 & \quad \left. \left. \left. (1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+n+p, -n, \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \left(2d(c+d)n(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \cos[ex+fx]^{1+p} \right. \\
 & \quad \left. \left(\sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2\right)^{-1-m} (c+d \sin[ex+fx])^{-1+n} \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \Big/ \\
 & \left((1+p) \left((c+d)(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] - 2 \left((-c+d)n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + (c+d) \right. \right. \right. \\
 & \quad \left. \left. \left. (1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+n+p, -n, \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) + \\
 & \left(2(c+d)p(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \operatorname{Cos}[e+f x]^{-1+p} \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} \\
 & \operatorname{Sin}[e+f x] (c+d \operatorname{Sin}[e+f x])^n \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \Big/ \\
 & \left((1+p) \left((c+d) (3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - 2 \left((-c+d) n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] + (c+d) \right. \right. \right. \\
 & \quad \left. \left. \left. (1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+n+p, -n, \frac{5+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) \right) + \\
 & \left(2(c+d) (-1-m) (3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Cos}[e+f x]^p \right. \\
 & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} (c+d \operatorname{Sin}[e+f x])^n \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) \right) \Big/ \\
 & \left((1+p) \left((c+d) (3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - 2 \left((-c+d) n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] + (c+d) \right. \right. \right. \\
 & \quad \left. \left. \left. (1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+n+p, -n, \frac{5+p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) \right) + \\
 & \left(2(c+d) (3+p) \operatorname{Cos}[e+f x]^p \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} (c+d \operatorname{Sin}[e+f x])^n \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left[\left((c-d)n(1+p) \operatorname{AppellF1}\left[1 + \frac{1+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right] / \left((c+d)(3+p) - \right. \\
 & \quad \left. \frac{1}{3+p}(1+p)(1+m+n+p) \operatorname{AppellF1}\left[1 + \frac{1+p}{2}, 2+m+n+p, -n, 1 + \frac{3+p}{2}, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right] / \\
 & \left((1+p) \left((c+d)(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] - 2 \left((-c+d)n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + (c+d) \right. \right. \\
 & \quad \left. \left. (1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+n+p, -n, \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \left(2(c+d)(3+p) \operatorname{AppellF1}\left[\frac{1+p}{2}, 1+m+n+p, -n, \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \cos[e+fx]^p \right. \\
 & \quad \left. \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{-1-m} (c+d \sin[e+fx])^n \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right. \\
 & \quad \left. \left(-2 \left((-c+d)n \operatorname{AppellF1}\left[\frac{3+p}{2}, 1+m+n+p, 1-n, \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] + (c+d)(1+m+n+p) \operatorname{AppellF1}\left[\frac{3+p}{2}, 2+m+ \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. n + p, -n, \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \Bigg) \\
 & \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] + (c+d)(3+p) \\
 & \left(\left((c-d)n(1+p) \operatorname{AppellF1}\left[1 + \frac{1+p}{2}, 1+m+n+p, 1-n, 1 + \frac{3+p}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) / ((c+d)(3+p)) - \\
 & \frac{1}{3+p}(1+p)(1+m+n+p) \operatorname{AppellF1}\left[1 + \frac{1+p}{2}, 2+m+n+p, -n, \right. \\
 & \quad \left. 1 + \frac{3+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \\
 & \quad \left. \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) - 2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \\
 & \left((-c+d)n \left(- \left(\left((c-d)(1-n)(3+p) \operatorname{AppellF1}\left[1 + \frac{3+p}{2}, 1+m+n+p, 2-n, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \right) / ((c+d)(5+p)) \right) - \\
 & \frac{1}{5+p}(3+p)(1+m+n+p) \operatorname{AppellF1}\left[1 + \frac{3+p}{2}, 2+m+n+p, 1-n, \right. \\
 & \quad \left. 1 + \frac{5+p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \\
 & \quad \left. \sec\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) + (c+d)(1+m+n+p) \\
 & \left(\left((c-d)n(3+p) \operatorname{AppellF1}\left[1 + \frac{3+p}{2}, 2+m+n+p, 1-n, 1 + \frac{5+p}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) \right)
 \end{aligned}$$

Problem 1044: Unable to integrate problem.

$$\int (g \cos[e + f x])^p (a + a \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

Optimal (type 6, 145 leaves, 3 steps):

$$-\frac{1}{f g (1+p)} 2^{\frac{3+p}{2}} a \operatorname{AppellF1}\left[\frac{1+p}{2}, \frac{1}{2}(-1-p), -n, \frac{3+p}{2}, \frac{1}{2}(1-\sin[e + f x]), \frac{d(1-\sin[e + f x])}{c+d}\right] (g \cos[e + f x])^{1+p} (1 + \sin[e + f x])^{\frac{1}{2}(-1-p)} (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d}\right)^{-n}$$

Result (type 8, 35 leaves):

$$\int (g \cos[e + f x])^p (a + a \sin[e + f x]) (c + d \sin[e + f x])^n dx$$

Problem 1045: Unable to integrate problem.

$$\int \frac{(g \cos[e + f x])^p (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

Optimal (type 6, 149 leaves, 3 steps):

$$-\frac{1}{a f g (1+p)} 2^{-\frac{1}{2}+\frac{p}{2}} \operatorname{AppellF1}\left[\frac{1+p}{2}, \frac{3-p}{2}, -n, \frac{3+p}{2}, \frac{1}{2}(1-\sin[e + f x]), \frac{d(1-\sin[e + f x])}{c+d}\right] (g \cos[e + f x])^{1+p} (1 + \sin[e + f x])^{-1+\frac{1-p}{2}} (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d}\right)^{-n}$$

Result (type 8, 37 leaves):

$$\int \frac{(g \cos[e + f x])^p (c + d \sin[e + f x])^n}{a + a \sin[e + f x]} dx$$

Problem 1046: Unable to integrate problem.

$$\int \frac{(g \cos[e + f x])^p (c + d \sin[e + f x])^n}{(a + a \sin[e + f x])^2} dx$$

Optimal (type 6, 149 leaves, 3 steps):

$$-\frac{1}{a^2 f g (1+p)} 2^{-\frac{3}{2}+\frac{p}{2}} \operatorname{AppellF1}\left[\frac{1+p}{2}, \frac{5-p}{2}, -n, \frac{3+p}{2}, \frac{1}{2}(1-\sin[e + f x]), \frac{d(1-\sin[e + f x])}{c+d}\right] (g \cos[e + f x])^{1+p} (1 + \sin[e + f x])^{-2+\frac{3-p}{2}} (c + d \sin[e + f x])^n \left(\frac{c + d \sin[e + f x]}{c + d}\right)^{-n}$$

Result (type 8, 37 leaves):

$$\int \frac{(g \cos [e + f x])^p (c + d \sin [e + f x])^n}{(a + a \sin [e + f x])^2} dx$$

Problem 1047: Unable to integrate problem.

$$\int \frac{(g \cos [e + f x])^p (c + d \sin [e + f x])^n}{(a + a \sin [e + f x])^3} dx$$

Optimal (type 6, 149 leaves, 3 steps):

$$-\frac{1}{a^3 f g (1+p)} 2^{-\frac{5+p}{2}} \text{AppellF1}\left[\frac{1+p}{2}, \frac{7-p}{2}, -n, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [e + f x]), \frac{d (1 - \sin [e + f x])}{c+d}\right] \\ (g \cos [e + f x])^{1+p} (1 + \sin [e + f x])^{-3+\frac{5-p}{2}} (c + d \sin [e + f x])^n \left(\frac{c + d \sin [e + f x]}{c+d}\right)^{-n}$$

Result (type 8, 37 leaves):

$$\int \frac{(g \cos [e + f x])^p (c + d \sin [e + f x])^n}{(a + a \sin [e + f x])^3} dx$$

Problem 1048: Unable to integrate problem.

$$\int \frac{(g \cos [e + f x])^p (c + d \sin [e + f x])^n}{(a + a \sin [e + f x])^4} dx$$

Optimal (type 6, 149 leaves, 3 steps):

$$-\frac{1}{a^4 f g (1+p)} 2^{-\frac{7+p}{2}} \text{AppellF1}\left[\frac{1+p}{2}, \frac{9-p}{2}, -n, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [e + f x]), \frac{d (1 - \sin [e + f x])}{c+d}\right] \\ (g \cos [e + f x])^{1+p} (1 + \sin [e + f x])^{-4+\frac{7-p}{2}} (c + d \sin [e + f x])^n \left(\frac{c + d \sin [e + f x]}{c+d}\right)^{-n}$$

Result (type 8, 37 leaves):

$$\int \frac{(g \cos [e + f x])^p (c + d \sin [e + f x])^n}{(a + a \sin [e + f x])^4} dx$$

Problem 1049: Result more than twice size of optimal antiderivative.

$$\int (g \sec [e + f x])^p (a + a \sin [e + f x])^m (c + d \sin [e + f x])^n dx$$

Optimal (type 6, 175 leaves, 5 steps):

$$\frac{1}{a f (1+2 m-p) 2^{\frac{1-p}{2}}}$$

$$\text{AppellF1}\left[\frac{1}{2}(1+2 m-p), \frac{1+p}{2}, -n, \frac{1}{2}(3+2 m-p), \frac{1}{2}(1+\text{Sin}[e+f x]), -\frac{d(1+\text{Sin}[e+f x])}{c-d}\right]$$

$$\text{Sec}[e+f x] (g \text{Sec}[e+f x])^p (1-\text{Sin}[e+f x])^{\frac{1+p}{2}}$$

$$(a+a \text{Sin}[e+f x])^{1+m} (c+d \text{Sin}[e+f x])^n \left(\frac{c+d \text{Sin}[e+f x]}{c-d}\right)^{-n}$$

Result(type 6, 4680 leaves):

$$-\left(\left(2(c+d)(-3+p) \text{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.$$

$$\left.\left.-\frac{(c-d) \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]\left(\text{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} \text{Sec}[e+f x]^p\right.$$

$$\left.\left.(g \text{Sec}[e+f x])^p (a+a \text{Sin}[e+f x])^m (c+d \text{Sin}[e+f x])^{2n} \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right/$$

$$\left(f(1-p)\left((c+d)(-3+p) \text{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2},\right.\right.\right.$$

$$\left.\left.-\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\frac{(c-d) \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]-\right.$$

$$2\left((c-d)n \text{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.$$

$$\left.\left.-\frac{(c-d) \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]-(c+d)(1+m+n-p) \text{AppellF1}\left[\frac{3-p}{2},\right.\right.$$

$$\left.\left.2+m+n-p, -n, \frac{5-p}{2}, -\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\frac{(c-d) \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]\right)$$

$$\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)\left(\left((c+d)(-3+p) \text{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n,\right.\right.\right.$$

$$\left.\left.\frac{3-p}{2}, -\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,-\frac{(c-d) \text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right]\right)^{-m} \text{Sec}[e+f x]^p (c+d \text{Sin}[e+f x])^n\right)\left/\left((1-p)\right.\right.$$

$$\left.\left((c+d)(-3+p) \text{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\text{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2,\right.\right.\right.$$

$$\begin{aligned}
 & - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \Bigg] - 2 \left((c-d) n \operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - (c+d) \right. \\
 & \quad \left. (1+m+n-p) \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \Bigg) - \\
 & \left(2 d (c+d) n (-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^{-1+p} (c+d \operatorname{Sin}[e+f x])^{-1+n} \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) / \left((1-p) \right. \\
 & \quad \left((c+d) (-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - 2 \left((c-d) n \operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - (c+d) \right. \\
 & \quad \left. (1+m+n-p) \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \Bigg) - \\
 & \left(2 (c+d) (-3+p) p \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right)^{-1-m} \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^{1+p} \operatorname{Sin}[e+f x] (c+d \operatorname{Sin}[e+f x])^n \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) / \\
 & \left((1-p) \left((c+d) (-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - \\
 & 2\left((c-d)n\operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \right. \\
 & \quad \left. -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - (c+d)(1+m+n-p) \\
 & \quad \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \\
 & \quad \left. -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) + \\
 & \left(2(c+d)(-1-m)(-3+p)\operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \\
 & \quad \left. \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)^{-1-m} \operatorname{Sec}[e+f x]^p (c+d \operatorname{Sin}[e+f x])^n \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) / \\
 & \left((1-p)\left((c+d)(-3+p)\operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - \right. \\
 & \quad \left. 2\left((c-d)n\operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] - (c+d)(1+m+n-p) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2\right) \right) + \\
 & \left(2(c+d)(-3+p)\left(\operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)^{-1-m} \operatorname{Sec}[e+f x]^p (c+d \operatorname{Sin}[e+f x])^n \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \left[\left((c-d)n(1-p) \operatorname{AppellF1}\left[1 + \frac{1-p}{2}, 1+m+n-p, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{3-p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right)^2 \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right] / ((c+d)(3-p)) - \\
 & \quad \frac{1}{3-p}(1-p)(1+m+n-p) \operatorname{AppellF1}\left[1 + \frac{1-p}{2}, 2+m+n-p, -n, 1 + \frac{3-p}{2}, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right] \right] / \\
 & \left((1-p) \left((c+d)(-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right)^2 - \right. \\
 & \quad \left. 2 \left((c-d)n \operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] - (c+d)(1+m+n-p) \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \right) \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right) \right) - \\
 & \left(2(c+d)(-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\frac{(c-d)\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{c+d}\right] \left(\operatorname{Sec}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \right)^{-1-m} \right. \\
 & \quad \left. \operatorname{Sec}[e+fx]^p (c+d \sin[e+fx])^n \tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \right) \\
 & \left(-2 \left((c-d)n \operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\tan\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & - \frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} - (c+d) (1+m+n-p) \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] + (c+d) (-3+p) \\
 & \left(\left((c-d) n (1-p) \operatorname{AppellF1}\left[1+\frac{1-p}{2}, 1+m+n-p, 1-n, 1+\frac{3-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) / ((c+d) (3-p)) - \right. \\
 & \left. \frac{1}{3-p} (1-p) (1+m+n-p) \operatorname{AppellF1}\left[1+\frac{1-p}{2}, 2+m+n-p, -n, 1+\frac{3-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) - 2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \\
 & \left((c-d) n \left(- \left(\left((c-d) (1-n) (3-p) \operatorname{AppellF1}\left[1+\frac{3-p}{2}, 1+m+n-p, 2-n, 1+\frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \right. \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) / ((c+d) (5-p)) \right) - \right. \\
 & \left. \frac{1}{5-p} (3-p) (1+m+n-p) \operatorname{AppellF1}\left[1+\frac{3-p}{2}, 2+m+n-p, 1-n, 1+\frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \right) - (c+d) (1+m+n-p) \\
 & \left(\left((c-d) n (3-p) \operatorname{AppellF1}\left[1+\frac{3-p}{2}, 2+m+n-p, 1-n, 1+\frac{5-p}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \\
 & \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right] \Bigg/ ((c+d)(5-p)) - \\
 & \frac{1}{5-p}(3-p)(2+m+n-p) \operatorname{AppellF1}\left[1+\frac{3-p}{2}, 3+m+n-p, -n, \right. \\
 & \left. 1+\frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]\right)\right] \Bigg/ \\
 & \left((1-p) \left((c+d)(-3+p) \operatorname{AppellF1}\left[\frac{1-p}{2}, 1+m+n-p, -n, \frac{3-p}{2}, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \right] - \right. \\
 & \left. 2 \left((c-d) n \operatorname{AppellF1}\left[\frac{3-p}{2}, 1+m+n-p, 1-n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \right] - (c+d)(1+m+n-p) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3-p}{2}, 2+m+n-p, -n, \frac{5-p}{2}, -\operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\frac{(c-d) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2}{c+d} \right] \right) \operatorname{Tan}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-f x\right)\right]^2 \right) \right) \Bigg)
 \end{aligned}$$

Problem 1065: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^2 \operatorname{Csc}[c+d x]^2 (a+b \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 96 leaves, 6 steps):

$$\begin{aligned}
 & -b^2 x + \frac{a b \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{d} + \frac{(a^2-2 b^2) \operatorname{Cot}[c+d x]}{3 d} - \\
 & \frac{a b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{3 d} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2 (a+b \operatorname{Sin}[c+d x])^2}{3 d}
 \end{aligned}$$

Result (type 3, 538 leaves):

$$\begin{aligned}
 & - \frac{b^2 (c + dx) (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sin}[c + dx]^2}{d (a + b \operatorname{Sin}[c + dx])^2} + \\
 & \left(\left(a^2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - 3b^2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \right) \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right] (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sin}[c + dx]^2 \right) / \\
 & \left(6d (a + b \operatorname{Sin}[c + dx])^2 \right) - \frac{ab \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^2 (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sin}[c + dx]^2}{4d (a + b \operatorname{Sin}[c + dx])^2} - \\
 & \left(a^2 \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^2 (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sin}[c + dx]^2 \right) / \\
 & \left(24d (a + b \operatorname{Sin}[c + dx])^2 \right) + \frac{ab (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right] \operatorname{Sin}[c + dx]^2}{d (a + b \operatorname{Sin}[c + dx])^2} - \\
 & \frac{ab (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \operatorname{Sin}[c + dx]^2}{d (a + b \operatorname{Sin}[c + dx])^2} + \\
 & \frac{ab (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Sin}[c + dx]^2}{4d (a + b \operatorname{Sin}[c + dx])^2} + \left((b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \right. \\
 & \left. \left(-a^2 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + 3b^2 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \operatorname{Sin}[c + dx]^2 \right) / \left(6d (a + b \operatorname{Sin}[c + dx])^2 \right) + \\
 & \left(a^2 (b + a \operatorname{Csc}[c + dx])^2 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Sin}[c + dx]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right) / \\
 & \left(24d (a + b \operatorname{Sin}[c + dx])^2 \right)
 \end{aligned}$$

Problem 1066: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c + dx]^2 \operatorname{Csc}[c + dx]^3 (a + b \operatorname{Sin}[c + dx])^2 dx$$

Optimal (type 3, 123 leaves, 8 steps):

$$\frac{(a^2 + 4b^2) \operatorname{ArcTanh}[\operatorname{Cos}[c + dx]]}{8d} + \frac{2ab \operatorname{Cot}[c + dx]}{3d} + \frac{(a^2 - 2b^2) \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]}{8d} - \\
 \frac{ab \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]^2}{6d} - \frac{\operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]^3 (a + b \operatorname{Sin}[c + dx])^2}{4d}$$

Result (type 3, 579 leaves):

$$\begin{aligned}
 & \frac{a b \cot\left[\frac{1}{2}(c+d x)\right] (b+a \csc [c+d x])^2 \sin [c+d x]^2}{3 d (a+b \sin [c+d x])^2} + \\
 & \frac{(a^2-4 b^2) \csc\left[\frac{1}{2}(c+d x)\right]^2 (b+a \csc [c+d x])^2 \sin [c+d x]^2}{32 d (a+b \sin [c+d x])^2} - \\
 & \left(a b \cot\left[\frac{1}{2}(c+d x)\right] \csc\left[\frac{1}{2}(c+d x)\right]^2 (b+a \csc [c+d x])^2 \sin [c+d x]^2 \right) / \\
 & \left(12 d (a+b \sin [c+d x])^2 \right) - \frac{a^2 \csc\left[\frac{1}{2}(c+d x)\right]^4 (b+a \csc [c+d x])^2 \sin [c+d x]^2}{64 d (a+b \sin [c+d x])^2} + \\
 & \frac{(a^2+4 b^2) (b+a \csc [c+d x])^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x]^2}{8 d (a+b \sin [c+d x])^2} + \\
 & \frac{(-a^2-4 b^2) (b+a \csc [c+d x])^2 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+d x)\right]\right] \sin [c+d x]^2}{8 d (a+b \sin [c+d x])^2} + \\
 & \frac{(-a^2+4 b^2) (b+a \csc [c+d x])^2 \sec\left[\frac{1}{2}(c+d x)\right]^2 \sin [c+d x]^2}{32 d (a+b \sin [c+d x])^2} + \\
 & \frac{a^2 (b+a \csc [c+d x])^2 \sec\left[\frac{1}{2}(c+d x)\right]^4 \sin [c+d x]^2}{64 d (a+b \sin [c+d x])^2} - \\
 & \frac{a b (b+a \csc [c+d x])^2 \sin [c+d x]^2 \tan\left[\frac{1}{2}(c+d x)\right]}{3 d (a+b \sin [c+d x])^2} + \\
 & \left(a b (b+a \csc [c+d x])^2 \sec\left[\frac{1}{2}(c+d x)\right]^2 \sin [c+d x]^2 \tan\left[\frac{1}{2}(c+d x)\right] \right) / \\
 & \left(12 d (a+b \sin [c+d x])^2 \right)
 \end{aligned}$$

Problem 1074: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^2 \csc [c+d x]^2 (a+b \sin [c+d x])^3 dx$$

Optimal (type 3, 138 leaves, 7 steps):

$$\begin{aligned}
 & -3 a b^2 x + \frac{b (3 a^2-2 b^2) \operatorname{ArcTanh}\left[\cos [c+d x]\right]}{2 d} + \frac{11 b^3 \cos [c+d x]}{6 d} + \frac{a (a^2-3 b^2) \cot [c+d x]}{3 d} - \\
 & \frac{b \cot [c+d x] \csc [c+d x] (a+b \sin [c+d x])^2}{2 d} - \frac{\cot [c+d x] \csc [c+d x]^2 (a+b \sin [c+d x])^3}{3 d}
 \end{aligned}$$

Result (type 3, 615 leaves):

$$\begin{aligned}
 & - \frac{3 a b^2 (c+d x) (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{d (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \frac{b^3 \operatorname{Cos}[c+d x] (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{d (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \left(\left(a^3 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - 9 a b^2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right] \right. \\
 & \quad \left. (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3 \right) / (6 d (a+b \operatorname{Sin}[c+d x])^3) - \\
 & \frac{3 a^2 b \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{8 d (a+b \operatorname{Sin}[c+d x])^3} - \\
 & \left(a^3 \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3 \right) / \\
 & \quad (24 d (a+b \operatorname{Sin}[c+d x])^3) + \\
 & \left((3 a^2 b - 2 b^3) (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x]^3 \right) / \\
 & \quad (2 d (a+b \operatorname{Sin}[c+d x])^3) + \\
 & \left((-3 a^2 b + 2 b^3) (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x]^3 \right) / \\
 & \quad (2 d (a+b \operatorname{Sin}[c+d x])^3) + \frac{3 a^2 b (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]^3}{8 d (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \left((b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \left(-a^3 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 9 a b^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right. \\
 & \quad \left. \operatorname{Sin}[c+d x]^3 \right) / (6 d (a+b \operatorname{Sin}[c+d x])^3) + \\
 & \left(a^3 (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right) / \\
 & \quad (24 d (a+b \operatorname{Sin}[c+d x])^3)
 \end{aligned}$$

Problem 1075: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^2 \operatorname{Csc}[c+d x]^3 (a+b \operatorname{Sin}[c+d x])^3 dx$$

Optimal (type 3, 152 leaves, 7 steps):

$$\begin{aligned}
 & -b^3 x + \frac{a (a^2 + 12 b^2) \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{8 d} + \\
 & \frac{b (2 a^2 - b^2) \operatorname{Cot}[c+d x]}{2 d} + \frac{a (a^2 - 2 b^2) \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{8 d} - \\
 & \frac{b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2 (a+b \operatorname{Sin}[c+d x])^2}{4 d} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3 (a+b \operatorname{Sin}[c+d x])^3}{4 d}
 \end{aligned}$$

Result (type 3, 690 leaves):

$$\begin{aligned}
 & - \frac{b^3 (c+dx) (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sin}[c+dx]^3}{d (a+b \operatorname{Sin}[c+dx])^3} + \\
 & \left(\left(a^2 b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - b^3 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right] (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sin}[c+dx]^3 \right) / \\
 & \left(2d (a+b \operatorname{Sin}[c+dx])^3 \right) + \frac{(a^3 - 12ab^2) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sin}[c+dx]^3}{32d (a+b \operatorname{Sin}[c+dx])^3} - \\
 & \left(a^2 b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sin}[c+dx]^3 \right) / \\
 & \left(8d (a+b \operatorname{Sin}[c+dx])^3 \right) - \frac{a^3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sin}[c+dx]^3}{64d (a+b \operatorname{Sin}[c+dx])^3} + \\
 & \left((a^3 + 12ab^2) (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx]^3 \right) / \\
 & \left(8d (a+b \operatorname{Sin}[c+dx])^3 \right) + \\
 & \left((-a^3 - 12ab^2) (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx]^3 \right) / \\
 & \left(8d (a+b \operatorname{Sin}[c+dx])^3 \right) + \frac{(-a^3 + 12ab^2) (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx]^3}{32d (a+b \operatorname{Sin}[c+dx])^3} + \\
 & \frac{a^3 (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Sin}[c+dx]^3}{64d (a+b \operatorname{Sin}[c+dx])^3} + \left((b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left(-a^2 b \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + b^3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sin}[c+dx]^3 \right) / \left(2d (a+b \operatorname{Sin}[c+dx])^3 \right) + \\
 & \left(a^2 b (b+a \operatorname{Csc}[c+dx])^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx]^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left(8d (a+b \operatorname{Sin}[c+dx])^3 \right)
 \end{aligned}$$

Problem 1091: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[e+fx]^2}{\sqrt{d \operatorname{Sin}[e+fx]} (a+b \operatorname{Sin}[e+fx])^{5/2}} dx$$

Optimal (type 4, 347 leaves, 5 steps):

$$\frac{2 \operatorname{Cos}[e + f x] \sqrt{d \operatorname{Sin}[e + f x]}}{3 a d f (a + b \operatorname{Sin}[e + f x])^{3/2}} + \frac{4 b \operatorname{Cos}[e + f x]}{3 a (a^2 - b^2) f \sqrt{d \operatorname{Sin}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]}} -$$

$$\frac{1}{3 a^3 \sqrt{a + b} \sqrt{d} f} 4 b \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}}$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}}\right], -\frac{a + b}{a - b}\right] \operatorname{Tan}[e + f x] -$$

$$\frac{1}{3 a^2 \sqrt{a + b} \sqrt{d} f} 4 \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}}$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}}\right], -\frac{a + b}{a - b}\right] \operatorname{Tan}[e + f x]$$

Result (type 4, 4525 leaves):

$$\left(\operatorname{Sin}[e + f x] \sqrt{a + b \operatorname{Sin}[e + f x]} \left(\frac{2 \operatorname{Cos}[e + f x]}{3 a (a + b \operatorname{Sin}[e + f x])^2} - \frac{4 b^2 \operatorname{Cos}[e + f x]}{3 a^2 (a^2 - b^2) (a + b \operatorname{Sin}[e + f x])} \right) \right) /$$

$$\left(f \sqrt{d \operatorname{Sin}[e + f x]} \right) +$$

$$\left(2 \sqrt{\operatorname{Sin}[e + f x]} \left(\frac{2 \sqrt{a + b \operatorname{Sin}[e + f x]}}{3 a (a^2 - b^2) \sqrt{\operatorname{Sin}[e + f x]}} - \frac{4 b \sqrt{\operatorname{Sin}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]}}{3 a^2 (a^2 - b^2)} \right) \right)$$

$$\sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2}}$$

$$\left(-\frac{2 b \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2} + 2 \sqrt{-a^2 + b^2} \sqrt{\frac{a \left(a + 2 b \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right)}{a^2 - b^2}} \right)$$

$$\left(-b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{-b + \sqrt{-a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}}{\sqrt{-a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{-a^2 + b^2}}{-b + \sqrt{-a^2 + b^2}}\right] \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] + \right)$$

$$a \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}}\right]$$

$$\left. \left. \left. \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\right| \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right| \right| /$$

$$\left. \left. \left. \left(\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\left(a+2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right| \right| /$$

$$\left(3a^2(a^2-b^2) f \sqrt{d \operatorname{Sin}[e+fx]} \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{2+2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}} \right)$$

$$\left(-\frac{1}{3a^2(a^2-b^2)\left(\frac{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{2+2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^{3/2}} \sqrt{\frac{a+2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}} \right)$$

$$\left(-\frac{2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(2+2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2\left(2+2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)} \right)$$

$$\left(-\frac{2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} + \right)$$

$$\left(2 \sqrt{-a^2 + b^2} \sqrt{\frac{a \left(a + 2 b \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] \right)^2}{a^2 - b^2}} \right.$$

$$\left. - b \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{-b + \sqrt{-a^2 + b^2} - a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{\sqrt{-a^2 + b^2}}}}{\sqrt{2}} \right] \right], \frac{2 \sqrt{-a^2 + b^2}}{-b + \sqrt{-a^2 + b^2}} \right]$$

$$\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{\sqrt{-a^2 + b^2}}}}{\sqrt{2}} \right] \right],$$

$$\left. \left. \frac{2 \sqrt{-a^2 + b^2}}{b + \sqrt{-a^2 + b^2}} \sqrt{\frac{a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{-b + \sqrt{-a^2 + b^2}}} \sqrt{-\frac{a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \right] \right) /$$

$$\left(\sqrt{\frac{a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{-b + \sqrt{-a^2 + b^2}}} \left(a + 2 b \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] \right)^2 \right) + \left(1 / \left(3 a^2 \right. \right.$$

$$\left. \left. (a^2 - b^2) \sqrt{\frac{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{2 + 2 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^2}} \sqrt{\frac{a + 2 b \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^2}{1 + \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^2}} \right) \right)$$

$$\left(\frac{b \operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 + a \operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^2} - \right.$$

$$\left. \left(\operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] \left(a + 2 b \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^2 \right) \right) /$$

$$\left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \left(-\frac{2b \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} + \right.$$

$$\left. 2\sqrt{-a^2+b^2} \sqrt{\frac{a\left(a+2b \tan\left[\frac{1}{2}(e+fx)\right]\right) + a \tan\left[\frac{1}{2}(e+fx)\right]^2}{a^2-b^2}} \right.$$

$$\left. -b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{-b+\sqrt{-a^2+b^2}-a \tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}\right], \frac{2\sqrt{-a^2+b^2}}{-b+\sqrt{-a^2+b^2}}\right] \right.$$

$$\left. \tan\left[\frac{1}{2}(e+fx)\right] + a \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{b+\sqrt{-a^2+b^2}+a \tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}\right], \sqrt{2}\right] \right),$$

$$\left. \left. \left. \frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \sqrt{\frac{a \tan\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}} \sqrt{\frac{a \tan\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right] \right) \right)$$

$$\left. \left. \left. \left. \left. \sqrt{\frac{a \tan\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}} \left(a+2b \tan\left[\frac{1}{2}(e+fx)\right]\right) + a \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \right) +$$

$$\frac{1}{3a^2(a^2-b^2)} \sqrt{\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{2+2 \tan\left[\frac{1}{2}(e+fx)\right]^2}} \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(e+fx)\right] + a \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}}$$

$$\left(\frac{2 b \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^3}{\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right)^2} - \frac{2 b \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{1+\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} \right) +$$

$$\left(a \sqrt{-a^2+b^2} \left(b \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 + a \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \right) \right)$$

$$\left(-b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{-b+\sqrt{-a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{-a^2+b^2}}{-b+\sqrt{-a^2+b^2}}\right] \right)$$

$$\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] + a \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}}\right], \right)$$

$$\left. \left. \left. \frac{2 \sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \right] \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{-b+\sqrt{-a^2+b^2}}} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{b+\sqrt{-a^2+b^2}}}\right) \right) \right)$$

$$\left((a^2-b^2) \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{-b+\sqrt{-a^2+b^2}}} \left(a+2 b \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right) \right)$$

$$\left(\sqrt{\frac{a \left(a+2 b \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)}{a^2-b^2}} \right) -$$

$$\left(1 / \left(\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]}{-b+\sqrt{-a^2+b^2}}} \left(a+2 b \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^2 \right) \right)$$

$$\begin{aligned}
 & 2\sqrt{-a^2+b^2} \left(b \operatorname{Sec} \left[\frac{1}{2} (e+fx) \right]^2 + a \operatorname{Sec} \left[\frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right] \right) \\
 & \sqrt{\frac{a \left(a + 2b \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]^2 \right)}{a^2 - b^2}} \\
 & \left(-b \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{-b+\sqrt{-a^2+b^2} - a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}} \right], \frac{2\sqrt{-a^2+b^2}}{-b+\sqrt{-a^2+b^2}} \right] \operatorname{Tan} \left[\right. \right. \\
 & \left. \left. \frac{1}{2} (e+fx) \right] + a \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2} + a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}} \right], \right. \right. \\
 & \left. \left. \frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \right] \sqrt{\frac{a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{-b+\sqrt{-a^2+b^2}}} \sqrt{\frac{a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{b+\sqrt{-a^2+b^2}}} \right) - \\
 & \left(a \sqrt{-a^2+b^2} \operatorname{Sec} \left[\frac{1}{2} (e+fx) \right]^2 \sqrt{\frac{a \left(a + 2b \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right] + a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]^2 \right)}{a^2 - b^2}} \right. \\
 & \left. -b \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{-b+\sqrt{-a^2+b^2} - a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}} \right], \frac{2\sqrt{-a^2+b^2}}{-b+\sqrt{-a^2+b^2}} \right] \operatorname{Tan} \left[\right. \right. \\
 & \left. \left. \frac{1}{2} (e+fx) \right] + a \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2} + a \operatorname{Tan} \left[\frac{1}{2} (e+fx) \right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}} \right], \frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \right] \right)
 \end{aligned}$$

$$\left. \left. \left. \left. \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\right]}{\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}}\right) \right) \right) / \left(2 \left(-b + \sqrt{-a^2+b^2} \right) \right)$$

$$\left(\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}} \right)^{3/2} \left(a + 2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) +$$

$$\left(1 / \left(\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\left(a + 2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right)$$

$$2\sqrt{-a^2+b^2} \sqrt{\frac{a \left(a + 2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)}{a^2-b^2}}$$

$$\left(-\frac{1}{2} b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{-b+\sqrt{-a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{-a^2+b^2}}{-b+\sqrt{-a^2+b^2}} \right] \right)$$

$$\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 - \left(a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}}\right], \right) \right)$$

$$\frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\right) / \left(4 \left(b + \sqrt{-a^2+b^2} \right) \right)$$

$$\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right) + \left(a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}}}{\sqrt{2}}}\right], \right) \right)$$

$$\left. \frac{2\sqrt{-a^2+b^2}}{b+\sqrt{-a^2+b^2}} \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right/$$

$$\left(4(-b+\sqrt{-a^2+b^2}) \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}} + a b \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \sqrt{1 - \frac{-b+\sqrt{-a^2+b^2} - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}}\right/$$

$$\left(4\sqrt{2} \sqrt{-a^2+b^2} \sqrt{\frac{-b+\sqrt{-a^2+b^2} - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}} \right.$$

$$\left. \sqrt{1 - \frac{-b+\sqrt{-a^2+b^2} - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{2\sqrt{-a^2+b^2}}}\right) + a^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2$$

$$\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{-b+\sqrt{-a^2+b^2}}} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right/ \left(4\sqrt{2} \sqrt{-a^2+b^2} \right.$$

$$\left. \sqrt{\frac{b+\sqrt{-a^2+b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{-a^2+b^2}}} \sqrt{1 - \frac{b+\sqrt{-a^2+b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{2\sqrt{-a^2+b^2}}}\right)$$

$$\left. \sqrt{1 - \frac{b+\sqrt{-a^2+b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\right)$$

Problem 1103: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^4 \operatorname{Csc}[c+dx]^4 (a+b \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 114 leaves, 8 steps):

$$\frac{-\frac{b \operatorname{ArcTanh}[\cos[c+dx]]}{16d} - \frac{a \cot[c+dx]^5}{5d} - \frac{a \cot[c+dx]^7}{7d}}{\frac{b \cot[c+dx] \operatorname{Csc}[c+dx]}{16d}} + \frac{b \cot[c+dx] \operatorname{Csc}[c+dx]^3}{8d} - \frac{b \cot[c+dx]^3 \operatorname{Csc}[c+dx]^3}{6d}$$

Result (type 3, 239 leaves):

$$\frac{2a \cot[c+dx]}{35d} - \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{64d} + \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64d} - \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{384d} - \frac{a \cot[c+dx] \operatorname{Csc}[c+dx]^2}{35d} + \frac{8a \cot[c+dx] \operatorname{Csc}[c+dx]^4}{35d} - \frac{a \cot[c+dx] \operatorname{Csc}[c+dx]^6}{7d} - \frac{b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right]}{16d} + \frac{b \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right]}{16d} + \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{64d} - \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64d} + \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{384d}$$

Problem 1104: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^4 \operatorname{Csc}[c+dx]^5 (a+b \sin[c+dx]) dx$$

Optimal (type 3, 136 leaves, 9 steps):

$$\frac{3a \operatorname{ArcTanh}[\cos[c+dx]]}{128d} - \frac{b \cot[c+dx]^5}{5d} - \frac{b \cot[c+dx]^7}{7d} - \frac{3a \cot[c+dx] \operatorname{Csc}[c+dx]}{128d}}{\frac{a \cot[c+dx] \operatorname{Csc}[c+dx]^3}{64d}} + \frac{a \cot[c+dx] \operatorname{Csc}[c+dx]^5}{16d} - \frac{a \cot[c+dx]^3 \operatorname{Csc}[c+dx]^5}{8d}$$

Result (type 3, 279 leaves):

$$\frac{2b \cot[c+dx]}{35d} - \frac{3a \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{512d} + \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} + \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{512d} - \frac{a \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{2048d} - \frac{b \cot[c+dx] \operatorname{Csc}[c+dx]^2}{35d} + \frac{8b \cot[c+dx] \operatorname{Csc}[c+dx]^4}{35d} - \frac{b \cot[c+dx] \operatorname{Csc}[c+dx]^6}{7d} - \frac{3a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right]}{128d} + \frac{3a \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right]}{128d} + \frac{3a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{512d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{1024d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6}{512d} + \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^8}{2048d}$$

Problem 1111: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^4 (a+b \sin[c+dx])^2 dx$$

Optimal (type 3, 133 leaves, 13 steps):

$$a^2 x - \frac{3 b^2 x}{2} + \frac{3 a b \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{d} - \frac{3 a b \operatorname{Cos}[c+d x]}{d} + \frac{a^2 \operatorname{Cot}[c+d x]}{d} - \frac{3 b^2 \operatorname{Cot}[c+d x]}{2 d} + \frac{b^2 \operatorname{Cos}[c+d x]^2 \operatorname{Cot}[c+d x]}{2 d} - \frac{a b \operatorname{Cos}[c+d x] \operatorname{Cot}[c+d x]^2}{d} - \frac{a^2 \operatorname{Cot}[c+d x]^3}{3 d}$$

Result (type 3, 293 leaves):

$$\begin{aligned} & \frac{(2 a^2 - 3 b^2) (c+d x)}{2 d} - \frac{2 a b \operatorname{Cos}[c+d x]}{d} + \\ & \frac{\left(4 a^2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - 3 b^2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right] - a b \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{6 d} - \\ & \frac{a^2 \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 d} + \frac{3 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]}{d} - \frac{3 a b \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} + \\ & \frac{a b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{4 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \left(-4 a^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}{6 d} - \\ & \frac{b^2 \operatorname{Sin}\left[2(c+d x)\right]}{4 d} + \frac{a^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 d} \end{aligned}$$

Problem 1122: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+d x]^4 \operatorname{Csc}[c+d x] (a+b \operatorname{Sin}[c+d x])^3 dx$$

Optimal (type 3, 187 leaves, 7 steps):

$$\begin{aligned} & \frac{3}{2} b (2 a^2 - b^2) x - \frac{3 a (a^2 - 12 b^2) \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{8 d} - \frac{b^2 (73 a^2 - 2 b^2) \operatorname{Cos}[c+d x]}{8 a d} - \\ & \frac{13 b^3 \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{4 d} + \frac{17 b \operatorname{Cot}[c+d x] (a+b \operatorname{Sin}[c+d x])^2}{8 d} + \\ & \frac{5 \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x] (a+b \operatorname{Sin}[c+d x])^3}{8 d} - \frac{\operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3 (a+b \operatorname{Sin}[c+d x])^4}{4 a d} \end{aligned}$$

Result (type 3, 381 leaves):

$$\begin{aligned}
 & - \frac{3 b (-2 a^2 + b^2) (c + d x)}{2 d} - \frac{3 a b^2 \operatorname{Cos}[c + d x]}{d} + \\
 & \frac{\left(4 a^2 b \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - b^3 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]}{2 d} + \\
 & \frac{\left(5 a^3 - 12 a b^2\right) \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{32 d} - \frac{a^2 b \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^2}{8 d} - \\
 & \frac{a^3 \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^4}{64 d} - \frac{3\left(a^3 - 12 a b^2\right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \\
 & \frac{3\left(a^3 - 12 a b^2\right) \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \frac{\left(-5 a^3 + 12 a b^2\right) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{32 d} + \\
 & \frac{a^3 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^4}{64 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] \left(-4 a^2 b \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + b^3 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)}{2 d} - \\
 & \frac{b^3 \operatorname{Sin}\left[2(c + d x)\right]}{4 d} + \frac{a^2 b \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{8 d}
 \end{aligned}$$

Problem 1135: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + d x]^4 \operatorname{Sin}[c + d x]^3}{(a + b \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 331 leaves, 9 steps):

$$\begin{aligned}
 & \frac{3\left(40 a^4 - 24 a^2 b^2 + b^4\right) x}{8 b^7} - \frac{3 a\left(10 a^4 - 11 a^2 b^2 + 2 b^4\right) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{b^7 \sqrt{a^2-b^2} d} + \\
 & \frac{a\left(30 a^2 - 13 b^2\right) \operatorname{Cos}[c + d x]}{2 b^6 d} - \frac{3\left(20 a^2 - 7 b^2\right) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{8 b^5 d} + \\
 & \frac{\left(10 a^2 - 3 b^2\right) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^2}{2 a b^4 d} - \frac{\left(15 a^2 - 4 b^2\right) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^3}{4 a^2 b^3 d} - \\
 & \frac{\left(a^2 - b^2\right) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^4}{2 a b^2 d (a + b \operatorname{Sin}[c + d x])^2} + \frac{\left(7 a^2 - 2 b^2\right) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]^4}{2 a^2 b^2 d (a + b \operatorname{Sin}[c + d x])}
 \end{aligned}$$

Result (type 3, 1264 leaves):

$$\begin{aligned}
 & \frac{1}{128 b^3 d} \left(-8(c + d x) + \frac{2 a\left(8 a^4 - 20 a^2 b^2 + 15 b^4\right) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\left(a^2 - b^2\right)^{5/2}} + \right. \\
 & \left. \frac{a b\left(4 a^2 - 3 b^2\right) \operatorname{Cos}[c + d x]}{(a - b)(a + b)(a + b \operatorname{Sin}[c + d x])^2} - \frac{3 b\left(4 a^4 - 7 a^2 b^2 + 2 b^4\right) \operatorname{Cos}[c + d x]}{(a - b)^2(a + b)^2(a + b \operatorname{Sin}[c + d x])} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{3 \left(\frac{6 a b \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{\operatorname{Cos}[c+d x] \left(a \left(2 a^2+b^2\right)+b \left(a^2+2 b^2\right) \operatorname{Sin}[c+d x]\right)}{\left(a+b \operatorname{Sin}[c+d x]\right)^2} \right)}{128 (a-b)^2 (a+b)^2 d} - \frac{1}{128 b^5 d} \\
 & \left(-24 (-8 a^2+b^2) (c+d x) - \frac{6 a \left(64 a^6-168 a^4 b^2+140 a^2 b^4-35 b^6\right) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\left(a^2-b^2\right)^{5/2}} + \right. \\
 & 96 a b \operatorname{Cos}[c+d x] + \frac{a b \left(-16 a^4+20 a^2 b^2-5 b^4\right) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} + \\
 & \left. \frac{b \left(112 a^6-220 a^4 b^2+115 a^2 b^4-10 b^6\right) \operatorname{Cos}[c+d x]}{(a-b)^2(a+b)^2(a+b \operatorname{Sin}[c+d x])} - 8 b^2 \operatorname{Sin}[2(c+d x)] \right) - \\
 & \frac{1}{256 b^7 d} \left(\frac{1}{\left(a^2-b^2\right)^{5/2}} 12 a \left(640 a^8-1920 a^6 b^2+2016 a^4 b^4-840 a^2 b^6+105 b^8\right) \right. \\
 & \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \\
 & \frac{1}{\left(a^2-b^2\right)^2(a+b \operatorname{Sin}[c+d x])^2} \left(-3840 a^{10}(c+d x)+7680 a^8 b^2(c+d x)-2976 a^6 b^4(c+d x) - \right. \\
 & 1776 a^4 b^6(c+d x)+960 a^2 b^8(c+d x)-48 b^{10}(c+d x)-3840 a^9 b \operatorname{Cos}[c+d x] + \\
 & 8640 a^7 b^3 \operatorname{Cos}[c+d x]-5696 a^5 b^5 \operatorname{Cos}[c+d x]+788 a^3 b^7 \operatorname{Cos}[c+d x]+114 a b^9 \operatorname{Cos}[c+d x] + \\
 & 1920 a^8 b^2(c+d x) \operatorname{Cos}[2(c+d x)]-4800 a^6 b^4(c+d x) \operatorname{Cos}[2(c+d x)] + \\
 & 3888 a^4 b^6(c+d x) \operatorname{Cos}[2(c+d x)]-1056 a^2 b^8(c+d x) \operatorname{Cos}[2(c+d x)] + \\
 & 48 b^{10}(c+d x) \operatorname{Cos}[2(c+d x)]+320 a^7 b^3 \operatorname{Cos}[3(c+d x)]-760 a^5 b^5 \operatorname{Cos}[3(c+d x)] + \\
 & 560 a^3 b^7 \operatorname{Cos}[3(c+d x)]-120 a b^9 \operatorname{Cos}[3(c+d x)]-8 a^5 b^5 \operatorname{Cos}[5(c+d x)] + \\
 & 16 a^3 b^7 \operatorname{Cos}[5(c+d x)]-8 a b^9 \operatorname{Cos}[5(c+d x)]-7680 a^9 b(c+d x) \operatorname{Sin}[c+d x] + \\
 & 19200 a^7 b^3(c+d x) \operatorname{Sin}[c+d x]-15552 a^5 b^5(c+d x) \operatorname{Sin}[c+d x] + \\
 & 4224 a^3 b^7(c+d x) \operatorname{Sin}[c+d x]-192 a b^9(c+d x) \operatorname{Sin}[c+d x] - \\
 & 2880 a^8 b^2 \operatorname{Sin}[2(c+d x)]+6880 a^6 b^4 \operatorname{Sin}[2(c+d x)]-5182 a^4 b^6 \operatorname{Sin}[2(c+d x)] + \\
 & 1221 a^2 b^8 \operatorname{Sin}[2(c+d x)]-36 b^{10} \operatorname{Sin}[2(c+d x)]-40 a^6 b^4 \operatorname{Sin}[4(c+d x)] + \\
 & 88 a^4 b^6 \operatorname{Sin}[4(c+d x)]-56 a^2 b^8 \operatorname{Sin}[4(c+d x)]+8 b^{10} \operatorname{Sin}[4(c+d x)] + \\
 & \left. \left. 2 a^4 b^6 \operatorname{Sin}[6(c+d x)]-4 a^2 b^8 \operatorname{Sin}[6(c+d x)]+2 b^{10} \operatorname{Sin}[6(c+d x)] \right) \right)
 \end{aligned}$$

Problem 1136: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+d x]^4 \operatorname{Sin}[c+d x]^2}{(a+b \operatorname{Sin}[c+d x])^3} dx$$

Optimal (type 3, 284 leaves, 8 steps):

$$\frac{a \left(9 - \frac{20a^2}{b^2}\right) x}{2b^4} + \frac{(20a^4 - 19a^2b^2 + 2b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{b^6 \sqrt{a^2-b^2} d} - \frac{(60a^2 - 17b^2) \cos[c+dx]}{6b^5 d} +$$

$$\frac{(5a^2 - b^2) \cos[c+dx] \sin[c+dx]}{ab^4 d} - \frac{(20a^2 - 3b^2) \cos[c+dx] \sin[c+dx]^2}{6a^2 b^3 d} -$$

$$\frac{(a^2 - b^2) \cos[c+dx] \sin[c+dx]^3}{2ab^2 d (a+b \sin[c+dx])^2} + \frac{(6a^2 - b^2) \cos[c+dx] \sin[c+dx]^3}{2a^2 b^2 d (a+b \sin[c+dx])}$$

Result (type 3, 1030 leaves):

$$\frac{1}{384 d}$$

$$\left(-\frac{1}{b^4} 12 \left(-48 a (c+d x) + \frac{6 (16 a^6 - 40 a^4 b^2 + 30 a^2 b^4 - 5 b^6) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} - 16 b \operatorname{Cos}[c+d x] + \frac{b (8 a^4 - 8 a^2 b^2 + b^4) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} + \frac{a b (-40 a^4 + 72 a^2 b^2 - 29 b^4) \operatorname{Cos}[c+d x]}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])} \right) + 12 \left(\frac{2 (2 a^2 + b^2) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} + \frac{b \operatorname{Cos}[c+d x] (4 a^2 - b^2 + 3 a b \operatorname{Sin}[c+d x])}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])^2} \right) + \frac{1}{(a-b)^2 (a+b)^2} 6 \left(-\frac{6 b^2 \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{\operatorname{Cos}[c+d x] (-b (2 a^2 + b^2) + a (2 a^2 - 5 b^2) \operatorname{Sin}[c+d x])}{(a+b \operatorname{Sin}[c+d x])^2} \right) - \frac{1}{b^6} \left(-\frac{1}{(a^2-b^2)^{5/2}} 12 (640 a^8 - 1792 a^6 b^2 + 1680 a^4 b^4 - 560 a^2 b^6 + 35 b^8) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \frac{1}{(a^2-b^2)^2 (a+b \operatorname{Sin}[c+d x])^2} (3840 a^9 (c+d x) - 6912 a^7 b^2 (c+d x) + 1728 a^5 b^4 (c+d x) + 1920 a^3 b^6 (c+d x) - 576 a b^8 (c+d x) + 3840 a^8 b \operatorname{Cos}[c+d x] - 7872 a^6 b^3 \operatorname{Cos}[c+d x] + 4256 a^4 b^5 \operatorname{Cos}[c+d x] - 172 a^2 b^7 \operatorname{Cos}[c+d x] - 70 b^9 \operatorname{Cos}[c+d x] - 1920 a^7 b^2 (c+d x) \operatorname{Cos}[2(c+d x)] + 4416 a^5 b^4 (c+d x) \operatorname{Cos}[2(c+d x)] - 3072 a^3 b^6 (c+d x) \operatorname{Cos}[2(c+d x)] + 576 a b^8 (c+d x) \operatorname{Cos}[2(c+d x)] - 320 a^6 b^3 \operatorname{Cos}[3(c+d x)] + 696 a^4 b^5 \operatorname{Cos}[3(c+d x)] - 432 a^2 b^7 \operatorname{Cos}[3(c+d x)] + 56 b^9 \operatorname{Cos}[3(c+d x)] + 8 a^4 b^5 \operatorname{Cos}[5(c+d x)] - 16 a^2 b^7 \operatorname{Cos}[5(c+d x)] + 8 b^9 \operatorname{Cos}[5(c+d x)] + 7680 a^8 b (c+d x) \operatorname{Sin}[c+d x] - 17664 a^6 b^3 (c+d x) \operatorname{Sin}[c+d x] + 12288 a^4 b^5 (c+d x) \operatorname{Sin}[c+d x] - 2304 a^2 b^7 (c+d x) \operatorname{Sin}[c+d x] + 2880 a^7 b^2 \operatorname{Sin}[2(c+d x)] - 6304 a^5 b^4 \operatorname{Sin}[2(c+d x)] + 4022 a^3 b^6 \operatorname{Sin}[2(c+d x)] - 607 a b^8 \operatorname{Sin}[2(c+d x)] + 40 a^5 b^4 \operatorname{Sin}[4(c+d x)] - 80 a^3 b^6 \operatorname{Sin}[4(c+d x)] + 40 a b^8 \operatorname{Sin}[4(c+d x)]) \right) \right)$$

Problem 1145: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos [c + d x]^3 \cot [c + d x] \sqrt{a + b \sin [c + d x]} dx$$

Optimal (type 4, 338 leaves, 10 steps):

$$\begin{aligned} & - \frac{2 (8 a^2 - 45 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{105 b^2 d} + \\ & \frac{8 a \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{35 b^2 d} - \frac{2 \cos [c + d x] \sin [c + d x] (a + b \sin [c + d x])^{3/2}}{7 b d} + \\ & \frac{2 a (8 a^2 - 51 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{105 b^3 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\ & \left(2 (8 a^4 - 53 a^2 b^2 - 60 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a + b \sin [c + d x]}{a+b}} \right) / \\ & \left(105 b^3 d \sqrt{a + b \sin [c + d x]} \right) + \frac{2 a \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{d \sqrt{a + b \sin [c + d x]}} \end{aligned}$$

Result (type 4, 435 leaves):

$$\begin{aligned}
 & \frac{1}{210 b^2 d} \left(\frac{1}{b^2 \sqrt{-\frac{1}{a+b}}} \right. \\
 & 2 i (-8 a^2 + 51 b^2) \left(-2 a (a-b) \text{EllipticE} \left[i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & b \left(-2 a \text{EllipticF} \left[i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \left. \left. b \text{EllipticPi} \left[\frac{a+b}{a}, i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \text{Sec} [c+d x] \sqrt{-\frac{b(-1+\sin [c+d x])}{a+b}} \sqrt{\frac{b(1+\sin [c+d x])}{-a+b}} - \\
 & \frac{8 b (a^2 + 30 b^2) \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \\
 & \left(2 a (8 a^2 + 159 b^2) \text{EllipticPi} \left[2, \frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
 & \left(\sqrt{a+b \sin [c+d x]} \right) + \\
 & \left. \left. 2 \text{Cos} [c+d x] \sqrt{a+b \sin [c+d x]} (8 a^2 + 75 b^2 + 15 b^2 \text{Cos} [2 (c+d x)] - 6 a b \sin [c+d x]) \right) \right)
 \end{aligned}$$

Problem 1146: Result unnecessarily involves imaginary or complex numbers.

$$\int \text{Cos} [c+d x]^2 \text{Cot} [c+d x]^2 \sqrt{a+b \sin [c+d x]} dx$$

Optimal (type 4, 323 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(4 a^2 + 15 b^2) \operatorname{Cos}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{15 a b d} - \\
 & \frac{2 \operatorname{Cos}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{5 b d} - \frac{\operatorname{Cot}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{a d} - \\
 & \frac{(4 a^2 + 57 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{15 b^2 d \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}} + \\
 & \frac{a (4 a^2 + 11 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{15 b^2 d \sqrt{a + b \operatorname{Sin}[c + d x]}} + \\
 & \frac{b \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{d \sqrt{a + b \operatorname{Sin}[c + d x]}}
 \end{aligned}$$

Result (type 4, 541 leaves):

$$\begin{aligned}
 & \frac{1}{60 b d} \left(\frac{184 a b \operatorname{EllipticF}\left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
 & \left. \left(2 \left(-4 a^2 - 27 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \\
 & \left. \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i \left(4 a^2 + 57 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right) \right. \\
 & \left. \left(2 a (a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
 & \left. \left. b \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
 & \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
 & \left. \left(\sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \right. \\
 & \left. \left. \left(-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2 \right) \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right) \right) + \\
 & \frac{\sqrt{a+b \sin [c+d x]} \left(-\frac{2 a \cos [c+d x]}{15 b} - \cot [c+d x] - \frac{1}{5} \sin [2(c+d x)] \right)}{d}
 \end{aligned}$$

Problem 1147: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos [c+d x] \cot [c+d x]^3 \sqrt{a+b \sin [c+d x]} dx$$

Optimal (type 4, 345 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{(8 a^2 + 3 b^2) \operatorname{Cos}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{12 a^2 d} + \\
 & \frac{b \operatorname{Cot}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{4 a^2 d} - \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{2 a d} + \\
 & \frac{(8 a^2 - 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{12 a b d \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}} - \\
 & \frac{(8 a^2 + 31 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{12 b d \sqrt{a + b \operatorname{Sin}[c + d x]}} - \\
 & \frac{(12 a^2 + b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{4 a d \sqrt{a + b \operatorname{Sin}[c + d x]}}
 \end{aligned}$$

Result (type 4, 547 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(-\frac{2}{3} \cos[c+dx] - \frac{b \cot[c+dx]}{4a} - \frac{1}{2} \cot[c+dx] \csc[c+dx] \right) \sqrt{a+b \sin[c+dx]} - \\
 & \frac{1}{48ad} \left(-\frac{136ab \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{\sqrt{a+b \sin[c+dx]}} - \right. \\
 & \left. \left(2(64a^2+9b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}} \right) / \right. \\
 & \left. \left(\sqrt{a+b \sin[c+dx]} \right) - \left(2i(8a^2-3b^2) \cos[c+dx] \cos[2(c+dx)] \right) \right. \\
 & \left. \left(2a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin[c+dx]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
 & \left. \left. b \left(2a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin[c+dx]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
 & \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin[c+dx]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
 & \left. \sqrt{\frac{b-b \sin[c+dx]}{a+b}} \sqrt{-\frac{b+b \sin[c+dx]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin[c+dx]^2} \right. \\
 & \left. \left(-2a^2+b^2+4a(a+b \sin[c+dx]) - 2(a+b \sin[c+dx])^2 \right) \right. \\
 & \left. \left. \sqrt{-\frac{a^2-b^2-2a(a+b \sin[c+dx])+(a+b \sin[c+dx])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1148: Result unnecessarily involves imaginary or complex numbers.

$$\int \cot[c+dx]^4 \sqrt{a+b \sin[c+dx]} dx$$

Optimal (type 4, 351 leaves, 10 steps):

$$\frac{(32 a^2 - 3 b^2) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{24 a^2 d} + \frac{b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{4 a^2 d} -$$

$$\frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 (a + b \operatorname{Sin}[c + d x])^{3/2}}{3 a d} +$$

$$\frac{(80 a^2 + 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{24 a^2 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}} -$$

$$\frac{(32 a^2 + b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}}{24 a d \sqrt{a + b \operatorname{Sin}[c + d x]}} -$$

$$\frac{b (12 a^2 - b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}}{8 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]}}$$

Result (type 4, 593 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{(32 a^2 \cos [c+d x]+3 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]}{24 a^2} - \right. \\
 & \quad \left. \frac{b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]}{12 a} - \frac{1}{3} \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2 \right) \sqrt{a+b \sin [c+d x]} + \\
 & \frac{1}{96 a^2 d} \left(-\frac{2\left(96 a^3+4 a b^2\right) \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
 & \quad \left. \left(2\left(8 a^2 b+9 b^3\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right) / \right. \\
 & \quad \left. \left(\sqrt{a+b \sin [c+d x]}\right) - \left(2 i\left(-80 a^2 b-3 b^3\right) \cos [c+d x] \cos [2(c+d x)]\right) \right. \\
 & \quad \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \\
 & \quad b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]\right)\right) \\
 & \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}}\right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2}\right. \\
 & \quad \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2\right) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}}\right)\right)
 \end{aligned}$$

Problem 1149: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cot}[c+d x]^4 \operatorname{Csc}[c+d x] \sqrt{a+b \sin [c+d x]} dx$$

Optimal (type 4, 412 leaves, 11 steps):

$$\begin{aligned}
 & \frac{b (68 a^2 - 15 b^2) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{192 a^3 d} + \\
 & \frac{5 (4 a^2 - b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{32 a^2 d} + \\
 & \frac{5 b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 (a + b \operatorname{Sin}[c + d x])^{3/2}}{24 a^2 d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{3/2}}{4 a d} + \\
 & \frac{b (68 a^2 - 15 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{192 a^3 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}} + \\
 & \frac{b (196 a^2 + 5 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}}{192 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]}} + \\
 & \left((48 a^4 + 24 a^2 b^2 - 5 b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & (64 a^3 d \sqrt{a + b \operatorname{Sin}[c + d x]})
 \end{aligned}$$

Result (type 4, 643 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{(68 a^2 b \cos [c+d x] - 15 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]}{192 a^3} + \right. \\
 & \quad \frac{5 (12 a^2 \cos [c+d x] + b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{96 a^2} - \\
 & \quad \left. \frac{b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2}{24 a} - \frac{1}{4} \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3 \right) \sqrt{a+b \sin [c+d x]} + \\
 & \frac{1}{768 a^3 d} \left(- \left(\left(2 (528 a^3 b - 20 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
 & \left(2 (288 a^4 + 212 a^2 b^2 - 45 b^4) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
 & \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (-68 a^2 b^2 + 15 b^4) \cos [c+d x] \cos [2 (c+d x)] \right. \\
 & \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \left. b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
 & \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \\
 & \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1150: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cot}[c+d x]^4 \operatorname{Csc}[c+d x]^2 \sqrt{a+b \sin [c+d x]} dx$$

Optimal (type 4, 484 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{(384 a^4 + 332 a^2 b^2 - 105 b^4) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{1920 a^4 d} + \\
 & \frac{b (108 a^2 - 35 b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{960 a^3 d} + \\
 & \frac{(96 a^2 - 35 b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 \sqrt{a + b \operatorname{Sin}[c + d x]}}{240 a^2 d} + \\
 & \frac{7 b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{3/2}}{40 a^2 d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^4 (a + b \operatorname{Sin}[c + d x])^{3/2}}{5 a d} - \\
 & \left((384 a^4 + 332 a^2 b^2 - 105 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}\right) / \\
 & \left(1920 a^4 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) + \\
 & \left((384 a^4 + 116 a^2 b^2 - 35 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(1920 a^3 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right) + \\
 & \left(b (48 a^4 - 24 a^2 b^2 + 7 b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(128 a^4 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right)
 \end{aligned}$$

Result(type 4, 702 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{1}{1920 a^4} (-384 a^4 \cos [c+d x] - 332 a^2 b^2 \cos [c+d x] + 105 b^4 \cos [c+d x]) \operatorname{Csc}[c+d x] + \right. \\
 & \quad \frac{(108 a^2 b \cos [c+d x] - 35 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{960 a^3} + \\
 & \quad \left. \frac{(96 a^2 \cos [c+d x] + 7 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^3}{240 a^2} - \right. \\
 & \quad \left. \frac{b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^3}{40 a} - \frac{1}{5} \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^4 \right) \sqrt{a+b \sin [c+d x]} + \\
 & \frac{1}{7680 a^4 d} b \left(- \left(\left(2 (-432 a^3 b + 140 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right], \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \left(2 (1056 a^4 - 1052 a^2 b^2 + 315 b^4) \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right], \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right] / \left(\sqrt{a+b \sin [c+d x]} \right) - \right. \\
 & \quad \left. \left(2 i (384 a^4 + 332 a^2 b^2 - 105 b^4) \cos [c+d x] \cos [2(c+d x)] \right. \right. \\
 & \quad \left. \left. \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \right. \\
 & \quad \left. \left. b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \right) \\
 & \quad \left. \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]}^2 \right. \right. \\
 & \quad \left. \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1151: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^4 \sin [c+d x]^2 (a+b \sin [c+d x])^{3 / 2} d x$$

Optimal (type 4, 528 leaves, 11 steps):

$$\begin{aligned} & \frac{8\left(64 a^6-174 a^4 b^2+81 a^2 b^4-195 b^6\right) \cos [c+d x] \sqrt{a+b \sin [c+d x]}}{45045 b^5 d}+ \\ & \frac{16 a\left(32 a^4-47 a^2 b^2-27 b^4\right) \cos [c+d x]\left(a+b \sin [c+d x]\right)^{3 / 2}}{45045 b^5 d}- \\ & \frac{8\left(160 a^4-375 a^2 b^2+117 b^4\right) \cos [c+d x]\left(a+b \sin [c+d x]\right)^{5 / 2}}{45045 b^5 d}+ \\ & \frac{8 a\left(8 a^2-21 b^2\right) \cos [c+d x] \sin [c+d x]\left(a+b \sin [c+d x]\right)^{5 / 2}}{1287 b^4 d}- \\ & \frac{2\left(80 a^2-221 b^2\right) \cos [c+d x] \sin [c+d x]^2\left(a+b \sin [c+d x]\right)^{5 / 2}}{2145 b^3 d}+ \\ & \frac{4 a \cos [c+d x] \sin [c+d x]^3\left(a+b \sin [c+d x]\right)^{5 / 2}}{39 b^2 d}- \\ & \frac{2 \cos [c+d x] \sin [c+d x]^4\left(a+b \sin [c+d x]\right)^{5 / 2}}{15 b d}- \\ & \left(16 a\left(32 a^6-111 a^4 b^2+102 a^2 b^4-471 b^6\right) \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{a+b \sin [c+d x]}\right) / \\ & \left(45045 b^6 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right)+\left(8\left(64 a^8-238 a^6 b^2+255 a^4 b^4-276 a^2 b^6+195 b^8\right)\right. \\ & \left.\operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right) / \left(45045 b^6 d \sqrt{a+b \sin [c+d x]}\right) \end{aligned}$$

Result (type 4, 1987 leaves):

$$\begin{aligned} & \frac{a \operatorname{EllipticE}\left[\frac{1}{4}(-2 c+\pi-2 d x), \frac{2 b}{a+b}\right] \sqrt{a+b \sin [c+d x]}}{8 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}- \\ & \left(b \cos [c+d x]\left(a+b \sin [c+d x]\right)+a(a+b) \operatorname{EllipticE}\left[\frac{1}{4}(-2 c+\pi-2 d x), \frac{2 b}{a+b}\right]\right. \\ & \left.\sqrt{\frac{a+b \sin [c+d x]}{a+b}}-\left(a^2-b^2\right) \operatorname{EllipticF}\left[\frac{1}{4}(-2 c+\pi-2 d x), \frac{2 b}{a+b}\right]\right) \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \left(24 d \sqrt{a+b \sin [c+d x]} \right) + \\
 & \left(a \left(-2 \left(4 a^3 + 4 a^2 b - 3 a b^2 - 3 b^3 \right) \text{EllipticE} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} + \right. \right. \\
 & \quad \left. \left. 8 a \left(a^2 - b^2 \right) \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} + 2 b \cos [c+d x] \right. \right. \\
 & \quad \left. \left. \left(2 a^2 + 3 b^2 - 3 b^2 \cos [2 (c+d x)] + 8 a b \sin [c+d x] \right) \right) \right) / \left(480 b^2 d \sqrt{a+b \sin [c+d x]} \right) + \\
 & \left(2 a \left(16 a^3 + 16 a^2 b + 3 a b^2 + 3 b^3 \right) \text{EllipticE} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} - \right. \\
 & \quad \left. 2 \left(16 a^4 - a^2 b^2 - 15 b^4 \right) \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} + \right. \\
 & \quad \left. b \cos [c+d x] \left(-16 a^3 + 66 a b^2 - 36 a b^2 \cos [2 (c+d x)] + \right. \right. \\
 & \quad \left. \left. \left(-4 a^2 b + 75 b^3 \right) \sin [c+d x] - 15 b^3 \sin [3 (c+d x)] \right) \right) / \\
 & \left(3360 b^2 d \sqrt{a+b \sin [c+d x]} \right) + \frac{1}{2520 b^4 d \sqrt{a+b \sin [c+d x]}} \\
 & a \left(b \left(-32 a^3 b + 27 a b^3 \right) \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} - \right. \\
 & \quad \left(128 a^4 - 144 a^2 b^2 + 21 b^4 \right) \\
 & \quad \left((a+b) \text{EllipticE} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] - a \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a+b} \right] \right) \\
 & \quad \sqrt{\frac{a+b \sin [c+d x]}{a+b}} - 2 b \cos [c+d x] (a+b \sin [c+d x]) \left(-32 a^3 + 22 a b^2 + \right. \\
 & \quad \left. \left. 10 a b^2 \cos [2 (c+d x)] + b \left(24 a^2 - 49 b^2 \right) \sin [c+d x] + 35 b^3 \sin [3 (c+d x)] \right) \right) - \\
 & \frac{1}{55440 b^4 d \sqrt{a+b \sin [c+d x]}} \left(-2 a \left(1024 a^5 + 1024 a^4 b - 864 a^3 b^2 - 864 a^2 b^3 - 93 a b^4 - 93 b^5 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticE}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}} + \\
 & 2(1024a^6 - 1120a^4b^2 + 51a^2b^4 + 45b^6) \text{EllipticF}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \\
 & \sqrt{\frac{a+b \sin[c+dx]}{a+b}} - \\
 & b \cos[c+dx] \left(-1024a^5 + 800a^3b^2 + 1034ab^4 - 32(2a^3b^2 + 57ab^4) \cos[2(c+dx)] + \right. \\
 & \quad 700a^4b^4 \cos[4(c+dx)] - 256a^4b \sin[c+dx] + 164a^2b^3 \sin[c+dx] + 1980b^5 \sin[c+dx] + \\
 & \quad \left. 20a^2b^3 \sin[3(c+dx)] - 1215b^5 \sin[3(c+dx)] + 315b^5 \sin[5(c+dx)] \right) - \\
 & \frac{1}{720720b^6d\sqrt{a+b \sin[c+dx]}} a \left(-b(10240a^5b - 13504a^3b^3 + 3579ab^5) \right. \\
 & \quad \text{EllipticF}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}} - \\
 & \quad (40960a^6 - 65536a^4b^2 + 26508a^2b^4 - 1617b^6) \left((a+b) \text{EllipticE}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] - \right. \\
 & \quad \left. a \text{EllipticF}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \right) \sqrt{\frac{a+b \sin[c+dx]}{a+b}} + b(a+b \sin[c+dx]) \\
 & \quad (2a(10240a^4 - 13504a^2b^2 + 3579b^4) \cos[c+dx] - 10ab^2(320a^2 - 257b^2) \cos[3(c+dx)] + \\
 & \quad 630ab^4 \cos[5(c+dx)] - 2b(3840a^4 - 4064a^2b^2 + 539b^4) \sin[2(c+dx)] + \\
 & \quad \left. 70b^3(20a^2 - 11b^2) \sin[4(c+dx)] + 3465b^5 \sin[6(c+dx)] \right) - \\
 & \frac{1}{1441440b^6d\sqrt{a+b \sin[c+dx]}} \left(2a(32768a^7 + 32768a^6b - 47104a^5b^2 - 47104a^4b^3 + \right. \\
 & \quad 13968a^3b^4 + 13968a^2b^5 + 711ab^6 + 711b^7) \text{EllipticE}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \\
 & \quad \sqrt{\frac{a+b \sin[c+dx]}{a+b}} - 2(32768a^8 - 55296a^6b^2 + 23440a^4b^4 - 717a^2b^6 - 195b^8) \\
 & \quad \text{EllipticF}\left[\frac{1}{4}(-2c + \pi - 2dx), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}} + \\
 & \quad b \cos[c+dx] \left(-32768a^7 + 45056a^5b^2 - 12208a^3b^4 + 7018ab^6 - \right. \\
 & \quad \left. 16(128a^5b^2 - 124a^3b^4 + 969ab^6) \cos[2(c+dx)] + 112(2a^3b^4 + 137ab^6) \cos[4(c+dx)] - \right. \\
 & \quad \left. 6468ab^6 \cos[6(c+dx)] - 8192a^6b \sin[c+dx] + 10112a^4b^3 \sin[c+dx] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1796 a^2 b^5 \sin[c + dx] + 15444 b^7 \sin[c + dx] + 640 a^4 b^3 \sin[3(c + dx)] - \\
 & 452 a^2 b^5 \sin[3(c + dx)] - 15756 b^7 \sin[3(c + dx)] - \\
 & \left. 84 a^2 b^5 \sin[5(c + dx)] + 10647 b^7 \sin[5(c + dx)] - 3003 b^7 \sin[7(c + dx)] \right)
 \end{aligned}$$

Problem 1153: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos[c + dx]^3 \cot[c + dx] (a + b \sin[c + dx])^{3/2} dx$$

Optimal (type 4, 390 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{2 a (8 a^2 - 87 b^2) \cos[c + dx] \sqrt{a + b \sin[c + dx]}}{315 b^2 d} - \\
 & \frac{2 (8 a^2 - 77 b^2) \cos[c + dx] (a + b \sin[c + dx])^{3/2}}{315 b^2 d} + \\
 & \frac{8 a \cos[c + dx] (a + b \sin[c + dx])^{5/2}}{63 b^2 d} - \frac{2 \cos[c + dx] \sin[c + dx] (a + b \sin[c + dx])^{5/2}}{9 b d} + \\
 & \left(2 (8 a^4 - 93 a^2 b^2 + 84 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{a + b \sin[c + dx]} \right) / \\
 & \left(315 b^3 d \sqrt{\frac{a + b \sin[c + dx]}{a + b}} \right) - \\
 & \left(2 a (8 a^4 - 95 a^2 b^2 - 228 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a + b}} \right) / \\
 & \left(315 b^3 d \sqrt{a + b \sin[c + dx]} \right) + \frac{2 a^2 \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a + b}}}{d \sqrt{a + b \sin[c + dx]}}
 \end{aligned}$$

Result (type 4, 611 leaves):

$$\begin{aligned}
 & -\frac{1}{630 b^2 d} \left(\left(\left(2 (-4 a^3 b - 624 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
 & \quad \left(2 (-8 a^4 - 537 a^2 b^2 - 84 b^4) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
 & \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (8 a^4 - 93 a^2 b^2 + 84 b^4) \cos [c+d x] \cos [2 (c+d x)] \right) \\
 & \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \quad \left(\sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
 & \quad \left. \left(-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2 \right) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right) + \\
 & \quad \frac{1}{d} \sqrt{a+b \sin [c+d x]} \left(\frac{a (8 a^2 + 303 b^2) \cos [c+d x]}{315 b^2} + \frac{5}{63} a \cos [3 (c+d x)] + \right. \\
 & \quad \left. \frac{(-6 a^2 + 119 b^2) \sin [2 (c+d x)]}{630 b} + \right. \\
 & \quad \left. \frac{1}{36} b \sin [4 (c+d x)] \right)
 \end{aligned}$$

Problem 1154: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos [c+d x]^2 \cot [c+d x]^2 (a+b \sin [c+d x])^{3/2} dx$$

Optimal (type 4, 374 leaves, 11 steps):

$$\begin{aligned}
 & \frac{(4 a^2 + 65 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{35 b d} + \frac{(4 a^2 + 35 b^2) \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{35 a b d} \\
 & \frac{2 \cos [c + d x] (a + b \sin [c + d x])^{5/2}}{7 b d} - \frac{\cot [c + d x] (a + b \sin [c + d x])^{5/2}}{a d} \\
 & \frac{a (4 a^2 + 167 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{35 b^2 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} + \\
 & \frac{(4 a^4 + 61 a^2 b^2 + 40 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{35 b^2 d \sqrt{a + b \sin [c + d x]}} + \\
 & \frac{3 a b \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result (type 4, 578 leaves):

$$\frac{1}{140 b d} \left(- \left(\left(2 (-212 a^2 b + 80 b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \right. \right. \\ \left. \left. \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) \right) - \right. \\ \left. \left(2 (-4 a^3 + 43 a b^2) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \right. \\ \left. \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) - \left(2 i (4 a^3 + 167 a b^2) \operatorname{Cos}[c + d x] \operatorname{Cos}[2 (c + d x)] \right) \right. \\ \left. \left(2 a (a - b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \right. \\ \left. \left. b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] - \right. \right. \right. \\ \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a + b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] \right) \right) \right) \\ \left. \left(\sqrt{\frac{b - b \operatorname{Sin}[c + d x]}{a + b}} \sqrt{-\frac{b + b \operatorname{Sin}[c + d x]}{a - b}} \right) / \left(a \sqrt{-\frac{1}{a + b}} \sqrt{1 - \operatorname{Sin}[c + d x]^2} \right) \right. \\ \left. \left(-2 a^2 + b^2 + 4 a (a + b \operatorname{Sin}[c + d x]) - 2 (a + b \operatorname{Sin}[c + d x])^2 \right) \right. \\ \left. \left. \left(\sqrt{-\frac{a^2 - b^2 - 2 a (a + b \operatorname{Sin}[c + d x]) + (a + b \operatorname{Sin}[c + d x])^2}{b^2}} \right) \right) \right) + \\ \frac{1}{d} \sqrt{a + b \operatorname{Sin}[c + d x]} \left(\frac{(-4 a^2 + 55 b^2) \operatorname{Cos}[c + d x]}{70 b} + \frac{1}{14} b \operatorname{Cos}[3 (c + d x)] \right) - \\ a \operatorname{Cot}[c + d x] - \frac{8}{35} a \operatorname{Sin}[2 (c + d x)] \Bigg)$$

Problem 1155: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cos}[c + d x] \operatorname{Cot}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{3/2} dx$$

Optimal (type 4, 383 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{(8a^2 - 15b^2) \cos[c+dx] \sqrt{a+b \sin[c+dx]}}{20ad} - \frac{(8a^2 - 5b^2) \cos[c+dx] (a+b \sin[c+dx])^{3/2}}{20a^2d} \\
 & \frac{b \cot[c+dx] (a+b \sin[c+dx])^{5/2}}{4a^2d} - \frac{\cot[c+dx] \csc[c+dx] (a+b \sin[c+dx])^{5/2}}{2ad} + \\
 & \frac{(8a^2 - 81b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a+b \sin[c+dx]}}{20bd \sqrt{\frac{a+b \sin[c+dx]}{a+b}}} - \\
 & \frac{a(8a^2 + 37b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{20bd \sqrt{a+b \sin[c+dx]}} - \\
 & \frac{3(4a^2 - b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{4d \sqrt{a+b \sin[c+dx]}}
 \end{aligned}$$

Result (type 4, 434 leaves):

$$\frac{1}{80 d} \left(\frac{1}{a b^2 \sqrt{-\frac{1}{a+b}}} \right. \\
2 i (-8 a^2 + 81 b^2) \left(-2 a (a - b) \text{EllipticE} \left[i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \\
b \left(-2 a \text{EllipticF} \left[i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \\
\left. \left. b \text{EllipticPi} \left[\frac{a + b}{a}, i \text{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] \right) \right) \\
\text{Sec}[c + d x] \sqrt{-\frac{b (-1 + \text{Sin}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sin}[c + d x])}{a - b}} + \\
\frac{472 a b \text{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \text{Sin}[c + d x]}{a + b}}}{\sqrt{a + b \text{Sin}[c + d x]}} + \\
\left(2 (112 a^2 + 51 b^2) \text{EllipticPi} \left[2, \frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \text{Sin}[c + d x]}{a + b}} \right) / \\
\left(\sqrt{a + b \text{Sin}[c + d x]} \right) + 4 \text{Cot}[c + d x] \text{Csc}[c + d x] \sqrt{a + b \text{Sin}[c + d x]} \\
\left. \left. \left. (-18 a + 8 a \text{Cos}[2 (c + d x)] - 31 b \text{Sin}[c + d x] + 2 b \text{Sin}[3 (c + d x)]) \right) \right) \right)$$

Problem 1156: Result unnecessarily involves imaginary or complex numbers.

$$\int \text{Cot}[c + d x]^4 (a + b \text{Sin}[c + d x])^{3/2} dx$$

Optimal (type 4, 386 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{b (16 a^2 + b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{8 a^2 d} + \\
 & \frac{(32 a^2 + b^2) \cot [c + d x] (a + b \sin [c + d x])^{3/2}}{24 a^2 d} + \frac{b \cot [c + d x] \csc [c + d x] (a + b \sin [c + d x])^{5/2}}{12 a^2 d} - \\
 & \frac{\cot [c + d x] \csc [c + d x]^2 (a + b \sin [c + d x])^{5/2}}{3 a d} + \\
 & \frac{(32 a^2 - b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{8 a d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{(16 a^2 + 21 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{8 d \sqrt{a + b \sin [c + d x]}} - \\
 & \frac{b (36 a^2 + b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{8 a d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result (type 4, 600 leaves):

$$\begin{aligned}
& \frac{1}{d} \left(-\frac{2}{3} b \cos [c+d x] + \frac{(32 a^2 \cos [c+d x] - 3 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]}{24 a} - \right. \\
& \quad \left. \frac{7}{12} b \cot [c+d x] \operatorname{Csc}[c+d x] - \frac{1}{3} a \cot [c+d x] \operatorname{Csc}[c+d x]^2 \right) \sqrt{a+b \sin [c+d x]} + \\
& \frac{1}{32 a d} \left(-\left(\left(2 (32 a^3 - 44 a b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
& \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
& \left(2 (-40 a^2 b - 3 b^3) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
& \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (-32 a^2 b + b^3) \cos [c+d x] \cos [2(c+d x)] \right. \\
& \quad \left(2 a (a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \\
& \quad \left. b \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \\
& \quad \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \\
& \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \quad \left. \left(-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2 \right) \right. \\
& \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1157: Result unnecessarily involves imaginary or complex numbers.

$$\int \cot [c+d x]^4 \operatorname{Csc}[c+d x] (a+b \sin [c+d x])^{3/2} dx$$

Optimal (type 4, 408 leaves, 11 steps):

$$\begin{aligned}
 & \frac{b (68 a^2 - 3 b^2) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{64 a^2 d} + \\
 & \frac{(20 a^2 - b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{32 a^2 d} + \\
 & \frac{b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 (a + b \operatorname{Sin}[c + d x])^{5/2}}{8 a^2 d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{5/2}}{4 a d} + \\
 & \frac{b (236 a^2 + 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{64 a^2 d \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}} - \\
 & \frac{b (20 a^2 + b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{64 a d \sqrt{a + b \operatorname{Sin}[c + d x]}} + \\
 & \left(\frac{3 (16 a^4 - 24 a^2 b^2 + b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}}{64 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]}} \right) /
 \end{aligned}$$

Result(type 4, 641 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{3 (36 a^2 b \cos [c+d x] + b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]}{64 a^2} + \right. \\
 & \quad \left. \frac{(20 a^2 \cos [c+d x] - b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{32 a} - \frac{3}{8} b \cot [c+d x] \operatorname{Csc}[c+d x]^2 - \right. \\
 & \quad \left. \frac{1}{4} a \cot [c+d x] \operatorname{Csc}[c+d x]^3 \right) \sqrt{a+b \sin [c+d x]} + \\
 & \frac{1}{256 a^2 d} \left(- \left(\left(2 (432 a^3 b + 4 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
 & \left(2 (96 a^4 + 92 a^2 b^2 + 9 b^4) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
 & \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (-236 a^2 b^2 - 3 b^4) \cos [c+d x] \cos [2 (c+d x)] \right. \\
 & \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \right) \\
 & \quad \left. \left. \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \right. \\
 & \quad \left. \left. \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right) \right)
 \end{aligned}$$

Problem 1158: Result unnecessarily involves imaginary or complex numbers.

$$\int \cot [c+d x]^4 \operatorname{Csc}[c+d x]^2 (a+b \sin [c+d x])^{3/2} dx$$

Optimal (type 4, 484 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{(128 a^4 - 116 a^2 b^2 + 15 b^4) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{640 a^3 d} + \\
 & \frac{3 b (36 a^2 - 5 b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{320 a^2 d} + \\
 & \frac{(32 a^2 - 5 b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 (a + b \operatorname{Sin}[c + d x])^{3/2}}{80 a^2 d} + \\
 & \frac{b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{5/2}}{8 a^2 d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^4 (a + b \operatorname{Sin}[c + d x])^{5/2}}{5 a d} - \\
 & \left((128 a^4 - 116 a^2 b^2 + 15 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}\right) / \\
 & \left(640 a^3 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) + \\
 & \left((128 a^4 + 692 a^2 b^2 + 5 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(640 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right) + \\
 & \left(3 b (48 a^4 + 8 a^2 b^2 - b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(128 a^3 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right)
 \end{aligned}$$

Result(type 4, 700 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{1}{640 a^3} (-128 a^4 \cos [c+d x]+116 a^2 b^2 \cos [c+d x]-15 b^4 \cos [c+d x]) \operatorname{Csc}[c+d x]+ \right. \\
 & \quad \frac{(236 a^2 b \cos [c+d x]+5 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{320 a^2} + \\
 & \quad \left. \frac{(32 a^2 \cos [c+d x]-b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^3}{80 a}-\frac{11}{40} b \cot [c+d x] \operatorname{Csc}[c+d x]^3-\right. \\
 & \quad \left. \frac{1}{5} a \cot [c+d x] \operatorname{Csc}[c+d x]^4\right) \sqrt{a+b \sin [c+d x]}+ \\
 & \frac{1}{2560 a^3 d} b \left(-\left(\left(2\left(1616 a^3 b-20 a b^3\right) \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right], \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right] \right) / \right. \\
 & \quad \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \\
 & \left(2\left(1312 a^4+356 a^2 b^2-45 b^4\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right], \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right) / \\
 & \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i\left(128 a^4-116 a^2 b^2+15 b^4\right) \cos [c+d x] \cos [2(c+d x)] \right. \\
 & \quad \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]+ \right. \\
 & \quad b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]- \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]\right)\right) \right) \\
 & \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}}\right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
 & \quad \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x])-2(a+b \sin [c+d x])^2\right) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}}\right) \right)
 \end{aligned}$$

Problem 1159: Result unnecessarily involves imaginary or complex numbers.

$$\int \text{Cot}[c + dx]^4 \text{Csc}[c + dx]^3 (a + b \text{Sin}[c + dx])^{3/2} dx$$

Optimal (type 4, 551 leaves, 13 steps):

$$\begin{aligned} & - \frac{b (2064 a^4 + 512 a^2 b^2 - 105 b^4) \text{Cot}[c + dx] \sqrt{a + b \text{Sin}[c + dx]}}{7680 a^4 d} - \\ & \frac{1}{3840 a^3 d} (240 a^4 - 168 a^2 b^2 + 35 b^4) \text{Cot}[c + dx] \text{Csc}[c + dx] \sqrt{a + b \text{Sin}[c + dx]} + \\ & \frac{b (156 a^2 - 35 b^2) \text{Cot}[c + dx] \text{Csc}[c + dx]^2 \sqrt{a + b \text{Sin}[c + dx]}}{960 a^2 d} + \\ & \frac{7 (4 a^2 - b^2) \text{Cot}[c + dx] \text{Csc}[c + dx]^3 (a + b \text{Sin}[c + dx])^{3/2}}{96 a^2 d} + \\ & \frac{7 b \text{Cot}[c + dx] \text{Csc}[c + dx]^4 (a + b \text{Sin}[c + dx])^{5/2}}{60 a^2 d} - \\ & \frac{\text{Cot}[c + dx] \text{Csc}[c + dx]^5 (a + b \text{Sin}[c + dx])^{5/2}}{6 a d} - \\ & \left(b (2064 a^4 + 512 a^2 b^2 - 105 b^4) \text{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{a + b \text{Sin}[c + dx]} \right) / \\ & \left(7680 a^4 d \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} \right) + \\ & \left(b (2544 a^4 + 176 a^2 b^2 - 35 b^4) \text{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} \right) / \\ & \left(7680 a^3 d \sqrt{a + b \text{Sin}[c + dx]} \right) + \\ & \left((64 a^6 + 144 a^4 b^2 - 36 a^2 b^4 + 7 b^6) \text{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} \right) / \\ & \left(512 a^4 d \sqrt{a + b \text{Sin}[c + dx]} \right) \end{aligned}$$

Result (type 4, 771 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{1}{7680 a^4} (-2064 a^4 b \cos [c+d x] - 512 a^2 b^3 \cos [c+d x] + 105 b^5 \cos [c+d x]) \operatorname{Csc}[c+d x] + \right. \\
 & \quad \frac{1}{3840 a^3} (-240 a^4 \cos [c+d x] + 168 a^2 b^2 \cos [c+d x] - 35 b^4 \cos [c+d x]) \operatorname{Csc}[c+d x]^2 + \\
 & \quad \left. \frac{(436 a^2 b \cos [c+d x] + 7 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]^3}{960 a^2} + \right. \\
 & \quad \left. \frac{(140 a^2 \cos [c+d x] - 3 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^4}{480 a} - \frac{13}{60} b \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^4 - \right. \\
 & \quad \left. \frac{1}{6} a \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^5 \right) \sqrt{a+b \sin [c+d x]} + \frac{1}{30720 a^4 d} \\
 & \left(- \left(\left(2 (960 a^5 b - 672 a^3 b^3 + 140 a b^5) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \left(2 (1920 a^6 + 2256 a^4 b^2 - 1592 a^2 b^4 + 315 b^6) \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \left(\sqrt{a+b \sin [c+d x]} \right) - \right. \\
 & \quad \left. \left(2 i (2064 a^4 b^2 + 512 a^2 b^4 - 105 b^6) \cos [c+d x] \cos [2(c+d x)] \right) \right. \\
 & \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]}^2 \right. \\
 & \quad \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1161: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos [c + d x]^3 \cot [c + d x] (a + b \sin [c + d x])^{5/2} dx$$

Optimal (type 4, 447 leaves, 12 steps):

$$\begin{aligned} & - \frac{2 (8 a^4 - 141 a^2 b^2 + 36 b^4) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{693 b^2 d} - \\ & \frac{2 a (8 a^2 - 131 b^2) \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{693 b^2 d} - \\ & \frac{2 (8 a^2 - 117 b^2) \cos [c + d x] (a + b \sin [c + d x])^{5/2}}{693 b^2 d} + \\ & \frac{8 a \cos [c + d x] (a + b \sin [c + d x])^{7/2}}{99 b^2 d} - \frac{2 \cos [c + d x] \sin [c + d x] (a + b \sin [c + d x])^{7/2}}{11 b d} + \\ & \left(2 a (8 a^4 - 147 a^2 b^2 + 444 b^4) \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{a + b \sin [c + d x]} \right) / \\ & \left(693 b^3 d \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) - \\ & \left(2 (8 a^6 - 149 a^4 b^2 - 516 a^2 b^4 - 36 b^6) \operatorname{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) / \\ & \left(693 b^3 d \sqrt{a + b \sin [c + d x]} \right) + \frac{2 a^3 \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}}}{d \sqrt{a + b \sin [c + d x]}} \end{aligned}$$

Result (type 4, 654 leaves):

$$\begin{aligned} & - \frac{1}{1386 b^2 d} \\ & \left(- \left(\left(2 (-4 a^4 b - 1920 a^2 b^3 - 72 b^5) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) / \right. \right. \\ & \left. \left. \left(\sqrt{a + b \sin [c + d x]} \right) \right) - \left(2 (-8 a^5 - 1239 a^3 b^2 - 444 a b^4) \right. \right. \\ & \left. \left. \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) / \left(\sqrt{a + b \sin [c + d x]} \right) - \right. \\ & \left. \left(2 i (8 a^5 - 147 a^3 b^2 + 444 a b^4) \cos [c + d x] \cos [2 (c + d x)] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(2 a (a - b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \left. \left(\sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \right. \\
 & \left. \left. (-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2) \right. \right. \\
 & \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right) + \\
 & \frac{1}{d} \sqrt{a+b \sin [c+d x]} \left(-\frac{(-32 a^4-2886 a^2 b^2+117 b^4) \cos [c+d x]}{2772 b^2} + \right. \\
 & \quad \frac{(452 a^2-279 b^2) \cos [3(c+d x)]}{5544} - \\
 & \quad \frac{1}{88} b^2 \cos [5(c+d x)] - \\
 & \quad \frac{a(6 a^2-569 b^2) \sin [2(c+d x)]}{1386 b} + \\
 & \quad \left. \left. \frac{23}{396} a b \sin [4(c+d x)] \right) \right)
 \end{aligned}$$

Problem 1162: Result unnecessarily involves imaginary or complex numbers.

$$\int \cos [c+d x]^2 \cot [c+d x]^2 (a+b \sin [c+d x])^{5/2} d x$$

Optimal (type 4, 426 leaves, 12 steps):

$$\begin{aligned}
 & \frac{a (20 a^2 + 759 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{315 b d} + \\
 & \frac{(20 a^2 + 469 b^2) \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{315 b d} + \\
 & \frac{(4 a^2 + 63 b^2) \cos [c + d x] (a + b \sin [c + d x])^{5/2}}{63 a b d} - \\
 & \frac{2 \cos [c + d x] (a + b \sin [c + d x])^{7/2}}{9 b d} - \frac{\cot [c + d x] (a + b \sin [c + d x])^{7/2}}{a d} - \\
 & \left((20 a^4 + 1689 a^2 b^2 - 168 b^4) \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{a + b \sin [c + d x]} \right) / \\
 & \left(315 b^2 d \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) + \\
 & \left(a (20 a^4 + 739 a^2 b^2 + 816 b^4) \operatorname{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) / \\
 & \left(315 b^2 d \sqrt{a + b \sin [c + d x]} \right) + \frac{5 a^2 b \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}}}{d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result (type 4, 622 leaves):

$$\begin{aligned}
 & \frac{1}{1260 b d} \left(- \left(\left(2 (-1900 a^3 b + 1968 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) \right) - \right. \\
 & \left(2 (-20 a^4 + 1461 a^2 b^2 + 168 b^4) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \quad \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) - \left(2 i (20 a^4 + 1689 a^2 b^2 - 168 b^4) \operatorname{Cos}[c + d x] \operatorname{Cos}[2 (c + d x)] \right. \\
 & \quad \left(2 a (a - b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] - \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a + b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] \right) \right) \right) \\
 & \quad \left. \left. \left. \left. \sqrt{\frac{b - b \operatorname{Sin}[c + d x]}{a + b}} \sqrt{-\frac{b + b \operatorname{Sin}[c + d x]}{a - b}} \right) / \left(a \sqrt{-\frac{1}{a + b}} \sqrt{1 - \operatorname{Sin}[c + d x]^2} \right. \right. \right. \\
 & \quad \left. \left. \left. \left. (-2 a^2 + b^2 + 4 a (a + b \operatorname{Sin}[c + d x]) - 2 (a + b \operatorname{Sin}[c + d x])^2 \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a + b \operatorname{Sin}[c + d x]) + (a + b \operatorname{Sin}[c + d x])^2}{b^2}} \right) \right) \right) \right) + \frac{1}{d} \\
 & \quad \sqrt{a + b \operatorname{Sin}[c + d x]} \left(-\frac{a (20 a^2 - 1101 b^2) \operatorname{Cos}[c + d x]}{630 b} + \frac{19}{126} a b \operatorname{Cos}[3 (c + d x)] \right) - \\
 & \quad a^2 \operatorname{Cot}[c + d x] - \frac{1}{630} (150 a^2 - 119 b^2) \operatorname{Sin}[2 (c + d x)] + \\
 & \quad \left. \frac{1}{36} b^2 \operatorname{Sin}[4 (c + d x)] \right)
 \end{aligned}$$

Problem 1163: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cos}[c + d x] \operatorname{Cot}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{5/2} dx$$

Optimal (type 4, 430 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{(8 a^2 - 73 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{28 d} - \\
 & \frac{(8 a^2 - 35 b^2) \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{28 a d} - \frac{(8 a^2 - 21 b^2) \cos [c + d x] (a + b \sin [c + d x])^{5/2}}{28 a^2 d} - \\
 & \frac{3 b \cot [c + d x] (a + b \sin [c + d x])^{7/2}}{4 a^2 d} - \frac{\cot [c + d x] \csc [c + d x] (a + b \sin [c + d x])^{7/2}}{2 a d} + \\
 & \frac{a (8 a^2 - 247 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{28 b d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{(8 a^4 + 3 a^2 b^2 - 32 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{28 b d \sqrt{a + b \sin [c + d x]}} - \\
 & \frac{3 a (4 a^2 - 5 b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{4 d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result(type 4, 597 leaves):

$$\begin{aligned}
& \frac{1}{112 d} \left(\frac{2 (500 a^2 b - 64 b^3) \operatorname{EllipticF}\left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{\sqrt{a+b \operatorname{Sin}[c+d x]}} + \right. \\
& \left. \left(2 (160 a^3 + 37 a b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}} \right) / \right. \\
& \left. \left(\sqrt{a+b \operatorname{Sin}[c+d x]} \right) + \left(2 i (8 a^3 - 247 a b^2) \operatorname{Cos}[c+d x] \operatorname{Cos}[2(c+d x)] \right) \right. \\
& \left. \left(2 a (a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
& \left. \left. b \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
& \left. \left(\sqrt{\frac{b-b \operatorname{Sin}[c+d x]}{a+b}} \sqrt{-\frac{b+b \operatorname{Sin}[c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\operatorname{Sin}[c+d x]^2} \right. \right. \\
& \left. \left. (-2 a^2 + b^2 + 4 a (a+b \operatorname{Sin}[c+d x]) - 2 (a+b \operatorname{Sin}[c+d x])^2) \right. \right. \\
& \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \operatorname{Sin}[c+d x]) + (a+b \operatorname{Sin}[c+d x])^2}{b^2}} \right) \right) + \frac{1}{d} \right. \\
& \left. \sqrt{a+b \operatorname{Sin}[c+d x]} \left(-\frac{1}{14} (12 a^2 - 11 b^2) \operatorname{Cos}[c+d x] + \frac{1}{14} b^2 \operatorname{Cos}[3(c+d x)] - \right. \right. \\
& \left. \left. \frac{9}{4} a b \operatorname{Cot}[c+d x] - \frac{1}{2} a^2 \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x] - \right. \right. \\
& \left. \left. \frac{3}{7} a b \operatorname{Sin}[2(c+d x)] \right) \right)
\end{aligned}$$

Problem 1164: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cot}[c+d x]^4 (a+b \operatorname{Sin}[c+d x])^{5/2} dx$$

Optimal (type 4, 429 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{b (96 a^2 - 25 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{40 a d} - \\
 & \frac{b (208 a^2 - 25 b^2) \cos [c + d x] (a + b \sin [c + d x])^{3/2}}{120 a^2 d} + \\
 & \frac{(32 a^2 - 3 b^2) \cot [c + d x] (a + b \sin [c + d x])^{5/2}}{24 a^2 d} - \\
 & \frac{b \cot [c + d x] \csc [c + d x] (a + b \sin [c + d x])^{7/2}}{12 a^2 d} - \\
 & \frac{\cot [c + d x] \csc [c + d x]^2 (a + b \sin [c + d x])^{7/2}}{3 a d} + \\
 & \frac{(176 a^2 - 167 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{40 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{a (96 a^2 + 179 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{40 d \sqrt{a + b \sin [c + d x]}} - \\
 & \frac{5 b (12 a^2 - b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{8 d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result (type 4, 615 leaves):

$$\begin{aligned}
 & \frac{1}{160 d} \left(- \left(\left(2 (160 a^3 - 692 a b^2) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) \right) - \right. \\
 & \left(2 (-424 a^2 b - 117 b^3) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \quad \left(\sqrt{a + b \operatorname{Sin}[c + d x]} \right) - \left(2 i (-176 a^2 b + 167 b^3) \operatorname{Cos}[c + d x] \operatorname{Cos}[2 (c + d x)] \right. \\
 & \quad \left(2 a (a - b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] - \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a + b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \operatorname{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] \right) \right) \right) \\
 & \quad \left. \left(\sqrt{\frac{b - b \operatorname{Sin}[c + d x]}{a + b}} \sqrt{-\frac{b + b \operatorname{Sin}[c + d x]}{a - b}} \right) / \left(a \sqrt{-\frac{1}{a + b}} \sqrt{1 - \operatorname{Sin}[c + d x]^2} \right. \right. \\
 & \quad \left. \left. (-2 a^2 + b^2 + 4 a (a + b \operatorname{Sin}[c + d x]) - 2 (a + b \operatorname{Sin}[c + d x])^2) \right. \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a + b \operatorname{Sin}[c + d x]) + (a + b \operatorname{Sin}[c + d x])^2}{b^2}} \right) \right) + \frac{1}{d} \\
 & \sqrt{a + b \operatorname{Sin}[c + d x]} \left(-\frac{22}{15} a b \operatorname{Cos}[c + d x] + \frac{1}{24} (32 a^2 \operatorname{Cos}[c + d x] - 33 b^2 \operatorname{Cos}[c + d x]) \operatorname{Csc}[c + d x] - \right. \\
 & \quad \frac{13}{12} a b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] - \\
 & \quad \left. \frac{1}{3} a^2 \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 - \frac{1}{5} b^2 \operatorname{Sin}[2 (c + d x)] \right)
 \end{aligned}$$

Problem 1165: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Cot}[c + d x]^4 \operatorname{Csc}[c + d x] (a + b \operatorname{Sin}[c + d x])^{5/2} dx$$

Optimal (type 4, 449 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{b^2 (196 a^2 + 5 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{64 a^2 d} + \\
 & \frac{5 b (68 a^2 + b^2) \cot [c + d x] (a + b \sin [c + d x])^{3/2}}{192 a^2 d} + \\
 & \frac{(60 a^2 + b^2) \cot [c + d x] \csc [c + d x] (a + b \sin [c + d x])^{5/2}}{96 a^2 d} + \\
 & \frac{b \cot [c + d x] \csc [c + d x]^2 (a + b \sin [c + d x])^{7/2}}{24 a^2 d} - \\
 & \frac{\cot [c + d x] \csc [c + d x]^3 (a + b \sin [c + d x])^{7/2}}{4 a d} + \\
 & \frac{b (492 a^2 - 5 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{64 a d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{b (148 a^2 + 169 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{64 d \sqrt{a + b \sin [c + d x]}} + \\
 & \left(\frac{(48 a^4 - 360 a^2 b^2 - 5 b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}}}{64 a d \sqrt{a + b \sin [c + d x]}} \right) /
 \end{aligned}$$

Result (type 4, 655 leaves):

$$\begin{aligned}
& \frac{1}{d} \left(-\frac{2}{3} b^2 \cos [c+d x] + \frac{5 \left(116 a^2 b \cos [c+d x] - 3 b^3 \cos [c+d x] \right) \operatorname{Csc}[c+d x]}{192 a} + \right. \\
& \quad \frac{1}{96} \left(60 a^2 \cos [c+d x] - 59 b^2 \cos [c+d x] \right) \operatorname{Csc}[c+d x]^2 - \\
& \quad \left. \frac{17}{24} a b \cot [c+d x] \operatorname{Csc}[c+d x]^2 - \frac{1}{4} a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^3 \right) \sqrt{a+b \sin [c+d x]} + \\
& \quad \frac{1}{256 a d} \left(- \left(\left(2 \left(688 a^3 b - 348 a b^3 \right) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
& \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
& \quad \left(2 \left(96 a^4 - 228 a^2 b^2 - 15 b^4 \right) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
& \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i \left(-492 a^2 b^2 + 5 b^4 \right) \cos [c+d x] \cos [2 (c+d x)] \right) \\
& \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
& \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
& \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
& \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \quad \left. \left(-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2 \right) \right. \\
& \quad \left. \left. \sqrt{-\frac{a^2-b^2-2 a (a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1166: Result unnecessarily involves imaginary or complex numbers.

$$\int \cot [c+d x]^4 \operatorname{Csc}[c+d x]^2 (a+b \sin [c+d x])^{5/2} dx$$

Optimal (type 4, 482 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{(128 a^4 - 580 a^2 b^2 + 15 b^4) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{640 a^2 d} + \\
 & \frac{b (36 a^2 - b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] (a + b \operatorname{Sin}[c + d x])^{3/2}}{64 a^2 d} + \\
 & \frac{(32 a^2 - b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 (a + b \operatorname{Sin}[c + d x])^{5/2}}{80 a^2 d} + \\
 & \frac{3 b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{7/2}}{40 a^2 d} - \\
 & \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^4 (a + b \operatorname{Sin}[c + d x])^{7/2}}{5 a d} - \\
 & \left((128 a^4 - 2476 a^2 b^2 - 15 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}\right) / \\
 & \left(640 a^2 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) + \\
 & \left((128 a^4 + 492 a^2 b^2 - 5 b^4) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(640 a d \sqrt{a + b \operatorname{Sin}[c + d x]} \right) + \\
 & \left(3 b (80 a^4 - 40 a^2 b^2 + b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(128 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right)
 \end{aligned}$$

Result(type 4, 700 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{1}{640 a^2} (-128 a^4 \cos [c+d x]+1196 a^2 b^2 \cos [c+d x]+15 b^4 \cos [c+d x]) \operatorname{Csc}[c+d x]+ \right. \\
 & \quad \left. \frac{(436 a^2 b \cos [c+d x]-5 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{320 a}+ \right. \\
 & \quad \frac{1}{80} (32 a^2 \cos [c+d x]-31 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^3- \\
 & \quad \left. \frac{21}{40} a b \cot [c+d x] \operatorname{Csc}[c+d x]^3-\frac{1}{5} a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^4 \right) \sqrt{a+b \sin [c+d x]}+ \\
 & \frac{1}{2560 a^2 d} b \left(-\left(\left(2 (5936 a^3 b+20 a b^3) \operatorname{EllipticF}\left[\frac{1}{2} \left(-c+\frac{\pi}{2}-d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) -\left(2 (2272 a^4+1276 a^2 b^2+45 b^4) \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(-c+\frac{\pi}{2}-d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \left(\sqrt{a+b \sin [c+d x]} \right) - \right. \\
 & \quad \left. \left(2 i (128 a^4-2476 a^2 b^2-15 b^4) \cos [c+d x] \cos [2(c+d x)] \right. \right. \\
 & \quad \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \right. \\
 & \quad \left. \left. b \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \right) \\
 & \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{-b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
 & \quad \left. (-2 a^2+b^2+4 a(a+b \sin [c+d x])-2(a+b \sin [c+d x])^2) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1167: Result unnecessarily involves imaginary or complex numbers.

$$\int \text{Cot}[c + dx]^4 \text{Csc}[c + dx]^3 (a + b \text{Sin}[c + dx])^{5/2} dx$$

Optimal (type 4, 551 leaves, 13 steps):

$$\begin{aligned} & - \frac{b (720 a^4 - 176 a^2 b^2 + 15 b^4) \text{Cot}[c + dx] \sqrt{a + b \text{Sin}[c + dx]}}{1536 a^3 d} - \\ & \frac{(16 a^4 - 56 a^2 b^2 + 5 b^4) \text{Cot}[c + dx] \text{Csc}[c + dx] \sqrt{a + b \text{Sin}[c + dx]}}{256 a^2 d} + \\ & \frac{b (52 a^2 - 5 b^2) \text{Cot}[c + dx] \text{Csc}[c + dx]^2 (a + b \text{Sin}[c + dx])^{3/2}}{192 a^2 d} + \\ & \frac{(28 a^2 - 3 b^2) \text{Cot}[c + dx] \text{Csc}[c + dx]^3 (a + b \text{Sin}[c + dx])^{5/2}}{96 a^2 d} + \\ & \frac{b \text{Cot}[c + dx] \text{Csc}[c + dx]^4 (a + b \text{Sin}[c + dx])^{7/2}}{12 a^2 d} - \\ & \frac{\text{Cot}[c + dx] \text{Csc}[c + dx]^5 (a + b \text{Sin}[c + dx])^{7/2}}{6 a d} - \\ & \left(b (720 a^4 - 176 a^2 b^2 + 15 b^4) \text{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{a + b \text{Sin}[c + dx]}\right) / \\ & \left(1536 a^3 d \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} \right) + \\ & \left(b (816 a^4 + 1696 a^2 b^2 + 5 b^4) \text{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} \right) / \\ & \left(1536 a^2 d \sqrt{a + b \text{Sin}[c + dx]} \right) + \\ & \left(64 a^6 + 720 a^4 b^2 + 60 a^2 b^4 - 5 b^6 \right) \text{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \text{Sin}[c + dx]}{a + b}} / \\ & \left(512 a^3 d \sqrt{a + b \text{Sin}[c + dx]} \right) \end{aligned}$$

Result (type 4, 771 leaves):

$$\begin{aligned}
 & \frac{1}{d} \left(\frac{1}{1536 a^3} (-720 a^4 b \cos [c+d x] + 176 a^2 b^3 \cos [c+d x] - 15 b^5 \cos [c+d x]) \operatorname{Csc}[c+d x] + \right. \\
 & \quad \frac{1}{768 a^2} (-48 a^4 \cos [c+d x] + 600 a^2 b^2 \cos [c+d x] + 5 b^4 \cos [c+d x]) \operatorname{Csc}[c+d x]^2 + \\
 & \quad \left. \frac{(164 a^2 b \cos [c+d x] - b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]^3}{192 a} + \right. \\
 & \quad \frac{1}{96} (28 a^2 \cos [c+d x] - 27 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^4 - \frac{5}{12} a b \cot [c+d x] \operatorname{Csc}[c+d x]^4 - \\
 & \quad \left. \frac{1}{6} a^2 \cot [c+d x] \operatorname{Csc}[c+d x]^5 \right) \sqrt{a+b \sin [c+d x]} + \frac{1}{6144 a^3 d} \\
 & \left(- \left(\left(2 (192 a^5 b + 3744 a^3 b^3 - 20 a b^5) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
 & \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \left(2 (384 a^6 + 3600 a^4 b^2 + 536 a^2 b^4 - 45 b^6) \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \left(\sqrt{a+b \sin [c+d x]} \right) - \right. \\
 & \quad \left. \left(2 i (720 a^4 b^2 - 176 a^2 b^4 + 15 b^6) \cos [c+d x] \cos [2 (c+d x)] \right) \right. \\
 & \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
 & \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
 & \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
 & \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
 & \quad \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \\
 & \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right)
 \end{aligned}$$

Problem 1171: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]}{\sqrt{a+b \sin [c+d x]}} d x$$

Optimal (type 4, 288 leaves, 9 steps):

$$\begin{aligned} & \frac{8 a \cos [c+d x] \sqrt{a+b \sin [c+d x]}}{15 b^2 d} - \frac{2 \cos [c+d x] \sin [c+d x] \sqrt{a+b \sin [c+d x]}}{5 b d} + \\ & \frac{2 \left(8 a^2 - 21 b^2\right) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a+b \sin [c+d x]}}{15 b^3 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\ & \frac{2 a \left(8 a^2 - 23 b^2\right) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{15 b^3 d \sqrt{a+b \sin [c+d x]}} + \\ & \frac{2 \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{d \sqrt{a+b \sin [c+d x]}} \end{aligned}$$

Result (type 4, 536 leaves):

$$\begin{aligned}
 & -\frac{1}{30 b^2 d} \left(\frac{8 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
 & \left. \left(2\left(-8 a^2-9 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right) / \right. \\
 & \left. \left(\sqrt{a+b \sin [c+d x]}\right) - \left(2 i\left(8 a^2-21 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right. \right. \\
 & \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
 & \left. \left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
 & \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]\right) \right) \right) \\
 & \left. \left(\sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{\frac{b+b \sin [c+d x]}{a-b}}\right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \right. \\
 & \left. \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2\right) \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right) + \right. \\
 & \left. \frac{\sqrt{a+b \sin [c+d x]}}{d} \left(\frac{8 a \cos [c+d x]}{15 b^2} - \frac{\sin [2(c+d x)]}{5 b} \right) \right)
 \end{aligned}$$

Problem 1172: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^2 \cot [c+d x]^2}{\sqrt{a+b \sin [c+d x]}} d x$$

Optimal (type 4, 285 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sin}[c+d x]}}{3 b d} - \frac{\operatorname{Cot}[c+d x] \sqrt{a+b \operatorname{Sin}[c+d x]}}{a d} \\
 & \frac{(4 a^2+3 b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{a+b \operatorname{Sin}[c+d x]}}{3 a b^2 d \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}} + \\
 & \frac{(4 a^2-7 b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{3 b^2 d \sqrt{a+b \operatorname{Sin}[c+d x]}} - \\
 & \frac{b \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{a d \sqrt{a+b \operatorname{Sin}[c+d x]}}
 \end{aligned}$$

Result (type 4, 534 leaves):

$$\frac{\left(-\frac{2 \operatorname{Cos}[c+d x]}{3 b}-\frac{\operatorname{Cot}[c+d x]}{a}\right) \sqrt{a+b \operatorname{Sin}[c+d x]}}{d} +$$

$$\frac{1}{12 a b d} \left(\frac{40 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{\sqrt{a+b \operatorname{Sin}[c+d x]}} - \right.$$

$$\left. \left(2\left(-4 a^2-9 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}} \right) / \right.$$

$$\left. \left(\sqrt{a+b \operatorname{Sin}[c+d x]} \right) - \left(2 i\left(4 a^2+3 b^2\right) \operatorname{Cos}[c+d x] \operatorname{Cos}\left[2(c+d x)\right] \right.$$

$$\left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] + \right.$$

$$\left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] - \right.$$

$$\left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \operatorname{Sin}[c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right)$$

$$\left. \left(\sqrt{\frac{b-b \operatorname{Sin}[c+d x]}{a+b}} \sqrt{-\frac{b+b \operatorname{Sin}[c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\operatorname{Sin}[c+d x]^2} \right.$$

$$\left. \left(-2 a^2+b^2+4 a(a+b \operatorname{Sin}[c+d x]) - 2(a+b \operatorname{Sin}[c+d x])^2 \right) \right)$$

$$\left. \left(\sqrt{-\frac{a^2-b^2-2 a(a+b \operatorname{Sin}[c+d x])+(a+b \operatorname{Sin}[c+d x])^2}{b^2}} \right) \right)$$

Problem 1173: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c+d x] \operatorname{Cot}[c+d x]^3}{\sqrt{a+b \operatorname{Sin}[c+d x]}} dx$$

Optimal (type 4, 307 leaves, 9 steps):

$$\begin{aligned}
 & \frac{3 b \cot [c+d x] \sqrt{a+b \sin [c+d x]}}{4 a^2 d} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x] \sqrt{a+b \sin [c+d x]}}{2 a d} + \\
 & \frac{(8 a^2+3 b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{a+b \sin [c+d x]}}{4 a^2 b d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{(8 a^2+b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{4 a b d \sqrt{a+b \sin [c+d x]}} - \\
 & \frac{3\left(4 a^2-b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{4 a^2 d \sqrt{a+b \sin [c+d x]}}
 \end{aligned}$$

Result (type 4, 443 leaves):

$$\frac{1}{16 d} \left(\frac{1}{a^3 b^2 \sqrt{-\frac{1}{a+b}} (-2 + \text{Csc}[c + d x])^2} - 2 i (8 a^2 + 3 b^2) \text{Cos}[2 (c + d x)] \text{Csc}[c + d x]^2 \right. \\ \left. \left(2 a (a - b) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] + \right. \right. \\ \left. \left. b \left(2 a \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] - \right. \right. \right. \\ \left. \left. \left. b \text{EllipticPi}\left[\frac{a + b}{a}, i \text{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \text{Sin}[c + d x]} \right], \frac{a + b}{a - b} \right] \right) \right) \right) \\ \text{Sec}[c + d x] \sqrt{-\frac{b (-1 + \text{Sin}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sin}[c + d x])}{a - b}} - \\ \frac{4 \text{Cot}[c + d x] (-3 b + 2 a \text{Csc}[c + d x]) \sqrt{a + b \text{Sin}[c + d x]}}{a^2} - \\ \frac{8 b \text{EllipticF}\left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \text{Sin}[c + d x]}{a + b}}}{a \sqrt{a + b \text{Sin}[c + d x]}} + \\ \left(2 (16 a^2 - 9 b^2) \text{EllipticPi}\left[2, \frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \text{Sin}[c + d x]}{a + b}} \right) / \\ \left. \left(a^2 \sqrt{a + b \text{Sin}[c + d x]} \right) \right)$$

Problem 1174: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Cot}[c + d x]^4}{\sqrt{a + b \text{Sin}[c + d x]}} dx$$

Optimal (type 4, 353 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(32 a^2 - 15 b^2) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{24 a^3 d} + \\
 & \frac{5 b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{12 a^2 d} - \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 \sqrt{a + b \operatorname{Sin}[c + d x]}}{3 a d} + \\
 & \frac{(32 a^2 - 15 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}}{24 a^3 d \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}} + \\
 & \frac{(16 a^2 + 5 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{24 a^2 d \sqrt{a + b \operatorname{Sin}[c + d x]}} + \\
 & \frac{b (12 a^2 - 5 b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+d x]}{a+b}}}{8 a^3 d \sqrt{a + b \operatorname{Sin}[c + d x]}}
 \end{aligned}$$

Result (type 4, 596 leaves):

$$\begin{aligned}
& \frac{1}{d} \left(\frac{(32 a^2 \cos [c+d x]-15 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]}{24 a^3} + \right. \\
& \quad \left. \frac{5 b \cot [c+d x] \operatorname{Csc}[c+d x]}{12 a^2} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^2}{3 a} \right) \sqrt{a+b \sin [c+d x]} + \\
& \frac{1}{96 a^3 d} \left(- \left(\left(2 (96 a^3 - 20 a b^2) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) \right) \right. \\
& \quad \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \\
& \left(2 (104 a^2 b - 45 b^3) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) \sqrt{ \\
& \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (-32 a^2 b + 15 b^3) \cos [c+d x] \cos [2 (c+d x)] \right) \\
& \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
& \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
& \quad \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \\
& \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \sqrt{a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2}} \\
& \left(-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2 \right) \\
& \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right)
\end{aligned}$$

Problem 1175: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cot [c+d x]^4 \operatorname{Csc}[c+d x]}{\sqrt{a+b \sin [c+d x]}} dx$$

Optimal (type 4, 412 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{b (188 a^2 - 105 b^2) \operatorname{Cot}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{192 a^4 d} + \\
 & \frac{5 (12 a^2 - 7 b^2) \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{a + b \operatorname{Sin}[c + d x]}}{96 a^3 d} + \\
 & \frac{7 b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 \sqrt{a + b \operatorname{Sin}[c + d x]}}{24 a^2 d} - \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^3 \sqrt{a + b \operatorname{Sin}[c + d x]}}{4 a d} - \\
 & \left(b (188 a^2 - 105 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{a + b \operatorname{Sin}[c + d x]}\right) / \\
 & \left(192 a^4 d \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) + \frac{b (68 a^2 - 35 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}}}{192 a^3 d \sqrt{a + b \operatorname{Sin}[c + d x]}} + \\
 & \left((48 a^4 - 72 a^2 b^2 + 35 b^4) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \operatorname{Sin}[c + d x]}{a + b}} \right) / \\
 & \left(64 a^4 d \sqrt{a + b \operatorname{Sin}[c + d x]} \right)
 \end{aligned}$$

Result (type 4, 647 leaves):

$$\begin{aligned}
& \frac{1}{d} \left(\frac{(-188 a^2 b \cos [c+d x] + 105 b^3 \cos [c+d x]) \operatorname{Csc}[c+d x]}{192 a^4} + \right. \\
& \quad \frac{5 (12 a^2 \cos [c+d x] - 7 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]^2}{96 a^3} + \\
& \quad \left. \frac{7 b \cot [c+d x] \operatorname{Csc}[c+d x]^2}{24 a^2} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^3}{4 a} \right) \sqrt{a+b \sin [c+d x]} + \\
& \frac{1}{768 a^4 d} \left(- \left(\left(2 (-240 a^3 b + 140 a b^3) \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \\
& \quad \left. \left. \left(\sqrt{a+b \sin [c+d x]} \right) \right) - \right. \\
& \left(2 (288 a^4 - 620 a^2 b^2 + 315 b^4) \operatorname{EllipticPi} \left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - d x \right), \frac{2 b}{a+b} \right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
& \quad \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i (188 a^2 b^2 - 105 b^4) \cos [c+d x] \cos [2 (c+d x)] \right. \\
& \quad \left(2 a (a-b) \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] + \right. \\
& \quad b \left(2 a \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] - \right. \\
& \quad \left. \left. \left. b \operatorname{EllipticPi} \left[\frac{a+b}{a}, i \operatorname{ArcSinh} \left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]} \right], \frac{a+b}{a-b} \right] \right) \right) \right) \\
& \quad \left. \left. \left. \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left. (-2 a^2 + b^2 + 4 a (a+b \sin [c+d x]) - 2 (a+b \sin [c+d x])^2) \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a+b \sin [c+d x]) + (a+b \sin [c+d x])^2}{b^2}} \right) \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 1179: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^3 \cot [c+d x]}{(a+b \sin [c+d x])^{3/2}} dx$$

Optimal (type 4, 296 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 (a^2 - b^2) \cos [c + d x]}{a b^2 d \sqrt{a + b \sin [c + d x]}} - \frac{2 \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{3 b^2 d} - \\
 & \frac{2 (8 a^2 - 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{3 a b^3 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} + \\
 & \frac{2 (8 a^2 - 5 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{3 b^3 d \sqrt{a + b \sin [c + d x]}} + \\
 & \frac{2 \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{a d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result (type 4, 565 leaves):

$$\begin{aligned}
& \frac{\sqrt{a+b \sin [c+d x]} \left(-\frac{2 \cos [c+d x]}{3 b^2} - \frac{2\left(a^2 \cos [c+d x]-b^2 \cos [c+d x]\right)}{a b^2(a+b \sin [c+d x])} \right)}{d} + \\
& \frac{1}{6 a b^2 d} \left(\frac{8 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
& \left. \left(2\left(-8 a^2+9 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \\
& \left. \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i\left(8 a^2-3 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right. \right. \\
& \left. \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \right. \\
& \left. \left. \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
& \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2 \right) \right. \\
& \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1180: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^2 \cot [c+d x]^2}{(a+b \sin [c+d x])^{3/2}} dx$$

Optimal (type 4, 294 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(2a^2 - 3b^2) \cos[c + dx]}{a^2 b d \sqrt{a + b \sin[c + dx]}} - \frac{\cot[c + dx]}{a d \sqrt{a + b \sin[c + dx]}} + \\
 & \frac{(4a^2 - 3b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a + b \sin[c + dx]}}{a^2 b^2 d \sqrt{\frac{a+b \sin[c+dx]}{a+b}}} - \\
 & \frac{(4a^2 - b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{a b^2 d \sqrt{a + b \sin[c + dx]}} - \\
 & \frac{3 b \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{a^2 d \sqrt{a + b \sin[c + dx]}}
 \end{aligned}$$

Result (type 4, 563 leaves):

$$\begin{aligned}
& \frac{\sqrt{a+b \sin [c+d x]} \left(-\frac{\cot [c+d x]}{a^2} + \frac{2\left(a^2 \cos [c+d x]-b^2 \cos [c+d x]\right)}{a^2 b(a+b \sin [c+d x])} \right)}{d} - \\
& \frac{1}{4 a^2 b d} \left(-\frac{8 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
& \left. \left(2\left(-4 a^2+9 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}\right) / \right. \\
& \left. \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i\left(4 a^2-3 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right) \right. \\
& \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
& \left. \left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right]\right) \right) \right) \\
& \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}}\right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2 \right) \right. \\
& \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1181: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x] \cot [c+d x]^3}{(a+b \sin [c+d x])^{3/2}} dx$$

Optimal (type 4, 366 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(4a^2 - 5b^2) \cot[c + dx]}{2a^2bd\sqrt{a+b\sin[c+dx]}} - \frac{\cot[c+dx] \operatorname{Csc}[c+dx]}{2ad\sqrt{a+b\sin[c+dx]}} - \\
 & \frac{(8a^2 - 15b^2) \cot[c+dx] \sqrt{a+b\sin[c+dx]}}{4a^3bd} - \\
 & \frac{(8a^2 - 15b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a+b\sin[c+dx]}}{4a^3bd \sqrt{\frac{a+b\sin[c+dx]}{a+b}}} + \\
 & \frac{(8a^2 - 5b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{4a^2bd\sqrt{a+b\sin[c+dx]}} - \\
 & \frac{3(4a^2 - 5b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{4a^3d\sqrt{a+b\sin[c+dx]}}
 \end{aligned}$$

Result (type 4, 579 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{a+b \sin [c+d x]} \\
& \left(\frac{7 b \cot [c+d x]}{4 a^3} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]}{2 a^2} - \frac{2\left(a^2 \cos [c+d x]-b^2 \cos [c+d x]\right)}{a^3(a+b \sin [c+d x])} \right) + \\
& \frac{1}{16 a^3 d} \left(-\frac{40 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
& \left. \left(2\left(-32 a^2+45 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \\
& \left. \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i\left(8 a^2-15 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right) \right. \\
& \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
& \left. \left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
& \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2 \right) \right. \\
& \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1182: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cot [c+d x]^4}{(a+b \sin [c+d x])^{3/2}} dx$$

Optimal (type 4, 416 leaves, 11 steps):

$$\begin{aligned}
 & \frac{(6a^2 - 7b^2) \cot[c+dx] \operatorname{Csc}[c+dx]}{3a^2bd\sqrt{a+b\sin[c+dx]}} - \\
 & \frac{\cot[c+dx] \operatorname{Csc}[c+dx]^2}{3ad\sqrt{a+b\sin[c+dx]}} + \frac{5(16a^2 - 21b^2) \cot[c+dx] \sqrt{a+b\sin[c+dx]}}{24a^4d} - \\
 & \frac{(24a^2 - 35b^2) \cot[c+dx] \operatorname{Csc}[c+dx] \sqrt{a+b\sin[c+dx]}}{12a^3bd} + \\
 & \frac{5(16a^2 - 21b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a+b\sin[c+dx]}}{24a^4d \sqrt{\frac{a+b\sin[c+dx]}{a+b}}} - \\
 & \frac{(32a^2 - 35b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{24a^3d\sqrt{a+b\sin[c+dx]}} + \\
 & \frac{b(36a^2 - 35b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{8a^4d\sqrt{a+b\sin[c+dx]}}
 \end{aligned}$$

Result (type 4, 636 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{a + b \sin[c + dx]} \\
& \left(\frac{(32 a^2 \cos[c + dx] - 57 b^2 \cos[c + dx]) \operatorname{Csc}[c + dx]}{24 a^4} + \frac{11 b \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]}{12 a^3} - \right. \\
& \quad \left. \frac{\operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]^2}{3 a^2} + \frac{2 (a^2 b \cos[c + dx] - b^3 \cos[c + dx])}{a^4 (a + b \sin[c + dx])} \right) + \\
& \frac{1}{96 a^4 d} \left(- \left(\left(2 (96 a^3 - 140 a b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a + b}} \right) / \right. \right. \\
& \quad \left. \left. (\sqrt{a + b \sin[c + dx]}) \right) - \right. \\
& \left(2 (296 a^2 b - 315 b^3) \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(-c + \frac{\pi}{2} - dx\right), \frac{2 b}{a + b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a + b}} \right) / \\
& \quad \left. (\sqrt{a + b \sin[c + dx]}) - \left(2 i (-80 a^2 b + 105 b^3) \cos[c + dx] \cos[2(c + dx)] \right) \right. \\
& \quad \left(2 a (a - b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a + b}{a - b}\right] + \right. \\
& \quad b \left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a + b}{a - b}\right] - \right. \\
& \quad \left. \left. b \operatorname{EllipticPi}\left[\frac{a + b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a + b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a + b}{a - b}\right] \right) \right) \\
& \quad \left. \left(\sqrt{\frac{b - b \sin[c + dx]}{a + b}} \sqrt{-\frac{b + b \sin[c + dx]}{a - b}} \right) / \left(a \sqrt{-\frac{1}{a + b}} \sqrt{1 - \sin[c + dx]^2} \right) \right. \\
& \quad \left. (-2 a^2 + b^2 + 4 a (a + b \sin[c + dx]) - 2 (a + b \sin[c + dx])^2) \right. \\
& \quad \left. \left. \sqrt{-\frac{a^2 - b^2 - 2 a (a + b \sin[c + dx]) + (a + b \sin[c + dx])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1183: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^4 \sin[c + dx]^3}{(a + b \sin[c + dx])^{5/2}} dx$$

Optimal (type 4, 469 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{2 (a^2 - b^2) \cos [c + d x] \sin [c + d x]^4}{3 a b^2 d (a + b \sin [c + d x])^{3/2}} + \frac{2 (13 a^2 - 5 b^2) \cos [c + d x] \sin [c + d x]^4}{3 a^2 b^2 d \sqrt{a + b \sin [c + d x]}} + \\
 & \frac{128 a (40 a^2 - 19 b^2) \cos [c + d x] \sqrt{a + b \sin [c + d x]}}{315 b^6 d} - \\
 & \frac{8 (480 a^2 - 203 b^2) \cos [c + d x] \sin [c + d x] \sqrt{a + b \sin [c + d x]}}{315 b^5 d} + \\
 & \frac{4 (160 a^2 - 63 b^2) \cos [c + d x] \sin [c + d x]^2 \sqrt{a + b \sin [c + d x]}}{63 a b^4 d} - \\
 & \frac{10 (8 a^2 - 3 b^2) \cos [c + d x] \sin [c + d x]^3 \sqrt{a + b \sin [c + d x]}}{9 a^2 b^3 d} + \\
 & \left(8 (1280 a^4 - 768 a^2 b^2 + 21 b^4) \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{a + b \sin [c + d x]} \right) / \\
 & \left(315 b^7 d \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) - \\
 & \left(8 a (1280 a^4 - 1088 a^2 b^2 + 123 b^4) \operatorname{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), \frac{2 b}{a + b} \right] \sqrt{\frac{a + b \sin [c + d x]}{a + b}} \right) / \\
 & \left(315 b^7 d \sqrt{a + b \sin [c + d x]} \right)
 \end{aligned}$$

Result (type 4, 1044 leaves):

$$\begin{aligned}
 & \frac{1}{10080 d (a + b \sin [c + d x])^{3/2}} \\
 & \left(315 \left(\frac{1}{(a - b)^2 b} \left((a^2 + 3 b^2) \operatorname{EllipticE} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] + a (-a + b) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \right) \left(\frac{a + b \sin [c + d x]}{a + b} \right)^{3/2} - \right. \\
 & \quad \left. \frac{\cos [c + d x] (2 a (a^2 + b^2) + b (a^2 + 3 b^2) \sin [c + d x])}{(a^2 - b^2)^2} \right) + \frac{1}{b^3} \\
 & 315 \left(\frac{1}{(a - b)^2} \left((32 a^4 - 57 a^2 b^2 + 21 b^4) \operatorname{EllipticE} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] + \right. \right. \\
 & \quad \left. \left. a (-32 a^3 + 32 a^2 b + 33 a b^2 - 33 b^3) \operatorname{EllipticF} \left[\frac{1}{4} (-2 c + \pi - 2 d x), \frac{2 b}{a + b} \right] \right) \right. \\
 & \quad \left. \left(\frac{a + b \sin [c + d x]}{a + b} \right)^{3/2} - \frac{1}{2 (a^2 - b^2)^2} \right. \\
 & \quad \left. \left. b (4 a (8 a^4 - 13 a^2 b^2 + 3 b^4) \cos [c + d x] + b (20 a^4 - 33 a^2 b^2 + 9 b^4) \sin [2 (c + d x)]) \right) \right) - \frac{1}{b^5}
 \end{aligned}$$

$$\begin{aligned}
 & 21 \left(\frac{1}{(a-b)^2} \left((-2048 a^6 + 4192 a^4 b^2 - 2355 a^2 b^4 + 231 b^6) \operatorname{EllipticE} \left[\frac{1}{4} (-2c + \pi - 2dx), \frac{2b}{a+b} \right] + \right. \right. \\
 & \quad a (2048 a^5 - 2048 a^4 b - 2656 a^3 b^2 + 2656 a^2 b^3 + 603 a b^4 - 603 b^5) \\
 & \quad \left. \operatorname{EllipticF} \left[\frac{1}{4} (-2c + \pi - 2dx), \frac{2b}{a+b} \right] \right) \left(\frac{a+b \operatorname{Sin}[c+dx]}{a+b} \right)^{3/2} + \frac{1}{(a^2-b^2)^2} b \operatorname{Cos}[c+dx] \\
 & \quad \left(-64 a b^2 (a^2-b^2)^2 \operatorname{Cos}[2(c+dx)] + b (1280 a^6 - 2536 a^4 b^2 + 1347 a^2 b^4 - 111 b^6) \right. \\
 & \quad \left. \operatorname{Sin}[c+dx] + 2 (512 a^7 - 952 a^5 b^2 + 423 a^3 b^4 + 7 a b^6 + 6 b^3 (a^2-b^2)^2 \operatorname{Sin}[3(c+dx)]) \right) \Big) - \\
 & \frac{1}{b^7} 5 (a+b \operatorname{Sin}[c+dx]) \left(\left(\left(-4b (-4096 a^7 b + 8960 a^5 b^3 - 5884 a^3 b^5 + 1041 a b^7) \right. \right. \right. \\
 & \quad \left. \operatorname{EllipticF} \left[\frac{1}{4} (-2c + \pi - 2dx), \frac{2b}{a+b} \right] + (65536 a^8 - 161792 a^6 b^2 + 129664 a^4 \right. \\
 & \quad \left. b^4 - 35109 a^2 b^6 + 1617 b^8) \left((a+b) \operatorname{EllipticE} \left[\frac{1}{4} (-2c + \pi - 2dx), \frac{2b}{a+b} \right] - a \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF} \left[\frac{1}{4} (-2c + \pi - 2dx), \frac{2b}{a+b} \right] \right) \sqrt{\frac{a+b \operatorname{Sin}[c+dx]}{a+b}} \right) / \\
 & \quad \left((a-b)^2 (a+b)^2 + b (a+b \operatorname{Sin}[c+dx]) \left(-128 a (88 a^2 - 27 b^2) \operatorname{Cos}[c+dx] + \right. \right. \\
 & \quad \left. \left. 416 a b^2 \operatorname{Cos}[3(c+dx)] + \frac{21 a (64 a^6 - 112 a^4 b^2 + 56 a^2 b^4 - 7 b^6) \operatorname{Cos}[c+dx]}{(a^2-b^2) (a+b \operatorname{Sin}[c+dx])^2} - \right. \right. \\
 & \quad \left. \left. (21 (1088 a^8 - 2576 a^6 b^2 + 1960 a^4 b^4 - 497 a^2 b^6 + 21 b^8) \operatorname{Cos}[c+dx]) / \right. \right. \\
 & \quad \left. \left. ((a^2-b^2)^2 (a+b \operatorname{Sin}[c+dx])) \right) - \right. \\
 & \quad \left. \left. 8 b (-276 a^2 + 35 b^2) \operatorname{Sin}[2(c+dx)] - 56 b^3 \operatorname{Sin}[4(c+dx)] \right) \right) \Big) \Big) \Big)
 \end{aligned}$$

Problem 1186: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c+dx]^3 \operatorname{Cot}[c+dx]}{(a+b \operatorname{Sin}[c+dx])^{5/2}} dx$$

Optimal (type 4, 313 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 (a^2 - b^2) \cos [c + d x]}{3 a b^2 d (a + b \sin [c + d x])^{3/2}} + \frac{2 (5 a^2 + 3 b^2) \cos [c + d x]}{3 a^2 b^2 d \sqrt{a + b \sin [c + d x]}} + \\
 & \frac{2 (8 a^2 + 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{a + b \sin [c + d x]}}{3 a^2 b^3 d \sqrt{\frac{a+b \sin [c+d x]}{a+b}}} - \\
 & \frac{2 (8 a^2 + b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{3 a b^3 d \sqrt{a + b \sin [c + d x]}} + \\
 & \frac{2 \operatorname{EllipticPi}\left[2, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{a^2 d \sqrt{a + b \sin [c + d x]}}
 \end{aligned}$$

Result(type 4, 599 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{a + b \sin[c + dx]} \\
& \left(-\frac{2(a^2 \cos[c + dx] - b^2 \cos[c + dx])}{3ab^2(a + b \sin[c + dx])^2} + \frac{2(5a^2 \cos[c + dx] + 3b^2 \cos[c + dx])}{3a^2b^2(a + b \sin[c + dx])} \right) - \\
& \frac{1}{6a^2b^2d} \left(\frac{8ab \operatorname{EllipticF}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{\sqrt{a + b \sin[c + dx]}} - \right. \\
& \left. \left(2(-8a^2 - 9b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a+b}} \right) / \right. \\
& \left. \left(\sqrt{a + b \sin[c + dx]} \right) - \left(2i(8a^2 + 3b^2) \cos[c + dx] \cos[2(c + dx)] \right) \right. \\
& \left. \left(2a(a - b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
& \left. \left. b \left(2a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
& \left. \left(\sqrt{\frac{b - b \sin[c + dx]}{a+b}} \sqrt{-\frac{b + b \sin[c + dx]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1 - \sin[c + dx]^2} \right) \right. \\
& \left. \left(-2a^2 + b^2 + 4a(a + b \sin[c + dx]) - 2(a + b \sin[c + dx])^2 \right) \right. \\
& \left. \left. \left. \sqrt{-\frac{a^2 - b^2 - 2a(a + b \sin[c + dx]) + (a + b \sin[c + dx])^2}{b^2}} \right) \right) \right)
\end{aligned}$$

Problem 1187: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c + dx]^2 \cot[c + dx]^2}{(a + b \sin[c + dx])^{5/2}} dx$$

Optimal (type 4, 346 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(2a^2 - 5b^2) \cos[c + dx]}{3a^2bd(a + b \sin[c + dx])^{3/2}} - \frac{\cot[c + dx]}{ad(a + b \sin[c + dx])^{3/2}} - \frac{(4a^2 + 15b^2) \cos[c + dx]}{3a^3bd\sqrt{a + b \sin[c + dx]}} - \\
 & \frac{(4a^2 + 15b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a + b \sin[c + dx]}}{3a^3b^2d\sqrt{\frac{a+b \sin[c+dx]}{a+b}}} + \\
 & \frac{(4a^2 + 5b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{3a^2b^2d\sqrt{a + b \sin[c + dx]}} - \\
 & \frac{5b \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{a^3d\sqrt{a + b \sin[c + dx]}}
 \end{aligned}$$

Result(type 4, 609 leaves):

$$\frac{1}{d} \sqrt{a + b \sin[c + dx]} \left(-\frac{\cot[c + dx]}{a^3} + \frac{2(a^2 \cos[c + dx] - b^2 \cos[c + dx])}{3a^2 b (a + b \sin[c + dx])^2} - \frac{4(a^2 \cos[c + dx] + 3b^2 \cos[c + dx])}{3a^3 b (a + b \sin[c + dx])} \right) +$$

$$\frac{1}{12a^3 b d} \left(\frac{40ab \operatorname{EllipticF}\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \sin[c+dx]}{a+b}}}{\sqrt{a + b \sin[c + dx]}} - \right.$$

$$\left. \left(2(-4a^2 - 45b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a + b \sin[c + dx]}{a + b}} \right) / \right.$$

$$\left. \left(\sqrt{a + b \sin[c + dx]} \right) - \left(2i(4a^2 + 15b^2) \cos[c + dx] \cos[2(c + dx)] \right) \right.$$

$$\left. \left(2a(a - b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] + \right. \right.$$

$$\left. b \left(2a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] - \right. \right.$$

$$\left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin[c + dx]}\right], \frac{a+b}{a-b}\right] \right) \right) \right.$$

$$\left. \left(\sqrt{\frac{b - b \sin[c + dx]}{a + b}} \sqrt{-\frac{b + b \sin[c + dx]}{a - b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1 - \sin[c + dx]^2} \right) \right.$$

$$\left. \left(-2a^2 + b^2 + 4a(a + b \sin[c + dx]) - 2(a + b \sin[c + dx])^2 \right) \right.$$

$$\left. \left. \sqrt{-\frac{a^2 - b^2 - 2a(a + b \sin[c + dx]) + (a + b \sin[c + dx])^2}{b^2}} \right) \right)$$

Problem 1188: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c + dx] \cot[c + dx]^3}{(a + b \sin[c + dx])^{5/2}} dx$$

Optimal (type 4, 407 leaves, 11 steps):

$$\begin{aligned}
 & \frac{(4a^2 - 7b^2) \operatorname{Cot}[c + dx]}{6a^2bd(a + b \operatorname{Sin}[c + dx])^{3/2}} - \frac{\operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]}{2ad(a + b \operatorname{Sin}[c + dx])^{3/2}} - \frac{(8a^2 - 105b^2) \operatorname{Cos}[c + dx]}{12a^4d\sqrt{a + b \operatorname{Sin}[c + dx]}} - \\
 & \frac{(8a^2 - 35b^2) \operatorname{Cot}[c + dx]}{12a^3bd\sqrt{a + b \operatorname{Sin}[c + dx]}} - \frac{(8a^2 - 105b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a + b \operatorname{Sin}[c + dx]}}{12a^4bd\sqrt{\frac{a+b \operatorname{Sin}[c+dx]}{a+b}}} + \\
 & \frac{(8a^2 - 35b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+dx]}{a+b}}}{12a^3bd\sqrt{a + b \operatorname{Sin}[c + dx]}} - \\
 & \frac{(12a^2 - 35b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b \operatorname{Sin}[c+dx]}{a+b}}}{4a^4d\sqrt{a + b \operatorname{Sin}[c + dx]}}
 \end{aligned}$$

Result(type 4, 622 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{a+b \sin [c+d x]} \left(\frac{11 b \cot [c+d x]}{4 a^4} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]}{2 a^3} - \right. \\
& \left. \frac{2\left(a^2 \cos [c+d x]-b^2 \cos [c+d x]\right)}{3 a^3(a+b \sin [c+d x])^2} - \frac{2\left(a^2 \cos [c+d x]-9 b^2 \cos [c+d x]\right)}{3 a^4(a+b \sin [c+d x])} \right) + \\
& \frac{1}{48 a^4 d} \left(-\frac{280 a b \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}}}{\sqrt{a+b \sin [c+d x]}} - \right. \\
& \left(2\left(-80 a^2+315 b^2\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \\
& \left(\sqrt{a+b \sin [c+d x]} \right) - \left(2 i\left(8 a^2-105 b^2\right) \cos [c+d x] \cos [2(c+d x)] \right. \\
& \left. \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \right. \\
& \left. \left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \right. \\
& \left. \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \right) \\
& \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x]) - 2(a+b \sin [c+d x])^2 \right) \right. \\
& \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1189: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cot [c+d x]^4}{(a+b \sin [c+d x])^{5/2}} dx$$

Optimal (type 4, 458 leaves, 12 steps):

$$\begin{aligned}
 & \frac{(2a^2 - 3b^2) \cot[c+dx] \operatorname{Csc}[c+dx]}{3a^2bd(a+b\sin[c+dx])^{3/2}} - \frac{\cot[c+dx] \operatorname{Csc}[c+dx]^2}{3ad(a+b\sin[c+dx])^{3/2}} + \frac{b(32a^2 - 105b^2) \cos[c+dx]}{8a^5d\sqrt{a+b\sin[c+dx]}} + \\
 & \frac{(16a^2 - 35b^2) \cot[c+dx]}{8a^4d\sqrt{a+b\sin[c+dx]}} - \frac{(8a^2 - 21b^2) \cot[c+dx] \operatorname{Csc}[c+dx]}{12a^3bd\sqrt{a+b\sin[c+dx]}} + \\
 & \frac{(32a^2 - 105b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{a+b\sin[c+dx]}}{8a^5d\sqrt{\frac{a+b\sin[c+dx]}{a+b}}} - \\
 & \frac{(16a^2 - 35b^2) \operatorname{EllipticF}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{8a^4d\sqrt{a+b\sin[c+dx]}} + \\
 & \frac{15b(4a^2 - 7b^2) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), \frac{2b}{a+b}\right] \sqrt{\frac{a+b\sin[c+dx]}{a+b}}}{8a^5d\sqrt{a+b\sin[c+dx]}}
 \end{aligned}$$

Result (type 4, 680 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{a+b \sin [c+d x]} \left(\frac{(32 a^2 \cos [c+d x]-123 b^2 \cos [c+d x]) \operatorname{Csc}[c+d x]}{24 a^5} + \right. \\
& \quad \frac{17 b \cot [c+d x] \operatorname{Csc}[c+d x]}{12 a^4} - \frac{\cot [c+d x] \operatorname{Csc}[c+d x]^2}{3 a^3} + \\
& \quad \left. \frac{2\left(a^2 b \cos [c+d x]-b^3 \cos [c+d x]\right)}{3 a^4(a+b \sin [c+d x])^2} + \frac{8\left(a^2 b \cos [c+d x]-3 b^3 \cos [c+d x]\right)}{3 a^5(a+b \sin [c+d x])} \right) + \\
& \frac{1}{32 a^5 d} \left(- \left(\left(\left(2\left(32 a^3-140 a b^2\right) \operatorname{EllipticF}\left[\frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \right. \right. \\
& \quad \left. \left. \left. \left(\sqrt{a+b \sin [c+d x]}\right) \right) - \right. \right. \\
& \quad \left. \left(2\left(152 a^2 b-315 b^3\right) \operatorname{EllipticPi}\left[2, \frac{1}{2}\left(-c+\frac{\pi}{2}-d x\right), \frac{2 b}{a+b}\right] \sqrt{\frac{a+b \sin [c+d x]}{a+b}} \right) / \right. \\
& \quad \left. \left(\sqrt{a+b \sin [c+d x]}\right) - \left(2 i\left(-32 a^2 b+105 b^3\right) \cos [c+d x] \cos [2(c+d x)] \right) \right. \\
& \quad \left(2 a(a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] + \right. \\
& \quad \left. b\left(2 a \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] - \right. \right. \\
& \quad \left. \left. b \operatorname{EllipticPi}\left[\frac{a+b}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin [c+d x]}\right], \frac{a+b}{a-b}\right] \right) \right) \\
& \quad \left. \sqrt{\frac{b-b \sin [c+d x]}{a+b}} \sqrt{-\frac{b+b \sin [c+d x]}{a-b}} \right) / \left(a \sqrt{-\frac{1}{a+b}} \sqrt{1-\sin [c+d x]^2} \right. \\
& \quad \left. \left(-2 a^2+b^2+4 a(a+b \sin [c+d x])-2(a+b \sin [c+d x])^2\right) \right. \\
& \quad \left. \left. \sqrt{-\frac{a^2-b^2-2 a(a+b \sin [c+d x])+(a+b \sin [c+d x])^2}{b^2}} \right) \right)
\end{aligned}$$

Problem 1190: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos[e + f x]^4}{\sqrt{d \sin[e + f x]} (a + b \sin[e + f x])^{9/2}} dx$$

Optimal (type 4, 510 leaves, 8 steps):

$$\begin{aligned} & \frac{2 \cos[e + f x]^3 \sqrt{d \sin[e + f x]}}{7 a d f (a + b \sin[e + f x])^{7/2}} + \frac{12 \cos[e + f x] \sqrt{d \sin[e + f x]}}{35 a^2 d f (a + b \sin[e + f x])^{5/2}} + \\ & \frac{8 (a^2 - 2 b^2) \cos[e + f x] \sqrt{d \sin[e + f x]}}{35 a^3 (a^2 - b^2) d f (a + b \sin[e + f x])^{3/2}} + \frac{32 b (2 a^2 - b^2) \cos[e + f x]}{35 a^3 (a^2 - b^2)^2 f \sqrt{d \sin[e + f x]} \sqrt{a + b \sin[e + f x]}} - \\ & \left(32 b (2 a^2 - b^2) \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \operatorname{EllipticE} \left[\right. \right. \\ & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a + b \sin[e + f x]}}{\sqrt{a + b} \sqrt{d \sin[e + f x]}} \right], -\frac{a + b}{a - b} \operatorname{Tan}[e + f x] \right] \right) / \left(35 a^5 (a - b) (a + b)^{3/2} \sqrt{d} f \right) - \\ & \left(8 (5 a^2 - 3 a b - 4 b^2) \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \operatorname{EllipticF} \left[\right. \right. \\ & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a + b \sin[e + f x]}}{\sqrt{a + b} \sqrt{d \sin[e + f x]}} \right], -\frac{a + b}{a - b} \operatorname{Tan}[e + f x] \right] \right) / \left(35 a^4 (a - b) (a + b)^{3/2} \sqrt{d} f \right) \end{aligned}$$

Result (type 4, 1670 leaves):

$$\begin{aligned} & \left(\sin[e + f x] \sqrt{a + b \sin[e + f x]} \right. \\ & \left. - \frac{2 (a^2 \cos[e + f x] - b^2 \cos[e + f x])}{7 a b^2 (a + b \sin[e + f x])^4} + \frac{4 (5 a^2 \cos[e + f x] + 3 b^2 \cos[e + f x])}{35 a^2 b^2 (a + b \sin[e + f x])^3} - \right. \\ & \left. \frac{2 (5 a^4 \cos[e + f x] - 9 a^2 b^2 \cos[e + f x] + 8 b^4 \cos[e + f x])}{35 a^3 b^2 (a^2 - b^2) (a + b \sin[e + f x])^2} - \right. \\ & \left. \frac{32 (2 a^2 b^2 \cos[e + f x] - b^4 \cos[e + f x])}{35 a^4 (a^2 - b^2)^2 (a + b \sin[e + f x])} \right) / \\ & \left(f \sqrt{d \sin[e + f x]} \right) + \frac{1}{35 a^4 (a - b)^2 (a + b)^2 f \sqrt{d \sin[e + f x]}} \end{aligned}$$

$$\begin{aligned}
 & 4 \sqrt{\sin[e+fx]} \left(\left(4 a (5 a^4 - 9 a^2 b^2 + 4 b^4) \sqrt{\frac{(a+b) \cot\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2}{-a+b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{\csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2 a}{-a+b}\right] \text{Sec}[e+fx] \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^4 \sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) / \\
 & \quad \left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) + \\
 & 4 a (-8 a^3 b + 4 a b^3) \left(\left(\sqrt{\frac{(a+b) \cot\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2}{-a+b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{\csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2 a}{-a+b}\right] \text{Sec}[e+fx] \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^4 \sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) / \\
 & \quad \left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - \left(\sqrt{\frac{(a+b) \cot\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2}{-a+b}} \right. \\
 & \quad \left. \text{EllipticPi}\left[-\frac{a}{b}, \text{ArcSin}\left[\frac{\sqrt{\frac{\csc\left[\frac{1}{2}(-e+\frac{\pi}{2}-fx)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2 a}{-a+b}\right] \text{Sec}[e+fx] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \left. \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) / \\
 & \left. \left(b \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) \right) + 2(8a^2b^2 - 4b^4) \\
 & \left(\frac{\cos[e+fx] \sqrt{a+b \sin[e+fx]}}{b \sqrt{\sin[e+fx]}} + \left(i \cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}[e+fx] \right. \right. \\
 & \left. \left. \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]}{\sqrt{\sin[e+fx]}} \right], -\frac{2a}{-a-b} \right] \sqrt{a+b \sin[e+fx]} \right) \right) / \\
 & \left(b \sqrt{\cos\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Csc}[e+fx]} \sqrt{\frac{\operatorname{Csc}[e+fx] (a+b \sin[e+fx])}{a+b}} \right) + \\
 & \frac{1}{b} 2a \left(\left(a \sqrt{\frac{(a+b) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-a+b}} \operatorname{EllipticF}\left[\right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}} \right], -\frac{2a}{-a+b} \right] \operatorname{Sec}[e+fx] \right. \right. \\
 & \left. \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \left. \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) /
 \end{aligned}$$

$$\left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - \left(a \sqrt{\frac{(a+b) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-a+b}} \right.$$

$$\left. \operatorname{EllipticPi}\left[-\frac{a}{b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{\csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{-\frac{(a+b) \csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sin[e+fx]}{a}} \right.$$

$$\left. \sqrt{\frac{\csc\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) \left. \right)$$

$$\left(b \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) \left. \right)$$

Problem 1208: Result more than twice size of optimal antiderivative.

$$\int \cot[c+dx]^5 \csc[c+dx] (a+b \sin[c+dx]) dx$$

Optimal (type 3, 86 leaves, 4 steps):

$$-\frac{a \csc[c+dx]}{d} + \frac{b \csc[c+dx]^2}{d} + \frac{2a \csc[c+dx]^3}{3d} - \frac{b \csc[c+dx]^4}{4d} - \frac{a \csc[c+dx]^5}{5d} + \frac{b \operatorname{Log}[\sin[c+dx]]}{d}$$

Result (type 3, 198 leaves):

$$-\frac{89a \cot\left[\frac{1}{2}(c+dx)\right]}{240d} + \frac{31a \cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^2}{480d} - \frac{a \cot\left[\frac{1}{2}(c+dx)\right] \csc\left[\frac{1}{2}(c+dx)\right]^4}{160d} + \frac{b \csc[c+dx]^2}{d} - \frac{b \csc[c+dx]^4}{4d} + \frac{b \operatorname{Log}[\sin[c+dx]]}{d} - \frac{89a \tan\left[\frac{1}{2}(c+dx)\right]}{240d} + \frac{31a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{480d} - \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{160d}$$

Problem 1209: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc}[c+d x]^2 (a+b \sin [c+d x]) d x$$

Optimal (type 3, 61 leaves, 6 steps):

$$-\frac{a \operatorname{Cot}[c+d x]^6}{6 d}-\frac{b \operatorname{Csc}[c+d x]}{d}+\frac{2 b \operatorname{Csc}[c+d x]^3}{3 d}-\frac{b \operatorname{Csc}[c+d x]^5}{5 d}$$

Result (type 3, 173 leaves):

$$\begin{aligned} &-\frac{89 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{240 d}-\frac{a \operatorname{Cot}[c+d x]^6}{6 d}+\frac{31 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{480 d} \\ &-\frac{b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{160 d}-\frac{89 b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{240 d}+ \\ &\frac{31 b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{480 d}-\frac{b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{160 d} \end{aligned}$$

Problem 1210: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc}[c+d x]^3 (a+b \sin [c+d x]) d x$$

Optimal (type 3, 65 leaves, 6 steps):

$$-\frac{b \operatorname{Cot}[c+d x]^6}{6 d}-\frac{a \operatorname{Csc}[c+d x]^3}{3 d}+\frac{2 a \operatorname{Csc}[c+d x]^5}{5 d}-\frac{a \operatorname{Csc}[c+d x]^7}{7 d}$$

Result (type 3, 233 leaves):

$$\begin{aligned} &-\frac{103 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{3360 d}-\frac{b \operatorname{Cot}[c+d x]^6}{6 d}-\frac{103 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{6720 d}+ \\ &\frac{9 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{1120 d}-\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{896 d} \\ &\frac{103 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{3360 d}-\frac{103 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{6720 d}+ \\ &\frac{9 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1120 d}-\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{896 d} \end{aligned}$$

Problem 1211: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc}[c+d x]^4 (a+b \sin [c+d x]) d x$$

Optimal (type 3, 81 leaves, 7 steps):

$$-\frac{a \cot [c+d x]^6}{6 d}-\frac{a \cot [c+d x]^8}{8 d}-\frac{b \csc [c+d x]^3}{3 d}+\frac{2 b \csc [c+d x]^5}{5 d}-\frac{b \csc [c+d x]^7}{7 d}$$

Result (type 3, 265 leaves):

$$\begin{aligned} &-\frac{103 b \cot \left[\frac{1}{2}(c+d x)\right]}{3360 d}-\frac{103 b \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^2}{6720 d}+ \\ &\frac{9 b \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^4}{1120 d}-\frac{b \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^6}{896 d}- \\ &\frac{a \csc [c+d x]^4}{4 d}+\frac{a \csc [c+d x]^6}{3 d}-\frac{a \csc [c+d x]^8}{8 d}- \\ &\frac{103 b \tan \left[\frac{1}{2}(c+d x)\right]}{3360 d}-\frac{103 b \sec \left[\frac{1}{2}(c+d x)\right]^2 \tan \left[\frac{1}{2}(c+d x)\right]}{6720 d}+ \\ &\frac{9 b \sec \left[\frac{1}{2}(c+d x)\right]^4 \tan \left[\frac{1}{2}(c+d x)\right]}{1120 d}-\frac{b \sec \left[\frac{1}{2}(c+d x)\right]^6 \tan \left[\frac{1}{2}(c+d x)\right]}{896 d} \end{aligned}$$

Problem 1212: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \csc [c+d x]^5 (a+b \sin [c+d x]) dx$$

Optimal (type 3, 81 leaves, 7 steps):

$$-\frac{b \cot [c+d x]^6}{6 d}-\frac{b \cot [c+d x]^8}{8 d}-\frac{a \csc [c+d x]^5}{5 d}+\frac{2 a \csc [c+d x]^7}{7 d}-\frac{a \csc [c+d x]^9}{9 d}$$

Result (type 3, 325 leaves):

$$\begin{aligned} &-\frac{649 a \cot \left[\frac{1}{2}(c+d x)\right]}{80640 d}-\frac{649 a \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^2}{161280 d}- \\ &\frac{31 a \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^4}{53760 d}+\frac{37 a \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^6}{32256 d}- \\ &\frac{a \cot \left[\frac{1}{2}(c+d x)\right] \csc \left[\frac{1}{2}(c+d x)\right]^8}{4608 d}-\frac{b \csc [c+d x]^4}{4 d}+ \\ &\frac{b \csc [c+d x]^6}{3 d}-\frac{b \csc [c+d x]^8}{8 d}-\frac{649 a \tan \left[\frac{1}{2}(c+d x)\right]}{80640 d}- \\ &\frac{649 a \sec \left[\frac{1}{2}(c+d x)\right]^2 \tan \left[\frac{1}{2}(c+d x)\right]}{161280 d}-\frac{31 a \sec \left[\frac{1}{2}(c+d x)\right]^4 \tan \left[\frac{1}{2}(c+d x)\right]}{53760 d}+ \\ &\frac{37 a \sec \left[\frac{1}{2}(c+d x)\right]^6 \tan \left[\frac{1}{2}(c+d x)\right]}{32256 d}-\frac{a \sec \left[\frac{1}{2}(c+d x)\right]^8 \tan \left[\frac{1}{2}(c+d x)\right]}{4608 d} \end{aligned}$$

Problem 1213: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc}[c+d x]^6 (a+b \sin [c+d x]) d x$$

Optimal (type 3, 97 leaves, 4 steps):

$$\begin{aligned} & -\frac{b \operatorname{Csc}[c+d x]^5}{5 d}-\frac{a \operatorname{Csc}[c+d x]^6}{6 d}+\frac{2 b \operatorname{Csc}[c+d x]^7}{7 d}+ \\ & \frac{a \operatorname{Csc}[c+d x]^8}{4 d}-\frac{b \operatorname{Csc}[c+d x]^9}{9 d}-\frac{a \operatorname{Csc}[c+d x]^{10}}{10 d} \end{aligned}$$

Result (type 3, 325 leaves):

$$\begin{aligned} & \frac{649 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{80640 d}-\frac{649 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{161280 d}- \\ & \frac{31 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{53760 d}+\frac{37 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{32256 d}- \\ & \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{4608 d}-\frac{a \operatorname{Csc}[c+d x]^6}{6 d}+ \\ & \frac{a \operatorname{Csc}[c+d x]^8}{4 d}-\frac{a \operatorname{Csc}[c+d x]^{10}}{10 d}-\frac{649 b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{80640 d}- \\ & \frac{649 b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{161280 d}-\frac{31 b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{53760 d}+ \\ & \frac{37 b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{32256 d}-\frac{b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{4608 d} \end{aligned}$$

Problem 1214: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 \operatorname{Csc}[c+d x]^7 (a+b \sin [c+d x]) d x$$

Optimal (type 3, 97 leaves, 4 steps):

$$\begin{aligned} & -\frac{b \operatorname{Csc}[c+d x]^6}{6 d}-\frac{a \operatorname{Csc}[c+d x]^7}{7 d}+\frac{b \operatorname{Csc}[c+d x]^8}{4 d}+ \\ & \frac{2 a \operatorname{Csc}[c+d x]^9}{9 d}-\frac{b \operatorname{Csc}[c+d x]^{10}}{10 d}-\frac{a \operatorname{Csc}[c+d x]^{11}}{11 d} \end{aligned}$$

Result (type 3, 385 leaves):

$$\begin{aligned}
 & - \frac{1109 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{354816 d} - \frac{1109 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{709632 d} - \\
 & \frac{13 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{29568 d} + \frac{173 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^6}{1419264 d} + \\
 & \frac{17 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^8}{101376 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^{10}}{22528 d} - \\
 & \frac{b \operatorname{Csc}[c+d x]^6}{6 d} + \frac{b \operatorname{Csc}[c+d x]^8}{4 d} - \frac{b \operatorname{Csc}[c+d x]^{10}}{10 d} - \\
 & \frac{1109 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{354816 d} - \frac{1109 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{709632 d} - \\
 & \frac{13 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{29568 d} + \frac{173 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1419264 d} + \\
 & \frac{17 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{101376 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^{10} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{22528 d}
 \end{aligned}$$

Problem 1232: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+d x] \operatorname{Cot}[c+d x]^4}{(a+b \operatorname{Sin}[c+d x])^2} dx$$

Optimal (type 3, 147 leaves, 4 steps):

$$\begin{aligned}
 & \frac{(2 a^2 - 3 b^2) \operatorname{Csc}[c+d x]}{a^4 d} + \frac{b \operatorname{Csc}[c+d x]^2}{a^3 d} - \frac{\operatorname{Csc}[c+d x]^3}{3 a^2 d} + \frac{4 b (a^2 - b^2) \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^5 d} - \\
 & \frac{4 b (a^2 - b^2) \operatorname{Log}[a+b \operatorname{Sin}[c+d x]]}{a^5 d} - \frac{(a^2 - b^2)^2}{a^4 b d (a+b \operatorname{Sin}[c+d x])}
 \end{aligned}$$

Result (type 3, 304 leaves):

$$\begin{aligned}
 & \frac{\left(11 a^2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - 18 b^2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]}{12 a^4 d} + \\
 & \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{4 a^3 d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 a^2 d} + \\
 & \frac{4 (a^2 b - b^3) \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^5 d} - \frac{4 (a^2 b - b^3) \operatorname{Log}[a+b \operatorname{Sin}[c+d x]]}{a^5 d} + \\
 & \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{4 a^3 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \left(11 a^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - 18 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}{12 a^4 d} - \\
 & \frac{(a-b)^2 (a+b)^2}{a^4 b d (a+b \operatorname{Sin}[c+d x])} - \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 a^2 d}
 \end{aligned}$$

Problem 1233: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^5}{(a + b \text{Sin}[c + d x])^2} dx$$

Optimal (type 3, 188 leaves, 3 steps):

$$\begin{aligned} & -\frac{4 b (a^2 - b^2) \text{Csc}[c + d x]}{a^5 d} + \frac{(2 a^2 - 3 b^2) \text{Csc}[c + d x]^2}{2 a^4 d} + \\ & \frac{2 b \text{Csc}[c + d x]^3}{3 a^3 d} - \frac{\text{Csc}[c + d x]^4}{4 a^2 d} + \frac{(a^4 - 6 a^2 b^2 + 5 b^4) \text{Log}[\text{Sin}[c + d x]]}{a^6 d} - \\ & \frac{(a^4 - 6 a^2 b^2 + 5 b^4) \text{Log}[a + b \text{Sin}[c + d x]]}{a^6 d} + \frac{(a^2 - b^2)^2}{a^5 d (a + b \text{Sin}[c + d x])} \end{aligned}$$

Result (type 3, 380 leaves):

$$\begin{aligned} & \frac{(-11 a^2 b \text{Cos}[\frac{1}{2}(c + d x)] + 12 b^3 \text{Cos}[\frac{1}{2}(c + d x)]) \text{Csc}[\frac{1}{2}(c + d x)]}{6 a^5 d} + \\ & \frac{(7 a^2 - 12 b^2) \text{Csc}[\frac{1}{2}(c + d x)]^2}{32 a^4 d} + \frac{b \text{Cot}[\frac{1}{2}(c + d x)] \text{Csc}[\frac{1}{2}(c + d x)]^2}{12 a^3 d} - \\ & \frac{\text{Csc}[\frac{1}{2}(c + d x)]^4}{64 a^2 d} + \frac{(a^4 - 6 a^2 b^2 + 5 b^4) \text{Log}[\text{Sin}[c + d x]]}{a^6 d} + \\ & \frac{(-a^4 + 6 a^2 b^2 - 5 b^4) \text{Log}[a + b \text{Sin}[c + d x]]}{a^6 d} + \frac{(7 a^2 - 12 b^2) \text{Sec}[\frac{1}{2}(c + d x)]^2}{32 a^4 d} - \\ & \frac{\text{Sec}[\frac{1}{2}(c + d x)]^4}{64 a^2 d} + \frac{\text{Sec}[\frac{1}{2}(c + d x)] (-11 a^2 b \text{Sin}[\frac{1}{2}(c + d x)] + 12 b^3 \text{Sin}[\frac{1}{2}(c + d x)])}{6 a^5 d} + \\ & \frac{(a - b)^2 (a + b)^2}{a^5 d (a + b \text{Sin}[c + d x])} + \frac{b \text{Sec}[\frac{1}{2}(c + d x)]^2 \text{Tan}[\frac{1}{2}(c + d x)]}{12 a^3 d} \end{aligned}$$

Problem 1235: Result more than twice size of optimal antiderivative.

$$\int \text{Cos}[c + d x]^5 \text{Sin}[c + d x]^n (a + b \text{Sin}[c + d x])^2 dx$$

Optimal (type 3, 170 leaves, 3 steps):

$$\begin{aligned} & \frac{a^2 \text{Sin}[c + d x]^{1+n}}{d (1+n)} + \frac{2 a b \text{Sin}[c + d x]^{2+n}}{d (2+n)} - \frac{(2 a^2 - b^2) \text{Sin}[c + d x]^{3+n}}{d (3+n)} - \\ & \frac{4 a b \text{Sin}[c + d x]^{4+n}}{d (4+n)} + \frac{(a^2 - 2 b^2) \text{Sin}[c + d x]^{5+n}}{d (5+n)} + \frac{2 a b \text{Sin}[c + d x]^{6+n}}{d (6+n)} + \frac{b^2 \text{Sin}[c + d x]^{7+n}}{d (7+n)} \end{aligned}$$

Result (type 3, 648 leaves):

1

$$32 d (1+n) (2+n) (3+n) (4+n) (5+n) (6+n) (7+n) \sin [c+d x]^{1+n} (119616 a^2 + 9888 b^2 + 164368 a^2 n + 20488 b^2 n + 89472 a^2 n^2 + 14576 b^2 n^2 + 25372 a^2 n^3 + 4654 b^2 n^3 + 4020 a^2 n^4 + 734 b^2 n^4 + 340 a^2 n^5 + 58 b^2 n^5 + 12 a^2 n^6 + 2 b^2 n^6 + (48 + 92 n + 56 n^2 + 13 n^3 + n^4) (16 a^2 (7+n)^2 + b^2 (-113 + 8 n + n^2))) \cos [2 (c+d x)] + 2 (144 + 324 n + 260 n^2 + 95 n^3 + 16 n^4 + n^5) (2 a^2 (7+n) - b^2 (13+n)) \cos [4 (c+d x)] - 720 b^2 \cos [6 (c+d x)] - 1764 b^2 n \cos [6 (c+d x)] - 1624 b^2 n^2 \cos [6 (c+d x)] - 735 b^2 n^3 \cos [6 (c+d x)] - 175 b^2 n^4 \cos [6 (c+d x)] - 21 b^2 n^5 \cos [6 (c+d x)] - b^2 n^6 \cos [6 (c+d x)] + 73920 a b \sin [c+d x] + 135664 a b n \sin [c+d x] + 81096 a b n^2 \sin [c+d x] + 22304 a b n^3 \sin [c+d x] + 3184 a b n^4 \sin [c+d x] + 240 a b n^5 \sin [c+d x] + 8 a b n^6 \sin [c+d x] + 23520 a b \sin [3 (c+d x)] + 53704 a b n \sin [3 (c+d x)] + 44460 a b n^2 \sin [3 (c+d x)] + 17392 a b n^3 \sin [3 (c+d x)] + 3432 a b n^4 \sin [3 (c+d x)] + 328 a b n^5 \sin [3 (c+d x)] + 12 a b n^6 \sin [3 (c+d x)] + 3360 a b \sin [5 (c+d x)] + 8152 a b n \sin [5 (c+d x)] + 7396 a b n^2 \sin [5 (c+d x)] + 3280 a b n^3 \sin [5 (c+d x)] + 760 a b n^4 \sin [5 (c+d x)] + 88 a b n^5 \sin [5 (c+d x)] + 4 a b n^6 \sin [5 (c+d x)]$$

Problem 1236: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^5 \sin [c+d x]^n (a+b \sin [c+d x]) dx$$

Optimal (type 3, 123 leaves, 3 steps):

$$\frac{a \sin [c+d x]^{1+n}}{d (1+n)} + \frac{b \sin [c+d x]^{2+n}}{d (2+n)} - \frac{2 a \sin [c+d x]^{3+n}}{d (3+n)} - \frac{2 b \sin [c+d x]^{4+n}}{d (4+n)} + \frac{a \sin [c+d x]^{5+n}}{d (5+n)} + \frac{b \sin [c+d x]^{6+n}}{d (6+n)}$$

Result (type 3, 371 leaves):

1

$$16 d (1+n) (2+n) (3+n) (4+n) (5+n) (6+n) \sin [c+d x]^{1+n} (8544 a + 10520 a n + 4888 a n^2 + 1114 a n^3 + 128 a n^4 + 6 a n^5 + 8 a (336 + 692 n + 484 n^2 + 147 n^3 + 20 n^4 + n^5) \cos [2 (c+d x)] + 2 a (144 + 324 n + 260 n^2 + 95 n^3 + 16 n^4 + n^5) \cos [4 (c+d x)] + 2640 b \sin [c+d x] + 4468 b n \sin [c+d x] + 2258 b n^2 \sin [c+d x] + 474 b n^3 \sin [c+d x] + 46 b n^4 \sin [c+d x] + 2 b n^5 \sin [c+d x] + 840 b \sin [3 (c+d x)] + 1798 b n \sin [3 (c+d x)] + 1331 b n^2 \sin [3 (c+d x)] + 431 b n^3 \sin [3 (c+d x)] + 61 b n^4 \sin [3 (c+d x)] + 3 b n^5 \sin [3 (c+d x)] + 120 b \sin [5 (c+d x)] + 274 b n \sin [5 (c+d x)] + 225 b n^2 \sin [5 (c+d x)] + 85 b n^3 \sin [5 (c+d x)] + 15 b n^4 \sin [5 (c+d x)] + b n^5 \sin [5 (c+d x)])$$

Problem 1237: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^5 \sin [c+d x]^n}{a+b \sin [c+d x]} dx$$

Optimal (type 5, 167 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{a(a^2 - 2b^2) \operatorname{Sin}[c + dx]^{1+n}}{b^4 d(1+n)} + \frac{1}{ab^4 d(1+n)} \\
 & (a^2 - b^2)^2 \operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, -\frac{b \operatorname{Sin}[c + dx]}{a}\right] \operatorname{Sin}[c + dx]^{1+n} + \\
 & \frac{(a^2 - 2b^2) \operatorname{Sin}[c + dx]^{2+n}}{b^3 d(2+n)} - \frac{a \operatorname{Sin}[c + dx]^{3+n}}{b^2 d(3+n)} + \frac{\operatorname{Sin}[c + dx]^{4+n}}{bd(4+n)}
 \end{aligned}$$

Result (type 8, 31 leaves):

$$\int \frac{\operatorname{Cos}[c + dx]^5 \operatorname{Sin}[c + dx]^n}{a + b \operatorname{Sin}[c + dx]} dx$$

Problem 1238: Unable to integrate problem.

$$\int \frac{\operatorname{Cos}[c + dx]^5 \operatorname{Sin}[c + dx]^n}{(a + b \operatorname{Sin}[c + dx])^2} dx$$

Optimal (type 5, 191 leaves, 5 steps):

$$\begin{aligned}
 & \frac{(3a^2 - 2b^2) \operatorname{Sin}[c + dx]^{1+n}}{b^4 d(1+n)} + \frac{1}{a^2 b^4 d(1+n)} \\
 & (a^2 - b^2)(b^2 n - a^2(4+n)) \operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, -\frac{b \operatorname{Sin}[c + dx]}{a}\right] \operatorname{Sin}[c + dx]^{1+n} - \\
 & \frac{2a \operatorname{Sin}[c + dx]^{2+n}}{b^3 d(2+n)} + \frac{\operatorname{Sin}[c + dx]^{3+n}}{b^2 d(3+n)} + \frac{(a^2 - b^2)^2 \operatorname{Sin}[c + dx]^{1+n}}{ab^4 d(a + b \operatorname{Sin}[c + dx])}
 \end{aligned}$$

Result (type 8, 31 leaves):

$$\int \frac{\operatorname{Cos}[c + dx]^5 \operatorname{Sin}[c + dx]^n}{(a + b \operatorname{Sin}[c + dx])^2} dx$$

Problem 1250: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c + dx]^6 \operatorname{Csc}[c + dx] (a + b \operatorname{Sin}[c + dx])^2 dx$$

Optimal (type 3, 175 leaves, 11 steps):

$$\begin{aligned}
 & -2abx + \frac{5(a^2 - 6b^2) \operatorname{ArcTanh}[\operatorname{Cos}[c + dx]]}{16d} + \frac{b^2 \operatorname{Cos}[c + dx]}{d} - \frac{2ab \operatorname{Cot}[c + dx]}{d} + \\
 & \frac{2ab \operatorname{Cot}[c + dx]^3}{3d} - \frac{2ab \operatorname{Cot}[c + dx]^5}{5d} - \frac{(11a^2 - 18b^2) \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]}{16d} + \\
 & \frac{(13a^2 - 6b^2) \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]^3}{24d} - \frac{a^2 \operatorname{Cot}[c + dx] \operatorname{Csc}[c + dx]^5}{6d}
 \end{aligned}$$

Result (type 3, 384 leaves):

$$\begin{aligned} & \frac{1}{1920 d} \left(-3840 a b c - 3840 a b d x + 1920 b^2 \cos [c + d x] - 2944 a b \cot \left[\frac{1}{2} (c + d x) \right] - \right. \\ & 330 a^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 540 b^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 60 a^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 - \\ & 30 b^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 - 5 a^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^6 + 600 a^2 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - \\ & 3600 b^2 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] \right] - 600 a^2 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] + 3600 b^2 \operatorname{Log} \left[\sin \left[\frac{1}{2} (c + d x) \right] \right] + \\ & 330 a^2 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 540 b^2 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 60 a^2 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 + \\ & 30 b^2 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 + 5 a^2 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^6 - 2624 a b \operatorname{Csc} [c + d x]^3 \sin \left[\frac{1}{2} (c + d x) \right]^4 + \\ & 768 a b \operatorname{Csc} [c + d x]^5 \sin \left[\frac{1}{2} (c + d x) \right]^6 + 164 a b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 \sin [c + d x] - \\ & \left. 12 a b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^6 \sin [c + d x] + 2944 a b \tan \left[\frac{1}{2} (c + d x) \right] \right) \end{aligned}$$

Problem 1256: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^6 \sin [c + d x]^3}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 3, 525 leaves, 11 steps):

$$\begin{aligned} & \frac{a (64 a^6 - 120 a^4 b^2 + 60 a^2 b^4 - 5 b^6) x}{8 b^9} - \frac{2 a^2 (8 a^2 - 3 b^2) (a^2 - b^2)^{3/2} \operatorname{ArcTan} \left[\frac{b + a \tan \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right]}{b^9 d} + \\ & \frac{(840 a^6 - 1435 a^4 b^2 + 588 a^2 b^4 - 15 b^6) \cos [c + d x]}{105 b^8 d} - \\ & \frac{a (32 a^4 - 52 a^2 b^2 + 19 b^4) \cos [c + d x] \sin [c + d x]}{8 b^7 d} + \\ & \frac{(280 a^4 - 441 a^2 b^2 + 150 b^4) \cos [c + d x] \sin [c + d x]^2}{105 b^6 d} - \\ & \frac{(24 a^4 - 37 a^2 b^2 + 12 b^4) \cos [c + d x] \sin [c + d x]^3}{12 a b^5 d} + \\ & \frac{(224 a^4 - 340 a^2 b^2 + 105 b^4) \cos [c + d x] \sin [c + d x]^4}{140 a^2 b^4 d} + \frac{\cos [c + d x] \sin [c + d x]^4}{4 a d (a + b \sin [c + d x])} - \\ & \frac{3 b \cos [c + d x] \sin [c + d x]^5}{20 a^2 d (a + b \sin [c + d x])} - \frac{(20 a^4 - 30 a^2 b^2 + 9 b^4) \cos [c + d x] \sin [c + d x]^5}{15 a^2 b^3 d (a + b \sin [c + d x])} - \\ & \frac{4 a \cos [c + d x] \sin [c + d x]^6}{21 b^2 d (a + b \sin [c + d x])} + \frac{\cos [c + d x] \sin [c + d x]^7}{7 b d (a + b \sin [c + d x])} \end{aligned}$$

Result (type 3, 1223 leaves):

$$\begin{aligned}
 & 3 \left(\frac{2 b \operatorname{ArcTan} \left[\frac{b+a \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right]}{\sqrt{a^2-b^2}} + \frac{a \operatorname{Cos} [c+d x]}{a+b \operatorname{Sin} [c+d x]} \right) \\
 & \frac{1}{128 (-a+b) (a+b) d} + \frac{1}{32 b^3 d} \\
 & \left(8 a (c+d x) - \frac{2 (8 a^4 - 12 a^2 b^2 + 3 b^4) \operatorname{ArcTan} \left[\frac{b+a \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right]}{(a^2-b^2)^{3/2}} + \right. \\
 & \left. 4 b \operatorname{Cos} [c+d x] + \frac{a b (4 a^2 - 3 b^2) \operatorname{Cos} [c+d x]}{(a-b) (a+b) (a+b \operatorname{Sin} [c+d x])} \right) - \\
 & \frac{1}{1280 b^7 d} \left(240 a (24 a^4 - 20 a^2 b^2 + 3 b^4) (c+d x) - \frac{1}{(a^2-b^2)^{3/2}} \right. \\
 & \left. 30 (384 a^8 - 896 a^6 b^2 + 672 a^4 b^4 - 168 a^2 b^6 + 7 b^8) \operatorname{ArcTan} \left[\frac{b+a \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right] + \right. \\
 & \left. 60 b (80 a^4 - 48 a^2 b^2 + 3 b^4) \operatorname{Cos} [c+d x] + 40 b^3 (-6 a^2 + b^2) \operatorname{Cos} [3 (c+d x)] + \right. \\
 & \left. 12 b^5 \operatorname{Cos} [5 (c+d x)] + \frac{15 a b (64 a^6 - 112 a^4 b^2 + 56 a^2 b^4 - 7 b^6) \operatorname{Cos} [c+d x]}{(a-b) (a+b) (a+b \operatorname{Sin} [c+d x])} - \right. \\
 & \left. 120 a b^2 (8 a^2 - 3 b^2) \operatorname{Sin} [2 (c+d x)] + 60 a b^4 \operatorname{Sin} [4 (c+d x)] \right) + \\
 & \frac{1}{256} \left(-\frac{1}{b^9 (a^2-b^2)^{3/2} d} 2 (2048 a^{10} - 5760 a^8 b^2 + 5760 a^6 b^4 - 2400 a^4 b^6 + 360 a^2 b^8 - 9 b^{10}) \right. \\
 & \left. \operatorname{ArcTan} \left[\frac{\operatorname{Sec} \left[\frac{1}{2} (c+d x) \right] \left(b \operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] + a \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right)}{\sqrt{a^2-b^2}} \right] + \right. \\
 & \left. \frac{1}{105 b^9 (-a^2+b^2) d (a+b \operatorname{Sin} [c+d x])} (-215040 a^{10} (c+d x) + 497280 a^8 b^2 (c+d x) - \right. \\
 & \left. 383040 a^6 b^4 (c+d x) + 109200 a^4 b^6 (c+d x) - 8400 a^2 b^8 (c+d x) - 215040 a^9 b \operatorname{Cos} [c+d x] + \right. \\
 & \left. 470400 a^7 b^3 \operatorname{Cos} [c+d x] - 334320 a^5 b^5 \operatorname{Cos} [c+d x] + 84000 a^3 b^7 \operatorname{Cos} [c+d x] - \right. \\
 & \left. 5145 a b^9 \operatorname{Cos} [c+d x] - 8960 a^7 b^3 \operatorname{Cos} [3 (c+d x)] + 17360 a^5 b^5 \operatorname{Cos} [3 (c+d x)] - \right. \\
 & \left. 9870 a^3 b^7 \operatorname{Cos} [3 (c+d x)] + 1470 a b^9 \operatorname{Cos} [3 (c+d x)] + 672 a^5 b^5 \operatorname{Cos} [5 (c+d x)] - \right. \\
 & \left. 994 a^3 b^7 \operatorname{Cos} [5 (c+d x)] + 322 a b^9 \operatorname{Cos} [5 (c+d x)] - 80 a^3 b^7 \operatorname{Cos} [7 (c+d x)] + \right. \\
 & \left. 80 a b^9 \operatorname{Cos} [7 (c+d x)] - 215040 a^9 b (c+d x) \operatorname{Sin} [c+d x] + 497280 a^7 b^3 (c+d x) \right. \\
 & \left. \operatorname{Sin} [c+d x] - 383040 a^5 b^5 (c+d x) \operatorname{Sin} [c+d x] + 109200 a^3 b^7 (c+d x) \operatorname{Sin} [c+d x] - \right. \\
 & \left. 8400 a b^9 (c+d x) \operatorname{Sin} [c+d x] - 53760 a^8 b^2 \operatorname{Sin} [2 (c+d x)] + 115360 a^6 b^4 \operatorname{Sin} [2 (c+d x)] - \right. \\
 & \left. 78400 a^4 b^6 \operatorname{Sin} [2 (c+d x)] + 17430 a^2 b^8 \operatorname{Sin} [2 (c+d x)] - 630 b^{10} \operatorname{Sin} [2 (c+d x)] + \right. \\
 & \left. 2240 a^6 b^4 \operatorname{Sin} [4 (c+d x)] - 3836 a^4 b^6 \operatorname{Sin} [4 (c+d x)] + 1722 a^2 b^8 \operatorname{Sin} [4 (c+d x)] - \right. \\
 & \left. 126 b^{10} \operatorname{Sin} [4 (c+d x)] - 224 a^4 b^6 \operatorname{Sin} [6 (c+d x)] + 278 a^2 b^8 \operatorname{Sin} [6 (c+d x)] - \right.
 \end{aligned}$$

$$\left. 54 b^{10} \sin [6 (c+d x)] + 30 a^2 b^8 \sin [8 (c+d x)] - 30 b^{10} \sin [8 (c+d x)] \right)$$

Problem 1257: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]^2}{(a+b \sin [c+d x])^2} dx$$

Optimal (type 3, 471 leaves, 10 steps):

$$\begin{aligned} & - \frac{(112 a^6 - 200 a^4 b^2 + 90 a^2 b^4 - 5 b^6) x}{16 b^8} + \frac{2 a (7 a^2 - 2 b^2) (a^2 - b^2)^{3/2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{b^8 d} \\ & \frac{a (105 a^4 - 170 a^2 b^2 + 61 b^4) \cos [c+d x]}{15 b^7 d} + \frac{(56 a^4 - 86 a^2 b^2 + 27 b^4) \cos [c+d x] \sin [c+d x]}{16 b^6 d} \\ & \frac{(35 a^4 - 52 a^2 b^2 + 15 b^4) \cos [c+d x] \sin [c+d x]^2}{15 a b^5 d} + \\ & \frac{(42 a^4 - 61 a^2 b^2 + 16 b^4) \cos [c+d x] \sin [c+d x]^3}{24 a^2 b^4 d} + \frac{\cos [c+d x] \sin [c+d x]^3}{3 a d (a+b \sin [c+d x])} \\ & \frac{b \cos [c+d x] \sin [c+d x]^4}{6 a^2 d (a+b \sin [c+d x])} - \frac{(14 a^4 - 20 a^2 b^2 + 5 b^4) \cos [c+d x] \sin [c+d x]^4}{10 a^2 b^3 d (a+b \sin [c+d x])} \\ & \frac{7 a \cos [c+d x] \sin [c+d x]^5}{30 b^2 d (a+b \sin [c+d x])} + \frac{\cos [c+d x] \sin [c+d x]^6}{6 b d (a+b \sin [c+d x])} \end{aligned}$$

Result (type 3, 1110 leaves):

$$\begin{aligned} & \frac{5 \left(\frac{2 a \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2}} + \frac{b \cos [c+d x]}{(a-b)(a+b)(a+b \sin [c+d x])} \right)}{128 d} + \\ & \frac{-2 (c+d x) + \frac{2 a (2 a^2-3 b^2) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2}} + \frac{b (-2 a^2+b^2) \cos [c+d x]}{(a-b)(a+b)(a+b \sin [c+d x])}}{32 b^2 d} - \frac{1}{32 b^4 d} \\ & \left(-4 (-6 a^2 + b^2) (c+d x) - \frac{2 a (24 a^4 - 40 a^2 b^2 + 15 b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2}} + \right. \\ & \left. 16 a b \cos [c+d x] + \frac{b (8 a^4 - 8 a^2 b^2 + b^4) \cos [c+d x]}{(a-b)(a+b)(a+b \sin [c+d x])} - 2 b^2 \sin [2 (c+d x)] \right) \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{96 b^6 d} \left(-6 (80 a^4 - 48 a^2 b^2 + 3 b^4) (c + d x) + \right. \\
 & \frac{6 a (160 a^6 - 336 a^4 b^2 + 210 a^2 b^4 - 35 b^6) \operatorname{ArcTan} \left[\frac{b+a \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right]}{(a^2 - b^2)^{3/2}} - 48 a b (8 a^2 - 3 b^2) \\
 & \left. \operatorname{Cos}[c + d x] + 16 a b^3 \operatorname{Cos}[3 (c + d x)] + \frac{3 b (-32 a^6 + 48 a^4 b^2 - 18 a^2 b^4 + b^6) \operatorname{Cos}[c + d x]}{(a - b) (a + b) (a + b \operatorname{Sin}[c + d x])} - \right. \\
 & \left. 12 b^2 (-6 a^2 + b^2) \operatorname{Sin}[2 (c + d x)] - 3 b^4 \operatorname{Sin}[4 (c + d x)] \right) - \\
 & \frac{1}{1920 b^8 d} \left(-\frac{1}{(a^2 - b^2)^{3/2}} 30 a (896 a^8 - 2304 a^6 b^2 + 2016 a^4 b^4 - 672 a^2 b^6 + 63 b^8) \right. \\
 & \left. \operatorname{ArcTan} \left[\frac{b + a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] + \frac{1}{(a^2 - b^2) (a + b \operatorname{Sin}[c + d x])} \right. \\
 & \left. (15 b (896 a^8 - 1744 a^6 b^2 + 1024 a^4 b^4 - 179 a^2 b^6 + 4 b^8) \operatorname{Cos}[c + d x] + (a^2 - b^2) \right. \\
 & (13440 a^7 c - 14400 a^5 b^2 c + 3600 a^3 b^4 c - 120 a b^6 c + 13440 a^7 d x - 14400 a^5 b^2 d x + 3600 a^3 \\
 & b^4 d x - 120 a b^6 d x + 10 (56 a^4 b^3 - 39 a^2 b^5 + 3 b^7) \operatorname{Cos}[3 (c + d x)] + (-42 a^2 b^5 + 10 b^7) \\
 & \operatorname{Cos}[5 (c + d x)] + 5 b^7 \operatorname{Cos}[7 (c + d x)] + 13440 a^6 b c \operatorname{Sin}[c + d x] - 14400 a^4 b^3 c \operatorname{Sin}[\\
 & c + d x] + 3600 a^2 b^5 c \operatorname{Sin}[c + d x] - 120 b^7 c \operatorname{Sin}[c + d x] + 13440 a^6 b d x \operatorname{Sin}[c + d x] - \\
 & 14400 a^4 b^3 d x \operatorname{Sin}[c + d x] + 3600 a^2 b^5 d x \operatorname{Sin}[c + d x] - 120 b^7 d x \operatorname{Sin}[c + d x] + \\
 & 3360 a^5 b^2 \operatorname{Sin}[2 (c + d x)] - 3040 a^3 b^4 \operatorname{Sin}[2 (c + d x)] + 510 a b^6 \operatorname{Sin}[2 (c + d x)] - \\
 & \left. \left. 140 a^3 b^4 \operatorname{Sin}[4 (c + d x)] + 66 a b^6 \operatorname{Sin}[4 (c + d x)] + 14 a b^6 \operatorname{Sin}[6 (c + d x)] \right) \right) \left. \right)
 \end{aligned}$$

Problem 1266: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + d x]^6 \operatorname{Sin}[c + d x]^3}{(a + b \operatorname{Sin}[c + d x])^3} dx$$

Optimal (type 3, 536 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{(448 a^6 - 600 a^4 b^2 + 180 a^2 b^4 - 5 b^6) x}{16 b^9} + \frac{a \sqrt{a^2 - b^2} (56 a^4 - 47 a^2 b^2 + 6 b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{b^9 d} \\
 & a \frac{(840 a^4 - 985 a^2 b^2 + 213 b^4) \operatorname{Cos}[c+d x]}{30 b^8 d} + \frac{(224 a^4 - 244 a^2 b^2 + 43 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{16 b^7 d} \\
 & \frac{(280 a^4 - 291 a^2 b^2 + 45 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^2}{30 a b^6 d} + \\
 & \frac{(168 a^4 - 169 a^2 b^2 + 24 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^3}{24 a^2 b^5 d} + \\
 & \frac{\operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^4}{4 a d (a+b \operatorname{Sin}[c+d x])^2} - \frac{b \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^5}{10 a^2 d (a+b \operatorname{Sin}[c+d x])^2} - \\
 & \frac{(56 a^4 - 60 a^2 b^2 + 9 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^5}{60 a^2 b^3 d (a+b \operatorname{Sin}[c+d x])^2} - \frac{4 a \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^6}{15 b^2 d (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \frac{\operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^7}{6 b d (a+b \operatorname{Sin}[c+d x])^2} - \frac{(112 a^4 - 110 a^2 b^2 + 15 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^4}{20 a^2 b^4 d (a+b \operatorname{Sin}[c+d x])^2}
 \end{aligned}$$

Result (type 3, 2044 leaves):

$$\begin{aligned}
 & \frac{1}{64 b^3 d} \left(-8 (c+d x) + \frac{2 a (8 a^4 - 20 a^2 b^2 + 15 b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2 - b^2)^{5/2}} + \right. \\
 & \left. \frac{a b (4 a^2 - 3 b^2) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} - \frac{3 b (4 a^4 - 7 a^2 b^2 + 2 b^4) \operatorname{Cos}[c+d x]}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])^2} \right) \\
 & \frac{3 \left(\frac{6 a b \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{\operatorname{Cos}[c+d x] (a (2 a^2+b^2)+b (a^2+2 b^2) \operatorname{Sin}[c+d x])}{(a+b \operatorname{Sin}[c+d x])^2} \right)}{256 (a-b)^2 (a+b)^2 d} \\
 & \frac{1}{1024 b^7 d} 3 \left(\frac{1}{(a^2 - b^2)^{5/2}} 12 a (640 a^8 - 1920 a^6 b^2 + 2016 a^4 b^4 - 840 a^2 b^6 + 105 b^8) \right. \\
 & \left. \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \frac{1}{(a^2 - b^2)^2 (a+b \operatorname{Sin}[c+d x])^2} \right. \\
 & \left. (-3840 a^{10} (c+d x) + 7680 a^8 b^2 (c+d x) - 2976 a^6 b^4 (c+d x) - 1776 a^4 b^6 (c+d x) + \right. \\
 & \left. 960 a^2 b^8 (c+d x) - 48 b^{10} (c+d x) - 3840 a^9 b \operatorname{Cos}[c+d x] + 8640 a^7 b^3 \operatorname{Cos}[c+d x] - \right. \\
 & \left. 5696 a^5 b^5 \operatorname{Cos}[c+d x] + 788 a^3 b^7 \operatorname{Cos}[c+d x] + 114 a b^9 \operatorname{Cos}[c+d x] + \right. \\
 & \left. 1920 a^8 b^2 (c+d x) \operatorname{Cos}[2(c+d x)] - 4800 a^6 b^4 (c+d x) \operatorname{Cos}[2(c+d x)] + \right. \\
 & \left. 3888 a^4 b^6 (c+d x) \operatorname{Cos}[2(c+d x)] - 1056 a^2 b^8 (c+d x) \operatorname{Cos}[2(c+d x)] + \right. \\
 & \left. 48 b^{10} (c+d x) \operatorname{Cos}[2(c+d x)] + 320 a^7 b^3 \operatorname{Cos}[3(c+d x)] - 760 a^5 b^5 \operatorname{Cos}[3(c+d x)] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 560 a^3 b^7 \operatorname{Cos}[3(c+dx)] - 120 a b^9 \operatorname{Cos}[3(c+dx)] - 8 a^5 b^5 \operatorname{Cos}[5(c+dx)] + \\
 & 16 a^3 b^7 \operatorname{Cos}[5(c+dx)] - 8 a b^9 \operatorname{Cos}[5(c+dx)] - 7680 a^9 b(c+dx) \operatorname{Sin}[c+dx] + \\
 & 19200 a^7 b^3(c+dx) \operatorname{Sin}[c+dx] - 15552 a^5 b^5(c+dx) \operatorname{Sin}[c+dx] + \\
 & 4224 a^3 b^7(c+dx) \operatorname{Sin}[c+dx] - 192 a b^9(c+dx) \operatorname{Sin}[c+dx] - \\
 & 2880 a^8 b^2 \operatorname{Sin}[2(c+dx)] + 6880 a^6 b^4 \operatorname{Sin}[2(c+dx)] - 5182 a^4 b^6 \operatorname{Sin}[2(c+dx)] + \\
 & 1221 a^2 b^8 \operatorname{Sin}[2(c+dx)] - 36 b^{10} \operatorname{Sin}[2(c+dx)] - 40 a^6 b^4 \operatorname{Sin}[4(c+dx)] + \\
 & 88 a^4 b^6 \operatorname{Sin}[4(c+dx)] - 56 a^2 b^8 \operatorname{Sin}[4(c+dx)] + 8 b^{10} \operatorname{Sin}[4(c+dx)] + \\
 & \left. \begin{aligned}
 & 2 a^4 b^6 \operatorname{Sin}[6(c+dx)] - 4 a^2 b^8 \operatorname{Sin}[6(c+dx)] + 2 b^{10} \operatorname{Sin}[6(c+dx)] \right) + \\
 & \frac{1}{256} \left(\frac{1}{b^9 (a^2 - b^2)^{5/2} d} a (14336 a^{10} - 49280 a^8 b^2 + 63360 a^6 b^4 - 36960 a^4 b^6 + 9240 a^2 b^8 - 693 b^{10}) \right. \\
 & \left. \operatorname{ArcTan} \left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)}{\sqrt{a^2 - b^2}} \right] - \right. \\
 & \left. \frac{1}{60 b^9 (-a^2 + b^2)^2 d (a + b \operatorname{Sin}[c+dx])^2} \right. \\
 & \left. \begin{aligned}
 & (430080 a^{12} (c+dx) - 1048320 a^{10} b^2 (c+dx) + 691200 a^8 b^4 (c+dx) + \\
 & 83040 a^6 b^6 (c+dx) - 198000 a^4 b^8 (c+dx) + 43200 a^2 b^{10} (c+dx) - 1200 b^{12} (c+dx) + \\
 & 430080 a^{11} b \operatorname{Cos}[c+dx] - 1155840 a^9 b^3 \operatorname{Cos}[c+dx] + 1042880 a^7 b^5 \operatorname{Cos}[c+dx] - \\
 & 332800 a^5 b^7 \operatorname{Cos}[c+dx] + 11060 a^3 b^9 \operatorname{Cos}[c+dx] + 4530 a b^{11} \operatorname{Cos}[c+dx] - \\
 & 215040 a^{10} b^2 (c+dx) \operatorname{Cos}[2(c+dx)] + 631680 a^8 b^4 (c+dx) \operatorname{Cos}[2(c+dx)] - \\
 & 661440 a^6 b^6 (c+dx) \operatorname{Cos}[2(c+dx)] + 289200 a^4 b^8 (c+dx) \operatorname{Cos}[2(c+dx)] - \\
 & 45600 a^2 b^{10} (c+dx) \operatorname{Cos}[2(c+dx)] + 1200 b^{12} (c+dx) \operatorname{Cos}[2(c+dx)] - \\
 & 35840 a^9 b^3 \operatorname{Cos}[3(c+dx)] + 100800 a^7 b^5 \operatorname{Cos}[3(c+dx)] - 98424 a^5 b^7 \operatorname{Cos}[3(c+dx)] + \\
 & 37808 a^3 b^9 \operatorname{Cos}[3(c+dx)] - 4344 a b^{11} \operatorname{Cos}[3(c+dx)] + 896 a^7 b^5 \operatorname{Cos}[5(c+dx)] - \\
 & 2184 a^5 b^7 \operatorname{Cos}[5(c+dx)] + 1680 a^3 b^9 \operatorname{Cos}[5(c+dx)] - 392 a b^{11} \operatorname{Cos}[5(c+dx)] - \\
 & 64 a^5 b^7 \operatorname{Cos}[7(c+dx)] + 128 a^3 b^9 \operatorname{Cos}[7(c+dx)] - 64 a b^{11} \operatorname{Cos}[7(c+dx)] + \\
 & 860160 a^{11} b (c+dx) \operatorname{Sin}[c+dx] - 2526720 a^9 b^3 (c+dx) \operatorname{Sin}[c+dx] + \\
 & 2645760 a^7 b^5 (c+dx) \operatorname{Sin}[c+dx] - 1156800 a^5 b^7 (c+dx) \operatorname{Sin}[c+dx] + \\
 & 182400 a^3 b^9 (c+dx) \operatorname{Sin}[c+dx] - 4800 a b^{11} (c+dx) \operatorname{Sin}[c+dx] + \\
 & 322560 a^{10} b^2 \operatorname{Sin}[2(c+dx)] - 911680 a^8 b^4 \operatorname{Sin}[2(c+dx)] + 903680 a^6 b^6 \operatorname{Sin}[2(c+dx)] - \\
 & 362830 a^4 b^8 \operatorname{Sin}[2(c+dx)] + 49125 a^2 b^{10} \operatorname{Sin}[2(c+dx)] - 900 b^{12} \operatorname{Sin}[2(c+dx)] + \\
 & 4480 a^8 b^4 \operatorname{Sin}[4(c+dx)] - 11816 a^6 b^6 \operatorname{Sin}[4(c+dx)] + 10392 a^4 b^8 \operatorname{Sin}[4(c+dx)] - \\
 & 3256 a^2 b^{10} \operatorname{Sin}[4(c+dx)] + 200 b^{12} \operatorname{Sin}[4(c+dx)] - 224 a^6 b^6 \operatorname{Sin}[6(c+dx)] + \\
 & 498 a^4 b^8 \operatorname{Sin}[6(c+dx)] - 324 a^2 b^{10} \operatorname{Sin}[6(c+dx)] + 50 b^{12} \operatorname{Sin}[6(c+dx)] + \\
 & \left. \left. \begin{aligned}
 & 20 a^4 b^8 \operatorname{Sin}[8(c+dx)] - 40 a^2 b^{10} \operatorname{Sin}[8(c+dx)] + 20 b^{12} \operatorname{Sin}[8(c+dx)] \right) \right)
 \end{aligned}
 \end{aligned}
 \end{aligned}$$

Problem 1267: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx]^6 \operatorname{Sin}[c+dx]^2}{(a+b \operatorname{Sin}[c+dx])^3} dx$$

Optimal (type 3, 485 leaves, 10 steps):

$$\begin{aligned} & \frac{a (168 a^4 - 200 a^2 b^2 + 45 b^4) x}{8 b^8} - \frac{\sqrt{a^2 - b^2} (42 a^4 - 29 a^2 b^2 + 2 b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{b^8 d} + \\ & \frac{(630 a^4 - 645 a^2 b^2 + 91 b^4) \operatorname{Cos}[c+d x]}{30 b^7 d} - \frac{(84 a^4 - 79 a^2 b^2 + 8 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{8 a b^6 d} + \\ & \frac{(210 a^4 - 187 a^2 b^2 + 15 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^2}{30 a^2 b^5 d} + \\ & \frac{\operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^3}{3 a d (a+b \operatorname{Sin}[c+d x])^2} - \frac{b \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^4}{12 a^2 d (a+b \operatorname{Sin}[c+d x])^2} - \\ & \frac{(63 a^4 - 60 a^2 b^2 + 5 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^4}{60 a^2 b^3 d (a+b \operatorname{Sin}[c+d x])^2} - \frac{7 a \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^5}{20 b^2 d (a+b \operatorname{Sin}[c+d x])^2} + \\ & \frac{\operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^6}{5 b d (a+b \operatorname{Sin}[c+d x])^2} - \frac{(63 a^4 - 54 a^2 b^2 + 4 b^4) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]^3}{12 a^2 b^4 d (a+b \operatorname{Sin}[c+d x])} \end{aligned}$$

Result (type 3, 1913 leaves):

$$\begin{aligned} & -\frac{1}{64 b^4 d} \\ & \left(-48 a (c+d x) + \frac{6 (16 a^6 - 40 a^4 b^2 + 30 a^2 b^4 - 5 b^6) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} - 16 b \operatorname{Cos}[c+d x] + \right. \\ & \left. \frac{b (8 a^4 - 8 a^2 b^2 + b^4) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} + \frac{a b (-40 a^4 + 72 a^2 b^2 - 29 b^4) \operatorname{Cos}[c+d x]}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])} \right) + \\ & \frac{5 \left(\frac{2 (2 a^2 + b^2) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} + \frac{b \operatorname{Cos}[c+d x] (4 a^2 - b^2 + 3 a b \operatorname{Sin}[c+d x])}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])^2} \right)}{256 d} + \\ & -\frac{6 b^2 \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{\operatorname{Cos}[c+d x] (-b (2 a^2 + b^2) + a (2 a^2 - 5 b^2) \operatorname{Sin}[c+d x])}{(a+b \operatorname{Sin}[c+d x])^2} \\ & \frac{1}{384 b^6 d} \left(-\frac{1}{(a^2-b^2)^{5/2}} 12 (640 a^8 - 1792 a^6 b^2 + 1680 a^4 b^4 - 560 a^2 b^6 + 35 b^8) \right. \\ & \left. \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \frac{1}{(a^2-b^2)^2 (a+b \operatorname{Sin}[c+d x])^2} \right) \end{aligned}$$

$$\begin{aligned}
 & \left(3840 a^9 (c+d x) - 6912 a^7 b^2 (c+d x) + 1728 a^5 b^4 (c+d x) + 1920 a^3 b^6 (c+d x) - \right. \\
 & 576 a b^8 (c+d x) + 3840 a^8 b \cos [c+d x] - 7872 a^6 b^3 \cos [c+d x] + 4256 a^4 b^5 \cos [c+d x] - \\
 & 172 a^2 b^7 \cos [c+d x] - 70 b^9 \cos [c+d x] - 1920 a^7 b^2 (c+d x) \cos [2(c+d x)] + \\
 & 4416 a^5 b^4 (c+d x) \cos [2(c+d x)] - 3072 a^3 b^6 (c+d x) \cos [2(c+d x)] + \\
 & 576 a b^8 (c+d x) \cos [2(c+d x)] - 320 a^6 b^3 \cos [3(c+d x)] + 696 a^4 b^5 \cos [3(c+d x)] - \\
 & 432 a^2 b^7 \cos [3(c+d x)] + 56 b^9 \cos [3(c+d x)] + 8 a^4 b^5 \cos [5(c+d x)] - \\
 & 16 a^2 b^7 \cos [5(c+d x)] + 8 b^9 \cos [5(c+d x)] + 7680 a^8 b (c+d x) \sin [c+d x] - \\
 & 17664 a^6 b^3 (c+d x) \sin [c+d x] + 12288 a^4 b^5 (c+d x) \sin [c+d x] - \\
 & 2304 a^2 b^7 (c+d x) \sin [c+d x] + 2880 a^7 b^2 \sin [2(c+d x)] - \\
 & 6304 a^5 b^4 \sin [2(c+d x)] + 4022 a^3 b^6 \sin [2(c+d x)] - 607 a b^8 \sin [2(c+d x)] + \\
 & \left. 40 a^5 b^4 \sin [4(c+d x)] - 80 a^3 b^6 \sin [4(c+d x)] + 40 a b^8 \sin [4(c+d x)] \right) + \\
 & \frac{1}{128} \left(-\frac{1}{b^8 (a^2 - b^2)^{5/2} d} 3 (1792 a^{10} - 5760 a^8 b^2 + 6720 a^6 b^4 - 3360 a^4 b^6 + 630 a^2 b^8 - 21 b^{10}) \right. \\
 & \left. \operatorname{ArcTan} \left[\frac{\sec \left[\frac{1}{2}(c+d x) \right] \left(b \cos \left[\frac{1}{2}(c+d x) \right] + a \sin \left[\frac{1}{2}(c+d x) \right] \right)}{\sqrt{a^2 - b^2}} \right] - \right. \\
 & \left. \frac{1}{20 b^8 (-a^2 + b^2)^2 d (a + b \sin [c+d x])^2} (-53760 a^{11} (c+d x) + 119040 a^9 b^2 (c+d x) - \right. \\
 & 62400 a^7 b^4 (c+d x) - 19680 a^5 b^6 (c+d x) + 19200 a^3 b^8 (c+d x) - 2400 a b^{10} (c+d x) - \\
 & 53760 a^{10} b \cos [c+d x] + 132480 a^8 b^3 \cos [c+d x] - 103360 a^6 b^5 \cos [c+d x] + \\
 & 23800 a^4 b^7 \cos [c+d x] + 1080 a^2 b^9 \cos [c+d x] - 210 b^{11} \cos [c+d x] + \\
 & 26880 a^9 b^2 (c+d x) \cos [2(c+d x)] - 72960 a^7 b^4 (c+d x) \cos [2(c+d x)] + \\
 & 67680 a^5 b^6 (c+d x) \cos [2(c+d x)] - 24000 a^3 b^8 (c+d x) \cos [2(c+d x)] + \\
 & 2400 a b^{10} (c+d x) \cos [2(c+d x)] + 4480 a^8 b^3 \cos [3(c+d x)] - \\
 & 11600 a^6 b^5 \cos [3(c+d x)] + 9928 a^4 b^7 \cos [3(c+d x)] - 2976 a^2 b^9 \cos [3(c+d x)] + \\
 & 168 b^{11} \cos [3(c+d x)] - 112 a^6 b^5 \cos [5(c+d x)] + 248 a^4 b^7 \cos [5(c+d x)] - \\
 & 160 a^2 b^9 \cos [5(c+d x)] + 24 b^{11} \cos [5(c+d x)] + 8 a^4 b^7 \cos [7(c+d x)] - \\
 & 16 a^2 b^9 \cos [7(c+d x)] + 8 b^{11} \cos [7(c+d x)] - 107520 a^{10} b (c+d x) \sin [c+d x] + \\
 & 291840 a^8 b^3 (c+d x) \sin [c+d x] - 270720 a^6 b^5 (c+d x) \sin [c+d x] + \\
 & 96000 a^4 b^7 (c+d x) \sin [c+d x] - 9600 a^2 b^9 (c+d x) \sin [c+d x] - \\
 & 40320 a^9 b^2 \sin [2(c+d x)] + 104960 a^7 b^4 \sin [2(c+d x)] - 91460 a^5 b^6 \sin [2(c+d x)] + \\
 & 29160 a^3 b^8 \sin [2(c+d x)] - 2325 a b^{10} \sin [2(c+d x)] - 560 a^7 b^4 \sin [4(c+d x)] + \\
 & 1352 a^5 b^6 \sin [4(c+d x)] - 1024 a^3 b^8 \sin [4(c+d x)] + 232 a b^{10} \sin [4(c+d x)] + \\
 & \left. \left. 28 a^5 b^6 \sin [6(c+d x)] - 56 a^3 b^8 \sin [6(c+d x)] + 28 a b^{10} \sin [6(c+d x)] \right) \right)
 \end{aligned}$$

Problem 1268: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6 \sin [c+d x]}{(a+b \sin [c+d x])^3} dx$$

Optimal (type 3, 237 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{15 (8 a^4 - 8 a^2 b^2 + b^4) x}{8 b^7} + \frac{15 a (2 a^4 - 3 a^2 b^2 + b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{b^7 \sqrt{a^2-b^2} d} + \\
 & \frac{\operatorname{Cos}[c+d x]^5 (3 a+b \operatorname{Sin}[c+d x])}{4 b^2 d (a+b \operatorname{Sin}[c+d x])^2} + \frac{5 \operatorname{Cos}[c+d x]^3 (4 a^2-b^2+a b \operatorname{Sin}[c+d x])}{4 b^4 d (a+b \operatorname{Sin}[c+d x])} - \\
 & \frac{15 \operatorname{Cos}[c+d x] (4 a (2 a^2-b^2)-b (4 a^2-b^2) \operatorname{Sin}[c+d x])}{8 b^6 d}
 \end{aligned}$$

Result (type 3, 1250 leaves):

$$\begin{aligned}
 & \frac{1}{256 d} \left(\frac{1}{b^3} \left(-8 (c+d x) + \frac{2 a (8 a^4 - 20 a^2 b^2 + 15 b^4) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} + \right. \right. \\
 & \left. \left. \frac{a b (4 a^2 - 3 b^2) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} - \frac{3 b (4 a^4 - 7 a^2 b^2 + 2 b^4) \operatorname{Cos}[c+d x]}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])} \right) - \right. \\
 & \left. \frac{10 \left(\frac{6 a b \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{\operatorname{Cos}[c+d x] (a (2 a^2+b^2)+b (a^2+2 b^2) \operatorname{Sin}[c+d x])}{(a+b \operatorname{Sin}[c+d x])^2} \right)}{(a-b)^2 (a+b)^2} + \frac{1}{b^5} \right. \\
 & \left. \frac{10 \left(-24 (-8 a^2 + b^2) (c+d x) - \frac{6 a (64 a^6 - 168 a^4 b^2 + 140 a^2 b^4 - 35 b^6) \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} + \right. \right. \\
 & \left. \left. 96 a b \operatorname{Cos}[c+d x] + \frac{a b (-16 a^4 + 20 a^2 b^2 - 5 b^4) \operatorname{Cos}[c+d x]}{(a-b)(a+b)(a+b \operatorname{Sin}[c+d x])^2} + \right. \right. \\
 & \left. \left. \frac{b (112 a^6 - 220 a^4 b^2 + 115 a^2 b^4 - 10 b^6) \operatorname{Cos}[c+d x]}{(a-b)^2 (a+b)^2 (a+b \operatorname{Sin}[c+d x])} - 8 b^2 \operatorname{Sin}[2(c+d x)] \right) + \right. \\
 & \left. \frac{1}{b^7} \left(\frac{1}{(a^2-b^2)^{5/2}} 12 a (640 a^8 - 1920 a^6 b^2 + 2016 a^4 b^4 - 840 a^2 b^6 + 105 b^8) \right. \right. \\
 & \left. \left. \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \frac{1}{(a^2-b^2)^2 (a+b \operatorname{Sin}[c+d x])^2} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & (-3840 a^{10} (c+d x) + 7680 a^8 b^2 (c+d x) - 2976 a^6 b^4 (c+d x) - 1776 a^4 b^6 (c+d x) + \\
 & 960 a^2 b^8 (c+d x) - 48 b^{10} (c+d x) - 3840 a^9 b \operatorname{Cos}[c+d x] + 8640 a^7 b^3 \operatorname{Cos}[c+d x] - \\
 & 5696 a^5 b^5 \operatorname{Cos}[c+d x] + 788 a^3 b^7 \operatorname{Cos}[c+d x] + 114 a b^9 \operatorname{Cos}[c+d x] + \\
 & 1920 a^8 b^2 (c+d x) \operatorname{Cos}[2(c+d x)] - 4800 a^6 b^4 (c+d x) \operatorname{Cos}[2(c+d x)] + \\
 & 3888 a^4 b^6 (c+d x) \operatorname{Cos}[2(c+d x)] - 1056 a^2 b^8 (c+d x) \operatorname{Cos}[2(c+d x)] + \\
 & 48 b^{10} (c+d x) \operatorname{Cos}[2(c+d x)] + 320 a^7 b^3 \operatorname{Cos}[3(c+d x)] - 760 a^5 b^5 \operatorname{Cos}[3(c+d x)] + \\
 & 560 a^3 b^7 \operatorname{Cos}[3(c+d x)] - 120 a b^9 \operatorname{Cos}[3(c+d x)] - 8 a^5 b^5 \operatorname{Cos}[5(c+d x)] + \\
 & 16 a^3 b^7 \operatorname{Cos}[5(c+d x)] - 8 a b^9 \operatorname{Cos}[5(c+d x)] - 7680 a^9 b (c+d x) \operatorname{Sin}[c+d x] + \\
 & 19200 a^7 b^3 (c+d x) \operatorname{Sin}[c+d x] - 15552 a^5 b^5 (c+d x) \operatorname{Sin}[c+d x] + \\
 & 4224 a^3 b^7 (c+d x) \operatorname{Sin}[c+d x] - 192 a b^9 (c+d x) \operatorname{Sin}[c+d x] - \\
 & 2880 a^8 b^2 \operatorname{Sin}[2(c+d x)] + 6880 a^6 b^4 \operatorname{Sin}[2(c+d x)] - 5182 a^4 b^6 \operatorname{Sin}[2(c+d x)] + \\
 & 1221 a^2 b^8 \operatorname{Sin}[2(c+d x)] - 36 b^{10} \operatorname{Sin}[2(c+d x)] - 40 a^6 b^4 \operatorname{Sin}[4(c+d x)] + \\
 & 88 a^4 b^6 \operatorname{Sin}[4(c+d x)] - 56 a^2 b^8 \operatorname{Sin}[4(c+d x)] + 8 b^{10} \operatorname{Sin}[4(c+d x)] + \\
 & \left. \begin{aligned} & 2 a^4 b^6 \operatorname{Sin}[6(c+d x)] - 4 a^2 b^8 \operatorname{Sin}[6(c+d x)] + 2 b^{10} \operatorname{Sin}[6(c+d x)] \end{aligned} \right)
 \end{aligned}$$

Problem 1276: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[e+fx]^6}{\sqrt{d \operatorname{Sin}[e+fx]} (a+b \operatorname{Sin}[e+fx])^{13/2}} dx$$

Optimal (type 4, 712 leaves, 8 steps):

$$\begin{aligned}
 & \frac{2 \operatorname{Cos}[e + f x]^5 \sqrt{d \operatorname{Sin}[e + f x]}}{11 a d f (a + b \operatorname{Sin}[e + f x])^{11/2}} - \frac{20 (a^2 - b^2) \operatorname{Cos}[e + f x] \sqrt{d \operatorname{Sin}[e + f x]}}{99 a^2 b^2 d f (a + b \operatorname{Sin}[e + f x])^{9/2}} + \\
 & \frac{80 (3 a^2 + 2 b^2) \operatorname{Cos}[e + f x] \sqrt{d \operatorname{Sin}[e + f x]}}{693 a^3 b^2 d f (a + b \operatorname{Sin}[e + f x])^{7/2}} - \\
 & \frac{4 (5 a^4 - 17 a^2 b^2 + 16 b^4) \operatorname{Cos}[e + f x] \sqrt{d \operatorname{Sin}[e + f x]}}{231 a^4 b^2 (a^2 - b^2) d f (a + b \operatorname{Sin}[e + f x])^{5/2}} - \\
 & \frac{8 (5 a^6 - 22 a^4 b^2 + 65 a^2 b^4 - 32 b^6) \operatorname{Cos}[e + f x] \sqrt{d \operatorname{Sin}[e + f x]}}{693 a^5 b^2 (a^2 - b^2)^2 d f (a + b \operatorname{Sin}[e + f x])^{3/2}} + \\
 & \frac{16 b (93 a^4 - 93 a^2 b^2 + 32 b^4) \operatorname{Cos}[e + f x]}{693 a^5 (a^2 - b^2)^3 f \sqrt{d \operatorname{Sin}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]}} - \\
 & \left(16 b (93 a^4 - 93 a^2 b^2 + 32 b^4) \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \operatorname{EllipticE} \left[\right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}} \right], -\frac{a + b}{a - b} \right] \operatorname{Tan}[e + f x] \right) / \left(693 a^7 (a - b)^2 (a + b)^{5/2} \sqrt{d} f \right) - \\
 & \left(16 (45 a^4 - 48 a^3 b - 69 a^2 b^2 + 24 a b^3 + 32 b^4) \sqrt{\frac{a (1 - \operatorname{Csc}[e + f x])}{a + b}} \right. \\
 & \quad \left. \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}} \right], -\frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \operatorname{Tan}[e + f x] \right) / \left(693 a^6 (a - b)^2 (a + b)^{5/2} \sqrt{d} f \right)
 \end{aligned}$$

Result (type 4, 1906 leaves):

$$\begin{aligned}
 & \frac{1}{f \sqrt{d \operatorname{Sin}[e + f x]}} \\
 & \operatorname{Sin}[e + f x] \sqrt{a + b \operatorname{Sin}[e + f x]} \left(\frac{2 (a^4 \operatorname{Cos}[e + f x] - 2 a^2 b^2 \operatorname{Cos}[e + f x] + b^4 \operatorname{Cos}[e + f x])}{11 a b^4 (a + b \operatorname{Sin}[e + f x])^6} - \right. \\
 & \quad \frac{4 (18 a^4 \operatorname{Cos}[e + f x] - 13 a^2 b^2 \operatorname{Cos}[e + f x] - 5 b^4 \operatorname{Cos}[e + f x])}{99 a^2 b^4 (a + b \operatorname{Sin}[e + f x])^5} + \\
 & \quad \left. \frac{4 (189 a^4 \operatorname{Cos}[e + f x] - 3 a^2 b^2 \operatorname{Cos}[e + f x] + 40 b^4 \operatorname{Cos}[e + f x])}{693 a^3 b^4 (a + b \operatorname{Sin}[e + f x])^4} - \right. \\
 & \quad \left. \frac{4 (42 a^6 \operatorname{Cos}[e + f x] - 37 a^4 b^2 \operatorname{Cos}[e + f x] - 17 a^2 b^4 \operatorname{Cos}[e + f x] + 16 b^6 \operatorname{Cos}[e + f x])}{(231 a^4 b^4 (a^2 - b^2) (a + b \operatorname{Sin}[e + f x])^3) +} \right) / \\
 & \quad \left(2 (63 a^8 \operatorname{Cos}[e + f x] - 146 a^6 b^2 \operatorname{Cos}[e + f x] + 151 a^4 b^4 \operatorname{Cos}[e + f x] - 260 a^2 b^6 \operatorname{Cos}[e + f x] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{128 b^8 \cos [e+f x]}{\left(693 a^5 b^4 (a^2-b^2)^2 (a+b \sin [e+f x])^2 \right)} - \right. \right. \\
 & \left. \left(\frac{16 \left(93 a^4 b^2 \cos [e+f x] - 93 a^2 b^4 \cos [e+f x] + 32 b^6 \cos [e+f x] \right)}{\left(693 a^6 (a^2-b^2)^3 (a+b \sin [e+f x]) \right)} \right) \right) + \\
 & \frac{1}{693 a^6 (a-b)^3 (a+b)^3 f \sqrt{d \sin [e+f x]}} 8 \sqrt{\sin [e+f x]} \\
 & \left(\left(4 a \left(45 a^6 - 114 a^4 b^2 + 101 a^2 b^4 - 32 b^6 \right) \sqrt{\frac{(a+b) \cot \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{-a+b}} \right. \right. \\
 & \left. \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{\sqrt{\frac{\csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}}}{\sqrt{2}}}, -\frac{2 a}{-a+b} \right] \text{Sec} [e+f x] \right. \right. \right. \\
 & \left. \left. \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{-\frac{(a+b) \csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{\csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}} \right] \right) \right) \right) / \\
 & \left((a+b) \sqrt{\sin [e+f x]} \sqrt{a+b \sin [e+f x]} \right) + \\
 & 4 a \left(-93 a^5 b + 93 a^3 b^3 - 32 a b^5 \right) \left(\left(\sqrt{\frac{(a+b) \cot \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2}{-a+b}} \right. \right. \\
 & \left. \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{\sqrt{\frac{\csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}}}{\sqrt{2}}}, -\frac{2 a}{-a+b} \right] \text{Sec} [e+f x] \right. \right. \right. \\
 & \left. \left. \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{-\frac{(a+b) \csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{\csc \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}} \right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - \sqrt{\frac{(a+b) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-a+b}} \\
 & \text{EllipticPi}\left[-\frac{a}{b}, \text{ArcSin}\left[\frac{\sqrt{\frac{\text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \text{Sec}[e+fx] \\
 & \text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{-\frac{(a+b) \text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \text{Sin}[e+fx]}{a}} \\
 & \left. \sqrt{\frac{\text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) / \\
 & \left. \left(b \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) \right) + 2 (93 a^4 b^2 - 93 a^2 b^4 + 32 b^6) \\
 & \left(\frac{\cos[e+fx] \sqrt{a+b \sin[e+fx]}}{b \sqrt{\sin[e+fx]}} + \left(i \cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right] \text{Csc}[e+fx] \right. \right. \\
 & \left. \left. \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\text{Sin}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]}{\sqrt{\sin[e+fx]}}\right], -\frac{2a}{-a-b}\right] \sqrt{a+b \sin[e+fx]} \right) \right) / \\
 & \left(b \sqrt{\cos\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \text{Csc}[e+fx]} \sqrt{\frac{\text{Csc}[e+fx] (a+b \sin[e+fx])}{a+b}} \right) + \\
 & \frac{1}{b} 2 a \left(\left(a \sqrt{\frac{(a+b) \cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2}{-a+b}} \text{EllipticF}\left[\right. \right. \right. \\
 & \left. \left. \left. \text{ArcSin}\left[\frac{\sqrt{\frac{\text{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \text{Sec}[e+fx] \right. \right. \right.
 \end{aligned}$$

$$\left(2 \left(-2 (2 a^2 - b^2) \operatorname{Cos}[e + f x]^2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{4}, \frac{5}{4}, \operatorname{Cos}[e + f x]^2\right] + (\operatorname{Sin}[e + f x]^2)^{1/4} (a^2 + b^2 + (2 a^2 - b^2) \operatorname{Cos}[e + f x]^2 + 2 a b \operatorname{Sin}[e + f x]) \right) \operatorname{Tan}[e + f x] \right) / \left(3 f g^2 \sqrt{g \operatorname{Cos}[e + f x]} \sqrt{d \operatorname{Sin}[e + f x]} (\operatorname{Sin}[e + f x]^2)^{1/4} \right)$$

Problem 1278: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Sin}[e + f x])^2}{(g \operatorname{Cos}[e + f x])^{7/2} \sqrt{d \operatorname{Sin}[e + f x]}} dx$$

Optimal (type 4, 193 leaves, 6 steps):

$$\frac{8 a^2 \sqrt{d \operatorname{Sin}[e + f x]}}{5 d f g^3 \sqrt{g \operatorname{Cos}[e + f x]}} + \frac{8 a b (d \operatorname{Sin}[e + f x])^{3/2}}{5 d^2 f g^3 \sqrt{g \operatorname{Cos}[e + f x]}} + \frac{2 \sqrt{d \operatorname{Sin}[e + f x]} (a + b \operatorname{Sin}[e + f x])^2}{5 d f g (g \operatorname{Cos}[e + f x])^{5/2}} - \frac{8 a b \sqrt{g \operatorname{Cos}[e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \operatorname{Sin}[e + f x]}}{5 d f g^4 \sqrt{\operatorname{Sin}[2 e + 2 f x]}}$$

Result (type 5, 156 leaves):

$$\left(4 a b \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{3}{4}, \frac{7}{4}, \operatorname{Cos}[e + f x]^2\right] \operatorname{Sin}[2 (e + f x)]^2 + 3 \operatorname{Sec}[e + f x] (\operatorname{Sin}[e + f x]^2)^{3/4} (6 a^2 + b^2 + (4 a^2 - b^2) \operatorname{Cos}[2 (e + f x)]) + 6 a b \operatorname{Sin}[e + f x] + 2 a b \operatorname{Sin}[3 (e + f x)] \right) \operatorname{Tan}[e + f x] / \left(15 f g^3 \sqrt{g \operatorname{Cos}[e + f x]} \sqrt{d \operatorname{Sin}[e + f x]} (\operatorname{Sin}[e + f x]^2)^{3/4} \right)$$

Problem 1292: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x]^2 \operatorname{Csc}[c + d x]^2}{a + b \operatorname{Sin}[c + d x]} dx$$

Optimal (type 3, 153 leaves, 9 steps):

$$-\frac{2 b^2 \sqrt{a^2 - b^2} \operatorname{ArcTan}\left[\frac{b + a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}{\sqrt{a^2 - b^2}}\right]}{a^4 d} - \frac{b (a^2 - 2 b^2) \operatorname{ArcTanh}[\operatorname{Cos}[c + d x]]}{2 a^4 d} + \frac{(a^2 - 3 b^2) \operatorname{Cot}[c + d x]}{3 a^3 d} + \frac{b \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]}{2 a^2 d} - \frac{\operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2}{3 a d}$$

Result (type 3, 351 leaves):

$$\begin{aligned}
 & \frac{2 b^2 \sqrt{a^2 - b^2} \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{\sqrt{a^2 - b^2}}\right]}{a^4 d} + \\
 & \frac{\left(a^2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - 3 b^2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]}{6 a^3 d} + \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8 a^2 d} - \\
 & \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24 a d} + \frac{\left(-a^2 b + 2 b^3\right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{2 a^4 d} + \\
 & \frac{\left(a^2 b - 2 b^3\right) \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2 a^4 d} - \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8 a^2 d} + \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(-a^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{6 a^3 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24 a d}
 \end{aligned}$$

Problem 1293: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx]^3}{a+b \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 194 leaves, 10 steps):

$$\begin{aligned}
 & \frac{2 b^3 \sqrt{a^2 - b^2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 - b^2}}\right]}{a^5 d} + \frac{\left(a^4 + 4 a^2 b^2 - 8 b^4\right) \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{8 a^5 d} - \\
 & \frac{b\left(a^2 - 3 b^2\right) \operatorname{Cot}[c+dx]}{3 a^4 d} + \frac{\left(a^2 - 4 b^2\right) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8 a^3 d} + \\
 & \frac{b \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{3 a^2 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4 a d}
 \end{aligned}$$

Result (type 3, 430 leaves):

$$\begin{aligned}
& \frac{2 b^3 \sqrt{a^2 - b^2} \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{\sqrt{a^2 - b^2}}\right]}{a^5 d} + \\
& \frac{\left(-a^2 b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + 3 b^3 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]}{6 a^4 d} + \\
& \frac{\left(a^2 - 4 b^2\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{32 a^3 d} + \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24 a^2 d} - \\
& \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64 a d} + \frac{\left(a^4 + 4 a^2 b^2 - 8 b^4\right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{8 a^5 d} + \\
& \frac{\left(-a^4 - 4 a^2 b^2 + 8 b^4\right) \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8 a^5 d} + \frac{\left(-a^2 + 4 b^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{32 a^3 d} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64 a d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(a^2 b \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - 3 b^3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{6 a^4 d} - \\
& \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24 a^2 d}
\end{aligned}$$

Problem 1294: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^2 \operatorname{Csc}[c+dx]^4}{a+b \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 238 leaves, 11 steps):

$$\begin{aligned}
& - \frac{2 b^4 \sqrt{a^2 - b^2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 - b^2}}\right]}{a^6 d} - \frac{b \left(a^4 + 4 a^2 b^2 - 8 b^4\right) \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{8 a^6 d} + \\
& \frac{\left(2 a^4 + 5 a^2 b^2 - 15 b^4\right) \operatorname{Cot}[c+dx]}{15 a^5 d} - \frac{b \left(a^2 - 4 b^2\right) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8 a^4 d} + \\
& \frac{\left(a^2 - 5 b^2\right) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{15 a^3 d} + \frac{b \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4 a^2 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^4}{5 a d}
\end{aligned}$$

Result (type 3, 506 leaves):

$$\frac{1}{960 a^6 d} \left(-1920 b^4 \sqrt{a^2 - b^2} \operatorname{ArcTan} \left[\frac{b + a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] + 32 (2 a^5 + 5 a^3 b^2 - 15 a b^4) \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] - \right. \\
 30 a^4 b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 120 a^2 b^3 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 15 a^4 b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 - \\
 120 a^4 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] - 480 a^2 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] + 960 b^5 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] + \\
 120 a^4 b \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + 480 a^2 b^3 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - 960 b^5 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \\
 30 a^4 b \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 120 a^2 b^3 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 15 a^4 b \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 - \\
 16 a^5 \operatorname{Csc} [c + d x]^3 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right]^4 + 320 a^3 b^2 \operatorname{Csc} [c + d x]^3 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right]^4 + \\
 a^5 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Sin} [c + d x] - 20 a^3 b^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Sin} [c + d x] - \\
 3 a^5 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^6 \operatorname{Sin} [c + d x] - 64 a^5 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] - 160 a^3 b^2 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] + \\
 \left. 480 a b^4 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] + 6 a^5 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] \right)$$

Problem 1307: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot} [c + d x]^4}{a + b \operatorname{Sin} [c + d x]} dx$$

Optimal (type 3, 154 leaves, 7 steps):

$$\frac{2 (a^2 - b^2)^{3/2} \operatorname{ArcTan} \left[\frac{b + a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right]}{a^4 d} - \frac{b (3 a^2 - 2 b^2) \operatorname{ArcTanh} [\operatorname{Cos} [c + d x]]}{2 a^4 d} + \\
 \frac{(4 a^2 - 3 b^2) \operatorname{Cot} [c + d x]}{3 a^3 d} + \frac{b \operatorname{Cot} [c + d x] \operatorname{Csc} [c + d x]}{2 a^2 d} - \frac{\operatorname{Cot} [c + d x] \operatorname{Csc} [c + d x]^2}{3 a d}$$

Result (type 3, 350 leaves):

$$\begin{aligned}
& \frac{2 (a^2 - b^2)^{3/2} \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{\sqrt{a^2-b^2}}\right]}{a^4 d} + \\
& \frac{\left(4 a^2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - 3 b^2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]}{6 a^3 d} + \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8 a^2 d} - \\
& \frac{\operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24 a d} + \frac{(-3 a^2 b + 2 b^3) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{2 a^4 d} + \\
& \frac{(3 a^2 b - 2 b^3) \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2 a^4 d} - \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8 a^2 d} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(-4 a^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{6 a^3 d} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24 a d}
\end{aligned}$$

Problem 1308: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^4 \operatorname{Csc}[c+dx]}{a+b \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 198 leaves, 8 steps):

$$\begin{aligned}
& - \frac{2 b (a^2 - b^2)^{3/2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{a^5 d} - \frac{(3 a^4 - 12 a^2 b^2 + 8 b^4) \operatorname{ArcTanh}\left[\operatorname{Cos}[c+dx]\right]}{8 a^5 d} - \\
& \frac{b (4 a^2 - 3 b^2) \operatorname{Cot}[c+dx]}{3 a^4 d} + \frac{(5 a^2 - 4 b^2) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8 a^3 d} + \\
& \frac{b \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{3 a^2 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4 a d}
\end{aligned}$$

Result (type 3, 433 leaves):

$$\begin{aligned}
 & \frac{2 b (a^2 - b^2)^{3/2} \operatorname{ArcTan} \left[\frac{\operatorname{Sec} \left[\frac{1}{2} (c+dx) \right] \left(b \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] + a \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right)}{\sqrt{a^2 - b^2}} \right]}{a^5 d} + \\
 & \frac{\left(-4 a^2 b \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] + 3 b^3 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \right) \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]}{6 a^4 d} + \\
 & \frac{\left(5 a^2 - 4 b^2 \right) \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]^2}{32 a^3 d} + \frac{b \operatorname{Cot} \left[\frac{1}{2} (c+dx) \right] \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]^2}{24 a^2 d} - \\
 & \frac{\operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]^4}{64 a d} + \frac{\left(-3 a^4 + 12 a^2 b^2 - 8 b^4 \right) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \right]}{8 a^5 d} + \\
 & \frac{\left(3 a^4 - 12 a^2 b^2 + 8 b^4 \right) \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right]}{8 a^5 d} + \frac{\left(-5 a^2 + 4 b^2 \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{32 a^3 d} + \\
 & \frac{\operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^4}{64 a d} + \frac{\operatorname{Sec} \left[\frac{1}{2} (c+dx) \right] \left(4 a^2 b \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] - 3 b^3 \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right)}{6 a^4 d} - \\
 & \frac{b \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{24 a^2 d}
 \end{aligned}$$

Problem 1309: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot} [c+dx]^4 \operatorname{Csc} [c+dx]^2}{a+b \operatorname{Sin} [c+dx]} dx$$

Optimal (type 3, 244 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 b^2 (a^2 - b^2)^{3/2} \operatorname{ArcTan} \left[\frac{b+a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{\sqrt{a^2 - b^2}} \right]}{a^6 d} + \frac{b \left(3 a^4 - 12 a^2 b^2 + 8 b^4 \right) \operatorname{ArcTanh} [\operatorname{Cos} [c+dx]]}{8 a^6 d} - \\
 & \frac{\left(3 a^4 - 20 a^2 b^2 + 15 b^4 \right) \operatorname{Cot} [c+dx]}{15 a^5 d} - \frac{b \left(5 a^2 - 4 b^2 \right) \operatorname{Cot} [c+dx] \operatorname{Csc} [c+dx]}{8 a^4 d} + \\
 & \frac{\left(6 a^2 - 5 b^2 \right) \operatorname{Cot} [c+dx] \operatorname{Csc} [c+dx]^2}{15 a^3 d} + \frac{b \operatorname{Cot} [c+dx] \operatorname{Csc} [c+dx]^3}{4 a^2 d} - \frac{\operatorname{Cot} [c+dx] \operatorname{Csc} [c+dx]^4}{5 a d}
 \end{aligned}$$

Result (type 3, 507 leaves):

$$\frac{1}{960 a^6 d} \left(1920 b^2 (a^2 - b^2)^{3/2} \operatorname{ArcTan}\left[\frac{b + a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 - b^2}}\right] - 32 (3 a^5 - 20 a^3 b^2 + 15 a b^4) \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] - 150 a^4 b \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^2 + 120 a^2 b^3 \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^2 + 15 a^4 b \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^4 + 360 a^4 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right] - 1440 a^2 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right] + 960 b^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right] - 360 a^4 b \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 1440 a^2 b^3 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - 960 b^5 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 150 a^4 b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 - 120 a^2 b^3 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 - 15 a^4 b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 - 336 a^5 \operatorname{Csc}[c + dx]^3 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]^4 + 320 a^3 b^2 \operatorname{Csc}[c + dx]^3 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]^4 + 21 a^5 \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^4 \operatorname{Sin}[c + dx] - 20 a^3 b^2 \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^4 \operatorname{Sin}[c + dx] - 3 a^5 \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^6 \operatorname{Sin}[c + dx] + 96 a^5 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - 640 a^3 b^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + 480 a b^4 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + 6 a^5 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right)$$

Problem 1316: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + dx] \operatorname{Cot}[c + dx]^4}{a + b \operatorname{Sin}[c + dx]} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\frac{(2 a^2 - b^2) \operatorname{Csc}[c + dx]}{a^3 d} + \frac{b \operatorname{Csc}[c + dx]^2}{2 a^2 d} - \frac{\operatorname{Csc}[c + dx]^3}{3 a d} + \frac{b (2 a^2 - b^2) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{a^4 d} + \frac{(a^2 - b^2)^2 \operatorname{Log}[a + b \operatorname{Sin}[c + dx]]}{a^4 b d}$$

Result (type 3, 275 leaves):

$$\begin{aligned}
 & \frac{\left(11 a^2 \cos \left[\frac{1}{2}(c+d x)\right]-6 b^2 \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]}{12 a^3 d} + \\
 & \frac{b \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{8 a^2 d} - \frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 a d} + \\
 & \frac{\left(2 a^2 b-b^3\right) \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^4 d} + \frac{\left(a^4-2 a^2 b^2+b^4\right) \operatorname{Log}[a+b \operatorname{Sin}[c+d x]]}{a^4 b d} + \\
 & \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{8 a^2 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\left(11 a^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]-6 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}{12 a^3 d} - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 a d}
 \end{aligned}$$

Problem 1317: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+d x]^5}{a+b \operatorname{Sin}[c+d x]} dx$$

Optimal (type 3, 148 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{b\left(2 a^2-b^2\right) \operatorname{Csc}[c+d x]}{a^4 d} + \frac{\left(2 a^2-b^2\right) \operatorname{Csc}[c+d x]^2}{2 a^3 d} + \frac{b \operatorname{Csc}[c+d x]^3}{3 a^2 d} - \\
 & \frac{\operatorname{Csc}[c+d x]^4}{4 a d} + \frac{\left(a^2-b^2\right)^2 \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^5 d} - \frac{\left(a^2-b^2\right)^2 \operatorname{Log}[a+b \operatorname{Sin}[c+d x]]}{a^5 d}
 \end{aligned}$$

Result (type 3, 347 leaves):

$$\begin{aligned}
 & \frac{\left(-11 a^2 b \cos \left[\frac{1}{2}(c+d x)\right]+6 b^3 \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]}{12 a^4 d} + \frac{\left(7 a^2-4 b^2\right) \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{32 a^3 d} + \\
 & \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 a^2 d} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{64 a d} + \frac{\left(a^4-2 a^2 b^2+b^4\right) \operatorname{Log}[\operatorname{Sin}[c+d x]]}{a^5 d} + \\
 & \frac{\left(-a^4+2 a^2 b^2-b^4\right) \operatorname{Log}[a+b \operatorname{Sin}[c+d x]]}{a^5 d} + \frac{\left(7 a^2-4 b^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{32 a^3 d} - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4}{64 a d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\left(-11 a^2 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+6 b^3 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}{12 a^4 d} + \\
 & \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 a^2 d}
 \end{aligned}$$

Problem 1318: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+d x]^5 \operatorname{Csc}[c+d x]}{a+b \operatorname{Sin}[c+d x]} dx$$

Optimal (type 3, 179 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{(a^2 - b^2)^2 \operatorname{Csc}[c + dx]}{a^5 d} - \frac{b(2a^2 - b^2) \operatorname{Csc}[c + dx]^2}{2a^4 d} + \frac{(2a^2 - b^2) \operatorname{Csc}[c + dx]^3}{3a^3 d} + \frac{b \operatorname{Csc}[c + dx]^4}{4a^2 d} - \\
 & \frac{\operatorname{Csc}[c + dx]^5}{5a d} - \frac{b(a^2 - b^2)^2 \operatorname{Log}[\operatorname{Sin}[c + dx]]}{a^6 d} + \frac{b(a^2 - b^2)^2 \operatorname{Log}[a + b \operatorname{Sin}[c + dx]]}{a^6 d}
 \end{aligned}$$

Result (type 3, 492 leaves):

$$\begin{aligned}
 & \frac{1}{240 a^5 d} \left(-89 a^4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + 220 a^2 b^2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - 120 b^4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \right) \\
 & \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right] + \frac{(-7 a^2 b + 4 b^3) \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{32 a^4 d} + \\
 & \frac{\left(31 a^2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - 20 b^2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^3}{480 a^3 d} + \frac{b \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^4}{64 a^2 d} - \\
 & \frac{\operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c + dx)\right]^4}{160 a d} + \frac{(-a^4 b + 2 a^2 b^3 - b^5) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{a^6 d} + \\
 & \frac{(a^4 b - 2 a^2 b^3 + b^5) \operatorname{Log}[a + b \operatorname{Sin}[c + dx]]}{a^6 d} + \frac{(-7 a^2 b + 4 b^3) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2}{32 a^4 d} + \\
 & \frac{b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4}{64 a^2 d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^3 \left(31 a^2 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] - 20 b^2 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)}{480 a^3 d} + \frac{1}{240 a^5 d} \\
 & \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \left(-89 a^4 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + 220 a^2 b^2 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] - 120 b^4 \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) - \\
 & \frac{\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{160 a d}
 \end{aligned}$$

Problem 1319: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + dx]^5 \operatorname{Csc}[c + dx]^2}{a + b \operatorname{Sin}[c + dx]} dx$$

Optimal (type 3, 212 leaves, 4 steps):

$$\begin{aligned}
 & \frac{b(a^2 - b^2)^2 \operatorname{Csc}[c + dx]}{a^6 d} - \frac{(a^2 - b^2)^2 \operatorname{Csc}[c + dx]^2}{2a^5 d} - \\
 & \frac{b(2a^2 - b^2) \operatorname{Csc}[c + dx]^3}{3a^4 d} + \frac{(2a^2 - b^2) \operatorname{Csc}[c + dx]^4}{4a^3 d} + \frac{b \operatorname{Csc}[c + dx]^5}{5a^2 d} - \\
 & \frac{\operatorname{Csc}[c + dx]^6}{6a d} + \frac{b^2(a^2 - b^2)^2 \operatorname{Log}[\operatorname{Sin}[c + dx]]}{a^7 d} - \frac{b^2(a^2 - b^2)^2 \operatorname{Log}[a + b \operatorname{Sin}[c + dx]]}{a^7 d}
 \end{aligned}$$

Result (type 3, 493 leaves):

$$\begin{aligned}
 & \frac{1}{1920 a^7 d} \\
 & \left(8 (89 a^5 b - 220 a^3 b^3 + 120 a b^5) \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] - 30 (5 a^6 - 14 a^4 b^2 + 8 a^2 b^4) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & 1920 a^4 b^2 \operatorname{Log}[\operatorname{Sin}[c+dx]] - 3840 a^2 b^4 \operatorname{Log}[\operatorname{Sin}[c+dx]] + 1920 b^6 \operatorname{Log}[\operatorname{Sin}[c+dx]] - \\
 & 1920 a^4 b^2 \operatorname{Log}[a+b \operatorname{Sin}[c+dx]] + 3840 a^2 b^4 \operatorname{Log}[a+b \operatorname{Sin}[c+dx]] - \\
 & 1920 b^6 \operatorname{Log}[a+b \operatorname{Sin}[c+dx]] - 150 a^6 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 420 a^4 b^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 - 240 a^2 b^4 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 45 a^6 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 - 30 a^4 b^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 - 5 a^6 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 - \\
 & 992 a^5 b \operatorname{Csc}[c+dx]^3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]^4 + 640 a^3 b^3 \operatorname{Csc}[c+dx]^3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]^4 + \\
 & 384 a^5 b \operatorname{Csc}[c+dx]^5 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]^6 + a^5 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6 (-5 a + 6 b \operatorname{Sin}[c+dx]) + \\
 & a^3 \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4 (45 a^3 - 30 a b^2 + (-62 a^2 b + 40 b^3) \operatorname{Sin}[c+dx]) + \\
 & \left. 712 a^5 b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 1760 a^3 b^3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 960 a b^5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)
 \end{aligned}$$

Problem 1327: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+dx] \operatorname{Cot}[c+dx]^5}{a+b \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 195 leaves, 15 steps):

$$\begin{aligned}
 & -\frac{x}{b} + \frac{2 (a^2 - b^2)^{5/2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{a^5 b d} - \\
 & \frac{(15 a^4 - 20 a^2 b^2 + 8 b^4) \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{8 a^5 d} + \frac{b (-2 a^2 + b^2) \operatorname{Cot}[c+dx]}{a^4 d} + \\
 & \frac{b \operatorname{Cot}[c+dx]^3}{3 a^2 d} + \frac{(7 a^2 - 4 b^2) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8 a^3 d} - \frac{\operatorname{Cot}[c+dx]^3 \operatorname{Csc}[c+dx]}{4 a d}
 \end{aligned}$$

Result (type 3, 448 leaves):

$$\begin{aligned}
& -\frac{c+dx}{bd} + \frac{2(a^2-b^2)^{5/2} \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + a \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{\sqrt{a^2-b^2}}\right]}{a^5 b d} + \\
& \frac{\left(-7 a^2 b \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + 3 b^3 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]}{6 a^4 d} + \\
& \frac{\left(9 a^2 - 4 b^2\right) \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{32 a^3 d} + \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24 a^2 d} - \\
& \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{64 a d} + \frac{\left(-15 a^4 + 20 a^2 b^2 - 8 b^4\right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right]}{8 a^5 d} + \\
& \frac{\left(15 a^4 - 20 a^2 b^2 + 8 b^4\right) \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8 a^5 d} + \frac{\left(-9 a^2 + 4 b^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{32 a^3 d} + \\
& \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4}{64 a d} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left(7 a^2 b \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - 3 b^3 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)}{6 a^4 d} - \\
& \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24 a^2 d}
\end{aligned}$$

Problem 1328: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c+dx]^6}{a+b \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 241 leaves, 9 steps):

$$\begin{aligned}
& -\frac{2(a^2-b^2)^{5/2} \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{a^6 d} + \frac{b(15 a^4 - 20 a^2 b^2 + 8 b^4) \operatorname{ArcTanh}[\operatorname{Cos}[c+dx]]}{8 a^6 d} - \\
& \frac{(23 a^4 - 35 a^2 b^2 + 15 b^4) \operatorname{Cot}[c+dx]}{15 a^5 d} + \frac{b(-9 a^2 + 4 b^2) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]}{8 a^4 d} + \\
& \frac{(11 a^2 - 5 b^2) \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{15 a^3 d} + \frac{b \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^3}{4 a^2 d} - \frac{\operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^4}{5 a d}
\end{aligned}$$

Result (type 3, 504 leaves):

$$\frac{1}{960 a^6 d} \left(-1920 (a^2 - b^2)^{5/2} \operatorname{ArcTan} \left[\frac{b + a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] - 32 (23 a^5 - 35 a^3 b^2 + 15 a b^4) \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] - 270 a^4 b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 120 a^2 b^3 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 + 15 a^4 b \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 + 1800 a^4 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] - 2400 a^2 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] + 960 b^5 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] - 1800 a^4 b \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + 2400 a^2 b^3 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] - 960 b^5 \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + 270 a^4 b \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 120 a^2 b^3 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 - 15 a^4 b \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 - 656 a^5 \operatorname{Csc} [c + d x]^3 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right]^4 + 320 a^3 b^2 \operatorname{Csc} [c + d x]^3 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right]^4 + 41 a^5 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Sin} [c + d x] - 20 a^3 b^2 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Sin} [c + d x] - 3 a^5 \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^6 \operatorname{Sin} [c + d x] + 736 a^5 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] - 1120 a^3 b^2 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] + 480 a b^4 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] + 6 a^5 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^4 \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right] \right)$$

Problem 1356: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc} [c + d x] \operatorname{Sec} [c + d x]^4}{a + b \operatorname{Sin} [c + d x]} dx$$

Optimal (type 3, 194 leaves, 12 steps):

$$\frac{2 b^5 \operatorname{ArcTan} \left[\frac{b + a \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right]}{a (a^2 - b^2)^{5/2} d} - \frac{\operatorname{ArcTanh} [\operatorname{Cos} [c + d x]]}{a d} + \frac{\operatorname{Sec} [c + d x]}{a d} + \frac{\operatorname{Sec} [c + d x]^3}{3 a d} + \frac{b \operatorname{Sec} [c + d x]^3 (b - a \operatorname{Sin} [c + d x])}{3 a (a^2 - b^2) d} - \frac{b \operatorname{Sec} [c + d x] (3 b^3 + a (2 a^2 - 5 b^2) \operatorname{Sin} [c + d x])}{3 a (a^2 - b^2)^2 d}$$

Result (type 3, 408 leaves):

$$\begin{aligned}
 & - \frac{2 b^5 \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\left(b \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+a \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}{\sqrt{a^2-b^2}}\right]}{a\left(a^2-b^2\right)^{5 / 2} d}-\frac{\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]}{a d}+ \\
 & \frac{\operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{a d}+\frac{1}{12(a+b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}+ \\
 & \frac{\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a+b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3}- \\
 & \frac{\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a-b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3}+ \\
 & \frac{1}{12(a-b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}+ \\
 & \frac{-7 a \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+10 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a-b)^2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}+ \\
 & \frac{7 a \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+10 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a+b)^2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}
 \end{aligned}$$

Problem 1357: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c+d x]^2 \operatorname{Sec}[c+d x]^4}{a+b \operatorname{Sin}[c+d x]} d x$$

Optimal (type 3, 220 leaves, 15 steps):

$$\begin{aligned}
 & \frac{2 b^6 \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{a^2\left(a^2-b^2\right)^{5 / 2} d}+\frac{b \operatorname{ArcTanh}\left[\operatorname{Cos}[c+d x]\right]}{a^2 d}-\frac{\operatorname{Cot}[c+d x]}{a d}+\frac{b\left(-a^2+2 b^2\right) \operatorname{Sec}[c+d x]}{\left(a^2-b^2\right)^2 d}+ \\
 & \frac{b \operatorname{Sec}[c+d x]^3(-a+b \operatorname{Sin}[c+d x])}{3 a\left(a^2-b^2\right) d}+\frac{\left(6 a^4-10 a^2 b^2+b^4\right) \operatorname{Tan}[c+d x]}{3 a\left(a^2-b^2\right)^2 d}+\frac{\operatorname{Tan}[c+d x]^3}{3 a d}
 \end{aligned}$$

Result (type 3, 450 leaves):

$$\begin{aligned}
 & \frac{2 b^6 \operatorname{ArcTan}\left[\frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\left(b \cos\left[\frac{1}{2}(c+d x)\right]+a \sin\left[\frac{1}{2}(c+d x)\right]\right)}{\sqrt{a^2-b^2}}\right]}{a^2\left(a^2-b^2\right)^{5 / 2} d}-\frac{\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{2 a d}+\frac{b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]}{a^2 d}- \\
 & \frac{b \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{a^2 d}+\frac{1}{12(a+b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}+ \\
 & \frac{\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a+b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3}+ \\
 & \frac{\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a-b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3}- \\
 & \frac{1}{12(a-b) d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}+ \\
 & \frac{10 a \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]-13 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a-b)^2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}+ \\
 & \frac{10 a \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+13 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{6(a+b)^2 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)}+\frac{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{2 a d}
 \end{aligned}$$

Problem 1358: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x]^4}{a+b \operatorname{Sin}[c+d x]} d x$$

Optimal (type 3, 332 leaves, 20 steps):

$$\begin{aligned}
 & -\frac{2 b^7 \operatorname{ArcTan}\left[\frac{b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{a^3\left(a^2-b^2\right)^{5 / 2} d}-\frac{5 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{2 a d}-\frac{b^2 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{a^3 d}+ \\
 & \frac{b \operatorname{Cot}[c+d x]}{a^2 d}+\frac{5 \operatorname{Sec}[c+d x]}{2 a d}+\frac{b^2 \operatorname{Sec}[c+d x]}{a^3 d}+\frac{5 \operatorname{Sec}[c+d x]^3}{6 a d}+ \\
 & \frac{b^2 \operatorname{Sec}[c+d x]^3}{3 a^3 d}-\frac{\operatorname{Csc}[c+d x]^2 \operatorname{Sec}[c+d x]^3}{2 a d}+\frac{b^3 \operatorname{Sec}[c+d x]^3(b-a \operatorname{Sin}[c+d x])}{3 a^3\left(a^2-b^2\right) d}- \\
 & \frac{b^3 \operatorname{Sec}[c+d x]\left(3 b^3+a\left(2 a^2-5 b^2\right) \operatorname{Sin}[c+d x]\right)}{3 a^3\left(a^2-b^2\right)^2 d}-\frac{2 b \operatorname{Tan}[c+d x]}{a^2 d}-\frac{b \operatorname{Tan}[c+d x]^3}{3 a^2 d}
 \end{aligned}$$

Result (type 3, 947 leaves):

$$16 \left(\frac{a\left(13 a^2-19 b^2\right) \operatorname{Csc}[c+d x]\left(a+b \operatorname{Sin}[c+d x]\right)}{96\left(a^2-b^2\right)^2 d\left(b+a \operatorname{Csc}[c+d x]\right)} - \right.$$

$$\begin{aligned}
 & \left(b^7 \operatorname{ArcTan} \left[\frac{\operatorname{Sec} \left[\frac{1}{2} (c + d x) \right] \left(b \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + a \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)}{\sqrt{a^2 - b^2}} \right] \right. \\
 & \quad \left. \operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x]) \right) / \left(8 a^3 (a^2 - b^2)^{5/2} d (b + a \operatorname{Csc} [c + d x]) \right) + \\
 & \frac{b \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x])}{32 a^2 d (b + a \operatorname{Csc} [c + d x])} - \\
 & \frac{\operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^2 \operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x])}{128 a d (b + a \operatorname{Csc} [c + d x])} + \\
 & \left((-5 a^2 - 2 b^2) \operatorname{Csc} [c + d x] \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] \right] (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad (32 a^3 d (b + a \operatorname{Csc} [c + d x])) + \\
 & \left((5 a^2 + 2 b^2) \operatorname{Csc} [c + d x] \operatorname{Log} \left[\operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad (32 a^3 d (b + a \operatorname{Csc} [c + d x])) + \\
 & \frac{\operatorname{Csc} [c + d x] \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 (a + b \operatorname{Sin} [c + d x])}{128 a d (b + a \operatorname{Csc} [c + d x])} + (\operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x])) / \\
 & \quad \left(192 (a + b) d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
 & \left(\operatorname{Csc} [c + d x] \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad \left(96 (a + b) d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^3 \right) - \\
 & \left(\operatorname{Csc} [c + d x] \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad \left(96 (a - b) d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
 & \left(\operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad \left(192 (a - b) d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
 & \left(\operatorname{Csc} [c + d x] \left(-13 a \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] + 16 b \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad \left(96 (a - b)^2 d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \right) + \\
 & \left(\operatorname{Csc} [c + d x] \left(13 a \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] + 16 b \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) (a + b \operatorname{Sin} [c + d x]) \right) / \\
 & \quad \left(96 (a + b)^2 d (b + a \operatorname{Csc} [c + d x]) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \right) - \\
 & \left. \frac{b \operatorname{Csc} [c + d x] (a + b \operatorname{Sin} [c + d x]) \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{32 a^2 d (b + a \operatorname{Csc} [c + d x])} \right)
 \end{aligned}$$

Problem 1359: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sin [c+d x]^3 \tan [c+d x]^5}{a+b \sin [c+d x]} d x$$

Optimal (type 3, 240 leaves, 6 steps):

$$\begin{aligned} & -\frac{(35 a^2+57 a b+24 b^2) \operatorname{Log}[1-\sin [c+d x]]}{16(a+b)^3 d}+\frac{(35 a^2-57 a b+24 b^2) \operatorname{Log}[1+\sin [c+d x]]}{16(a-b)^3 d}- \\ & \frac{a^8 \operatorname{Log}[a+b \sin [c+d x]]}{b^3\left(a^2-b^2\right)^3 d}+\frac{a \sin [c+d x]}{b^2 d}-\frac{\sin [c+d x]^2}{2 b d}-\frac{\operatorname{Sec}[c+d x]^4(b-a \sin [c+d x])}{4\left(a^2-b^2\right) d}+ \\ & \frac{\operatorname{Sec}[c+d x]^2\left(4 b\left(4 a^2-3 b^2\right)-a\left(13 a^2-9 b^2\right) \sin [c+d x]\right)}{8\left(a^2-b^2\right)^2 d} \end{aligned}$$

Result (type 3, 542 leaves):

$$\begin{aligned} & \frac{2 i\left(6 a^4 b-8 a^2 b^3+3 b^5\right)(c+d x)}{(a-b)^3(a+b)^3 d}+\frac{1}{8(a+b)^3 d} i\left(-35 a^2-57 a b-24 b^2\right) \operatorname{ArcTan}\left[\right. \\ & \left. \operatorname{Csc}[c+d x]\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)\right]+ \\ & \frac{1}{8(a-b)^3 d} i\left(35 a^2-57 a b+24 b^2\right) \operatorname{ArcTan}\left[\right. \\ & \left. \operatorname{Csc}[c+d x]\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)\right]+ \\ & \frac{\cos [2(c+d x)]}{4 b d}+\frac{\left(-35 a^2-57 a b-24 b^2\right) \operatorname{Log}\left[\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2\right]}{16(a+b)^3 d}+ \\ & \frac{\left(35 a^2-57 a b+24 b^2\right) \operatorname{Log}\left[\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2\right]}{16(a-b)^3 d}- \\ & \frac{a^8 \operatorname{Log}[a+b \sin [c+d x]]}{b^3\left(a^2-b^2\right)^3 d}+\frac{1}{16(a+b) d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}+ \\ & \frac{-13 a-11 b}{16(a+b)^2 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}- \\ & \frac{1}{16(a-b) d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}+ \\ & \frac{13 a-11 b}{16(a-b)^2 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}+\frac{a \sin [c+d x]}{b^2 d} \end{aligned}$$

Problem 1360: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int \frac{\sin [c+d x]^2 \tan [c+d x]^5}{a+b \sin [c+d x]} d x$$

Optimal (type 3, 221 leaves, 6 steps):

$$\begin{aligned} & -\frac{(24 a^2+37 a b+15 b^2) \operatorname{Log}[1-\sin [c+d x]]}{16(a+b)^3 d}-\frac{(24 a^2-37 a b+15 b^2) \operatorname{Log}[1+\sin [c+d x]]}{16(a-b)^3 d} \\ & +\frac{a^7 \operatorname{Log}[a+b \sin [c+d x]]}{b^2\left(a^2-b^2\right)^3 d}-\frac{\sin [c+d x]}{b d}+\frac{\sec [c+d x]^4(a-b \sin [c+d x])}{4\left(a^2-b^2\right) d}- \\ & \frac{\sec [c+d x]^2\left(4 a\left(3 a^2-2 b^2\right)-b\left(13 a^2-9 b^2\right) \sin [c+d x]\right)}{8\left(a^2-b^2\right)^2 d} \end{aligned}$$

Result (type 3, 522 leaves):

$$\begin{aligned} & -\frac{2 i\left(3 a^5-3 a^3 b^2+a b^4\right)(c+d x)}{(a-b)^3(a+b)^3 d}+\frac{1}{8(a+b)^3 d} i\left(-24 a^2-37 a b-15 b^2\right) \operatorname{ArcTan}\left[\right. \\ & \left.\operatorname{Csc}[c+d x]\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)\right]+ \\ & \frac{1}{8(a-b)^3 d} i\left(-24 a^2+37 a b-15 b^2\right) \operatorname{ArcTan}\left[\right. \\ & \left.\operatorname{Csc}[c+d x]\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)\right]+ \\ & \frac{\left(-24 a^2-37 a b-15 b^2\right) \operatorname{Log}\left[\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2\right]}{16(a+b)^3 d}+ \\ & \frac{\left(-24 a^2+37 a b-15 b^2\right) \operatorname{Log}\left[\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2\right]}{16(a-b)^3 d}+ \\ & \frac{a^7 \operatorname{Log}[a+b \sin [c+d x]]}{b^2\left(a^2-b^2\right)^3 d}+\frac{1}{16(a+b) d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}+ \\ & \frac{-11 a-9 b}{16(a+b)^2 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}+ \\ & \frac{1}{16(a-b) d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}+ \\ & \frac{-11 a+9 b}{16(a-b)^2 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}-\frac{\sin [c+d x]}{b d} \end{aligned}$$

Problem 1361: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sin [c+d x] \tan [c+d x]^5}{a+b \sin [c+d x]} dx$$

Optimal (type 3, 208 leaves, 6 steps):

$$\begin{aligned} & - \frac{(15 a^2 + 21 a b + 8 b^2) \operatorname{Log}[1 - \sin [c+d x]]}{16 (a+b)^3 d} + \\ & \frac{(15 a^2 - 21 a b + 8 b^2) \operatorname{Log}[1 + \sin [c+d x]]}{16 (a-b)^3 d} - \frac{a^6 \operatorname{Log}[a+b \sin [c+d x]]}{b (a^2 - b^2)^3 d} - \\ & \frac{\operatorname{Sec}[c+d x]^4 (b - a \sin [c+d x])}{4 (a^2 - b^2) d} + \frac{\operatorname{Sec}[c+d x]^2 (4 b (3 a^2 - 2 b^2) - a (9 a^2 - 5 b^2) \sin [c+d x])}{8 (a^2 - b^2)^2 d} \end{aligned}$$

Result (type 3, 508 leaves):

$$\begin{aligned} & 2 i \frac{(3 a^4 b - 3 a^2 b^3 + b^5) (c+d x)}{(a-b)^3 (a+b)^3 d} + \frac{1}{8 (a+b)^3 d} \\ & i (-15 a^2 - 21 a b - 8 b^2) \operatorname{ArcTan}[\operatorname{Csc}[c+d x] \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)] \\ & \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) + \frac{1}{8 (a-b)^3 d} i (15 a^2 - 21 a b + 8 b^2) \operatorname{ArcTan}[\operatorname{Csc}[c+d x] \\ & \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right) \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)] + \\ & \frac{(-15 a^2 - 21 a b - 8 b^2) \operatorname{Log} \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right]}{16 (a+b)^3 d} + \\ & \frac{(15 a^2 - 21 a b + 8 b^2) \operatorname{Log} \left[\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \right]}{16 (a-b)^3 d} - \\ & \frac{a^6 \operatorname{Log}[a+b \sin [c+d x]]}{b (a^2 - b^2)^3 d} + \frac{1}{16 (a+b) d \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^4} + \\ & \frac{-9 a - 7 b}{16 (a+b)^2 d \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2} - \\ & \frac{1}{16 (a-b) d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^4} + \\ & \frac{9 a - 7 b}{16 (a-b)^2 d \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2} \end{aligned}$$

Problem 1367: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + dx] \text{Sec}[c + dx]^5}{a + b \text{Sin}[c + dx]} dx$$

Optimal (type 3, 233 leaves, 4 steps):

$$\begin{aligned} & - \frac{(8a^2 + 21ab + 15b^2) \text{Log}[1 - \text{Sin}[c + dx]]}{16(a+b)^3 d} + \frac{\text{Log}[\text{Sin}[c + dx]]}{ad} - \\ & \frac{(8a^2 - 21ab + 15b^2) \text{Log}[1 + \text{Sin}[c + dx]]}{16(a-b)^3 d} + \frac{b^6 \text{Log}[a + b \text{Sin}[c + dx]]}{a(a^2 - b^2)^3 d} + \\ & \frac{1}{16(a+b)d(1 - \text{Sin}[c + dx])^2} + \frac{5a + 7b}{16(a+b)^2 d(1 - \text{Sin}[c + dx])} + \\ & \frac{1}{16(a-b)d(1 + \text{Sin}[c + dx])^2} + \frac{5a - 7b}{16(a-b)^2 d(1 + \text{Sin}[c + dx])} \end{aligned}$$

Result (type 3, 521 leaves):

$$\begin{aligned} & - \frac{2i(a^5 - 3a^3b^2 + 3ab^4)(c + dx)}{(a-b)^3(a+b)^3d} + \frac{1}{8(a+b)^3d} i(-8a^2 - 21ab - 15b^2) \text{ArcTan}\left[\right. \\ & \quad \left. \text{Csc}[c + dx] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \right] + \\ & \frac{1}{8(a-b)^3d} i(-8a^2 + 21ab - 15b^2) \text{ArcTan}\left[\right. \\ & \quad \left. \text{Csc}[c + dx] \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \right] + \\ & \frac{(-8a^2 - 21ab - 15b^2) \text{Log}\left[\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2\right]}{16(a+b)^3d} + \\ & \frac{(-8a^2 + 21ab - 15b^2) \text{Log}\left[\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2\right]}{16(a-b)^3d} + \\ & \frac{\text{Log}[\text{Sin}[c + dx]]}{ad} + \frac{b^6 \text{Log}[a + b \text{Sin}[c + dx]]}{a(a^2 - b^2)^3d} + \\ & \frac{1}{16(a+b)d\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\ & \frac{5a + 7b}{16(a+b)^2d\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\ & \frac{1}{16(a-b)d\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\ & \frac{5a - 7b}{16(a-b)^2d\left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} \end{aligned}$$

Problem 1368: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + d x]^2 \text{Sec}[c + d x]^5}{a + b \text{Sin}[c + d x]} dx$$

Optimal (type 3, 250 leaves, 4 steps):

$$\begin{aligned} & -\frac{\text{Csc}[c + d x]}{a d} - \frac{(15 a^2 + 37 a b + 24 b^2) \text{Log}[1 - \text{Sin}[c + d x]]}{16 (a + b)^3 d} - \frac{b \text{Log}[\text{Sin}[c + d x]]}{a^2 d} + \\ & \frac{(15 a^2 - 37 a b + 24 b^2) \text{Log}[1 + \text{Sin}[c + d x]]}{16 (a - b)^3 d} - \frac{b^7 \text{Log}[a + b \text{Sin}[c + d x]]}{a^2 (a^2 - b^2)^3 d} + \\ & \frac{1}{16 (a + b) d (1 - \text{Sin}[c + d x])^2} + \frac{7 a + 9 b}{16 (a + b)^2 d (1 - \text{Sin}[c + d x])} - \\ & \frac{1}{16 (a - b) d (1 + \text{Sin}[c + d x])^2} - \frac{7 a - 9 b}{16 (a - b)^2 d (1 + \text{Sin}[c + d x])} \end{aligned}$$

Result (type 3, 565 leaves):

$$\begin{aligned}
& \frac{2 \operatorname{Im} \left(a^4 b - 3 a^2 b^3 + 3 b^5 \right) (c + d x)}{(a - b)^3 (a + b)^3 d} + \frac{1}{8 (a + b)^3 d} \operatorname{Im} \left(-15 a^2 - 37 a b - 24 b^2 \right) \operatorname{ArcTan} \left[\right. \\
& \quad \left. \operatorname{Csc} [c + d x] \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \right] + \\
& \frac{1}{8 (a - b)^3 d} \operatorname{Im} \left(15 a^2 - 37 a b + 24 b^2 \right) \operatorname{ArcTan} \left[\right. \\
& \quad \left. \operatorname{Csc} [c + d x] \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \right] - \\
& \frac{\operatorname{Cot} \left[\frac{1}{2} (c + d x) \right]}{2 a d} + \frac{(-15 a^2 - 37 a b - 24 b^2) \operatorname{Log} \left[\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2 \right]}{16 (a + b)^3 d} + \\
& \frac{(15 a^2 - 37 a b + 24 b^2) \operatorname{Log} \left[\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2 \right]}{16 (a - b)^3 d} - \\
& \frac{b \operatorname{Log} [\operatorname{Sin} [c + d x]]}{a^2 d} - \frac{b^7 \operatorname{Log} [a + b \operatorname{Sin} [c + d x]]}{a^2 (a^2 - b^2)^3 d} + \\
& \frac{1}{16 (a + b) d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\
& \frac{7 a + 9 b}{16 (a + b)^2 d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} - \\
& \frac{1}{16 (a - b) d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\
& \frac{-7 a + 9 b}{16 (a - b)^2 d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} - \frac{\operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{2 a d}
\end{aligned}$$

Problem 1369: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc} [c + d x]^3 \operatorname{Sec} [c + d x]^5}{a + b \operatorname{Sin} [c + d x]} dx$$

Optimal (type 3, 274 leaves, 4 steps):

$$\frac{b \operatorname{Csc}[c+dx]}{a^2 d} - \frac{\operatorname{Csc}[c+dx]^2}{2 a d} - \frac{(24 a^2 + 57 a b + 35 b^2) \operatorname{Log}[1 - \operatorname{Sin}[c+dx]]}{16 (a+b)^3 d} +$$

$$\frac{(3 a^2 + b^2) \operatorname{Log}[\operatorname{Sin}[c+dx]]}{a^3 d} - \frac{(24 a^2 - 57 a b + 35 b^2) \operatorname{Log}[1 + \operatorname{Sin}[c+dx]]}{16 (a-b)^3 d} +$$

$$\frac{b^8 \operatorname{Log}[a+b \operatorname{Sin}[c+dx]]}{a^3 (a^2 - b^2)^3 d} + \frac{1}{16 (a+b) d (1 - \operatorname{Sin}[c+dx])^2} + \frac{9 a + 11 b}{16 (a+b)^2 d (1 - \operatorname{Sin}[c+dx])} +$$

$$\frac{1}{16 (a-b) d (1 + \operatorname{Sin}[c+dx])^2} + \frac{9 a - 11 b}{16 (a-b)^2 d (1 + \operatorname{Sin}[c+dx])}$$

Result (type 3, 618 leaves):

$$- \frac{2 i (3 a^5 - 8 a^3 b^2 + 6 a b^4) (c+dx)}{(a-b)^3 (a+b)^3 d} + \frac{1}{8 (a+b)^3 d} i (-24 a^2 - 57 a b - 35 b^2) \operatorname{ArcTan}\left[\right.$$

$$\left. \operatorname{Csc}[c+dx] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right] +$$

$$\frac{1}{8 (a-b)^3 d} i (-24 a^2 + 57 a b - 35 b^2) \operatorname{ArcTan}\left[\operatorname{Csc}[c+dx] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right]$$

$$\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right] + \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{2 a^2 d} - \frac{\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{8 a d} +$$

$$\frac{(-24 a^2 - 57 a b - 35 b^2) \operatorname{Log}\left[\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2\right]}{16 (a+b)^3 d} +$$

$$\frac{(-24 a^2 + 57 a b - 35 b^2) \operatorname{Log}\left[\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2\right]}{16 (a-b)^3 d} +$$

$$\frac{(3 a^2 + b^2) \operatorname{Log}[\operatorname{Sin}[c+dx]]}{a^3 d} + \frac{b^8 \operatorname{Log}[a+b \operatorname{Sin}[c+dx]]}{a^3 (a^2 - b^2)^3 d} -$$

$$\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{8 a d} + \frac{1}{16 (a+b) d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4} +$$

$$\frac{9 a + 11 b}{16 (a+b)^2 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2} +$$

$$\frac{1}{16 (a-b) d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4} +$$

$$\frac{9 a - 11 b}{16 (a-b)^2 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2} + \frac{b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2 a^2 d}$$

Problem 1370: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e + f x]} \sin[e + f x]^4}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 500 leaves, 21 steps):

$$\frac{a^4 \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} (-a^2 + b^2)^{1/4} f} - \frac{a^4 \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} (-a^2 + b^2)^{1/4} f} -$$

$$\frac{2 a^2 (g \cos[e + f x])^{3/2}}{3 b^3 f g} - \frac{2 (g \cos[e + f x])^{3/2}}{3 b f g} + \frac{2 (g \cos[e + f x])^{7/2}}{7 b f g^3} -$$

$$\frac{2 a^3 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2} (e + f x), 2\right]}{b^4 f \sqrt{\cos[e + f x]}} - \frac{4 a \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2} (e + f x), 2\right]}{5 b^2 f \sqrt{\cos[e + f x]}} +$$

$$\frac{a^5 g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^5 (b - \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} +$$

$$\frac{a^5 g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^5 (b + \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} + \frac{2 a (g \cos[e + f x])^{3/2} \sin[e + f x]}{5 b^2 f g}$$

Result (type 6, 1210 leaves):

$$-\frac{1}{5 b^3 f \sqrt{\cos[e + f x]}}$$

$$a \sqrt{g \cos[e + f x]} \left(\frac{1}{6 \sqrt{1 - \cos[e + f x]^2} (a + b \sin[e + f x])} - a b \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right.$$

$$\left. - \left(\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right.$$

$$\left. \left. \left. \cos[e + f x]^{3/2} \right) / \left(\sqrt{1 - \cos[e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right.$$

$$\left. \left. \left. - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) \right) -$$

$$\left((3 + 3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right.$$

$$\begin{aligned}
 & 1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} - \text{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \\
 & \left. \sqrt{\cos[e+fx]} + ib\cos[e+fx]\right] + \text{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \\
 & \left. \sqrt{\cos[e+fx]} + ib\cos[e+fx]\right] \Big/ \left(\sqrt{b}(-a^2+b^2)^{1/4}\right) \sin[e+fx] - \\
 & \frac{1}{(1-\cos[e+fx]^2)(a+b\sin[e+fx])} 2(5a^2+2b^2)\left(a+b\sqrt{1-\cos[e+fx]^2}\right) \\
 & \left(\left(7b(a^2-b^2)\text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\right.\right. \\
 & \left.\left.\cos[e+fx]^{3/2}\sqrt{1-\cos[e+fx]^2}\right)\right) \Big/ \\
 & \left(3\left(-7(a^2-b^2)\text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + 2\right.\right. \\
 & \left.\left(2b^2\text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + \right.\right. \\
 & \left.\left.(a^2-b^2)\text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\right)\right) \\
 & \left.\cos[e+fx]^2\right)(a^2+b^2(-1+\cos[e+fx]^2)) \Big) + \\
 & \left(a\left(-2\text{ArcTan}\left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] + 2\text{ArcTan}\left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right]\right) + \right. \\
 & \left.\text{Log}\left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[e+fx]} + b\cos[e+fx]\right] - \right. \\
 & \left.\text{Log}\left[\sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[e+fx]} + \right.\right. \\
 & \left.\left. b\cos[e+fx]\right]\right) \Big/ \left(4\sqrt{2}b^{3/2}(a^2-b^2)^{1/4}\right) \sin[e+fx]^2 \Big) + \\
 & \frac{\sqrt{g\cos[e+fx]}\left(-\frac{(28a^2+19b^2)\cos[e+fx]}{42b^3} + \frac{\cos[3(e+fx)]}{14b} + \frac{a\sin[2(e+fx)]}{5b^2}\right)}{f}
 \end{aligned}$$

Problem 1371: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g\cos[e+fx]}\sin[e+fx]^3}{a+b\sin[e+fx]} dx$$

Optimal (type 4, 448 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{a^3 \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} (-a^2+b^2)^{1/4} f} + \frac{a^3 \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} (-a^2+b^2)^{1/4} f} + \frac{2 a (g \cos[e+fx])^{3/2}}{3 b^2 f g} + \\
 & \frac{2 a^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2} (e+fx), 2\right]}{b^3 f \sqrt{\cos[e+fx]}} + \frac{4 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2} (e+fx), 2\right]}{5 b f \sqrt{\cos[e+fx]}} - \\
 & \frac{a^4 g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^4 (b-\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} - \\
 & \frac{a^4 g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^4 (b+\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} - \frac{2 (g \cos[e+fx])^{3/2} \sin[e+fx]}{5 b f g}
 \end{aligned}$$

Result(type 6, 1183 leaves):

$$\begin{aligned}
 & \frac{1}{5 b^2 f \sqrt{\cos[e+fx]}} \\
 & \sqrt{g \cos[e+fx]} \left(\frac{1}{6 \sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} a b \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \right. \\
 & \left. - \left(\left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \cos[e+fx]^{3/2} \right) \right) / \right. \right. \\
 & \left. \left(\sqrt{1-\cos[e+fx]^2} \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 \right) \right) \right) - \\
 & \left((3+3i) \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \left. \right) \sin[e+fx] - \\
 & \frac{1}{(1-\cos[e+fx]^2) (a+b \sin[e+fx])} 2 (5 a^2+2 b^2) \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\cos [e+f x]^{3/2} \sqrt{1-\cos [e+f x]^2} \right) / \right. \\
 & \left(3 \left(-7 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \quad 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [e+f x]^2 \left(a^2+b^2 \left(-1+\cos [e+f x]^2 \right) \right) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2 \right)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2 \right)^{1/4}} \right] \right) + \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b} \left(a^2-b^2 \right)^{1/4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right]- \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b} \left(a^2-b^2 \right)^{1/4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} b^{3/2} \left(a^2-b^2 \right)^{1/4} \right) \left. \sin [e+f x]^2 \right) + \\
 & \frac{\sqrt{g \cos [e+f x]} \left(\frac{2 a \cos [e+f x]}{3 b^2}-\frac{\sin [2(e+f x)]}{5 b} \right)}{f}
 \end{aligned}$$

Problem 1372: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{g \cos [e+f x]} \sin [e+f x]^2}{a+b \sin [e+f x]} dx$$

Optimal (type 4, 369 leaves, 15 steps):

$$\begin{aligned}
 & \frac{a^2 \sqrt{g} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{g}} \right]}{b^{5/2} \left(-a^2+b^2 \right)^{1/4} f} - \frac{a^2 \sqrt{g} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{g}} \right]}{b^{5/2} \left(-a^2+b^2 \right)^{1/4} f} - \\
 & \frac{2 \left(g \cos [e+f x] \right)^{3/2}}{3 b f g} - \frac{2 a \sqrt{g \cos [e+f x]} \operatorname{EllipticE} \left[\frac{1}{2} (e+f x), 2 \right]}{b^2 f \sqrt{\cos [e+f x]}} + \\
 & \frac{a^3 g \sqrt{\cos [e+f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (e+f x), 2 \right]}{b^3 \left(b-\sqrt{-a^2+b^2} \right) f \sqrt{g \cos [e+f x]}} + \\
 & \frac{a^3 g \sqrt{\cos [e+f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (e+f x), 2 \right]}{b^3 \left(b+\sqrt{-a^2+b^2} \right) f \sqrt{g \cos [e+f x]}}
 \end{aligned}$$

Result (type 6, 608 leaves):

$$\begin{aligned}
& - \frac{2 \operatorname{Cos}[e + f x] \sqrt{g \operatorname{Cos}[e + f x]}}{3 b f} + \\
& \frac{1}{b f \sqrt{\operatorname{Cos}[e + f x]} (1 - \operatorname{Cos}[e + f x]^2) (a + b \operatorname{Sin}[e + f x])} 2 a \sqrt{g \operatorname{Cos}[e + f x]} \\
& \left((a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2}) \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \operatorname{Cos}[e + f x]^{3/2} \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \right) / \\
& \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \quad \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \right) \right) \\
& \quad \left. \operatorname{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2)) \Big) + \\
& \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] \right) + \right. \\
& \quad \left. \operatorname{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x]\right] - \right. \\
& \quad \left. \operatorname{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x]\right] \right) \Big) / \\
& \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \operatorname{Sin}[e + f x]^2
\end{aligned}$$

Problem 1373: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{g \operatorname{Cos}[e + f x]} \operatorname{Sin}[e + f x]}{a + b \operatorname{Sin}[e + f x]} dx$$

Optimal (type 4, 341 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{a \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{1/4} f} + \frac{a \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{1/4} f} + \\
 & \frac{2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b f \sqrt{\cos[e+fx]}} - \\
 & \frac{a^2 g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (b-\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} - \\
 & \frac{a^2 g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (b+\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result(type 6, 575 leaves):

$$\begin{aligned}
 & - \frac{1}{f \sqrt{\cos[e+fx]} (1-\cos[e+fx]^2) (a+b \sin[e+fx])} \\
 & \frac{2 \sqrt{g \cos[e+fx]} \left(a + b \sqrt{1-\cos[e+fx]^2} \right)}{\left(\left(7 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \\
 & \left. \left. \cos[e+fx]^{3/2} \sqrt{1-\cos[e+fx]^2} \right) \right) /} \\
 & \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) + \right. \\
 & \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) + \right. \\
 & \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \\
 & \left. \cos[e+fx]^2 \right) (a^2+b^2 (-1+\cos[e+fx]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] \right) + \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] - \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] \right) \Big) / \\
 & \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin[e+fx]^2
 \end{aligned}$$

Problem 1374: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{g \cos[e + f x]} \operatorname{Csc}[e + f x]}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 355 leaves, 16 steps):

$$\frac{\sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a f} - \frac{\sqrt{b} \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{1/4} f} - \frac{\sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a f} +$$

$$\frac{\sqrt{b} \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{1/4} f} - \frac{g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{(b - \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}}$$

$$\frac{g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{(b + \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}}$$

Result (type 6, 700 leaves):

$$-\frac{1}{f \sqrt{\cos[e + f x]} (1 - \cos[e + f x]^2) (b + a \operatorname{Csc}[e + f x])}$$

$$2 \sqrt{g \cos[e + f x]} (-1 + \cos[e + f x]^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \operatorname{Csc}[e + f x]$$

$$\left(\left(7 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \cos[e + f x]^{3/2} \right) / \right.$$

$$\left(3 \sqrt{1 - \cos[e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - \right. \right.$$

$$2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + \right.$$

$$\left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \right)$$

$$\cos[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \left. \right) +$$

$$\frac{1}{8 a (a^2 - b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] - \right.$$

$$2 \sqrt{2} \sqrt{b} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{1/4} \operatorname{ArcTan}\left[\sqrt{\cos[e + f x]}\right] +$$

$$2 (a^2 - b^2)^{1/4} \operatorname{Log}\left[1 - \sqrt{\cos[e + f x]}\right] - 2 (a^2 - b^2)^{1/4} \operatorname{Log}\left[1 + \sqrt{\cos[e + f x]}\right] -$$

$$\sqrt{2} \sqrt{b} \operatorname{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] +$$

$$\left. \left. \sqrt{2} \sqrt{b} \operatorname{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] \right) \right)$$

Problem 1375: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e+fx]} \operatorname{Csc}[e+fx]^2}{a+b \sin[e+fx]} dx$$

Optimal (type 4, 433 leaves, 19 steps):

$$\begin{aligned} & -\frac{b \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a^2 f} + \frac{b^{3/2} \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2+b^2)^{1/4} f} + \\ & \frac{b \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a^2 f} - \frac{b^{3/2} \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2+b^2)^{1/4} f} - \\ & \frac{(g \cos[e+fx])^{3/2} \operatorname{Csc}[e+fx]}{a f g} - \frac{\sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{a f \sqrt{\cos[e+fx]}} + \\ & \frac{b g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{-2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{a (b-\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} + \\ & \frac{b g \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{-2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{a (b+\sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} \end{aligned}$$

Result (type 6, 2385 leaves):

$$\begin{aligned} & -\frac{\sqrt{g \cos[e+fx]} \operatorname{Cot}[e+fx]}{a f} + \\ & \frac{1}{4 a f \sqrt{\cos[e+fx]}} \sqrt{g \cos[e+fx]} \left(-\frac{1}{6 \sqrt{1-\cos[e+fx]^2} (b+a \operatorname{Csc}[e+fx])} \right. \\ & \left. a (a+b \sqrt{1-\cos[e+fx]^2}) \left(-\left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \cos[e+fx]^{3/2} \right) / \left(\sqrt{1-\cos[e+fx]^2} \right. \right. \right. \\ & \left. \left. \left. \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - \right. \right. \right. \\ & \left. \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + \right. \right. \right. \\ & \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \right) \right) \right) - \\ & \left. \cos[e+fx]^2 \right) (a^2+b^2 (-1+\cos[e+fx]^2)) \left. \right) \left. \right) - \end{aligned}$$

$$\begin{aligned}
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + ib \cos[e+fx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b} \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + ib \cos[e+fx] \right] \right) \right) / \left(\sqrt{b}(-a^2+b^2)^{1/4} \right) - \\
 & \frac{1}{(1 - \cos[e+fx]^2)(-1 + 2 \cos[e+fx]^2)(b + a \operatorname{Csc}[e+fx])} \\
 & 2 \\
 & b \\
 & (-1 + \cos[e+fx]^2) \\
 & (a + b \sqrt{1 - \cos[e+fx]^2}) \\
 & \cos[2(e+fx)] \\
 & \operatorname{Csc}[e+fx] \\
 & \left(\left((a^2 - b^2)^{3/4} (-2a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2}(a^2 - b^2)^{1/4} + 2\sqrt{b}\sqrt{\cos[e+fx]}}{\sqrt{2}(a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \quad \left(2\sqrt{2}ab^{3/2}(-a^2 + b^2) \right) + \\
 & \left((a^2 - b^2)^{3/4} (-2a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2}(a^2 - b^2)^{1/4} + 2\sqrt{b}\sqrt{\cos[e+fx]}}{\sqrt{2}(a^2 - b^2)^{1/4}} \right] \right) / \\
 & \quad \left(2\sqrt{2}ab^{3/2}(-a^2 + b^2) \right) + \frac{\operatorname{ArcTan}[\sqrt{\cos[e+fx]}}{2a} - \\
 & \left(7b(a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \cos[e+fx]^{3/2} \right) / \\
 & \left(3\sqrt{1 - \cos[e+fx]^2} \left(7(a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - 2 \left(2b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 (a^2 + b^2(-1 + \cos[e+fx]^2)) \right) + \\
 & \left(22b(a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos[e+fx]^{7/2} \right) / \left(7\sqrt{1 - \cos[e+fx]^2} \right) \\
 & \left(11(a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \\
 & (a^2+b^2 (-1+\cos [e+f x]^2)) \Big) + \frac{\operatorname{Log} [1-\sqrt{\cos [e+f x]}]}{4 a} - \\
 & \frac{\operatorname{Log} [1+\sqrt{\cos [e+f x]}]}{4 a} + \left((a^2-b^2)^{3/4} (-2 a^2+b^2) \operatorname{Log} [\sqrt{a^2-b^2} - \right. \\
 & \quad \left. \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x] \right] \Big) / \left(4 \sqrt{2} a b^{3/2} (-a^2+b^2) \right) - \\
 & \left((a^2-b^2)^{3/4} (-2 a^2+b^2) \operatorname{Log} [\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + \right. \\
 & \quad \left. b \cos [e+f x] \right] \Big) / \left(4 \sqrt{2} a b^{3/2} (-a^2+b^2) \right) \Big) + \\
 & \frac{1}{(1-\cos [e+f x]^2) (b+a \operatorname{Csc} [e+f x])} 10 b (-1+\cos [e+f x]^2) \\
 & \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \operatorname{Csc} [e+f x] \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \cos [e+f x]^{3/2} \right) / \right. \\
 & \left(3 \sqrt{1-\cos [e+f x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \Big) \Big) + \\
 & \frac{1}{8 a (a^2-b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] - 2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + 4 (a^2-b^2)^{1/4} \operatorname{ArcTan} [\sqrt{\cos [e+f x]}] + \right. \\
 & \quad 2 (a^2-b^2)^{1/4} \operatorname{Log} [1-\sqrt{\cos [e+f x]}] - 2 (a^2-b^2)^{1/4} \operatorname{Log} [1+\sqrt{\cos [e+f x]}] - \\
 & \quad \left. \sqrt{2} \sqrt{b} \operatorname{Log} [\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] + \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} \operatorname{Log} [\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] \right) \right) \Big) \Big)
 \end{aligned}$$

Problem 1376: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e + f x]} \operatorname{Csc}[e + f x]^3}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 544 leaves, 25 steps):

$$\frac{\sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{4 a f} + \frac{b^2 \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^3 f} -$$

$$\frac{b^{5/2} \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^3 (-a^2 + b^2)^{1/4} f} - \frac{\sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{4 a f} - \frac{b^2 \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^3 f} +$$

$$\frac{b^{5/2} \sqrt{g} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^3 (-a^2 + b^2)^{1/4} f} + \frac{b (g \cos[e + f x])^{3/2} \operatorname{Csc}[e + f x]}{a^2 f g} -$$

$$\frac{(g \cos[e + f x])^{3/2} \operatorname{Csc}[e + f x]^2}{2 a f g} + \frac{b \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2} (e + f x), 2\right]}{a^2 f \sqrt{\cos[e + f x]}} -$$

$$\frac{b^2 g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{a^2 (b - \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} -$$

$$\frac{b^2 g \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{a^2 (b + \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}}$$

Result (type 6, 2419 leaves):

$$\frac{\sqrt{g \cos[e + f x]} \left(\frac{b \operatorname{Cot}[e + f x]}{a^2} - \frac{\operatorname{Cot}[e + f x] \operatorname{Csc}[e + f x]}{2 a} \right)}{f} -$$

$$\frac{1}{4 a^2 f \sqrt{\cos[e + f x]}} \sqrt{g \cos[e + f x]} \left(- \frac{1}{4 \sqrt{1 - \cos[e + f x]^2} (b + a \operatorname{Csc}[e + f x])} \right.$$

$$a b \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \left(- \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \right.$$

$$\left. \left. \left. \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \cos[e + f x]^{3/2} \right) / \left(\sqrt{1 - \cos[e + f x]^2} \right. \right.$$

$$\left. \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] - \right. \right.$$

$$\left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right.$$

$$\left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \right)$$

$$\left. \left. \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) \right) -$$

$$\left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) - \frac{1}{(1 - \cos[e+fx]^2) (-1 + 2 \cos[e+fx]^2) (b + a \operatorname{Csc}[e+fx])} \frac{2 b^2 (-1 + \cos[e+fx]^2) (a + b \sqrt{1 - \cos[e+fx]^2}) \cos[2(e+fx)] \operatorname{Csc}[e+fx]}{\left(\left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e+fx]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e+fx]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \frac{\operatorname{ArcTan}[\sqrt{\cos[e+fx]}}{2 a} \right) - \left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \cos[e+fx]^{3/2} \right) / \left(3 \sqrt{1 - \cos[e+fx]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 \right) (a^2 + b^2 (-1 + \cos[e+fx]^2)) \right) + \left(22 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \cos[e+fx]^{7/2} \right) / \left(7 \sqrt{1 - \cos[e+fx]^2} \right) - \left(11 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - \right.$$

$$\begin{aligned}
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \\
 & (a^2+b^2 (-1+\cos [e+f x]^2)) \Big) + \frac{\log [1-\sqrt{\cos [e+f x]}]}{4 a} - \\
 & \frac{\log [1+\sqrt{\cos [e+f x]}]}{4 a} + \left((a^2-b^2)^{3/4} (-2 a^2+b^2) \log [\sqrt{a^2-b^2} - \right. \\
 & \quad \left. \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x] \right] \Big) / \left(4 \sqrt{2} a b^{3/2} (-a^2+b^2) \right) - \\
 & \left((a^2-b^2)^{3/4} (-2 a^2+b^2) \log [\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + \right. \\
 & \quad \left. b \cos [e+f x] \right] \Big) / \left(4 \sqrt{2} a b^{3/2} (-a^2+b^2) \right) \Big) - \\
 & \frac{1}{(1-\cos [e+f x]^2) (b+a \operatorname{Csc} [e+f x])} 2 (-a^2-5 b^2) (-1+\cos [e+f x]^2) \\
 & \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \operatorname{Csc} [e+f x] \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \cos [e+f x]^{3/2} \right) / \right. \\
 & \left(3 \sqrt{1-\cos [e+f x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \Big) + \\
 & \frac{1}{8 a (a^2-b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] - 2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + 4 (a^2-b^2)^{1/4} \operatorname{ArcTan} [\sqrt{\cos [e+f x]}] + \right. \\
 & \quad 2 (a^2-b^2)^{1/4} \log [1-\sqrt{\cos [e+f x]}] - 2 (a^2-b^2)^{1/4} \log [1+\sqrt{\cos [e+f x]}] - \\
 & \quad \left. \sqrt{2} \sqrt{b} \log [\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] + \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} \log [\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] \right) \right) \Big)
 \end{aligned}$$

Problem 1377: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{3/2} \sin[e + f x]^3}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 621 leaves, 24 steps):

$$\frac{a^3 (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} f} + \frac{a^3 (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} f} -$$

$$\frac{2 a^3 g \sqrt{g \cos[e + f x]}}{b^4 f} + \frac{2 a (g \cos[e + f x])^{5/2}}{5 b^2 f g} - \frac{2 a^4 g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{b^5 f \sqrt{g \cos[e + f x]}} +$$

$$\frac{2 a^2 g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{3 b^3 f \sqrt{g \cos[e + f x]}} + \frac{4 g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{21 b f \sqrt{g \cos[e + f x]}} +$$

$$\frac{a^4 (a^2 - b^2) g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{b^5 (a^2 - b (b - \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e + f x]}} +$$

$$\frac{a^4 (a^2 - b^2) g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{b^5 (a^2 - b (b + \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e + f x]}} +$$

$$\frac{2 a^2 g \sqrt{g \cos[e + f x]} \sin[e + f x]}{3 b^3 f} +$$

$$\frac{4 g \sqrt{g \cos[e + f x]} \sin[e + f x]}{21 b f} - \frac{2 (g \cos[e + f x])^{5/2} \sin[e + f x]}{7 b f g}$$

Result (type 6, 2191 leaves):

$$-\frac{1}{420 b^3 f \cos[e + f x]^{3/2}} (g \cos[e + f x])^{3/2}$$

$$\left(-\frac{1}{\sqrt{1 - \cos[e + f x]^2} (a + b \sin[e + f x])} 2 (70 a^3 - 19 a b^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right.$$

$$\left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right.$$

$$\left(\sqrt{1 - \cos[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \right. \right. \right.$$

$$\left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right) - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \right. \right. \right.$$

$$\left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right) + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \right. \right.$$

$$\left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right) \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \left. \right) -$$

$$\begin{aligned}
 & \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}} \right] - \right. \\
 & \quad \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}} \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \quad \left. \left. (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \right. \right. \\
 & \quad \left. \left. (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] \right) \operatorname{Sin}[e+fx] + \\
 & \frac{1}{\sqrt{1 - \cos[e+fx]^2} (-1 + 2 \cos[e+fx]^2) (a + b \operatorname{Sin}[e+fx])} \\
 & (210 a^3 - 21 a b^2) \\
 & \left(a + b \sqrt{1 - \cos[e+fx]^2} \right) \cos[2(e+fx)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \quad \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos[e+fx]}}{b} + \right. \\
 & \quad \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \sqrt{\cos[e+fx]} \right) / \right. \\
 & \quad \left(\sqrt{1 - \cos[e+fx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 (a^2 + b^2 (-1 + \cos[e+fx]^2)) \right) - \\
 & \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos[e+fx]^{5/2} \right) / \left(5 \sqrt{1 - \cos[e+fx]^2} \right. \\
 & \quad \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right. \right. \\
 & \quad \left. \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) - \right. \\
 & \left. \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + \right. \right. \right. \\
 & \quad \left. \left. \left. i b \cos [e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \right) \operatorname{Sin}[e + f x] - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (a + b \operatorname{Sin}[e + f x])} 2 (-98 a^2 b - 40 b^3) \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [e + f x]} \sqrt{1 - \cos [e + f x]^2} \right) / \right. \\
 & \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right. \\
 & \quad \left. \left. \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] + \operatorname{Log} \left[\right. \right. \\
 & \quad \left. \left. \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) / \right. \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin}[e + f x]^2 \right) + \frac{1}{f} \\
 & (g \cos [e + f x])^{3/2} \operatorname{Sec}[e + f x] \left(\frac{a \cos [2 (e + f x)]}{5 b^2} + \right. \\
 & \quad \frac{(28 a^2 + 5 b^2) \operatorname{Sin}[e + f x]}{42 b^3} - \\
 & \quad \left. \frac{\operatorname{Sin}[3 (e + f x)]}{14 b} \right)
 \end{aligned}$$

Problem 1378: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos [e + f x])^{3/2} \sin [e + f x]^2}{a + b \sin [e + f x]} dx$$

Optimal (type 4, 514 leaves, 20 steps):

$$\frac{a^2 (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} f} -$$

$$\frac{a^2 (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} f} + \frac{2 a^2 g \sqrt{g \cos [e + f x]}}{b^3 f} - \frac{2 (g \cos [e + f x])^{5/2}}{5 b f g} +$$

$$\frac{2 a^3 g^2 \sqrt{\cos [e + f x]} \operatorname{EllipticF}\left[\frac{1}{2} (e + f x), 2\right]}{b^4 f \sqrt{g \cos [e + f x]}} - \frac{2 a g^2 \sqrt{\cos [e + f x]} \operatorname{EllipticF}\left[\frac{1}{2} (e + f x), 2\right]}{3 b^2 f \sqrt{g \cos [e + f x]}} -$$

$$\frac{a^3 (a^2 - b^2) g^2 \sqrt{\cos [e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^4 (a^2 - b (b - \sqrt{-a^2 + b^2})) f \sqrt{g \cos [e + f x]}} -$$

$$\frac{a^3 (a^2 - b^2) g^2 \sqrt{\cos [e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^4 (a^2 - b (b + \sqrt{-a^2 + b^2})) f \sqrt{g \cos [e + f x]}} -$$

$$\frac{2 a g \sqrt{g \cos [e + f x]} \sin [e + f x]}{3 b^2 f}$$

Result (type 6, 2153 leaves):

$$\frac{(g \cos [e + f x])^{3/2} \operatorname{Sec}[e + f x] \left(-\frac{\cos [2 (e + f x)]}{5 b} - \frac{2 a \sin [e + f x]}{3 b^2}\right)}{f} +$$

$$\frac{1}{60 b^2 f \cos [e + f x]^{3/2}} (g \cos [e + f x])^{3/2}$$

$$\left(-\frac{1}{\sqrt{1 - \cos [e + f x]^2} (a + b \sin [e + f x])} 2 (10 a^2 + 3 b^2) \left(a + b \sqrt{1 - \cos [e + f x]^2}\right) \right.$$

$$\left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos [e + f x]} \right) / \right.$$

$$\left. \left(\sqrt{1 - \cos [e + f x]^2} \right. \right.$$

$$\left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] - 2 \right. \right.$$

$$\begin{aligned}
 & \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \\
 & \quad \left. (a^2+b^2 (-1+\cos [e+f x]^2)) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] \right) + \\
 & \quad \left(\operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] \right) \\
 & \quad \sin [e+f x] + \frac{1}{\sqrt{1-\cos [e+f x]^2} (-1+2 \cos [e+f x]^2) (a+b \sin [e+f x])} \\
 & (30 a^2 - 3 b^2) \left(a + b \sqrt{1-\cos [e+f x]^2} \right) \cos [2 (e+f x)] \\
 & \quad \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} - \right. \\
 & \quad \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} + \frac{4 \sqrt{\cos [e+f x]}}{b} \right) + \\
 & \quad \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \sqrt{\cos [e+f x]} \right) / \\
 & \quad \left(\sqrt{1-\cos [e+f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left. \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \right) - \\
 & \quad \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right. \\
 & \quad \left. \cos [e+f x]^{5/2} \right) / \left(5 \sqrt{1-\cos [e+f x]^2} \right) \\
 & \quad \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - \right. \\
 & \quad \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\text{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \text{Cos}[e + f x]^2 \right) \right. \\
 & \left. \left(a^2 + b^2 (-1 + \text{Cos}[e + f x]^2) \right) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \text{Log}[\sqrt{-a^2 + b^2} - \right. \\
 & \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + i b \text{Cos}[e + f x]] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} - \right. \\
 & \left. \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \text{Log}[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + \right. \right. \\
 & \left. \left. i b \text{Cos}[e + f x]] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \right) \text{Sin}[e + f x] + \\
 & \frac{1}{(1 - \text{Cos}[e + f x]^2) (a + b \text{Sin}[e + f x])} 28 a b \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \\
 & \left(\left(5 b (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\text{Cos}[e + f x]} \sqrt{1 - \text{Cos}[e + f x]^2} \right) / \right. \\
 & \left(\left(-5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left(2 b^2 \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \left. \text{Cos}[e + f x]^2 (a^2 + b^2 (-1 + \text{Cos}[e + f x]^2)) \right) + \\
 & \left(a \left(-2 \text{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. \text{Log}[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]] + \right. \right. \\
 & \left. \left. \text{Log}[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]] \right) \right) / \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \right) \text{Sin}[e + f x]^2 \Bigg)
 \end{aligned}$$

Problem 1379: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \text{Cos}[e + f x])^{3/2} \text{Sin}[e + f x]}{a + b \text{Sin}[e + f x]} dx$$

Optimal (type 4, 426 leaves, 13 steps):

$$\frac{a (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} f} + \frac{a (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} f} -$$

$$\frac{2 (3 a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2} (e+fx), 2\right]}{3 b^3 f \sqrt{g \cos[e+fx]}} +$$

$$\frac{a^2 (a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^3 (a^2 - b (b - \sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}} +$$

$$\frac{a^2 (a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^3 (a^2 - b (b + \sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}} -$$

$$\frac{2 g \sqrt{g \cos[e+fx]} (3 a - b \sin[e+fx])}{3 b^2 f}$$

Result (type 6, 2109 leaves):

$$-\frac{1}{6 b f \cos[e+fx]^{3/2}}$$

$$(g \cos[e+fx])^{3/2} \left(-\frac{1}{\sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} - 2 a (a+b \sqrt{1-\cos[e+fx]^2}) \right.$$

$$\left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \sqrt{\cos[e+fx]} \right) / \right.$$

$$\left(\sqrt{1-\cos[e+fx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 (a^2+b^2 (-1+\cos[e+fx]^2)) \right) \right) -$$

$$\frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - \right.$$

$$2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} - \right.$$

$$\left. \left. \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} + \right. \right. \right.$$

$$\left. \left. \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] \right) \right) \right) \sin[e+fx] +$$

$$\begin{aligned}
 & \frac{1}{\sqrt{1 - \cos[e + f x]^2} (-1 + 2 \cos[e + f x]^2) (a + b \sin[e + f x])} \\
 & 3 a \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \cos[2 (e + f x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+f x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+f x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos[e + f x]}}{b} + \right. \\
 & \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \cos[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) \right) - \right. \\
 & \left. \left(36 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \cos[e + f x]^{5/2} \right) / \left(5 \sqrt{1 - \cos[e + f x]^2} \right. \right. \\
 & \left. \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \right. \\
 & \left. (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]} + i b \cos[e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
 & \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]} + \right. \right. \\
 & \left. \left. i b \cos[e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \left. \right) \sin[e + f x] +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(1 - \cos[e + f x]^2) (a + b \sin[e + f x])} 4 b \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos[e + f x]} \sqrt{1 - \cos[e + f x]^2} \right) / \right. \\
 & \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \right. \\
 & \quad \left. \left. \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x] \right] + \operatorname{Log} \left[\right. \right. \\
 & \quad \left. \left. \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x] \right] \right) \right) / \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[e + f x]^2 \right) + \frac{2 (g \cos[e + f x])^{3/2} \tan[e + f x]}{3 b f}
 \end{aligned}$$

Problem 1380: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos[e + f x])^{3/2} \operatorname{Csc}[e + f x]}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 439 leaves, 21 steps):

$$\begin{aligned}
 & - \frac{g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a f} + \frac{(-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a \sqrt{b} f} - \\
 & \frac{g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a f} + \frac{(-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a \sqrt{b} f} - \\
 & \frac{2 g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{b f \sqrt{g \cos[e+fx]}} + \\
 & \frac{(a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{b \left(a^2 - b \left(b - \sqrt{-a^2 + b^2}\right)\right) f \sqrt{g \cos[e+fx]}} + \\
 & \frac{(a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{b \left(a^2 - b \left(b + \sqrt{-a^2 + b^2}\right)\right) f \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result(type 6, 700 leaves):

$$\begin{aligned}
 & - \frac{1}{f \cos[e+fx]^{3/2} (1 - \cos[e+fx]^2) (b + a \operatorname{Csc}[e+fx])} \\
 & 2 (g \cos[e+fx])^{3/2} (-1 + \cos[e+fx]^2) \left(a + b \sqrt{1 - \cos[e+fx]^2}\right) \operatorname{Csc}[e+fx] \\
 & \left(\left(9 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \cos[e+fx]^{5/2} \right) / \right. \\
 & \left. \left(5 \sqrt{1 - \cos[e+fx]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] - \right. \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \right) \right) \right) \cos[e+fx]^2 \left(a^2 + b^2 (-1 + \cos[e+fx]^2)\right) \right) - \\
 & \frac{1}{8 a \sqrt{b}} \left(2 \sqrt{2} (a^2 - b^2)^{1/4} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2 - b^2)^{1/4}}\right] - \right. \\
 & \left. 2 \sqrt{2} (a^2 - b^2)^{1/4} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2 - b^2)^{1/4}}\right] + 4 \sqrt{b} \operatorname{ArcTan}\left[\sqrt{\cos[e+fx]}\right] - \right. \\
 & \left. 2 \sqrt{b} \operatorname{Log}\left[1 - \sqrt{\cos[e+fx]}\right] + 2 \sqrt{b} \operatorname{Log}\left[1 + \sqrt{\cos[e+fx]}\right] + \right. \\
 & \left. \sqrt{2} (a^2 - b^2)^{1/4} \operatorname{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] - \right. \\
 & \left. \sqrt{2} (a^2 - b^2)^{1/4} \operatorname{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] \right)
 \end{aligned}$$

Problem 1381: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{3/2} \csc[e + f x]^2}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 469 leaves, 24 steps):

$$\begin{aligned} & \frac{b g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f} - \frac{\sqrt{b} (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 f} + \\ & \frac{b g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f} - \frac{\sqrt{b} (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 f} - \\ & \frac{g \sqrt{g \cos[e + f x]} \csc[e + f x]}{a f} + \frac{g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{a f \sqrt{g \cos[e + f x]}} - \\ & \frac{(a^2 - b^2) g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{-2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a \left(a^2 - b \left(b - \sqrt{-a^2 + b^2}\right)\right) f \sqrt{g \cos[e + f x]}} - \\ & \frac{(a^2 - b^2) g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a \left(a^2 - b \left(b + \sqrt{-a^2 + b^2}\right)\right) f \sqrt{g \cos[e + f x]}} \end{aligned}$$

Result (type 6, 2381 leaves):

$$\begin{aligned} & -\frac{1}{4 a f \cos[e + f x]^{3/2}} \\ & (g \cos[e + f x])^{3/2} \left(-\frac{1}{\sqrt{1 - \cos[e + f x]^2} (b + a \csc[e + f x])} 4 a \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \\ & \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right. \\ & \left(\sqrt{1 - \cos[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \\ & \left. \left. \left. + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) - \\ & \left. \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}}\right] - \right. \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] + \\
 & \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] - \\
 & \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] \Bigg) - \\
 & \frac{1}{(1-\cos [e+f x]^2) (-1+2 \cos [e+f x]^2) (b+a \operatorname{Csc} [e+f x])} \\
 & b (-1+\cos [e+f x]^2) \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \operatorname{Cos} [2(e+f x)] \operatorname{Csc} [e+f x] \\
 & \left(\left((a^2-b^2)^{1/4} (-2 a^2+b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2-b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e+f x]}}{\sqrt{2} (a^2-b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2+b^2)) + \right. \\
 & \left. \left((a^2-b^2)^{1/4} (-2 a^2+b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2-b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e+f x]}}{\sqrt{2} (a^2-b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2+b^2)) - \frac{\operatorname{ArcTan} [\sqrt{\cos [e+f x]}}{a} \right. \\
 & \left. \left(10 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \sqrt{\cos [e+f x]} \right) / \right. \\
 & \left. \left(\sqrt{1-\cos [e+f x]^2} \left(5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left. \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \Bigg) + \\
 & \left(36 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \cos [e+f x]^{5/2} \right) / \\
 & \left(5 \sqrt{1-\cos [e+f x]^2} \left(9 (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left. \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \Bigg) + \\
 & \frac{\operatorname{Log} [1-\sqrt{\cos [e+f x]}]}{2 a} - \frac{\operatorname{Log} [1+\sqrt{\cos [e+f x]}]}{2 a} - \left((a^2-b^2)^{1/4} (-2 a^2+b^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{\text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right]}{\left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2)\right) + \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right]\right)} \right) - \right. \\
 & \frac{1}{(1 - \text{Cos}[e + f x]^2) (b + a \text{Csc}[e + f x])} 6 b (-1 + \text{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \\
 & \text{Csc}[e + f x] \\
 & \left(\left(5 b (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\text{Cos}[e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \text{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \text{Cos}[e + f x]^2 \left. \left. \left. \left(a^2 + b^2 (-1 + \text{Cos}[e + f x]^2) \right) \right) \right) - \right. \\
 & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 2 \sqrt{2} b^{3/2} \right. \\
 & \left. \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{3/4} \text{ArcTan}\left[\sqrt{\text{Cos}[e + f x]}\right] - \right. \\
 & 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 - \sqrt{\text{Cos}[e + f x]}\right] + 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 + \sqrt{\text{Cos}[e + f x]}\right] - \\
 & \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] + \\
 & \left. \left. \left. \left. \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] \right) \right) \right) \right) - \\
 & \frac{(g \text{Cos}[e + f x])^{3/2} \text{Csc}[e + f x] \text{Sec}[e + f x]}{a f}
 \end{aligned}$$

Problem 1382: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \text{Cos}[e + f x])^{3/2} \text{Csc}[e + f x]^3}{a + b \text{Sin}[e + f x]} dx$$

Optimal (type 4, 574 leaves, 30 steps):

$$\frac{g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{4 a f} - \frac{b^2 g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a^3 f} +$$

$$\frac{b^{3/2} (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^3 f} + \frac{g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{4 a f} -$$

$$\frac{b^2 g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a^3 f} + \frac{b^{3/2} (-a^2 + b^2)^{1/4} g^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^3 f} +$$

$$\frac{b g \sqrt{g \cos[e+fx]} \operatorname{Csc}[e+fx]}{a^2 f} - \frac{g \sqrt{g \cos[e+fx]} \operatorname{Csc}[e+fx]^2}{2 a f} -$$

$$\frac{b g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{a^2 f \sqrt{g \cos[e+fx]}} +$$

$$\frac{b (a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{a^2 (a^2 - b (b - \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e+fx]}} +$$

$$\frac{b (a^2 - b^2) g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{a^2 (a^2 - b (b + \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e+fx]}}$$

Result (type 6, 2411 leaves):

$$\frac{1}{4 a^2 f \cos[e+fx]^{3/2}}$$

$$(g \cos[e+fx])^{3/2} \left(-\frac{1}{\sqrt{1 - \cos[e+fx]^2} (b + a \operatorname{Csc}[e+fx])} - 2 a b (a + b \sqrt{1 - \cos[e+fx]^2}) \right.$$

$$\left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \sqrt{\cos[e+fx]} \right) / \right.$$

$$\left. \left(\sqrt{1 - \cos[e+fx]^2} \right. \right.$$

$$\left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] - 2 \right.

$$\left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right.$$

$$\left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \right) \cos[e+fx]^2 \right)$$

$$(a^2 + b^2 (-1 + \cos[e+fx]^2)) \left. \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b}$$

$$\left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4}}\right] \right) +$$$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + i b \text{Cos}[e + f x] \right] - \\
 & \text{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + i b \text{Cos}[e + f x] \right] \right) \Bigg) - \\
 & \frac{1}{(1 - \text{Cos}[e + f x]^2) (-1 + 2 \text{Cos}[e + f x]^2) (b + a \text{Csc}[e + f x])} \\
 & b^2 (-1 + \text{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \\
 & \text{Cos}[2(e + f x)] \text{Csc}[e + f x] \\
 & \left(\left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) + \right. \\
 & \left. \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) - \frac{\text{ArcTan}[\sqrt{\text{Cos}[e + f x]}}{a} \right. \\
 & \left. \left(10 b (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\text{Cos}[e + f x]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \text{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \text{Cos}[e + f x]^2 \left. \right) (a^2 + b^2 (-1 + \text{Cos}[e + f x]^2)) \right) + \\
 & \left(36 b (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \text{Cos}[e + f x]^{5/2} \right) / \\
 & \left(5 \sqrt{1 - \text{Cos}[e + f x]^2} \left(9 (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \text{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \text{Cos}[e + f x]^2 \left. \right) (a^2 + b^2 (-1 + \text{Cos}[e + f x]^2)) \right) + \\
 & \frac{\text{Log}[1 - \sqrt{\text{Cos}[e + f x]}]}{2 a} - \frac{\text{Log}[1 + \sqrt{\text{Cos}[e + f x]}]}{2 a} - \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \right. \\
 & \left. \text{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x] \right] \right) /
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) + \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{a^2 - b^2} + \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] \right) / \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) \Bigg) - \\
 & \frac{1}{(1 - \operatorname{Cos}[e + f x]^2) (b + a \operatorname{Csc}[e + f x])} 2 (-a^2 + 3 b^2) (-1 + \operatorname{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \\
 & \operatorname{Csc}[e + f x] \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\operatorname{Cos}[e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \operatorname{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \operatorname{Cos}[e + f x]^2 \left. \left. \left. \left(a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2) \right) \right) \right) \right) - \\
 & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \sqrt{2} b^{3/2} \right. \\
 & \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 4 (a^2 - b^2)^{3/4} \operatorname{ArcTan} \left[\sqrt{\operatorname{Cos}[e + f x]} \right] - \\
 & 2 (a^2 - b^2)^{3/4} \operatorname{Log} \left[1 - \sqrt{\operatorname{Cos}[e + f x]} \right] + 2 (a^2 - b^2)^{3/4} \operatorname{Log} \left[1 + \sqrt{\operatorname{Cos}[e + f x]} \right] - \\
 & \sqrt{2} b^{3/2} \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] + \\
 & \left. \left. \left. \left. \sqrt{2} b^{3/2} \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] \right) \right) \right) \right) \Bigg) + \\
 & \frac{(g \operatorname{Cos}[e + f x])^{3/2} \left(\frac{b \operatorname{Csc}[e + f x]}{a^2} - \frac{\operatorname{Csc}[e + f x]^2}{2 a} \right) \operatorname{Sec}[e + f x]}{f}
 \end{aligned}$$

Problem 1383: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \operatorname{Cos}[e + f x])^{5/2} \operatorname{Sin}[e + f x]^3}{a + b \operatorname{Sin}[e + f x]} dx$$

Optimal (type 4, 610 leaves, 24 steps):

$$\begin{aligned}
 & - \frac{a^3 (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{11/2} f} + \\
 & \frac{a^3 (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{11/2} f} - \frac{2 a^3 g (g \cos[e+fx])^{3/2}}{3 b^4 f} + \\
 & \frac{2 a (g \cos[e+fx])^{7/2}}{7 b^2 f g} - \frac{2 a^4 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b^5 f \sqrt{\cos[e+fx]}} + \\
 & \frac{6 a^2 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{5 b^3 f \sqrt{\cos[e+fx]}} + \\
 & \frac{4 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{15 b f \sqrt{\cos[e+fx]}} + \\
 & \frac{a^4 (a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^6 (b - \sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} + \\
 & \frac{a^4 (a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^6 (b + \sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} + \\
 & \frac{2 a^2 g (g \cos[e+fx])^{3/2} \sin[e+fx]}{5 b^3 f} + \\
 & \frac{4 g (g \cos[e+fx])^{3/2} \sin[e+fx]}{45 b f} - \frac{2 (g \cos[e+fx])^{7/2} \sin[e+fx]}{9 b f g}
 \end{aligned}$$

Result (type 6, 1261 leaves):

$$\begin{aligned}
 & - \frac{1}{15 b^4 f \cos[e+fx]^{5/2}} \\
 & (g \cos[e+fx])^{5/2} \left(\frac{1}{12 \sqrt{1 - \cos[e+fx]^2} (a+b \sin[e+fx])} (6 a^3 b - 2 a b^3) \right. \\
 & \left. (a+b \sqrt{1 - \cos[e+fx]^2}) \left(- \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \right) \right. \right. \\
 & \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right) \cos[e+fx]^{3/2} \right) / \left(\sqrt{1 - \cos[e+fx]^2} \right. \\
 & \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] - \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \right) \right)
 \end{aligned}$$

$$\frac{\sin[4(e+fx)]}{36b}$$

Problem 1384: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{5/2} \sin[e+fx]^2}{a+b \sin[e+fx]} dx$$

Optimal (type 4, 501 leaves, 20 steps):

$$\frac{a^2 (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} f} -$$

$$\frac{a^2 (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{9/2} f} + \frac{2 a^2 g (g \cos[e+fx])^{3/2}}{3 b^3 f} -$$

$$\frac{2 (g \cos[e+fx])^{7/2}}{7 b f g} + \frac{2 a^3 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b^4 f \sqrt{\cos[e+fx]}} -$$

$$\frac{6 a g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{5 b^2 f \sqrt{\cos[e+fx]}} -$$

$$\frac{a^3 (a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^5 (b - \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e+fx]}} -$$

$$\frac{a^3 (a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^5 (b + \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e+fx]}} -$$

$$\frac{2 a g (g \cos[e+fx])^{3/2} \sin[e+fx]}{5 b^2 f}$$

Result (type 6, 1218 leaves):

$$\frac{1}{5 b^3 f \cos[e+fx]^{5/2}}$$

$$a (g \cos[e+fx])^{5/2} \left(\frac{1}{6 \sqrt{1 - \cos[e+fx]^2} (a+b \sin[e+fx])} a b \left(a + b \sqrt{1 - \cos[e+fx]^2} \right) \right.$$

$$\left. - \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \cos[e+fx]^{3/2} \right) / \right.$$

$$\left. \left(\sqrt{1 - \cos[e+fx]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \right. \right. \right. \right.$$

$$\begin{aligned}
& \left. \left(\frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right) - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left(a^2+b^2 (-1+\cos [e+f x]^2) \right) \Big) - \\
& \left((3+3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
& \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] \right) \Big) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin [e+f x] - \\
& \frac{1}{(1-\cos [e+f x]^2) (a+b \sin [e+f x])} 2 (5 a^2-3 b^2) \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
& \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right. \right. \\
& \left. \left. \cos [e+f x]^{3/2} \sqrt{1-\cos [e+f x]^2} \right) \Big) / \right. \\
& \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
& \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \right) \\
& \left. \cos [e+f x]^2 \left(a^2+b^2 (-1+\cos [e+f x]^2) \right) \right) + \\
& \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x] \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x] \right] \right) \right) \Big) / \\
& \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin [e+f x]^2 \Big) + \frac{1}{f} \\
& (g \cos [e+f x])^{5/2} \sec [e+f x]^2 \left(-\frac{(-28 a^2+9 b^2) \cos [e+f x]}{42 b^3} - \right. \\
& \left. \frac{\cos [3 (e+f x)]}{14 b} \right)
\end{aligned}$$

$$\frac{a \operatorname{Sin}[2(e + f x)]}{5 b^2}$$

Problem 1385: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \operatorname{Cos}[e + f x])^{5/2} \operatorname{Sin}[e + f x]}{a + b \operatorname{Sin}[e + f x]} dx$$

Optimal (type 4, 413 leaves, 13 steps):

$$\begin{aligned} & - \frac{a (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \operatorname{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} f} + \frac{a (-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \operatorname{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} f} \\ & + \frac{2 (5 a^2 - 3 b^2) g^2 \sqrt{g \operatorname{Cos}[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2} (e + f x), 2\right]}{5 b^3 f \sqrt{\operatorname{Cos}[e + f x]}} \\ & + \frac{a^2 (a^2 - b^2) g^3 \sqrt{\operatorname{Cos}[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^4 (b - \sqrt{-a^2 + b^2}) f \sqrt{g \operatorname{Cos}[e + f x]}} \\ & - \frac{a^2 (a^2 - b^2) g^3 \sqrt{\operatorname{Cos}[e + f x]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{b^4 (b + \sqrt{-a^2 + b^2}) f \sqrt{g \operatorname{Cos}[e + f x]}} \\ & - \frac{2 g (g \operatorname{Cos}[e + f x])^{3/2} (5 a - 3 b \operatorname{Sin}[e + f x])}{15 b^2 f} \end{aligned}$$

Result (type 6, 1191 leaves):

$$\begin{aligned} & - \frac{1}{5 b^2 f \operatorname{Cos}[e + f x]^{5/2}} \\ & (g \operatorname{Cos}[e + f x])^{5/2} \left(\frac{1}{6 \sqrt{1 - \operatorname{Cos}[e + f x]^2} (a + b \operatorname{Sin}[e + f x])} a b (a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2}) \right. \\ & \left. - \left(\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \\ & \left. \left. \left. \operatorname{Cos}[e + f x]^{3/2} \right) / \left(\sqrt{1 - \operatorname{Cos}[e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \right. \\ & \left. \left. \left. - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \right. \\ & \left. \left. \left. + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) \operatorname{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2)) \right) \right) - \end{aligned}$$

$$\begin{aligned}
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + ib\cos[e+fx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + ib\cos[e+fx] \right] \right) \right) / \left(\sqrt{b}(-a^2+b^2)^{1/4} \right) \sin[e+fx] - \\
 & \frac{1}{(1-\cos[e+fx]^2)(a+b\sin[e+fx])} 2(5a^2-3b^2) \left(a+b\sqrt{1-\cos[e+fx]^2} \right) \\
 & \left(\left(7b(a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos[e+fx]^{3/2} \sqrt{1-\cos[e+fx]^2} \right) / \right. \\
 & \left(3 \left(-7(a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \quad \left(2b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2} \right] \right) \right. \\
 & \quad \left. \left. \cos[e+fx]^2 \right) (a^2+b^2(-1+\cos[e+fx]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}} \right] \right) + \right. \\
 & \quad \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b\cos[e+fx] \right] - \\
 & \quad \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + \right. \\
 & \quad \left. \left. b\cos[e+fx] \right] \right) / \left(4\sqrt{2}b^{3/2}(a^2-b^2)^{1/4} \right) \sin[e+fx]^2 + \\
 & \frac{(g \cos[e+fx])^{5/2} \operatorname{Sec}[e+fx]^2 \left(-\frac{2a \cos[e+fx]}{3b^2} + \frac{\sin[2(e+fx)]}{5b} \right)}{f}
 \end{aligned}$$

Problem 1386: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{5/2} \operatorname{Csc}[e+fx]}{a+b\sin[e+fx]} dx$$

Optimal (type 4, 425 leaves, 21 steps):

$$\begin{aligned}
 & \frac{g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a f} - \frac{(-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a b^{3/2} f} - \frac{g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g}}\right]}{a f} + \\
 & \frac{(-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a b^{3/2} f} - \frac{2 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b f \sqrt{\cos[e+fx]}} + \\
 & \frac{(a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (b - \sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} + \\
 & \frac{(a^2 - b^2) g^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (b + \sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result (type 6, 1818 leaves):

$$\begin{aligned}
 & \frac{1}{2 f \cos[e+fx]^{5/2}} \\
 & (g \cos[e+fx])^{5/2} \left(-\frac{1}{(1 - \cos[e+fx])^2 (-1 + 2 \cos[e+fx])^2 (b + a \operatorname{Csc}[e+fx])} \right. \\
 & \quad 2 (-1 + \cos[e+fx])^2 \left(a + b \sqrt{1 - \cos[e+fx]} \right) \cos[2(e+fx)] \operatorname{Csc}[e+fx] \\
 & \quad \left(\left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e+fx]}}{\sqrt{2} (a^2 - b^2)^{1/4}}\right] \right) / \right. \\
 & \quad \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \\
 & \quad \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e+fx]}}{\sqrt{2} (a^2 - b^2)^{1/4}}\right] \right) / \\
 & \quad \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \frac{\operatorname{ArcTan}\left[\sqrt{\cos[e+fx]}\right]}{2 a} - \\
 & \quad \left(7 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \cos[e+fx]^{3/2} \right) / \\
 & \quad \left(3 \sqrt{1 - \cos[e+fx]} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 \left. \right) (a^2 + b^2 (-1 + \cos[e+fx])^2) \left. \right) + \\
 & \quad \left(22 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \cos[e+fx]^{7/2} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(7 \sqrt{1 - \cos [e + f x]^2} \left(11 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \Big) + \\
 & \frac{\log [1 - \sqrt{\cos [e + f x]}]}{4 a} - \frac{\log [1 + \sqrt{\cos [e + f x]}]}{4 a} + \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \right. \\
 & \quad \left. \log \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) / \\
 & \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) - \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \log \left[\sqrt{a^2 - b^2} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) \Big) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} 2 (-1 + \cos [e + f x]^2) \\
 & \quad \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \operatorname{Csc} [e + f x] \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{3/2} \right) / \right. \\
 & \quad \left(3 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \quad \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - \right. \\
 & \quad \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \quad \left. \cos [e + f x]^2 \right) \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \Big) + \\
 & \frac{1}{8 a (a^2 - b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \\
 & \quad 2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 4 (a^2 - b^2)^{1/4} \operatorname{ArcTan} \left[\sqrt{\cos [e + f x]} \right] + \\
 & \quad 2 (a^2 - b^2)^{1/4} \log [1 - \sqrt{\cos [e + f x]}] - 2 (a^2 - b^2)^{1/4} \log [1 + \sqrt{\cos [e + f x]}] - \\
 & \quad \sqrt{2} \sqrt{b} \log \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] + \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} \log \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) \right) \Big) \Big)
 \end{aligned}$$

Problem 1387: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2} \operatorname{Csc}[e + f x]^2}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 462 leaves, 24 steps):

$$\begin{aligned} & -\frac{b g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f} + \frac{(-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 \sqrt{b} f} + \\ & \frac{b g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f} - \frac{(-a^2 + b^2)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 \sqrt{b} f} - \\ & \frac{g (g \cos[e + f x])^{3/2} \operatorname{Csc}[e + f x]}{a f} - \frac{g^2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{a f \sqrt{\cos[e + f x]}} - \\ & \frac{(a^2 - b^2) g^3 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{-2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a b (b - \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} - \\ & \frac{(a^2 - b^2) g^3 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{-2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a b (b + \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} \end{aligned}$$

Result (type 6, 2391 leaves):

$$\begin{aligned} & \frac{1}{4 a f \cos[e + f x]^{5/2}} \\ & (g \cos[e + f x])^{5/2} \left(-\frac{1}{2 \sqrt{1 - \cos[e + f x]^2} (b + a \operatorname{Csc}[e + f x])} a (a + b \sqrt{1 - \cos[e + f x]^2}) \right. \\ & \left. - \left(\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \\ & \left. \left. \left. \left. \operatorname{Cos}[e + f x]^{3/2} \right) / \left(\sqrt{1 - \cos[e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \right) \right) \right) \operatorname{Cos}[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \left. \right) - \\ & \left((3 + 3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} - \text{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \\
 & \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] + \text{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}\right. \\
 & \left. (-a^2+b^2)^{1/4}\sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] \Bigg) / \left(\sqrt{b}(-a^2+b^2)^{1/4}\right) - \\
 & \frac{1}{(1-\cos[e+fx]^2)(-1+2\cos[e+fx]^2)(b+a\csc[e+fx])} \\
 & \frac{2}{b} \\
 & \frac{(-1+\cos[e+fx]^2)}{(a+b\sqrt{1-\cos[e+fx]^2})} \\
 & \cos[2(e+fx)] \\
 & \csc[e+fx] \\
 & \left(\left((a^2-b^2)^{3/4}(-2a^2+b^2)\text{ArcTan}\left[\frac{-\sqrt{2}(a^2-b^2)^{1/4}+2\sqrt{b}\sqrt{\cos[e+fx]}}{\sqrt{2}(a^2-b^2)^{1/4}}\right]\right) / \right. \\
 & \left. (2\sqrt{2}ab^{3/2}(-a^2+b^2)) + \right. \\
 & \left. \left((a^2-b^2)^{3/4}(-2a^2+b^2)\text{ArcTan}\left[\frac{\sqrt{2}(a^2-b^2)^{1/4}+2\sqrt{b}\sqrt{\cos[e+fx]}}{\sqrt{2}(a^2-b^2)^{1/4}}\right]\right) / \right. \\
 & \left. (2\sqrt{2}ab^{3/2}(-a^2+b^2)) + \frac{\text{ArcTan}\left[\sqrt{\cos[e+fx]}\right]}{2a} - \right. \\
 & \left. \left(7b(a^2-b^2)\text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\cos[e+fx]^{3/2}\right) / \right. \\
 & \left. \left(3\sqrt{1-\cos[e+fx]^2}\left(7(a^2-b^2)\text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] - 2\left(2b^2\text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2)\text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\right)\cos[e+fx]^2\right)(a^2+b^2(-1+\cos[e+fx]^2))\Bigg) + \\
 & \left(22b(a^2-b^2)\text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] \right. \\
 & \left. \cos[e+fx]^{7/2}\right) / \left(7\sqrt{1-\cos[e+fx]^2}\right) \\
 & \left(11(a^2-b^2)\text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] - \right. \\
 & \left. 2\left(2b^2\text{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2)\right. \right. \\
 & \left. \left.\text{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\right)\cos[e+fx]^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(a^2 + b^2 (-1 + \cos[e + f x]^2) \right) \right) + \frac{\text{Log}\left[1 - \sqrt{\cos[e + f x]}\right]}{4 a} - \\
 & \frac{\text{Log}\left[1 + \sqrt{\cos[e + f x]}\right]}{4 a} + \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \text{Log}\left[\sqrt{a^2 - b^2} - \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) - \\
 & \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + \right. \right. \\
 & \quad \left. \left. b \cos[e + f x]\right] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) \Bigg) + \\
 & \frac{1}{(1 - \cos[e + f x]^2) (b + a \text{Csc}[e + f x])} 10 b (-1 + \cos[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \\
 & \text{Csc}[e + f x] \\
 & \left(\left(7 b (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \cos[e + f x]^{3/2} \right) / \right. \\
 & \quad \left(3 \sqrt{1 - \cos[e + f x]^2} \left(7 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) \Bigg) + \\
 & \frac{1}{8 a (a^2 - b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] - 2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{1/4} \text{ArcTan}\left[\sqrt{\cos[e + f x]}\right] + \\
 & \quad 2 (a^2 - b^2)^{1/4} \text{Log}\left[1 - \sqrt{\cos[e + f x]}\right] - 2 (a^2 - b^2)^{1/4} \text{Log}\left[1 + \sqrt{\cos[e + f x]}\right] - \\
 & \quad \sqrt{2} \sqrt{b} \text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] + \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{b} \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] \right) \right) \right) \Bigg) - \\
 & \frac{(g \cos[e + f x])^{5/2} \text{Csc}[e + f x] \text{Sec}[e + f x]}{a f}
 \end{aligned}$$

Problem 1388: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos [e + f x])^{5/2} \operatorname{Csc}[e + f x]^3}{a + b \sin [e + f x]} dx$$

Optimal (type 4, 557 leaves, 30 steps):

$$\begin{aligned} & -\frac{3 g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{4 a f} + \frac{b^2 g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{a^3 f} - \\ & \frac{\sqrt{b} \left(-a^2 + b^2\right)^{3/4} g^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{\left(-a^2 + b^2\right)^{1/4} \sqrt{g}}\right]}{a^3 f} + \frac{3 g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{4 a f} - \\ & \frac{b^2 g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{a^3 f} + \frac{\sqrt{b} \left(-a^2 + b^2\right)^{3/4} g^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{\left(-a^2 + b^2\right)^{1/4} \sqrt{g}}\right]}{a^3 f} + \\ & \frac{b g (g \cos [e + f x])^{3/2} \operatorname{Csc}[e + f x]}{a^2 f} - \frac{g (g \cos [e + f x])^{3/2} \operatorname{Csc}[e + f x]^2}{2 a f} + \\ & \frac{b g^2 \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{a^2 f \sqrt{\cos [e + f x]}} + \\ & \frac{\left(a^2 - b^2\right) g^3 \sqrt{\cos [e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a^2 \left(b - \sqrt{-a^2 + b^2}\right) f \sqrt{g \cos [e + f x]}} + \\ & \frac{\left(a^2 - b^2\right) g^3 \sqrt{\cos [e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a^2 \left(b + \sqrt{-a^2 + b^2}\right) f \sqrt{g \cos [e + f x]}} \end{aligned}$$

Result (type 6, 2427 leaves):

$$\begin{aligned} & -\frac{1}{4 a^2 f \cos [e + f x]^{5/2}} \\ & (g \cos [e + f x])^{5/2} \left(-\frac{1}{4 \sqrt{1 - \cos [e + f x]^2} (b + a \operatorname{Csc}[e + f x])} a b \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \right. \\ & \left. - \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] \right. \right. \right. \\ & \left. \left. \left. \operatorname{Cos}[e + f x]^{3/2} \right) / \left(\sqrt{1 - \cos [e + f x]^2} \right) \right. \right. \\ & \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] - \right. \right. \\ & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] + \right. \right. \right. \\ & \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2}\right] \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \cos [e+f x]^2 \left(a^2+b^2 \left(-1+\cos [e+f x]^2 \right) \right) \right) \right) \right) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan} \left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{\left(-a^2+b^2\right)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \right. \\
 & \left. \left. \left. 1+\frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{\left(-a^2+b^2\right)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b} \left(-a^2+b^2\right)^{1/4} \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos [e+f x]}+i b \cos [e+f x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b} \right. \right. \right. \right. \\
 & \left. \left. \left. \left(-a^2+b^2\right)^{1/4} \sqrt{\cos [e+f x]}+i b \cos [e+f x] \right] \right) \right) / \left(\sqrt{b} \left(-a^2+b^2\right)^{1/4} \right) \left. \right) - \\
 & \frac{1}{(1-\cos [e+f x]^2) (-1+2 \cos [e+f x]^2) (b+a \operatorname{Csc} [e+f x])} \\
 & \frac{2}{b^2} \\
 & (-1+\cos [e+f x]^2) \\
 & \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \cos [2(e+f x)] \operatorname{Csc} [e+f x] \\
 & \left(\left(\left(a^2-b^2 \right)^{3/4} \left(-2 a^2+b^2 \right) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \left(a^2-b^2 \right)^{1/4}+2 \sqrt{b} \sqrt{\cos [e+f x]}}{\sqrt{2} \left(a^2-b^2 \right)^{1/4}} \right] \right) / \right. \\
 & \left. \left(2 \sqrt{2} a b^{3/2} \left(-a^2+b^2 \right) \right) + \right. \\
 & \left. \left(\left(a^2-b^2 \right)^{3/4} \left(-2 a^2+b^2 \right) \operatorname{ArcTan} \left[\frac{\sqrt{2} \left(a^2-b^2 \right)^{1/4}+2 \sqrt{b} \sqrt{\cos [e+f x]}}{\sqrt{2} \left(a^2-b^2 \right)^{1/4}} \right] \right) / \right. \\
 & \left. \left(2 \sqrt{2} a b^{3/2} \left(-a^2+b^2 \right) \right) + \frac{\operatorname{ArcTan} \left[\sqrt{\cos [e+f x]} \right]}{2 a} \right. \\
 & \left. \left(7 b \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \cos [e+f x]^{3/2} \right) / \right. \\
 & \left. \left(3 \sqrt{1-\cos [e+f x]^2} \left(7 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \left(-a^2+b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left(a^2+b^2 \left(-1+\cos [e+f x]^2 \right) \right) \right) \left. \right) + \\
 & \left(22 b \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right. \\
 & \left. \cos [e+f x]^{7/2} \right) / \left(7 \sqrt{1-\cos [e+f x]^2} \right) \\
 & \left(11 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 b^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] \right) \cos [e+f x]^2 \\
 & \quad \left. (a^2+b^2(-1+\cos [e+f x]^2))\right) + \frac{\operatorname{Log}\left[1-\sqrt{\cos [e+f x]}\right]}{4 a} - \\
 & \frac{\operatorname{Log}\left[1+\sqrt{\cos [e+f x]}\right]}{4 a} + \left((a^2-b^2)^{3 / 4}(-2 a^2+b^2) \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\right. \right. \\
 & \quad \left. \left. (a^2-b^2)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x]\right]\right) / \left(4 \sqrt{2} a b^{3 / 2}(-a^2+b^2)\right) - \\
 & \left((a^2-b^2)^{3 / 4}(-2 a^2+b^2) \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [e+f x]}+ \right. \right. \\
 & \quad \left. \left. b \cos [e+f x]\right]\right) / \left(4 \sqrt{2} a b^{3 / 2}(-a^2+b^2)\right) \Bigg) - \\
 & \frac{1}{(1-\cos [e+f x]^2)(b+a \operatorname{Csc}[e+f x])} 2\left(3 a^2-5 b^2\right)(-1+\cos [e+f x]^2) \\
 & \quad \left(a+b \sqrt{1-\cos [e+f x]^2}\right) \\
 & \operatorname{Csc}[e+f x] \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] \cos [e+f x]^{3 / 2}\right) / \right. \\
 & \quad \left(3 \sqrt{1-\cos [e+f x]^2}\left(7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]-2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]+(-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]\right) \cos [e+f x]^2\left(a^2+b^2(-1+\cos [e+f x]^2)\right) \Bigg) + \\
 & \frac{1}{8 a\left(a^2-b^2\right)^{1 / 4}}\left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]-2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]+4\left(a^2-b^2\right)^{1 / 4} \operatorname{ArcTan}\left[\sqrt{\cos [e+f x]}\right]+ \right. \\
 & \quad 2\left(a^2-b^2\right)^{1 / 4} \operatorname{Log}\left[1-\sqrt{\cos [e+f x]}\right]-2\left(a^2-b^2\right)^{1 / 4} \operatorname{Log}\left[1+\sqrt{\cos [e+f x]}\right]- \\
 & \quad \sqrt{2} \sqrt{b} \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x]\right]+ \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x]\right]\right)\right) \Bigg) + \\
 & \frac{\left(g \cos [e+f x]\right)^{5 / 2}\left(\frac{b \operatorname{Cot}[e+f x]}{a^2}-\frac{\operatorname{Cot}[e+f x] \operatorname{Csc}[e+f x]}{2 a}\right) \operatorname{Sec}[e+f x]^2}{f}
 \end{aligned}$$

Problem 1389: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e+fx]^4}{\sqrt{g \cos[e+fx]} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 509 leaves, 23 steps):

$$\begin{aligned} & -\frac{a^4 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} (-a^2+b^2)^{3/4} f \sqrt{g}} - \frac{a^4 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{7/2} (-a^2+b^2)^{3/4} f \sqrt{g}} - \\ & \frac{2 a^2 \sqrt{g \cos[e+fx]}}{b^3 f g} - \frac{2 \sqrt{g \cos[e+fx]}}{b f g} + \frac{2 (g \cos[e+fx])^{5/2}}{5 b f g^3} - \\ & \frac{2 a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2} (e+fx), 2\right]}{b^4 f \sqrt{g \cos[e+fx]}} - \frac{4 a \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2} (e+fx), 2\right]}{3 b^2 f \sqrt{g \cos[e+fx]}} + \\ & \frac{a^5 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^4 (a^2-b (b-\sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}} + \\ & \frac{a^5 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b^4 (a^2-b (b+\sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}} + \frac{2 a \sqrt{g \cos[e+fx]} \sin[e+fx]}{3 b^2 f g} \end{aligned}$$

Result (type 6, 2153 leaves):

$$\begin{aligned} & \frac{\cos[e+fx] \left(\frac{\cos[2(e+fx)]}{5b} + \frac{2a \sin[e+fx]}{3b^2} \right)}{f \sqrt{g \cos[e+fx]}} - \\ & \frac{1}{60 b^2 f \sqrt{g \cos[e+fx]}} \sqrt{\cos[e+fx]} \left(-\frac{1}{\sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} \right. \\ & \left. 2 (10 a^2 - 27 b^2) (a+b \sqrt{1-\cos[e+fx]^2}) \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \left. \left. \left. \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \sqrt{\cos[e+fx]} \right) / \left(\sqrt{1-\cos[e+fx]^2} \right. \right. \\ & \left. \left. \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - 2 \right. \right. \right. \\ & \left. \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \right. \\ & \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \cos[e+fx]^2 \right) \end{aligned}$$

$$\begin{aligned}
 & \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) \\
 & \sin [e + f x] + \frac{1}{\sqrt{1 - \cos [e + f x]^2} (-1 + 2 \cos [e + f x]^2) (a + b \sin [e + f x])} \\
 & (30 a^2 + 27 b^2) \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \cos [2 (e + f x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos [e + f x]}}{b} + \right. \\
 & \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left. \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \left. \right) - \\
 & \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \left. \cos [e + f x]^{5/2} \right) / \left(5 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - \right. \\
 & \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) \\
 & \left. (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left((1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) - \right. \\
 & \left. \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2+b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + \right. \right. \right. \\
 & \left. \left. \left. i b \cos[e+fx] \right] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) \right) \sin[e+fx] + \\
 & \frac{1}{(1-\cos[e+fx]^2)(a+b \sin[e+fx])} 28 a b \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \\
 & \left(\left(5 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\cos[e+fx]} \sqrt{1-\cos[e+fx]^2} \right) / \right. \\
 & \left(\left(-5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
 & \left. \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \right) \right. \\
 & \left. \cos[e+fx]^2 \right) (a^2+b^2(-1+\cos[e+fx]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx] \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx] \right] \right) \right) / \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \right) \sin[e+fx]^2 \Big)
 \end{aligned}$$

Problem 1390: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e+fx]^3}{\sqrt{g \cos[e+fx]} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 457 leaves, 19 steps):

$$\frac{a^3 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} (-a^2+b^2)^{3/4} f \sqrt{g}} + \frac{a^3 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} (-a^2+b^2)^{3/4} f \sqrt{g}} + \frac{2 a \sqrt{g \cos[e+fx]}}{b^2 f g} +$$

$$\frac{2 a^2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{b^3 f \sqrt{g \cos[e+fx]}} + \frac{4 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{3 b f \sqrt{g \cos[e+fx]}} -$$

$$\frac{a^4 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^3 \left(a^2 - b \left(b - \sqrt{-a^2+b^2}\right)\right) f \sqrt{g \cos[e+fx]}} -$$

$$\frac{a^4 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^3 \left(a^2 - b \left(b + \sqrt{-a^2+b^2}\right)\right) f \sqrt{g \cos[e+fx]}} - \frac{2 \sqrt{g \cos[e+fx]} \operatorname{Sin}[e+fx]}{3 b f g}$$

Result (type 6, 2115 leaves):

$$-\frac{2 \cos[e+fx] \operatorname{Sin}[e+fx]}{3 b f \sqrt{g \cos[e+fx]}} +$$

$$\frac{1}{6 b f \sqrt{g \cos[e+fx]}} \sqrt{\cos[e+fx]} \left(-\frac{1}{\sqrt{1-\cos[e+fx]^2} (a+b \operatorname{Sin}[e+fx])} \right.$$

$$2 a \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \left(\left(5 a \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right.$$

$$\left. \left. \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \sqrt{\cos[e+fx]} \right) / \left(\sqrt{1-\cos[e+fx]^2} \right.$$

$$\left. \left(5 \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - 2 \right.$$

$$\left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + \left(-a^2+b^2 \right) \right.$$

$$\left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \cos[e+fx]^2 \right)$$

$$\left. \left(a^2+b^2 \left(-1+\cos[e+fx]^2 \right) \right) \right) - \frac{1}{\left(-a^2+b^2 \right)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b}$$

$$\left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{\left(-a^2+b^2 \right)^{1/4}} \right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{\left(-a^2+b^2 \right)^{1/4}} \right] \right) +$$

$$\left(\operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] - \right.$$

$$\left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] \right)$$

$$\operatorname{Sin}[e+fx] + \frac{1}{\sqrt{1-\cos[e+fx]^2} (-1+2 \cos[e+fx]^2) (a+b \operatorname{Sin}[e+fx])}$$

$$\begin{aligned}
 & 3 a \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \cos [2 (e + f x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos [e + f x]}}{b} + \right. \\
 & \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left. \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \right) - \\
 & \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \left. \cos [e + f x]^{5/2} \right) / \left(5 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - \right. \\
 & \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) \\
 & \left. \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
 & \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + \right. \right. \\
 & \left. \left. i b \cos [e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \left. \right) \sin [e + f x] - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (a + b \sin [e + f x])} 8 b \left(a + b \sqrt{1 - \cos [e + f x]^2} \right)
 \end{aligned}$$

$$\left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\ \left. \left. \sqrt{\cos [e + f x]} \sqrt{1 - \cos [e + f x]^2} \right) / \right. \\ \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\ \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\ \left. \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Big) + \\ \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] + \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) \Big) / \\ \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [e + f x]^2 \Big)$$

Problem 1391: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin [e + f x]^2}{\sqrt{g \cos [e + f x]} (a + b \sin [e + f x])} dx$$

Optimal (type 4, 380 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{a^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{3/4} f \sqrt{g}} - \frac{a^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{3/4} f \sqrt{g}} \\
 & - \frac{2 \sqrt{g \cos[e+fx]}}{b f g} - \frac{2 a \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{b^2 f \sqrt{g \cos[e+fx]}} + \\
 & \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (a^2-b (b-\sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}} + \\
 & \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2 (a^2-b (b+\sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result (type 6, 1526 leaves):

$$\begin{aligned}
 & \frac{1}{2 f \sqrt{g \cos[e+fx]}} \\
 & \sqrt{\cos[e+fx]} \left(- \frac{1}{\sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} - 2 (a+b \sqrt{1-\cos[e+fx]^2}) \right. \\
 & \left. \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \sqrt{\cos[e+fx]} \right) / \right. \right. \\
 & \left. \left(\sqrt{1-\cos[e+fx]^2} \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \right. \right. \\
 & \left. \left. \left. + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 (a^2+b^2 (-1+\cos[e+fx]^2)) \right) \right) - \\
 & \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - \right. \\
 & \left. 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] + \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] - \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] \right) \left. \right) \\
 & \sin[e+fx] - \frac{1}{\sqrt{1-\cos[e+fx]^2} (-1+2 \cos[e+fx]^2) (a+b \sin[e+fx])}
 \end{aligned}$$

$$\begin{aligned}
 & \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \cos[2(e + f x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos[e + f x]}}{b} + \\
 & \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \cos[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - \right. \right. \\
 & 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \\
 & \left. (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) - \left(36 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \right. \right. \\
 & \left. \left. \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \cos[e + f x]^{5/2} \right) / \left(5 \sqrt{1 - \cos[e + f x]^2} \right. \\
 & \left. \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - \right. \right. \\
 & 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \\
 & \left. (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]} + i b \cos[e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} - \right. \\
 & \left. \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]} + \right. \right. \right. \\
 & \left. \left. \left. i b \cos[e + f x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \right) \left. \sin[e + f x] \right)
 \end{aligned}$$

Problem 1392: Result unnecessarily involves higher level functions.

$$\int \frac{\sin[e + f x]}{\sqrt{g \cos[e + f x]} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 352 leaves, 12 steps):

$$\frac{a \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{\sqrt{b} (-a^2+b^2)^{3/4} f \sqrt{g}} + \frac{a \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{\sqrt{b} (-a^2+b^2)^{3/4} f \sqrt{g}} +$$

$$\frac{2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{b f \sqrt{g \cos[e+fx]}} -$$

$$\frac{a^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b (a^2-b^2+b \sqrt{-a^2+b^2}) f \sqrt{g \cos[e+fx]}} -$$

$$\frac{a^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b (a^2-b (b+\sqrt{-a^2+b^2})) f \sqrt{g \cos[e+fx]}}$$

Result (type 6, 573 leaves):

$$\frac{1}{f \sqrt{g \cos[e+fx]} (1-\cos[e+fx]^2) (a+b \sin[e+fx])}$$

$$\frac{2 \sqrt{\cos[e+fx]} (a+b \sqrt{1-\cos[e+fx]^2})}{\left(\left(5b(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right.}$$

$$\left. \left. \sqrt{\cos[e+fx]} \sqrt{1-\cos[e+fx]^2} \right) /$$

$$\left(\left(-5(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right.$$

$$2 \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \right.$$

$$\left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \right)$$

$$\cos[e+fx]^2 (a^2+b^2(-1+\cos[e+fx]^2)) \Big) +$$

$$\left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] \right) - \right.$$

$$\log\left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] +$$

$$\left. \log\left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] \right) /$$

$$\left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \sin[e+fx]^2$$

Problem 1393: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Csc}[e + f x]}{\sqrt{g \cos[e + f x]} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 369 leaves, 16 steps):

$$\begin{aligned} & -\frac{\text{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a f \sqrt{g}} + \frac{b^{3/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{3/4} f \sqrt{g}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a f \sqrt{g}} + \\ & \frac{b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{3/4} f \sqrt{g}} - \frac{b \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{(a^2 - b(b - \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e + f x]}} - \\ & \frac{b \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{(a^2 - b(b + \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e + f x]}} \end{aligned}$$

Result (type 6, 698 leaves):

$$\begin{aligned} & -\frac{1}{f \sqrt{g \cos[e + f x]} (1 - \cos[e + f x]^2) (b + a \text{Csc}[e + f x])} \\ & 2 \sqrt{\cos[e + f x]} (-1 + \cos[e + f x]^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \text{Csc}[e + f x] \\ & \left(\left(5 b (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right. \\ & \left(\sqrt{1 - \cos[e + f x]^2} \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - \right. \right. \\ & \left. \left. 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + \right. \right. \right. \\ & \left. \left. \left. (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \right) \right) \\ & \left. \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) - \\ & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + \right. \\ & 2 \sqrt{2} b^{3/2} \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{3/4} \text{ArcTan}\left[\sqrt{\cos[e + f x]}\right] - \\ & 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 - \sqrt{\cos[e + f x]}\right] + 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 + \sqrt{\cos[e + f x]}\right] - \\ & \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] + \\ & \left. \left. \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] \right) \right) \end{aligned}$$

Problem 1394: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[e + f x]^2}{\sqrt{g \cos[e + f x]} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 448 leaves, 19 steps):

$$\begin{aligned} & \frac{b \text{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f \sqrt{g}} - \frac{b^{5/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{3/4} f \sqrt{g}} + \\ & \frac{b \text{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f \sqrt{g}} - \frac{b^{5/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{3/4} f \sqrt{g}} - \\ & \frac{\sqrt{g \cos[e + f x]} \text{Csc}[e + f x]}{a f g} + \frac{\sqrt{\cos[e + f x]} \text{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{a f \sqrt{g \cos[e + f x]}} + \\ & \frac{b^2 \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2 + b \sqrt{-a^2 + b^2}) f \sqrt{g \cos[e + f x]}} + \\ & \frac{b^2 \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b (b + \sqrt{-a^2 + b^2})) f \sqrt{g \cos[e + f x]}} \end{aligned}$$

Result (type 6, 2375 leaves):

$$\begin{aligned} & -\frac{\text{Cot}[e + f x]}{a f \sqrt{g \cos[e + f x]}} - \\ & \frac{1}{4 a f \sqrt{g \cos[e + f x]}} \sqrt{\cos[e + f x]} \left(\frac{1}{\sqrt{1 - \cos[e + f x]^2} (b + a \text{Csc}[e + f x])} \right. \\ & \left. 4 a (a + b \sqrt{1 - \cos[e + f x]^2}) \left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \left. \left. \left. \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \left(\sqrt{1 - \cos[e + f x]^2} \right. \right. \\ & \left. \left. \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - \right. \right. \right. \\ & \left. \left. \left. 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \right. \right. \\ & \left. \left. \left. \left. \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) \Bigg) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (-1 + 2 \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} \\
 & b (-1 + \cos [e + f x]^2) \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \cos [2 (e + f x)] \operatorname{Csc} [e + f x] \\
 & \left(\left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) + \right. \\
 & \left. \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) - \frac{\operatorname{ArcTan} [\sqrt{\cos [e + f x]}}{a} \right. \\
 & \left. \left(10 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \Bigg) + \\
 & \left(36 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{5/2} \right) / \Bigg) \\
 & \left(5 \sqrt{1 - \cos [e + f x]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\text{Log}\left[1 - \sqrt{\text{Cos}[e + f x]}\right]}{2 a} - \frac{\text{Log}\left[1 + \sqrt{\text{Cos}[e + f x]}\right]}{2 a} - \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \right. \\
 & \quad \left. \text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] \right) / \\
 & \quad \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) + \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{Log}\left[\sqrt{a^2 - b^2} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] \right) / \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) \Bigg) - \\
 & \frac{1}{(1 - \text{Cos}[e + f x]^2) (b + a \text{Csc}[e + f x])} 6 b (-1 + \text{Cos}[e + f x]^2) \\
 & \quad \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \\
 & \quad \text{Csc}[e + f x] \\
 & \quad \left(\left(5 b (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\text{Cos}[e + f x]} \right) / \right. \\
 & \quad \left(\sqrt{1 - \text{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) \text{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \text{Cos}[e + f x]^2)) \Bigg) - \\
 & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 2 \sqrt{2} b^{3/2} \right. \\
 & \quad \left. \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{3/4} \text{ArcTan}\left[\sqrt{\text{Cos}[e + f x]}\right] - \right. \\
 & \quad 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 - \sqrt{\text{Cos}[e + f x]}\right] + 2 (a^2 - b^2)^{3/4} \text{Log}\left[1 + \sqrt{\text{Cos}[e + f x]}\right] - \\
 & \quad \left. \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] + \right. \\
 & \quad \left. \left. \sqrt{2} b^{3/2} \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] \right) \right) \Bigg)
 \end{aligned}$$

Problem 1395: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[e + f x]^3}{\sqrt{g \text{Cos}[e + f x]} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 557 leaves, 25 steps):

$$\begin{aligned}
 & - \frac{3 \operatorname{ArcTan}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{4 a f \sqrt{g}} - \frac{b^2 \operatorname{ArcTan}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{a^3 f \sqrt{g}} + \\
 & \frac{b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a^3 (-a^2+b^2)^{3/4} f \sqrt{g}} - \frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{4 a f \sqrt{g}} - \frac{b^2 \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g}}\right]}{a^3 f \sqrt{g}} + \\
 & \frac{b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos [e+f x]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{a^3 (-a^2+b^2)^{3/4} f \sqrt{g}} + \frac{b \sqrt{g \cos [e+f x]} \operatorname{Csc}[e+f x]}{a^2 f g} - \\
 & \frac{\sqrt{g \cos [e+f x]} \operatorname{Csc}[e+f x]^2}{2 a f g} - \frac{b \sqrt{\cos [e+f x]} \operatorname{EllipticF}\left[\frac{1}{2}(e+f x), 2\right]}{a^2 f \sqrt{g \cos [e+f x]}} - \\
 & \frac{b^3 \sqrt{\cos [e+f x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+f x), 2\right]}{a^2\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) f \sqrt{g \cos [e+f x]}} - \\
 & \frac{b^3 \sqrt{\cos [e+f x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+f x), 2\right]}{a^2\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) f \sqrt{g \cos [e+f x]}}
 \end{aligned}$$

Result (type 6, 2411 leaves):

$$\begin{aligned}
 & \frac{\cos [e+f x]\left(\frac{b \operatorname{Csc}[e+f x]}{a^2}-\frac{\operatorname{Csc}[e+f x]^2}{2 a}\right)}{f \sqrt{g \cos [e+f x]}} + \\
 & \frac{1}{4 a^2 f \sqrt{g \cos [e+f x]}} \sqrt{\cos [e+f x]} \left(-\frac{1}{\sqrt{1-\cos [e+f x]^2}\left(b+a \operatorname{Csc}[e+f x]\right)}\right. \\
 & \left.2 a b\left(a+b \sqrt{1-\cos [e+f x]^2}\right)\left(\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4},\right.\right.\right. \right. \\
 & \left.\left.\left.\cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] \sqrt{\cos [e+f x]}\right) / \left(\sqrt{1-\cos [e+f x]^2}\right)^2\right. \\
 & \left.\left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]-2\right.\right. \\
 & \left.\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]+(-a^2+b^2)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right]\right) \cos [e+f x]^2\right) \\
 & \left.\left(a^2+b^2(-1+\cos [e+f x]^2)\right)\right) - \frac{1}{(-a^2+b^2)^{3/4}}\left(\frac{1}{8}-\frac{i}{8}\right) \sqrt{b} \\
 & \left.\left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}}\right]-2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}}\right]\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\begin{aligned} & \text{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + i b \text{Cos}[e + f x] \right] - \right. \\ & \left. \text{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + i b \text{Cos}[e + f x] \right] \right) \right) - \\
 & \frac{1}{(1 - \text{Cos}[e + f x]^2) (-1 + 2 \text{Cos}[e + f x]^2) (b + a \text{Csc}[e + f x])} \\
 & b^2 (-1 + \text{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \\
 & \text{Cos}[2(e + f x)] \text{Csc}[e + f x] \\
 & \left(\left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) + \right. \\
 & \left. \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \text{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\text{Cos}[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) - \frac{\text{ArcTan}[\sqrt{\text{Cos}[e + f x]}}{a} \right. \\
 & \left. \left(10 b (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\text{Cos}[e + f x]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \text{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \text{Cos}[e + f x]^2 \left(a^2 + b^2 (-1 + \text{Cos}[e + f x]^2) \right) \right) + \\
 & \left(36 b (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \text{Cos}[e + f x]^{5/2} \right) / \\
 & \left(5 \sqrt{1 - \text{Cos}[e + f x]^2} \left(9 (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \text{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \text{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \text{Cos}[e + f x]^2 \left(a^2 + b^2 (-1 + \text{Cos}[e + f x]^2) \right) \right) + \\
 & \frac{\text{Log}[1 - \sqrt{\text{Cos}[e + f x]}]}{2 a} - \frac{\text{Log}[1 + \sqrt{\text{Cos}[e + f x]}]}{2 a} - \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \right. \\
 & \left. \text{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x] \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) + \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{a^2 - b^2} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] \right) / \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) \Bigg) - \\
 & \frac{1}{(1 - \operatorname{Cos}[e + f x]^2) (b + a \operatorname{Csc}[e + f x])} 2 (3 a^2 + 3 b^2) (-1 + \operatorname{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \\
 & \operatorname{Csc}[e + f x] \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\operatorname{Cos}[e + f x]} \right) / \right. \\
 & \quad \left(\sqrt{1 - \operatorname{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \operatorname{Cos}[e + f x]^2 \left(a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2) \right) \Bigg) - \\
 & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \sqrt{2} b^{3/2} \right. \\
 & \quad \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 4 (a^2 - b^2)^{3/4} \operatorname{ArcTan} \left[\sqrt{\operatorname{Cos}[e + f x]} \right] - \\
 & \quad 2 (a^2 - b^2)^{3/4} \operatorname{Log} \left[1 - \sqrt{\operatorname{Cos}[e + f x]} \right] + 2 (a^2 - b^2)^{3/4} \operatorname{Log} \left[1 + \sqrt{\operatorname{Cos}[e + f x]} \right] - \\
 & \quad \sqrt{2} b^{3/2} \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] + \\
 & \quad \left. \left. \left. \left. \sqrt{2} b^{3/2} \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x] \right] \right] \right) \right) \right) \Bigg)
 \end{aligned}$$

Problem 1396: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sin}[e + f x]^4}{(g \operatorname{Cos}[e + f x])^{3/2} (a + b \operatorname{Sin}[e + f x])} dx$$

Optimal (type 4, 584 leaves, 22 steps):

$$\begin{aligned}
 & \frac{a^4 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} (-a^2+b^2)^{5/4} f g^{3/2}} - \frac{a^4 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{5/2} (-a^2+b^2)^{5/4} f g^{3/2}} - \\
 & \frac{2 b}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}} + \frac{2 a^2 (g \cos[e+fx])^{3/2}}{3 b (a^2-b^2) f g^3} - \frac{2 b (g \cos[e+fx])^{3/2}}{3 (a^2-b^2) f g^3} - \\
 & \frac{4 a \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{(a^2-b^2) f g^2 \sqrt{\cos[e+fx]}} + \frac{2 a^3 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b^2 (a^2-b^2) f g^2 \sqrt{\cos[e+fx]}} - \\
 & \frac{a^5 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^3 (a^2-b^2) (b-\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} - \\
 & \frac{a^5 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^3 (a^2-b^2) (b+\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} + \frac{2 a \sin[e+fx]}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result (type 6, 1214 leaves):

$$\begin{aligned}
 & \frac{\cos[e+fx]^2 \left(\frac{2 \cos[e+fx]}{3 b} + \frac{2 \operatorname{Sec}[e+fx] (-b+a \sin[e+fx])}{a^2-b^2} \right)}{f (g \cos[e+fx])^{3/2}} + \\
 & \frac{1}{(a-b) b (a+b) f (g \cos[e+fx])^{3/2}} a \cos[e+fx]^{3/2} \\
 & \left(- \frac{1}{6 \sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} a b \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \left(- \left(\left(56 a (a^2-b^2) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \cos[e+fx]^{3/2} \right) / \right. \right. \\
 & \quad \left. \left(\sqrt{1-\cos[e+fx]^2} \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \cos[e+fx]^2 \left(a^2+b^2 (-1+\cos[e+fx]^2) \right) \right) \right) - \\
 & \left((3+3i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right) \right) \right) \right) \left. \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin[e+fx] - \\
 & \frac{1}{(1-\cos[e+fx]^2)(a+b\sin[e+fx])^2(a^2-2b^2)(a+b\sqrt{1-\cos[e+fx]^2})} \\
 & \left(\left(7b(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \\
 & \left. \left. \cos[e+fx]^{3/2} \sqrt{1-\cos[e+fx]^2} \right) \right) / \\
 & \left(3 \left(-7(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \left. \left. 2 \left(2b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \right) \right) + \\
 & \left. \left. \cos[e+fx]^2 (a^2+b^2(-1+\cos[e+fx]^2)) \right) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] \right) + \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] - \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[e+fx]} + b \cos[e+fx]\right] \right) \right) / \\
 & \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin[e+fx]^2 \Bigg)
 \end{aligned}$$

Problem 1397: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e+fx]^3}{(g \cos[e+fx])^{3/2} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 509 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{a^3 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{5/4} f g^{3/2}} + \frac{a^3 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{b^{3/2} (-a^2+b^2)^{5/4} f g^{3/2}} + \frac{2a}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}} - \\
 & \frac{2a^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{b(a^2-b^2) f g^2 \sqrt{\cos[e+fx]}} + \frac{4b \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{(a^2-b^2) f g^2 \sqrt{\cos[e+fx]}} + \\
 & \frac{a^4 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2(a^2-b^2)(b-\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} + \\
 & \frac{a^4 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b^2(a^2-b^2)(b+\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} - \frac{2b \sin[e+fx]}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}}
 \end{aligned}$$

Result (type 6, 1187 leaves):

$$\begin{aligned}
 & \frac{2 \cos[e+fx] (a-b \sin[e+fx])}{(a^2-b^2) f (g \cos[e+fx])^{3/2}} - \\
 & \frac{1}{(a-b)(a+b) f (g \cos[e+fx])^{3/2}} \cos[e+fx]^{3/2} \left(- \frac{1}{6 \sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} \right. \\
 & \quad a b \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \left(- \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \cos[e+fx]^{3/2} \right) / \left(\sqrt{1-\cos[e+fx]^2} \right. \right. \\
 & \quad \left. \left. \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \right) \right) \\
 & \quad \left. \left. \left. \cos[e+fx]^2 \right) (a^2+b^2 (-1+\cos[e+fx]^2)) \right) \right) - \\
 & \quad \left((3+3i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \right) \sin[e+fx] -
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{(1 - \cos[e + f x]^2) (a + b \sin[e + f x])} 2 (a^2 - 2 b^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \\
& \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \quad \left. \left. \cos[e + f x]^{3/2} \sqrt{1 - \cos[e + f x]^2} \right) / \right. \\
& \quad \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \quad \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \quad \quad \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\
& \quad \left. \cos[e + f x]^2 \right) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \Big) + \\
& \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\
& \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x] \right] - \right. \\
& \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x] \right] \right) \Big) / \\
& \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[e + f x]^2 \Big)
\end{aligned}$$

Problem 1398: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e + f x]^2}{(g \cos[e + f x])^{3/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 453 leaves, 15 steps):

$$\frac{a^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{\sqrt{b} (-a^2+b^2)^{5/4} f g^{3/2}} - \frac{a^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{\sqrt{b} (-a^2+b^2)^{5/4} f g^{3/2}} - \frac{2b}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}} - \frac{2a \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[\frac{1}{2}(e+fx), 2\right]}{(a^2-b^2) f g^2 \sqrt{\cos[e+fx]}} - \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b(a^2-b^2)(b-\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} - \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{b(a^2-b^2)(b+\sqrt{-a^2+b^2}) f g \sqrt{g \cos[e+fx]}} + \frac{2a \sin[e+fx]}{(a^2-b^2) f g \sqrt{g \cos[e+fx]}}$$

Result (type 6, 1180 leaves):

$$\frac{2 \cos[e+fx] (-b+a \sin[e+fx])}{(a^2-b^2) f (g \cos[e+fx])^{3/2}} - \frac{1}{(a-b)(a+b) f (g \cos[e+fx])^{3/2}} + a \cos[e+fx]^{3/2} \left(\frac{1}{6 \sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} a \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \right. \\ \left. - \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \cos[e+fx]^{3/2} \right) / \right. \right. \\ \left. \left(\sqrt{1-\cos[e+fx]^2} \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 (a^2+b^2(-1+\cos[e+fx]^2)) \right) \right) \right) - \\ \left. \left((3+3i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin[e+fx] - \frac{1}{(1-\cos[e+fx]^2)(a+b \sin[e+fx])} 2b \left(a+b \sqrt{1-\cos[e+fx]^2} \right)$$

$$\left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\ \left. \left. \cos [e + f x]^{3/2} \sqrt{1 - \cos [e + f x]^2} \right) / \right. \\ \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\ \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\ \left. \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Big) + \\ \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] - \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) \Big) / \\ \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [e + f x]^2 \Big)$$

Problem 1399: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin [e + f x]}{(g \cos [e + f x])^{3/2} (a + b \sin [e + f x])} dx$$

Optimal (type 4, 413 leaves, 13 steps):

$$- \frac{a \sqrt{b} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{(-a^2 + b^2)^{5/4} f g^{3/2}} + \frac{a \sqrt{b} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{(-a^2 + b^2)^{5/4} f g^{3/2}} + \\ \frac{2 b \sqrt{g \cos [e + f x]} \operatorname{EllipticE} \left[\frac{1}{2} (e + f x), 2 \right]}{(a^2 - b^2) f g^2 \sqrt{\cos [e + f x]}} + \\ \frac{a^2 \sqrt{\cos [e + f x]} \operatorname{EllipticPi} \left[\frac{-2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{(a^2 - b^2) (b - \sqrt{-a^2 + b^2}) f g \sqrt{g \cos [e + f x]}} + \\ \frac{a^2 \sqrt{\cos [e + f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{(a^2 - b^2) (b + \sqrt{-a^2 + b^2}) f g \sqrt{g \cos [e + f x]}} + \frac{2 (a - b \sin [e + f x])}{(a^2 - b^2) f g \sqrt{g \cos [e + f x]}}$$

Result (type 6, 1178 leaves):

$$\begin{aligned}
 & \frac{2 \cos [e+f x] (a-b \sin [e+f x])}{(a^2-b^2) f (g \cos [e+f x])^{3/2}} + \frac{1}{(a-b)(a+b) f (g \cos [e+f x])^{3/2}} \\
 & b \cos [e+f x]^{3/2} \left(\frac{1}{6 \sqrt{1-\cos [e+f x]^2} (a+b \sin [e+f x])} a \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \right. \\
 & \left. - \left(\left(56 a (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \cos [e+f x]^{3/2} \right) / \right. \right. \\
 & \left. \left(\sqrt{1-\cos [e+f x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \right) \left. \right) - \\
 & \left((3+3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e+f x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \right) \sin [e+f x] - \\
 & \frac{1}{(1-\cos [e+f x]^2) (a+b \sin [e+f x])} 2 b \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \cos [e+f x]^{3/2} \sqrt{1-\cos [e+f x]^2} \right) / \right. \\
 & \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [e+f x]^2 \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] \right) + \right.
 \end{aligned}$$

$$\left(\frac{\text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] - \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right]}{4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4}} \right) \text{Sin}[e + f x]^2$$

Problem 1400: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[e + f x]}{(g \text{Cos}[e + f x])^{3/2} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 507 leaves, 21 steps):

$$\frac{\text{ArcTan}\left[\frac{\sqrt{g \text{Cos}[e + f x]}}{\sqrt{g}}\right]}{a f g^{3/2}} - \frac{b^{5/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{5/4} f g^{3/2}} -$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{g \text{Cos}[e + f x]}}{\sqrt{g}}\right]}{a f g^{3/2}} + \frac{b^{5/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{5/4} f g^{3/2}} +$$

$$\frac{2}{a f g \sqrt{g \text{Cos}[e + f x]}} + \frac{2 b \sqrt{g \text{Cos}[e + f x]} \text{EllipticE}\left[\frac{1}{2} (e + f x), 2\right]}{(a^2 - b^2) f g^2 \sqrt{\text{Cos}[e + f x]}} +$$

$$\frac{b^2 \sqrt{\text{Cos}[e + f x]} \text{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{(a^2 - b^2) (b - \sqrt{-a^2 + b^2}) f g \sqrt{g \text{Cos}[e + f x]}} +$$

$$\frac{b^2 \sqrt{\text{Cos}[e + f x]} \text{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{(a^2 - b^2) (b + \sqrt{-a^2 + b^2}) f g \sqrt{g \text{Cos}[e + f x]}} + \frac{2 b (b - a \text{Sin}[e + f x])}{a (a^2 - b^2) f g \sqrt{g \text{Cos}[e + f x]}}$$

Result (type 6, 2424 leaves):

$$-\frac{1}{2 (a - b) (a + b) f (g \text{Cos}[e + f x])^{3/2}}$$

$$\text{Cos}[e + f x]^{3/2} \left(-\frac{1}{3 \sqrt{1 - \text{Cos}[e + f x]^2} (b + a \text{Csc}[e + f x])} a b \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \right.$$

$$\left. - \left(\left(56 a (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) \right) \right)$$

$$\text{Cos}[e + f x]^{3/2} \left. \right) / \left(\sqrt{1 - \text{Cos}[e + f x]^2} \right)$$

$$\begin{aligned}
 & \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] - \right. \\
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \\
 & \left. \cos[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) - \\
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e + f x]}}{(-a^2 + b^2)^{1/4}} \left. \left. \left. \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[e + f x]} + i b \cos[e + f x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]} + i b \cos[e + f x] \right] \right) \right) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) - \\
 & \frac{1}{(1 - \cos[e + f x]^2) (-1 + 2 \cos[e + f x]^2) (b + a \operatorname{Csc}[e + f x])} \\
 & \frac{2}{b^2} \\
 & (-1 + \cos[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \\
 & \operatorname{Cos}[2(e + f x)] \operatorname{Csc}[e + f x] \\
 & \left(\left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \quad \left. (2 \sqrt{2} a b^{3/2} (-a^2 + b^2)) + \right. \\
 & \left. \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos[e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \quad \left. (2 \sqrt{2} a b^{3/2} (-a^2 + b^2)) + \frac{\operatorname{ArcTan}[\sqrt{\cos[e + f x]}]}{2 a} \right) - \\
 & \left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \cos[e + f x]^{3/2} \right) / \\
 & \left(3 \sqrt{1 - \cos[e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(22 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos [e + f x]^{7/2} \right) / \left(7 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \quad \left(11 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \\
 & \quad \left. (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) + \frac{\operatorname{Log} [1 - \sqrt{\cos [e + f x]}]}{4 a} - \\
 & \frac{\operatorname{Log} [1 + \sqrt{\cos [e + f x]}]}{4 a} + \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{Log} [\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) - \\
 & \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{Log} [\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + \right. \\
 & \quad \left. b \cos [e + f x] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) \Bigg) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} 2 (-2 a^2 + b^2) (-1 + \cos [e + f x]^2) \\
 & \quad \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \operatorname{Csc} [e + f x] \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{3/2} \right) / \right. \\
 & \quad \left(3 \sqrt{1 - \cos [e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Bigg) + \\
 & \frac{1}{8 a (a^2 - b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] - 2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 4 (a^2 - b^2)^{1/4} \operatorname{ArcTan} [\sqrt{\cos [e + f x]}] + \right. \\
 & \quad 2 (a^2 - b^2)^{1/4} \operatorname{Log} [1 - \sqrt{\cos [e + f x]}] - 2 (a^2 - b^2)^{1/4} \operatorname{Log} [1 + \sqrt{\cos [e + f x]}] - \\
 & \quad \left. \sqrt{2} \sqrt{b} \operatorname{Log} [\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x]] + \right.
 \end{aligned}$$

$$\sqrt{2} \sqrt{b} \operatorname{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x]\right] + \frac{2 \cos[e + f x] (a - b \sin[e + f x])}{(a^2 - b^2) f (g \cos[e + f x])^{3/2}}$$

Problem 1401: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[e + f x]^2}{(g \cos[e + f x])^{3/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 627 leaves, 25 steps):

$$\begin{aligned} & -\frac{b \operatorname{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f g^{3/2}} + \frac{b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{5/4} f g^{3/2}} + \frac{b \operatorname{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f g^{3/2}} \\ & -\frac{b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{5/4} f g^{3/2}} - \frac{2 b}{a^2 f g \sqrt{g \cos[e + f x]}} - \frac{\operatorname{Csc}[e + f x]}{a f g \sqrt{g \cos[e + f x]}} \\ & -\frac{3 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{a f g^2 \sqrt{\cos[e + f x]}} - \frac{2 b^2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[\frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2) f g^2 \sqrt{\cos[e + f x]}} \\ & -\frac{b^3 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2) (b - \sqrt{-a^2 + b^2}) f g \sqrt{g \cos[e + f x]}} \\ & +\frac{b^3 \sqrt{\cos[e + f x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2) (b + \sqrt{-a^2 + b^2}) f g \sqrt{g \cos[e + f x]}} \\ & -\frac{3 \operatorname{Sin}[e + f x]}{a f g \sqrt{g \cos[e + f x]}} - \frac{2 b^2 (b - a \operatorname{Sin}[e + f x])}{a^2 (a^2 - b^2) f g \sqrt{g \cos[e + f x]}} \end{aligned}$$

Result (type 6, 2469 leaves):

$$\begin{aligned} & -\frac{1}{4 a (a - b) (a + b) f (g \cos[e + f x])^{3/2}} \\ & \operatorname{Cos}[e + f x]^{3/2} \left(\frac{1}{12 \sqrt{1 - \cos[e + f x]^2} (b + a \operatorname{Csc}[e + f x])} (6 a^3 + 2 a b^2) \right. \\ & \left. (a + b \sqrt{1 - \cos[e + f x]^2}) \left(-\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[e + f x]^2\right], \right. \right. \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right) \operatorname{Cos}[e + f x]^{3/2} \right) / \left(\sqrt{1 - \cos[e + f x]^2} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - \right. \\
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \cos [e + f x]^2 \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \Big) - \\
 & \left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \left. \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} \right. \right. \right. \\
 & \left. \left. \left. (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) \right) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (-1 + 2 \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} \\
 & 2 (-3 a^2 b + b^3) \\
 & (-1 + \cos [e + f x]^2) \\
 & \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \cos [2 (e + f x)] \operatorname{Csc} [e + f x] \\
 & \left(\left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \right. \\
 & \left. \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. \left(2 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) + \frac{\operatorname{ArcTan} [\sqrt{\cos [e + f x]}]}{2 a} \right) - \\
 & \left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{3/2} \right) / \\
 & \left(3 \sqrt{1 - \cos [e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \right) \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(22 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos [e + f x]^{7/2} \right) / \left(7 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \quad \left(11 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \\
 & \quad \left. (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) + \frac{\operatorname{Log} [1 - \sqrt{\cos [e + f x]}]}{4 a} - \\
 & \frac{\operatorname{Log} [1 + \sqrt{\cos [e + f x]}]}{4 a} + \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{Log} [\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) - \\
 & \left((a^2 - b^2)^{3/4} (-2 a^2 + b^2) \operatorname{Log} [\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + \right. \\
 & \quad \left. b \cos [e + f x] \right) / \left(4 \sqrt{2} a b^{3/2} (-a^2 + b^2) \right) \Bigg) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} 2 (7 a^2 b - 5 b^3) (-1 + \cos [e + f x]^2) \\
 & \quad \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \operatorname{Csc} [e + f x] \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{3/2} \right) / \right. \\
 & \quad \left(3 \sqrt{1 - \cos [e + f x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Bigg) + \\
 & \frac{1}{8 a (a^2 - b^2)^{1/4}} \left(2 \sqrt{2} \sqrt{b} \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] - 2 \sqrt{2} \sqrt{b} \right. \\
 & \quad \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 4 (a^2 - b^2)^{1/4} \operatorname{ArcTan} [\sqrt{\cos [e + f x]}] + \right. \\
 & \quad 2 (a^2 - b^2)^{1/4} \operatorname{Log} [1 - \sqrt{\cos [e + f x]}] - 2 (a^2 - b^2)^{1/4} \operatorname{Log} [1 + \sqrt{\cos [e + f x]}] - \\
 & \quad \left. \sqrt{2} \sqrt{b} \operatorname{Log} [\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x]] + \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \sqrt{2} \sqrt{b} \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[e + f x]} + b \cos[e + f x] \right] \right] \right] \right] \right] +$$

$$\frac{\cos[e + f x]^2 \left(-\frac{\cot[e + f x]}{a} + \frac{2 \operatorname{Sec}[e + f x] (-b + a \sin[e + f x])}{a^2 - b^2} \right)}{f (g \cos[e + f x])^{3/2}}$$

Problem 1402: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e + f x]^4}{(g \cos[e + f x])^{5/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 601 leaves, 22 steps):

$$\begin{aligned} & -\frac{a^4 \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{b^{3/2} (-a^2 + b^2)^{7/4} f g^{5/2}} - \frac{a^4 \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{b^{3/2} (-a^2 + b^2)^{7/4} f g^{5/2}} \\ & - \frac{2 b}{3 (a^2 - b^2) f g (g \cos[e + f x])^{3/2}} + \frac{2 a^2 \sqrt{g \cos[e + f x]}}{b (a^2 - b^2) f g^3} - \frac{2 b \sqrt{g \cos[e + f x]}}{(a^2 - b^2) f g^3} \\ & - \frac{4 a \sqrt{\cos[e + f x]} \operatorname{EllipticF} \left[\frac{1}{2} (e + f x), 2 \right]}{3 (a^2 - b^2) f g^2 \sqrt{g \cos[e + f x]}} + \frac{2 a^3 \sqrt{\cos[e + f x]} \operatorname{EllipticF} \left[\frac{1}{2} (e + f x), 2 \right]}{b^2 (a^2 - b^2) f g^2 \sqrt{g \cos[e + f x]}} \\ & - \frac{a^5 \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{b^2 (a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos[e + f x]}} \\ & + \frac{a^5 \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{b^2 (a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos[e + f x]}} + \frac{2 a \sin[e + f x]}{3 (a^2 - b^2) f g (g \cos[e + f x])^{3/2}} \end{aligned}$$

Result (type 6, 2158 leaves):

$$\begin{aligned} & \frac{2 \cos[e + f x] (-b + a \sin[e + f x])}{3 (a^2 - b^2) f (g \cos[e + f x])^{5/2}} + \\ & \frac{1}{6 (a - b) (a + b) f (g \cos[e + f x])^{5/2}} \cos[e + f x]^{5/2} \left(-\frac{1}{\sqrt{1 - \cos[e + f x]^2} (a + b \sin[e + f x])} \right. \\ & \left. 2 (-7 a^2 + 3 b^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4} \right. \right. \right. \right. \\ & \left. \left. \left. \left. \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos[e + f x]} \right) \right) / \left(\sqrt{1 - \cos[e + f x]^2} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \quad \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \\
 & \quad \left. (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \quad \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) \\
 & \quad \sin [e + f x] + \frac{1}{\sqrt{1 - \cos [e + f x]^2} (-1 + 2 \cos [e + f x]^2) (a + b \sin [e + f x])} \\
 & \quad (3 a^2 - 3 b^2) \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \cos [2 (e + f x)] \\
 & \quad \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \quad \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos [e + f x]}}{b} + \right. \\
 & \quad \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) \right) / \\
 & \quad \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) - \\
 & \quad \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos [e + f x]^{5/2} \right) / \left(5 \sqrt{1 - \cos [e + f x]^2} \right. \\
 & \quad \left. \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \\
 & (a^2+b^2 (-1+\cos [e+f x]^2)) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log} [\sqrt{-a^2+b^2} - \right. \\
 & \quad \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + i b \cos [e+f x] \right] \Big/ (b^{3/2} (-a^2+b^2)^{3/4}) - \\
 & \left. \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log} [\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]} + \right. \right. \\
 & \quad \left. \left. i b \cos [e+f x] \right] \right) \Big/ (b^{3/2} (-a^2+b^2)^{3/4}) \right) \sin [e+f x] - \\
 & \frac{1}{(1-\cos [e+f x]^2) (a+b \sin [e+f x])} 4 a b \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \left(\left(5 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [e+f x]} \sqrt{1-\cos [e+f x]^2} \right) \Big/ \right. \\
 & \left(\left(-5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \quad 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \quad \left. \cos [e+f x]^2 \right) (a^2+b^2 (-1+\cos [e+f x]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} [\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} [\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [e+f x]} + b \cos [e+f x]] \right) \right) \Big/ \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \right) \sin [e+f x]^2 \Big)
 \end{aligned}$$

Problem 1403: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sin}[e + f x]^3}{(g \text{Cos}[e + f x])^{5/2} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 528 leaves, 18 steps):

$$\begin{aligned} & \frac{a^3 \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right] - a^3 \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{\sqrt{b} (-a^2+b^2)^{7/4} f g^{5/2}} + \frac{2 a}{\sqrt{b} (-a^2+b^2)^{7/4} f g^{5/2}} + \frac{2 a}{3 (a^2-b^2) f g (g \text{Cos}[e+fx])^{3/2}} - \\ & \frac{2 a^2 \sqrt{\text{Cos}[e+fx]} \text{EllipticF}\left[\frac{1}{2} (e+fx), 2\right]}{b (a^2-b^2) f g^2 \sqrt{g \text{Cos}[e+fx]}} + \frac{4 b \sqrt{\text{Cos}[e+fx]} \text{EllipticF}\left[\frac{1}{2} (e+fx), 2\right]}{3 (a^2-b^2) f g^2 \sqrt{g \text{Cos}[e+fx]}} + \\ & \frac{a^4 \sqrt{\text{Cos}[e+fx]} \text{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b (a^2-b^2) (a^2-b (b-\sqrt{-a^2+b^2})) f g^2 \sqrt{g \text{Cos}[e+fx]}} + \\ & \frac{a^4 \sqrt{\text{Cos}[e+fx]} \text{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (e+fx), 2\right]}{b (a^2-b^2) (a^2-b (b+\sqrt{-a^2+b^2})) f g^2 \sqrt{g \text{Cos}[e+fx]}} - \frac{2 b \text{Sin}[e+fx]}{3 (a^2-b^2) f g (g \text{Cos}[e+fx])^{3/2}} \end{aligned}$$

Result (type 6, 1193 leaves):

$$\begin{aligned} & \frac{2 \text{Cos}[e+fx] (a-b \text{Sin}[e+fx])}{3 (a^2-b^2) f (g \text{Cos}[e+fx])^{5/2}} - \\ & \frac{1}{3 (a-b) (a+b) f (g \text{Cos}[e+fx])^{5/2}} \text{Cos}[e+fx]^{5/2} \left(\frac{1}{\sqrt{1-\text{Cos}[e+fx]^2} (a+b \text{Sin}[e+fx])} \right. \\ & \quad \left. 4 a b (a+b \sqrt{1-\text{Cos}[e+fx]^2}) \left(\left(5 a (a^2-b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \quad \left. \left. \left. \text{Cos}[e+fx]^2, \frac{b^2 \text{Cos}[e+fx]^2}{-a^2+b^2}\right] \sqrt{\text{Cos}[e+fx]} \right) / \left(\sqrt{1-\text{Cos}[e+fx]^2} \right. \right. \\ & \quad \left. \left. \left(5 (a^2-b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e+fx]^2, \frac{b^2 \text{Cos}[e+fx]^2}{-a^2+b^2}\right] - \right. \right. \right. \\ & \quad \left. \left. \left. 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[e+fx]^2, \frac{b^2 \text{Cos}[e+fx]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \right. \right. \\ & \quad \left. \left. \left. \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Cos}[e+fx]^2, \frac{b^2 \text{Cos}[e+fx]^2}{-a^2+b^2}\right] \right) \text{Cos}[e+fx]^2 \right) \right. \right. \\ & \quad \left. \left. (a^2+b^2 (-1+\text{Cos}[e+fx]^2)) \right) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\ & \quad \left(2 \text{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\text{Cos}[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \text{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\text{Cos}[e+fx]}}{(-a^2+b^2)^{1/4}}\right] \right) + \\ & \quad \left. \left. \left. \left. \left. \text{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\text{Cos}[e+fx]} + i b \text{Cos}[e+fx]\right] - \right. \right. \right. \right. \\ & \quad \left. \left. \left. \left. \left. \text{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\text{Cos}[e+fx]} + i b \text{Cos}[e+fx]\right] \right) \right) \right) \right) \right) \end{aligned}$$

$$\begin{aligned} & \frac{\sin[e+fx] - \frac{1}{(1-\cos[e+fx]^2)(a+b\sin[e+fx])^2(3a^2-2b^2)}}{(a+b\sqrt{1-\cos[e+fx]^2})} \\ & \left(\left(5b(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \\ & \quad \left. \left. \sqrt{\cos[e+fx]} \sqrt{1-\cos[e+fx]^2} \right) / \right. \\ & \left(\left(-5(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right. \\ & \quad 2 \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + \right. \\ & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] \right) \right) \\ & \quad \left. \cos[e+fx]^2 \right) (a^2+b^2(-1+\cos[e+fx]^2)) \Big) + \\ & \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[e+fx]}}{(a^2-b^2)^{1/4}}\right] \right) - \right. \\ & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[e+fx]} + b\cos[e+fx]\right] + \right. \\ & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[e+fx]} + b\cos[e+fx]\right] \right) \Big) / \\ & \left(4\sqrt{2}\sqrt{b}(a^2-b^2)^{3/4} \right) \sin[e+fx]^2 \Big) \end{aligned}$$

Problem 1404: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sin[e+fx]^2}{(g \cos[e+fx])^{5/2} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 468 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{a^2 \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{(-a^2+b^2)^{7/4} f g^{5/2}} - \frac{a^2 \sqrt{b} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e+fx]}}{(-a^2+b^2)^{1/4} \sqrt{g}}\right]}{(-a^2+b^2)^{7/4} f g^{5/2}} - \\
 & \frac{2b}{3(a^2-b^2) f g (g \cos[e+fx])^{3/2}} + \frac{2a \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\frac{1}{2}(e+fx), 2\right]}{3(a^2-b^2) f g^2 \sqrt{g \cos[e+fx]}} - \\
 & \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{(a^2-b^2) \left(a^2-b(b-\sqrt{-a^2+b^2})\right) f g^2 \sqrt{g \cos[e+fx]}} - \\
 & \frac{a^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(e+fx), 2\right]}{(a^2-b^2) \left(a^2-b(b+\sqrt{-a^2+b^2})\right) f g^2 \sqrt{g \cos[e+fx]}} + \frac{2a \sin[e+fx]}{3(a^2-b^2) f g (g \cos[e+fx])^{3/2}}
 \end{aligned}$$

Result (type 6, 1184 leaves):

$$\begin{aligned}
 & \frac{2 \cos[e+fx] (-b+a \sin[e+fx])}{3(a^2-b^2) f (g \cos[e+fx])^{5/2}} - \\
 & \frac{1}{3(a-b)(a+b) f (g \cos[e+fx])^{5/2}} a \cos[e+fx]^{5/2} \left(- \frac{1}{\sqrt{1-\cos[e+fx]^2} (a+b \sin[e+fx])} \right. \\
 & \quad 4a \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \left(\left(5a(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \sqrt{\cos[e+fx]} \right) / \left(\sqrt{1-\cos[e+fx]^2} \right. \right. \\
 & \quad \left. \left. \left(5(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] - 2 \right. \right. \right. \\
 & \quad \left. \left. \left. \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right] \right) \cos[e+fx]^2 \right) \right. \\
 & \quad \left. \left. \left. (a^2+b^2(-1+\cos[e+fx]^2)) \right) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \right. \\
 & \quad \left. \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4}}\right] \right) + \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]} + i b \cos[e+fx]\right] \right) \left. \right) \\
 & \sin[e+fx] + \frac{1}{(1-\cos[e+fx]^2) (a+b \sin[e+fx])} 2b \left(a+b \sqrt{1-\cos[e+fx]^2} \right)
 \end{aligned}$$

$$\left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right. \right. \\ \left. \left. \sqrt{\cos [e + f x]} \sqrt{1 - \cos [e + f x]^2} \right) / \right. \\ \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\ \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\ \left. \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Big) + \\ \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e + f x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] + \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [e + f x]} + b \cos [e + f x] \right] \right) \Big) / \\ \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin} [e + f x]^2 \Big)$$

Problem 1405: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sin} [e + f x]}{(g \cos [e + f x])^{5/2} (a + b \operatorname{Sin} [e + f x])} dx$$

Optimal (type 4, 432 leaves, 13 steps):

$$\frac{a b^{3/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{(-a^2 + b^2)^{7/4} f g^{5/2}} + \frac{a b^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{g \cos [e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}} \right]}{(-a^2 + b^2)^{7/4} f g^{5/2}} - \\ \frac{2 b \sqrt{\cos [e + f x]} \operatorname{EllipticF} \left[\frac{1}{2} (e + f x), 2 \right]}{3 (a^2 - b^2) f g^2 \sqrt{g \cos [e + f x]}} + \\ \frac{a^2 b \sqrt{\cos [e + f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{(a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos [e + f x]}} + \\ \frac{a^2 b \sqrt{\cos [e + f x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2 \right]}{(a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos [e + f x]}} + \frac{2 (a - b \operatorname{Sin} [e + f x])}{3 (a^2 - b^2) f g (g \cos [e + f x])^{3/2}}$$

Result (type 6, 1183 leaves):

$$\begin{aligned}
 & \frac{2 \operatorname{Cos}[e+f x] (a-b \operatorname{Sin}[e+f x])}{3 (a^2-b^2) f (g \operatorname{Cos}[e+f x])^{5/2}} + \\
 & \frac{1}{3 (a-b) (a+b) f (g \operatorname{Cos}[e+f x])^{5/2}} b \operatorname{Cos}[e+f x]^{5/2} \left(-\frac{1}{\sqrt{1-\operatorname{Cos}[e+f x]^2} (a+b \operatorname{Sin}[e+f x])} \right. \\
 & 4 a \left(a+b \sqrt{1-\operatorname{Cos}[e+f x]^2} \right) \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] \sqrt{\operatorname{Cos}[e+f x]} \right) / \left(\sqrt{1-\operatorname{Cos}[e+f x]^2} \right. \right. \\
 & \quad \left. \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] - 2 \right. \right. \\
 & \quad \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] \right) \operatorname{Cos}[e+f x]^2 \right) \\
 & \quad \left. \left. (a^2+b^2 (-1+\operatorname{Cos}[e+f x]^2)) \right) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\operatorname{Cos}[e+f x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\operatorname{Cos}[e+f x]}}{(-a^2+b^2)^{1/4}}\right] \right) + \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[e+f x]} + i b \operatorname{Cos}[e+f x]\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[e+f x]} + i b \operatorname{Cos}[e+f x]\right] \right) \right) \\
 & \operatorname{Sin}[e+f x] + \frac{1}{(1-\operatorname{Cos}[e+f x]^2) (a+b \operatorname{Sin}[e+f x])} 2 b \left(a+b \sqrt{1-\operatorname{Cos}[e+f x]^2} \right) \\
 & \left(\left(5 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\operatorname{Cos}[e+f x]} \sqrt{1-\operatorname{Cos}[e+f x]^2} \right) / \right. \\
 & \quad \left(\left(-5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \quad \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[e+f x]^2, \frac{b^2 \operatorname{Cos}[e+f x]^2}{-a^2+b^2}\right] \right) \right) \\
 & \quad \left. \left. \operatorname{Cos}[e+f x]^2 \right) (a^2+b^2 (-1+\operatorname{Cos}[e+f x]^2)) \right) + \\
 & \quad \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e+f x]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e+f x]}}{(a^2-b^2)^{1/4}}\right] \right) - \right.
 \end{aligned}$$

$$\left(\frac{\text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right] + \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[e + f x]} + b \text{Cos}[e + f x]\right]}{4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4}} \right) \text{Sin}[e + f x]^2$$

Problem 1406: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[e + f x]}{(g \text{Cos}[e + f x])^{5/2} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 527 leaves, 21 steps):

$$\begin{aligned} & -\frac{\text{ArcTan}\left[\frac{\sqrt{g \text{Cos}[e + f x]}}{\sqrt{g}}\right]}{a f g^{5/2}} + \frac{b^{7/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{7/4} f g^{5/2}} - \\ & \frac{\text{ArcTanh}\left[\frac{\sqrt{g \text{Cos}[e + f x]}}{\sqrt{g}}\right]}{a f g^{5/2}} + \frac{b^{7/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \text{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a (-a^2 + b^2)^{7/4} f g^{5/2}} + \\ & \frac{2}{3 a f g (g \text{Cos}[e + f x])^{3/2}} - \frac{2 b \sqrt{\text{Cos}[e + f x]} \text{EllipticF}\left[\frac{1}{2} (e + f x), 2\right]}{3 (a^2 - b^2) f g^2 \sqrt{g \text{Cos}[e + f x]}} + \\ & \frac{b^3 \sqrt{\text{Cos}[e + f x]} \text{EllipticPi}\left[\frac{-2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{(a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \text{Cos}[e + f x]}} + \\ & \frac{b^3 \sqrt{\text{Cos}[e + f x]} \text{EllipticPi}\left[\frac{-2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (e + f x), 2\right]}{(a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \text{Cos}[e + f x]}} + \frac{2 b (b - a \text{Sin}[e + f x])}{3 a (a^2 - b^2) f g (g \text{Cos}[e + f x])^{3/2}} \end{aligned}$$

Result (type 6, 2418 leaves):

$$\begin{aligned} & \frac{1}{6 (a - b) (a + b) f (g \text{Cos}[e + f x])^{5/2}} \\ & \text{Cos}[e + f x]^{5/2} \left(-\frac{1}{\sqrt{1 - \text{Cos}[e + f x]^2} (b + a \text{Csc}[e + f x])} - 8 a b \left(a + b \sqrt{1 - \text{Cos}[e + f x]^2} \right) \right. \\ & \left. \left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[e + f x]^2, \frac{b^2 \text{Cos}[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\text{Cos}[e + f x]} \right) \right) \right) / \\ & \left(\sqrt{1 - \text{Cos}[e + f x]^2} \right) \end{aligned}$$

$$\begin{aligned}
 & \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \quad \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \\
 & \quad \left. (a^2 + b^2 (-1 + \cos [e + f x]^2)) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \quad \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \right) \Bigg) - \\
 & \quad \frac{1}{(1 - \cos [e + f x]^2) (-1 + 2 \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} \\
 & \quad b^2 (-1 + \cos [e + f x]^2) \\
 & \quad \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \\
 & \quad \operatorname{Cos} [2 (e + f x)] \operatorname{Csc} [e + f x] \\
 & \quad \left(\left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \quad \left(\sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) + \\
 & \quad \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \\
 & \quad \left(\sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) - \frac{\operatorname{ArcTan} [\sqrt{\cos [e + f x]}]}{a} - \\
 & \quad \left(10 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) / \\
 & \quad \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Bigg) + \\
 & \quad \left(36 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{5/2} \right) / \\
 & \quad \left(5 \sqrt{1 - \cos [e + f x]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \operatorname{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2)) \Big) + \\
 & \frac{\operatorname{Log}[1 - \sqrt{\operatorname{Cos}[e + f x]}]}{2 a} - \frac{\operatorname{Log}[1 + \sqrt{\operatorname{Cos}[e + f x]}]}{2 a} - \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x]\right] \right) / \\
 & \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) + \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{a^2 - b^2} + \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x]\right] \right) / \left(2 \sqrt{2} a \sqrt{b} (-a^2 + b^2) \right) \Big) - \\
 & \frac{1}{(1 - \operatorname{Cos}[e + f x]^2) (b + a \operatorname{Csc}[e + f x])} 2 (6 a^2 - 7 b^2) (-1 + \operatorname{Cos}[e + f x]^2) \\
 & \left(a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \\
 & \operatorname{Csc}[e + f x] \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\operatorname{Cos}[e + f x]} \right) / \right. \\
 & \left(\sqrt{1 - \operatorname{Cos}[e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \operatorname{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2)) \Big) - \\
 & \frac{1}{8 a (a^2 - b^2)^{3/4}} \left(-2 \sqrt{2} b^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 2 \sqrt{2} b^{3/2} \right. \\
 & \left. \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[e + f x]}}{(a^2 - b^2)^{1/4}}\right] + 4 (a^2 - b^2)^{3/4} \operatorname{ArcTan}\left[\sqrt{\operatorname{Cos}[e + f x]}\right] - \right. \\
 & 2 (a^2 - b^2)^{3/4} \operatorname{Log}\left[1 - \sqrt{\operatorname{Cos}[e + f x]}\right] + 2 (a^2 - b^2)^{3/4} \operatorname{Log}\left[1 + \sqrt{\operatorname{Cos}[e + f x]}\right] - \\
 & \sqrt{2} b^{3/2} \operatorname{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \operatorname{Cos}[e + f x]\right] + \\
 & \sqrt{2} b^{3/2} \operatorname{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]} + b \right. \\
 & \left. \operatorname{Cos}[e + f x]\right] \Big) \Big) + \frac{2 \operatorname{Cos}[e + f x] (a - b \operatorname{Sin}[e + f x])}{3 (a^2 - b^2) f (g \operatorname{Cos}[e + f x])^{5/2}}
 \end{aligned}$$

Problem 1407: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[e + f x]^2}{(g \cos[e + f x])^{5/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 651 leaves, 25 steps):

$$\begin{aligned} & \frac{b \text{ArcTan}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f g^{5/2}} - \frac{b^{9/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{7/4} f g^{5/2}} + \frac{b \text{ArcTanh}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g}}\right]}{a^2 f g^{5/2}} - \\ & \frac{b^{9/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{g \cos[e + f x]}}{(-a^2 + b^2)^{1/4} \sqrt{g}}\right]}{a^2 (-a^2 + b^2)^{7/4} f g^{5/2}} - \frac{2b}{3 a^2 f g (g \cos[e + f x])^{3/2}} - \frac{\text{Csc}[e + f x]}{a f g (g \cos[e + f x])^{3/2}} + \\ & \frac{5 \sqrt{\cos[e + f x]} \text{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{3 a f g^2 \sqrt{g \cos[e + f x]}} + \frac{2 b^2 \sqrt{\cos[e + f x]} \text{EllipticF}\left[\frac{1}{2}(e + f x), 2\right]}{3 a (a^2 - b^2) f g^2 \sqrt{g \cos[e + f x]}} - \\ & \frac{b^4 \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos[e + f x]}} - \\ & \frac{b^4 \sqrt{\cos[e + f x]} \text{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(e + f x), 2\right]}{a (a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) f g^2 \sqrt{g \cos[e + f x]}} + \\ & \frac{5 \sin[e + f x]}{3 a f g (g \cos[e + f x])^{3/2}} - \frac{2 b^2 (b - a \sin[e + f x])}{3 a^2 (a^2 - b^2) f g (g \cos[e + f x])^{3/2}} \end{aligned}$$

Result (type 6, 2465 leaves):

$$\begin{aligned} & \frac{1}{12 a (a - b) (a + b) f (g \cos[e + f x])^{5/2}} \text{Cos}[e + f x]^{5/2} \\ & \left(- \frac{1}{\sqrt{1 - \cos[e + f x]^2} (b + a \text{Csc}[e + f x])} 2 (10 a^3 - 18 a b^2) (a + b \sqrt{1 - \cos[e + f x]^2}) \right. \\ & \quad \left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{\cos[e + f x]} \right) / \right. \\ & \quad \left. \left(\sqrt{1 - \cos[e + f x]^2} \right. \right. \\ & \quad \left. \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] - 2 \right. \right. \\ & \quad \left. \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \\ & \quad \left. \left. \left. \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \left(a^2 + b^2 (-1 + \cos [e + f x]^2) \right) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] - \\
 & \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]} + i b \cos [e + f x] \right] \Big) - \\
 & \frac{1}{(1 - \cos [e + f x]^2) (-1 + 2 \cos [e + f x]^2) (b + a \operatorname{Csc} [e + f x])} \\
 & (-5 a^2 b + 3 b^3) \\
 & (-1 + \cos [e + f x]^2) \\
 & (a + b \sqrt{1 - \cos [e + f x]^2}) \\
 & \cos [2 (e + f x)] \operatorname{Csc} [e + f x] \\
 & \left(\left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) + \right. \\
 & \left. \left((a^2 - b^2)^{1/4} (-2 a^2 + b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} (a^2 - b^2)^{1/4} + 2 \sqrt{b} \sqrt{\cos [e + f x]}}{\sqrt{2} (a^2 - b^2)^{1/4}} \right] \right) / \right. \\
 & \left. (\sqrt{2} a \sqrt{b} (-a^2 + b^2)) - \frac{\operatorname{ArcTan} [\sqrt{\cos [e + f x]}}{a} \right. \\
 & \left. \left(10 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \cos [e + f x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Big) + \\
 & \left(36 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \cos [e + f x]^{5/2} \right) / \\
 & \left(5 \sqrt{1 - \cos [e + f x]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [e + f x]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right) \cos [e+f x]^2 \left(a^2+b^2 (-1+\cos [e+f x]^2) \right) \right) \right) + \right. \\
 & \frac{\log [1-\sqrt{\cos [e+f x]}]}{2 a}-\frac{\log [1+\sqrt{\cos [e+f x]}]}{2 a}-\left(\left(a^2-b^2 \right)^{1 / 4} \left(-2 a^2+b^2 \right) \right. \\
 & \left. \log \left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right] \right) / \\
 & \left(2 \sqrt{2} a \sqrt{b}\left(-a^2+b^2 \right) \right)+\left(\left(a^2-b^2 \right)^{1 / 4} \left(-2 a^2+b^2 \right) \log \left[\sqrt{a^2-b^2}+\right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right] \right) / \left(2 \sqrt{2} a \sqrt{b}\left(-a^2+b^2 \right) \right) \left. \right) - \\
 & \frac{1}{\left(1-\cos [e+f x]^2 \right)\left(b+a \csc [e+f x] \right)} 2\left(-7 a^2 b+9 b^3 \right)\left(-1+\cos [e+f x]^2 \right) \\
 & \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \\
 & \csc [e+f x] \\
 & \left(\left(5 b\left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \sqrt{\cos [e+f x]} \right) / \right. \\
 & \left(\sqrt{1-\cos [e+f x]^2} \left(5\left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] -2\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] +\left(-a^2+b^2 \right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [e+f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left(a^2+b^2 \left(-1+\cos [e+f x]^2 \right) \right) \left. \right) - \\
 & \frac{1}{8 a\left(a^2-b^2 \right)^{3 / 4}} \left(-2 \sqrt{2} b^{3 / 2} \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2 \right)^{1 / 4}} \right]+2 \sqrt{2} b^{3 / 2} \right. \\
 & \left. \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [e+f x]}}{\left(a^2-b^2 \right)^{1 / 4}} \right]+4\left(a^2-b^2 \right)^{3 / 4} \operatorname{ArcTan}\left[\sqrt{\cos [e+f x]} \right]- \right. \\
 & 2\left(a^2-b^2 \right)^{3 / 4} \log [1-\sqrt{\cos [e+f x]}]+2\left(a^2-b^2 \right)^{3 / 4} \log [1+\sqrt{\cos [e+f x]}]- \\
 & \sqrt{2} b^{3 / 2} \log \left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right]+ \\
 & \left. \left. \left. \left. \left. \sqrt{2} b^{3 / 2} \log \left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [e+f x]}+b \cos [e+f x] \right] \right) \right) \right) \right) \right) + \\
 & \frac{\cos [e+f x]^3 \left(-\frac{\csc [e+f x]}{a}+\frac{2 \sec [e+f x]^2\left(-b+a \sin [e+f x] \right)}{3\left(a^2-b^2 \right)} \right)}{f\left(g \cos [e+f x] \right)^{5 / 2}}
 \end{aligned}$$

Problem 1408: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e + f x]} (d \sin[e + f x])^{5/2}}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 926 leaves, 31 steps):

$$\frac{a^2 d^{5/2} \sqrt{g} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{\sqrt{2} b^3 f} + \frac{d^{5/2} \sqrt{g} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{4 \sqrt{2} b f} -$$

$$\frac{a^2 d^{5/2} \sqrt{g} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{\sqrt{2} b^3 f} - \frac{d^{5/2} \sqrt{g} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{4 \sqrt{2} b f} -$$

$$\frac{a^2 d^{5/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e + f x] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{2 \sqrt{2} b^3 f} -$$

$$\frac{d^{5/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e + f x] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{8 \sqrt{2} b f} +$$

$$\frac{a^2 d^{5/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e + f x] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{2 \sqrt{2} b^3 f} +$$

$$\frac{d^{5/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e + f x] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{8 \sqrt{2} b f} -$$

$$\left(2 \sqrt{2} a^3 d^3 \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}\right) /$$

$$\left(b^3 \sqrt{-a + b} \sqrt{a + b} f \sqrt{d \sin[e + f x]}\right) +$$

$$\left(2 \sqrt{2} a^3 d^3 \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}\right) /$$

$$\left(b^3 \sqrt{-a + b} \sqrt{a + b} f \sqrt{d \sin[e + f x]}\right) - \frac{d^2 (g \cos[e + f x])^{3/2} \sqrt{d \sin[e + f x]}}{2 b f g} -$$

$$\frac{a d^2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin[e + f x]}}{b^2 f \sqrt{\sin[2 e + 2 f x]}}$$

Result (type 6, 2886 leaves):

$$-\frac{\sqrt{g \cos[e + f x]} \operatorname{Cot}[e + f x] \operatorname{Csc}[e + f x] (d \sin[e + f x])^{5/2}}{2 b f} + \frac{1}{4 b f \sqrt{\cos[e + f x]} \sin[e + f x]^{5/2}}$$

$$\begin{aligned}
 & \sqrt{g \cos[e+fx]} (d \sin[e+fx])^{5/2} \left(- \left(\left(14 b (a^2 - b^2) \cos[e+fx]^{3/2} \left(a + b \sqrt{1 - \cos[e+fx]^2} \right) \right. \right. \right. \\
 & \left. \left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos[e+fx]^2} \right) / \right. \\
 & \left. \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 \right) + \\
 & \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) / \\
 & \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + \right. \\
 & \left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 \right) \\
 & \sin[e+fx]^{3/2} \left. \right) / \left(3 (1 - \cos[e+fx]^2) (a^2 + b^2 (-1 + \cos[e+fx]^2)) \right. \\
 & \left. (a + b \sin[e+fx]) \right) - \\
 & \left(2 a \sqrt{\tan[e+fx]} \left(b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2} \right) \right. \\
 & \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + \right. \right. \\
 & \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2 - b^2} \tan[e+fx] \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2 - b^2} \tan[e+fx] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \tan[e+fx]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e+fx]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \right. \\
 & \left. \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \\
 & \left. \left. \left. \left. \left. \left. \left. \tan[e+fx]^2\right) \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right)\right)\right)\right)\right) \Big/ \\
 & \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a+b \sin[e+fx]) (1 + \tan[e+fx]^2)^{3/2} \right) + \\
 & \left(4 a \cos[2(e+fx)] \sqrt{\tan[e+fx]} \right. \\
 & \left. \left(b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2} \right) \right. \\
 & \left. \left(-\frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} + \right. \right. \\
 & \left. \left. \frac{(2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2} \sqrt{a} + 2(a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \right. \right. \\
 & \left. \left. \frac{(2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} + 2(a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \right. \right. \\
 & \left. \left. \frac{a \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[e+fx]} + \tan[e+fx]\right]}{2 \sqrt{2} b^2} - \right. \right. \\
 & \left. \left. \frac{a \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[e+fx]} + \tan[e+fx]\right]}{2 \sqrt{2} b^2} \right. \right. \\
 & \left. \left. \left((2 a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2 - b^2} \tan[e+fx]\right] \right) \right) \Big/ \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2 - b^2} \tan[e+fx]\right] \right) \Big/ \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\tan[e+fx]^{3/2}}{b \sqrt{1 + \tan[e+fx]^2}} + \\
 & \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \tan[e+fx]^{3/2} \right) \Big/ \\
 & \left(b \sqrt{1 + \tan[e+fx]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \\
 & \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right) - \\
 & \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
 & \left. \tan[e+fx]^{3/2}\right) / \left(3 \sqrt{1 + \tan[e+fx]^2}\right) \\
 & \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2\right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] +\right.\right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right]\right)\right. \\
 & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right) + \\
 & \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
 & \left. \tan[e+fx]^{7/2}\right) / \left(7 b \sqrt{1 + \tan[e+fx]^2}\right) \\
 & \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2\right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] +\right.\right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right]\right)\right. \\
 & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right) - \\
 & \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
 & \left. \tan[e+fx]^{7/2}\right) / \left(7 \sqrt{1 + \tan[e+fx]^2}\right) \\
 & \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2\right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] +\right.\right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right]\right)\right. \\
 & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right) \Bigg) /
 \end{aligned}$$

$$\left(\frac{\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a+b \sin[e+fx]) (-1+\tan[e+fx]^2)}{\sqrt{1+\tan[e+fx]^2}} \right)$$

Problem 1409: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{g \cos[e+fx]} (d \sin[e+fx])^{3/2}}{a+b \sin[e+fx]} dx$$

Optimal (type 4, 578 leaves, 19 steps):

$$\begin{aligned} & - \frac{a d^{3/2} \sqrt{g} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b^2 f} + \frac{a d^{3/2} \sqrt{g} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b^2 f} + \\ & \frac{a d^{3/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b^2 f} - \\ & \frac{a d^{3/2} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b^2 f} + \\ & \left(2 \sqrt{2} a^2 d^2 \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]} \right) / \\ & \left(b^2 \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \sin[e+fx]} \right) - \\ & \left(2 \sqrt{2} a^2 d^2 \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]} \right) / \\ & \left(b^2 \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \sin[e+fx]} \right) + \\ & \frac{d \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e+fx]}}{b f \sqrt{\sin[2e+2fx]}} \end{aligned}$$

Result (type 6, 520 leaves):

$$\begin{aligned}
 & \frac{1}{3 f (-a + b \sin [e + f x]) (a + b \sin [e + f x])^2} \\
 & 14 (a^2 - b^2) \sqrt{g \cos [e + f x]} \cot [e + f x] (d \sin [e + f x])^{3/2} \left(a + b \sqrt{\sin [e + f x]^2} \right) \\
 & \left(\left(a \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) / \right. \\
 & \quad \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) + \\
 & \left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{3}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\sin [e + f x]^2} \right) / \\
 & \quad \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{3}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{3}{4}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{4}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) \Big)
 \end{aligned}$$

Problem 1410: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sqrt{g \cos [e + f x]} \sqrt{d \sin [e + f x]}}{a + b \sin [e + f x]} dx$$

Optimal (type 4, 509 leaves, 16 steps):

$$\begin{aligned}
& \frac{\sqrt{d} \sqrt{g} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b f} - \frac{\sqrt{d} \sqrt{g} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b f} \\
& - \frac{\sqrt{d} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b f} + \\
& - \frac{\sqrt{d} \sqrt{g} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b f} \\
& - \left(2 \sqrt{2} a d \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]}\right) / \\
& \left(b \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \sin[e+fx]}\right) + \\
& - \left(2 \sqrt{2} a d \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]}\right) / \\
& \left(b \sqrt{-a+b} \sqrt{a+b} f \sqrt{d \sin[e+fx]}\right)
\end{aligned}$$

Result (type 4, 201 leaves):

$$\begin{aligned}
& - \left(\left(2 \sqrt{2} d \sqrt{g \cos[e+fx]} \left(\operatorname{EllipticPi}\left[-i, -\operatorname{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right], -1\right] + \right. \right. \right. \\
& \operatorname{EllipticPi}\left[i, -\operatorname{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right], -1\right] - \\
& \operatorname{EllipticPi}\left[\frac{a}{-b + \sqrt{-a^2 + b^2}}, -\operatorname{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right], -1\right] - \\
& \left. \left. \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, -\operatorname{ArcSin}\left[\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right], -1\right] \right) \right) \\
& \left. \sqrt{\tan\left[\frac{1}{2}(e+fx)\right]} \right) / \left(b f \sqrt{\frac{\cos[e+fx]}{1 + \cos[e+fx]}} \sqrt{d \sin[e+fx]} \right)
\end{aligned}$$

Problem 1411: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]} (a + b \sin[e+fx])} dx$$

Optimal (type 4, 208 leaves, 5 steps):

$$\left(2\sqrt{2}\sqrt{g}\operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g}\cos[e+fx]}{\sqrt{g}\sqrt{1+\sin[e+fx]}}\right], -1\right]\sqrt{\sin[e+fx]} \right) /$$

$$\left(\sqrt{-a+b}\sqrt{a+b}f\sqrt{d\sin[e+fx]} \right) -$$

$$\left(2\sqrt{2}\sqrt{g}\operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g}\cos[e+fx]}{\sqrt{g}\sqrt{1+\sin[e+fx]}}\right], -1\right]\sqrt{\sin[e+fx]} \right) /$$

$$\left(\sqrt{-a+b}\sqrt{a+b}f\sqrt{d\sin[e+fx]} \right)$$

Result (type 6, 577 leaves):

$$\frac{1}{f\sqrt{d\sin[e+fx]}(a+b\sin[e+fx])(1+\tan[e+fx]^2)^{3/2}}$$

$$2\sqrt{g}\cos[e+fx]\sec[e+fx]^2\sqrt{\tan[e+fx]}\left(b\tan[e+fx]+a\sqrt{1+\tan[e+fx]^2}\right)$$

$$\left(\left(-2\operatorname{ArcTan}\left[1-\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right]+2\operatorname{ArcTan}\left[1+\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right]\right)-$$

$$\operatorname{Log}\left[-a+\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}-\sqrt{a^2-b^2}\tan[e+fx]\right]+\operatorname{Log}\left[a+$$

$$\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}+\sqrt{a^2-b^2}\tan[e+fx]\right]\bigg/\left(4\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\right)+$$

$$\left(7a^2b\operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]\tan[e+fx]^{3/2}\right)/$$

$$\left(3\sqrt{1+\tan[e+fx]^2}\left(-7a^2\operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]+\right.\right.$$

$$2\left(2(a^2-b^2)\operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]+\right.$$

$$a^2\operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]\left.\right)$$

$$\tan[e+fx]^2\left(-b^2\tan[e+fx]^2+a^2(1+\tan[e+fx]^2)\right)\bigg)$$

Problem 1412: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g\cos[e+fx]}}{(d\sin[e+fx])^{3/2}(a+b\sin[e+fx])} dx$$

Optimal (type 4, 320 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 (g \cos[e + f x])^{3/2}}{a d f g \sqrt{d \sin[e + f x]}} - \\
 & \left(\frac{2 \sqrt{2} b \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}}{\left(a \sqrt{-a+b} \sqrt{a+b} d f \sqrt{d \sin[e + f x]}\right) +} \right) / \\
 & \left(\frac{2 \sqrt{2} b \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}}{\left(a \sqrt{-a+b} \sqrt{a+b} d f \sqrt{d \sin[e + f x]}\right) -} \right) / \\
 & \frac{2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin[e + f x]}}{a d^2 f \sqrt{\sin[2 e + 2 f x]}}
 \end{aligned}$$

Result(type 6, 2881 leaves):

$$\begin{aligned}
 & - \frac{2 \cos[e + f x] \sqrt{g \cos[e + f x]} \sin[e + f x]}{a f (d \sin[e + f x])^{3/2}} + \frac{1}{a f \sqrt{\cos[e + f x]} (d \sin[e + f x])^{3/2}} \\
 & \sqrt{g \cos[e + f x]} \sin[e + f x]^{3/2} \left(\left(28 a (a^2 - b^2) \cos[e + f x]^{3/2} \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \right. \\
 & \left. \left(\left(b \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \sqrt{1 - \cos[e + f x]^2} \right) / \right. \right. \\
 & \left. \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + \right. \right. \\
 & \left. \left(4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) + \\
 & \left(a \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) / \\
 & \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + \right. \\
 & \left. \left(-4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2}\right] \right) \cos[e + f x]^2 \right) \\
 & \sin[e + f x]^{3/2} \left. \right) / \left(3 (1 - \cos[e + f x]^2) (a^2 + b^2 (-1 + \cos[e + f x]^2)) \right) \\
 & (a + b \sin[e + f x]) - \\
 & \left(4 b \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + \right. \right. \\
 & \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e + f x]^2} \right. \\
 & \quad \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
 & \quad \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right) \right) / \\
 & \quad \left. \left. \tan[e + f x]^2 \right) (-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2)) \right) \right) / \\
 & \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (1 + \tan[e + f x]^2)^{3/2} \right) + \\
 & \left(2 b \cos[2(e + f x)] \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right) \\
 & \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \frac{a \operatorname{Log} \left[1 - \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} - \\
 & \quad \left. \frac{a \operatorname{Log} \left[1 + \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left((2 a^2 - b^2) \operatorname{Log}[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} + \right. \\
 & \left. (2 a^2 - b^2) \operatorname{Log}[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} + \frac{\operatorname{Tan}[e + f x]^{3/2}}{b \sqrt{1 + \operatorname{Tan}[e + f x]^2}} + \right. \\
 & \left. \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \operatorname{Tan}[e + f x]^{3/2} \right) / \right. \\
 & \left. \left(b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \right. \\
 & \left. \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \right. \\
 & \left. \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right) \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) - \\
 & \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right) \right) \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) + \\
 & \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{7/2} \right) / \left(7 b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right) \right)
 \end{aligned}$$

$$\left. \left. \begin{aligned} & \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) - \\ & \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\ & \tan[e+fx]^{7/2} \bigg) / \left(7 \sqrt{1 + \tan[e+fx]^2} \right. \\ & \left. \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \right. \\ & \left. \left((a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \right. \\ & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \right. \\ & \left. \left. \left. \left. \left. \left. \tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \right) \right) \right) / \\ & \left. \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (-1 + \tan[e+fx]^2) \right. \right. \\ & \left. \left. \sqrt{1 + \tan[e+fx]^2} \right) \right) \end{aligned} \right)$$

Problem 1413: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e+fx]}}{(d \sin[e+fx])^{5/2} (a + b \sin[e+fx])} dx$$

Optimal (type 4, 366 leaves, 11 steps):

$$\begin{aligned} & -\frac{2 (g \cos[e+fx])^{3/2}}{3 a d f g (d \sin[e+fx])^{3/2}} + \frac{2 b (g \cos[e+fx])^{3/2}}{a^2 d^2 f g \sqrt{d \sin[e+fx]}} + \\ & \left(2 \sqrt{2} b^2 \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1 + \sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]} \right) / \\ & \left(a^2 \sqrt{-a+b} \sqrt{a+b} d^2 f \sqrt{d \sin[e+fx]} \right) - \\ & \left(2 \sqrt{2} b^2 \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1 + \sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]} \right) / \\ & \left(a^2 \sqrt{-a+b} \sqrt{a+b} d^2 f \sqrt{d \sin[e+fx]} \right) + \\ & \frac{2 b \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e+fx]}}{a^2 d^3 f \sqrt{\sin[2e + 2fx]}} \end{aligned}$$

Result (type 6, 2907 leaves):

$$\frac{\sqrt{g \cos [e+f x]} \left(\frac{2 b \cot [e+f x]}{a^2} - \frac{2 \cot [e+f x] \csc [e+f x]}{3 a} \right) \sin [e+f x]^3}{f (d \sin [e+f x])^{5/2}} -$$

$$\frac{1}{a^2 f \sqrt{\cos [e+f x]} (d \sin [e+f x])^{5/2}}$$

$$b \sqrt{g \cos [e+f x]} \sin [e+f x]^{5/2} \left(\left(28 a (a^2 - b^2) \cos [e+f x]^{3/2} \left(a + b \sqrt{1 - \cos [e+f x]^2} \right) \right. \right.$$

$$\left. \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos [e+f x]^2} \right) / \right. \right.$$

$$\left. \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] + \right. \right.$$

$$\left. \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right.$$

$$\left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] \right) \cos [e+f x]^2 \right) +$$

$$\left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] \right) /$$

$$\left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] + \right.$$

$$\left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right.$$

$$\left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2} \right] \right) \cos [e+f x]^2 \right) \Bigg)$$

$$\sin [e+f x]^{3/2} \Bigg) / \left(3 (1 - \cos [e+f x]^2) (a^2 + b^2 (-1 + \cos [e+f x]^2)) \right)$$

$$(a + b \sin [e+f x]) -$$

$$\left(4 b \sqrt{\tan [e+f x]} \left(b \tan [e+f x] + a \sqrt{1 + \tan [e+f x]^2} \right) \right.$$

$$\left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] + \right. \right.$$

$$\left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] - \right. \right.$$

$$\left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan [e+f x]} - \sqrt{a^2 - b^2} \tan [e+f x] \right] + \right. \right.$$

$$\left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan [e+f x]} + \sqrt{a^2 - b^2} \tan [e+f x] \right] \right) \Bigg) /$$

$$\left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+f x]^2, \right. \right.$$

$$\begin{aligned}
 & \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \tan[e+fx]^{3/2} \Big/ \left(3 \sqrt{1 + \tan[e+fx]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \right) \Big/ \\
 & \left. \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \right) \Big/ \\
 & \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (1 + \tan[e+fx]^2)^{3/2} \right) + \\
 & \left(2 b \cos[2(e+fx)] \sqrt{\tan[e+fx]} \left(b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2} \right) \right) \\
 & \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e+fx]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e+fx]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
 & \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log} \left[1 - \sqrt{2} \sqrt{\tan[e+fx]} + \tan[e+fx] \right]}{2 \sqrt{2} b^2} - \\
 & \frac{a \operatorname{Log} \left[1 + \sqrt{2} \sqrt{\tan[e+fx]} + \tan[e+fx] \right]}{2 \sqrt{2} b^2} \\
 & \left. \left((2 a^2 - b^2) \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2 - b^2} \tan[e+fx] \right] \right) \Big/ \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
 & \left((2 a^2 - b^2) \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2 - b^2} \tan[e+fx] \right] \right) \Big/ \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\tan[e+fx]^{3/2}}{b \sqrt{1 + \tan[e+fx]^2}} + \\
 & \left(7 a^4 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \tan[e+fx]^{3/2} \right) \Big/ \\
 & \left(b \sqrt{1 + \tan[e+fx]^2} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) - \\
& \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+f x]^2, \frac{(-a^2 + b^2) \tan[e+f x]^2}{a^2}\right] \right. \\
& \quad \left. \tan[e+f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e+f x]^2} \right) \\
& \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) + \\
& \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \frac{(-a^2 + b^2) \tan[e+f x]^2}{a^2}\right] \right. \\
& \quad \left. \tan[e+f x]^{7/2} \right) / \left(7 b \sqrt{1 + \tan[e+f x]^2} \right) \\
& \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) - \\
& \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \frac{(-a^2 + b^2) \tan[e+f x]^2}{a^2}\right] \right. \\
& \quad \left. \tan[e+f x]^{7/2} \right) / \left(7 \sqrt{1 + \tan[e+f x]^2} \right) \\
& \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right)
\end{aligned}$$

$$\left. \left. \left. \left. \left. \left. \tan[e + fx]^2 \right) (-b^2 \tan[e + fx]^2 + a^2 (1 + \tan[e + fx]^2)) \right) \right) \right) \right) \right) /$$

$$\left(\cos[e + fx]^{3/2} \sqrt{\sin[e + fx]} (a + b \sin[e + fx]) (-1 + \tan[e + fx]^2) \right.$$

$$\left. \left. \left. \left. \left. \left. \sqrt{1 + \tan[e + fx]^2} \right) \right) \right) \right) \right)$$

Problem 1414: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e + fx]}}{(d \sin[e + fx])^{7/2} (a + b \sin[e + fx])} dx$$

Optimal (type 4, 513 leaves, 16 steps):

$$-\frac{2(g \cos[e + fx])^{3/2}}{5 a d f g (d \sin[e + fx])^{5/2}} + \frac{2 b (g \cos[e + fx])^{3/2}}{3 a^2 d^2 f g (d \sin[e + fx])^{3/2}} -$$

$$\frac{4 (g \cos[e + fx])^{3/2}}{5 a d^3 f g \sqrt{d \sin[e + fx]}} - \frac{2 b^2 (g \cos[e + fx])^{3/2}}{a^3 d^3 f g \sqrt{d \sin[e + fx]}} -$$

$$\left(2 \sqrt{2} b^3 \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + fx]}}{\sqrt{g} \sqrt{1 + \sin[e + fx]}}\right], -1\right] \sqrt{\sin[e + fx]} \right) /$$

$$\left(a^3 \sqrt{-a+b} \sqrt{a+b} d^3 f \sqrt{d \sin[e + fx]} \right) +$$

$$\left(2 \sqrt{2} b^3 \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + fx]}}{\sqrt{g} \sqrt{1 + \sin[e + fx]}}\right], -1\right] \sqrt{\sin[e + fx]} \right) /$$

$$\left(a^3 \sqrt{-a+b} \sqrt{a+b} d^3 f \sqrt{d \sin[e + fx]} \right) -$$

$$\frac{4 \sqrt{g \cos[e + fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e + fx]}}{5 a d^4 f \sqrt{\sin[2 e + 2 f x]}}$$

$$\frac{2 b^2 \sqrt{g \cos[e + fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e + fx]}}{a^3 d^4 f \sqrt{\sin[2 e + 2 f x]}}$$

Result (type 6, 2987 leaves):

$$\left(\sqrt{g \cos[e + fx]} \left(-\frac{2 (2 a^2 \cos[e + fx] + 5 b^2 \cos[e + fx]) \operatorname{Csc}[e + fx]}{5 a^3} + \right. \right.$$

$$\left. \left. \frac{2 b \cot[e + fx] \operatorname{Csc}[e + fx]}{3 a^2} - \frac{2 \cot[e + fx] \operatorname{Csc}[e + fx]^2}{5 a} \right) \sin[e + fx]^4 \right) /$$

$$\left(f (d \sin[e + fx])^{7/2} - \frac{1}{5 a^3 f \sqrt{\cos[e + fx]} (d \sin[e + fx])^{7/2}} \sqrt{g \cos[e + fx]} \right)$$

$$\begin{aligned}
& \sin[e + f x]^{7/2} \left(- \left(\left(14 (a^2 - b^2) (4 a^3 + 10 a b^2) \cos[e + f x]^{3/2} \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \right. \right. \\
& \left. \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos[e + f x]^2} \right) \right) / \right. \\
& \left. \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right) + \\
& \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) / \left(7 (a^2 - b^2) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \right. \\
& \left. \left. \frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \right. \right. \\
& \left. \left. \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \left. \right) \sin[e + f x]^{3/2} \left. \right) / \\
& \left(3 (1 - \cos[e + f x]^2) (a^2 + b^2 (-1 + \cos[e + f x]^2)) (a + b \sin[e + f x]) \right) \left. \right) + \\
& \left(2 (2 a^2 b + 10 b^3) \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right. \\
& \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + \right. \right. \\
& \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) \right) / \\
& \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e + f x]^2} \right. \\
& \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
& \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \\
& \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right)
\end{aligned}$$

$$\left. \sqrt{1 + \tan[e + fx]^2} \right)$$

Problem 1415: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{g \cos[e + fx]}}{(d \sin[e + fx])^{9/2} (a + b \sin[e + fx])} dx$$

Optimal (type 4, 598 leaves, 19 steps):

$$\begin{aligned} & -\frac{2 (g \cos[e + fx])^{3/2}}{7 a d f g (d \sin[e + fx])^{7/2}} + \frac{2 b (g \cos[e + fx])^{3/2}}{5 a^2 d^2 f g (d \sin[e + fx])^{5/2}} - \frac{8 (g \cos[e + fx])^{3/2}}{21 a d^3 f g (d \sin[e + fx])^{3/2}} - \\ & \frac{2 b^2 (g \cos[e + fx])^{3/2}}{3 a^3 d^3 f g (d \sin[e + fx])^{3/2}} + \frac{4 b (g \cos[e + fx])^{3/2}}{5 a^2 d^4 f g \sqrt{d \sin[e + fx]}} + \frac{2 b^3 (g \cos[e + fx])^{3/2}}{a^4 d^4 f g \sqrt{d \sin[e + fx]}} + \\ & \left(2 \sqrt{2} b^4 \sqrt{g} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + fx]}}{\sqrt{g} \sqrt{1 + \sin[e + fx]}}\right], -1\right] \sqrt{\sin[e + fx]} \right) / \\ & \left(a^4 \sqrt{-a+b} \sqrt{a+b} d^4 f \sqrt{d \sin[e + fx]} \right) - \\ & \left(2 \sqrt{2} b^4 \sqrt{g} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + fx]}}{\sqrt{g} \sqrt{1 + \sin[e + fx]}}\right], -1\right] \sqrt{\sin[e + fx]} \right) / \\ & \left(a^4 \sqrt{-a+b} \sqrt{a+b} d^4 f \sqrt{d \sin[e + fx]} \right) + \\ & \frac{4 b \sqrt{g \cos[e + fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e + fx]}}{5 a^2 d^5 f \sqrt{\sin[2e + 2fx]}} + \\ & \frac{2 b^3 \sqrt{g \cos[e + fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e + fx]}}{a^4 d^5 f \sqrt{\sin[2e + 2fx]}} \end{aligned}$$

Result (type 6, 3029 leaves):

$$\begin{aligned} & \left(\sqrt{g \cos[e + fx]} \left(\frac{2 (2 a^2 b \cos[e + fx] + 5 b^3 \cos[e + fx]) \operatorname{Csc}[e + fx]}{5 a^4} - \right. \right. \\ & \frac{2 (4 a^2 \cos[e + fx] + 7 b^2 \cos[e + fx]) \operatorname{Csc}[e + fx]^2}{21 a^3} + \frac{2 b \operatorname{Cot}[e + fx] \operatorname{Csc}[e + fx]^2}{5 a^2} - \\ & \left. \left. \frac{2 \operatorname{Cot}[e + fx] \operatorname{Csc}[e + fx]^3}{7 a} \right) \operatorname{Sin}[e + fx]^5 \right) / \left(f (d \sin[e + fx])^{9/2} \right) + \\ & \frac{1}{5 a^4 f \sqrt{\cos[e + fx]} (d \sin[e + fx])^{9/2}} b \sqrt{g \cos[e + fx]} \operatorname{Sin}[e + fx]^{9/2} \\ & \left(- \left(\left(14 (a^2 - b^2) (4 a^3 + 10 a b^2) \cos[e + fx]^{3/2} (a + b \sqrt{1 - \cos[e + fx]^2}) \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \sqrt{1-\cos [e+f x]^2} \right) / \right. \\
& \left(-7 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
& \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \left(a^2-b^2 \right) \right. \\
& \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) + \\
& \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) / \left(7 \left(a^2-b^2 \right) \right. \\
& \left. \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \right. \\
& \left. \left. \frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \right. \right. \\
& \left. \left. \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \left. \right) \sin [e+f x]^{3/2} \left. \right) / \\
& \left(3 \left(1-\cos [e+f x]^2 \right) \left(a^2+b^2 \left(-1+\cos [e+f x]^2 \right) \right) \left(a+b \sin [e+f x] \right) \right) \left. \right) + \\
& \left(2 \left(2 a^2 b+10 b^3 \right) \sqrt{\tan [e+f x]} \left(b \tan [e+f x]+a \sqrt{1+\tan [e+f x]^2} \right) \right. \\
& \left(\left(-2 \operatorname{ArcTan} \left[1-\frac{\sqrt{2} \left(a^2-b^2 \right)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] + \right. \right. \\
& \left. \left. 2 \operatorname{ArcTan} \left[1+\frac{\sqrt{2} \left(a^2-b^2 \right)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[-a+\sqrt{2} \sqrt{a} \left(a^2-b^2 \right)^{1/4} \sqrt{\tan [e+f x]}-\sqrt{a^2-b^2} \tan [e+f x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[a+\sqrt{2} \sqrt{a} \left(a^2-b^2 \right)^{1/4} \sqrt{\tan [e+f x]}+\sqrt{a^2-b^2} \tan [e+f x] \right] \right) \right) / \\
& \left(4 \sqrt{2} \sqrt{a} \left(a^2-b^2 \right)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+f x]^2, \right. \right. \\
& \left. \left. \left(-1+\frac{b^2}{a^2} \right) \tan [e+f x]^2 \right) \tan [e+f x]^{3/2} \right) / \left(3 \sqrt{1+\tan [e+f x]^2} \right) \\
& \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + 2 \right. \\
& \left(2 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan [e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + \right. \\
& \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan [e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] \right) \\
& \left. \left. \tan [e+f x]^2 \right) \left(-b^2 \tan [e+f x]^2+a^2 \left(1+\tan [e+f x]^2 \right) \right) \right) \left. \right) / \\
& \left(\cos [e+f x]^{3/2} \sqrt{\sin [e+f x]} \left(a+b \sin [e+f x] \right) \left(1+\tan [e+f x]^2 \right)^{3/2} \right) +
\end{aligned}$$

$$\begin{aligned}
 & \left(2 (-2 a^2 b - 5 b^3) \operatorname{Cos}[2 (e + f x)] \sqrt{\operatorname{Tan}[e + f x]} \right. \\
 & \left. (b \operatorname{Tan}[e + f x] + a \sqrt{1 + \operatorname{Tan}[e + f x]^2}) \right. \\
 & \left. - \frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2} + 2 \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2} + 2 \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} \right. + \\
 & \frac{(2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \frac{(2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Tan}[e + f x]} + \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b^2} - \\
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[e + f x]} + \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b^2} - \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\operatorname{Tan}[e + f x]^{3/2}}{b \sqrt{1 + \operatorname{Tan}[e + f x]^2}} + \\
 & \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \operatorname{Tan}[e + f x]^{3/2} \right) / \\
 & \left(b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right) \\
 & \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \left. \right) - \\
 & \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(\frac{\tan[e+fx]^{3/2}}{3\sqrt{1+\tan[e+fx]^2}} \right) \left(\begin{aligned} & \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \\ & \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \\ & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \right. \\ & \left. \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \right) + \\ & \left(11a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right) \\ & \left(\frac{\tan[e+fx]^{7/2}}{7b\sqrt{1+\tan[e+fx]^2}} \right) \left(\begin{aligned} & \left(-11a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \\ & \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \\ & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \right. \\ & \left. \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \right) - \\ & \left(11a^2b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right) \\ & \left(\frac{\tan[e+fx]^{7/2}}{7\sqrt{1+\tan[e+fx]^2}} \right) \left(\begin{aligned} & \left(-11a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \\ & \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \\ & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \right. \\ & \left. \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \right) \right) \left. \right) \left. \right) \\ & \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (-1 + \tan[e+fx]^2) \right) \\ & \left(\sqrt{1 + \tan[e+fx]^2} \right) \Bigg)
\end{aligned}
\end{aligned}$$

Problem 1416: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos [e + f x])^{3/2} (d \sin [e + f x])^{3/2}}{a + b \sin [e + f x]} dx$$

Optimal (type 4, 982 leaves, 31 steps):

$$\begin{aligned}
 & \frac{3 d^{3/2} g^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+f x]}}\right]}{4 \sqrt{2} b f} + \\
 & \frac{(a^2 - b^2) d^{3/2} g^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+f x]}}\right]}{\sqrt{2} b^3 f} - \frac{3 d^{3/2} g^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+f x]}}\right]}{4 \sqrt{2} b f} - \\
 & \frac{(a^2 - b^2) d^{3/2} g^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+f x]}}\right]}{\sqrt{2} b^3 f} + \left(2 \sqrt{2} a \sqrt{-a^2 + b^2} d^{3/2} g^2 \right. \\
 & \left. \sqrt{\operatorname{Cos}[e+f x]} \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+f x]}}\right], -1\right]\right) / \\
 & \left(b^3 f \sqrt{g \operatorname{Cos}[e+f x]}\right) - \left(2 \sqrt{2} a \sqrt{-a^2 + b^2} d^{3/2} g^2 \sqrt{\operatorname{Cos}[e+f x]} \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+f x]}}\right], -1\right]\right) / \left(b^3 f \sqrt{g \operatorname{Cos}[e+f x]}\right) - \\
 & \frac{3 d^{3/2} g^{3/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{g \operatorname{Cos}[e+f x]}} + \sqrt{d} \operatorname{Tan}[e+f x]\right]}{8 \sqrt{2} b f} - \\
 & \frac{(a^2 - b^2) d^{3/2} g^{3/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{g \operatorname{Cos}[e+f x]}} + \sqrt{d} \operatorname{Tan}[e+f x]\right]}{2 \sqrt{2} b^3 f} + \\
 & \frac{3 d^{3/2} g^{3/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{g \operatorname{Cos}[e+f x]}} + \sqrt{d} \operatorname{Tan}[e+f x]\right]}{8 \sqrt{2} b f} + \\
 & \frac{(a^2 - b^2) d^{3/2} g^{3/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+f x]}}{\sqrt{g \operatorname{Cos}[e+f x]}} + \sqrt{d} \operatorname{Tan}[e+f x]\right]}{2 \sqrt{2} b^3 f} - \\
 & \frac{a d g \sqrt{g \operatorname{Cos}[e+f x]} \sqrt{d \operatorname{Sin}[e+f x]}}{b^2 f} + \frac{g \sqrt{g \operatorname{Cos}[e+f x]} (d \operatorname{Sin}[e+f x])^{3/2}}{2 b f} + \\
 & \frac{a d^2 g^2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\operatorname{Sin}[2 e + 2 f x]}}{2 b^2 f \sqrt{g \operatorname{Cos}[e+f x]} \sqrt{d \operatorname{Sin}[e+f x]}}
 \end{aligned}$$

Result (type 6, 2370 leaves):

$$\frac{(g \operatorname{Cos}[e+f x])^{3/2} \operatorname{Sec}[e+f x] (d \operatorname{Sin}[e+f x])^{3/2}}{2 b f} - \frac{1}{4 b f \operatorname{Cos}[e+f x]^{3/2} \operatorname{Sin}[e+f x]^{3/2}} (g \operatorname{Cos}[e+f x])^{3/2} (d \operatorname{Sin}[e+f x])^{3/2}$$

$$\left(\frac{1}{(1 - \cos[e + f x])^2 (a^2 + b^2 (-1 + \cos[e + f x])^2) (a + b \sin[e + f x])} \right)$$

$$10 b (a^2 - b^2) \sqrt{\cos[e + f x]} \left(a + b \sqrt{1 - \cos[e + f x]^2} \right)$$

$$\left(\left(b \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos[e + f x]^2} \right) / \right.$$

$$\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right.$$

$$\left(4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{3}{4}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + 3 (a^2 - b^2) \right.$$

$$\left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right) +$$

$$\left(a \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) /$$

$$\left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right.$$

$$\left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{4}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right.$$

$$\left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right)$$

$$\sin[e + f x]^{5/2} + \left(4 a \cos[2(e + f x)] \sqrt{\sin[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right)$$

$$\left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right.$$

$$\frac{\sqrt{a} (2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} b^2 (a^2 - b^2)^{3/4}} +$$

$$\frac{\sqrt{a} (2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} b^2 (a^2 - b^2)^{3/4}} -$$

$$\frac{a \operatorname{Log} \left[1 - \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} +$$

$$\frac{a \operatorname{Log} \left[1 + \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} + \left(\sqrt{a} (2 a^2 - b^2) \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} \right. \right.$$

$$\left. \left. (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) / \left(4 \sqrt{2} b^2 (a^2 - b^2)^{3/4} \right) -$$

$$\begin{aligned}
 & \left(\sqrt{a} (2a^2 - b^2) \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + fx]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + fx] \right] \right) / \\
 & \left(4 \sqrt{2} b^2 (a^2 - b^2)^{3/4} - \frac{\sqrt{\operatorname{Tan}[e + fx]}}{b \sqrt{1 + \operatorname{Tan}[e + fx]^2}} - \left(5 a^4 \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \left. \left. \left. - \operatorname{Tan}[e + fx]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + fx]^2}{a^2} \right] \sqrt{\operatorname{Tan}[e + fx]} \right) \right) / \left(b \sqrt{1 + \operatorname{Tan}[e + fx]^2} \right. \\
 & \left. \left(-5 a^2 \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + fx]^2 \right) (-b^2 \operatorname{Tan}[e + fx]^2 + a^2 (1 + \operatorname{Tan}[e + fx]^2)) \right) + \\
 & \left(9 a^4 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e + fx]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + fx]^2}{a^2} \right] \right. \\
 & \left. \operatorname{Tan}[e + fx]^{5/2} \right) / \left(5 b \sqrt{1 + \operatorname{Tan}[e + fx]^2} \right. \\
 & \left. \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\operatorname{Tan}[e + fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + fx]^2 \right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + fx]^2 \right) (-b^2 \operatorname{Tan}[e + fx]^2 + a^2 (1 + \operatorname{Tan}[e + fx]^2)) \right) \right) / \\
 & \left(\operatorname{Cos}[e + fx]^{5/2} (a + b \operatorname{Sin}[e + fx]) \sqrt{\operatorname{Tan}[e + fx]} (-1 + \operatorname{Tan}[e + fx]^2) \right. \\
 & \left. \sqrt{1 + \operatorname{Tan}[e + fx]^2} \right) + \\
 & \left(2 a \sqrt{\operatorname{Sin}[e + fx]} \left(b \operatorname{Tan}[e + fx] + a \sqrt{1 + \operatorname{Tan}[e + fx]^2} \right) \right. \\
 & \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + fx]}}{\sqrt{a}} \right] + 2 \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + fx]}}{\sqrt{a}} \right] + \operatorname{Log} \left[\right. \right. \right. \\
 & \left. \left. \left. -a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + fx]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + fx] \right] - \operatorname{Log} \left[\right. \right. \right.
 \end{aligned}$$

$$\left. \begin{aligned}
 & a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \Bigg) \Bigg) / \\
 & \left(4 \sqrt{2} (a^2 - b^2)^{3/4} + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{5/2} \right) / \left(5 \sqrt{1 + \tan[e + f x]^2} \right. \right. \\
 & \quad \left. \left. \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \right. \\
 & \quad \left. \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right. \right. \right. \\
 & \quad \left. \left. \tan[e + f x]^2 \right) (-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2)) \right) \Bigg) \Bigg) / \\
 & \left. \left(\cos[e + f x]^{5/2} (a + b \sin[e + f x]) \sqrt{\tan[e + f x]} (1 + \tan[e + f x]^2)^{3/2} \right) \right)
 \end{aligned}$$

Problem 1417: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos[e + f x])^{3/2} \sqrt{d \sin[e + f x]}}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 611 leaves, 19 steps):

$$\begin{aligned}
 & - \frac{a \sqrt{d} g^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+fx]}}\right]}{\sqrt{2} b^2 f} + \\
 & \frac{a \sqrt{d} g^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+fx]}}\right]}{\sqrt{2} b^2 f} - \left(2 \sqrt{2} \sqrt{-a^2 + b^2} \sqrt{d} g^2 \sqrt{\operatorname{Cos}[e+fx]}\right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+fx]}}\right], -1\right]\right) / \\
 & \left(b^2 f \sqrt{g \operatorname{Cos}[e+fx]}\right) + \left(2 \sqrt{2} \sqrt{-a^2 + b^2} \sqrt{d} g^2 \sqrt{\operatorname{Cos}[e+fx]}\right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+fx]}}\right], -1\right]\right) / \left(b^2 f \sqrt{g \operatorname{Cos}[e+fx]}\right) + \\
 & \frac{a \sqrt{d} g^{3/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{g \operatorname{Cos}[e+fx]}} + \sqrt{d} \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b^2 f} - \\
 & \frac{a \sqrt{d} g^{3/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{g \operatorname{Cos}[e+fx]}} + \sqrt{d} \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b^2 f} + \\
 & \frac{g \sqrt{g \operatorname{Cos}[e+fx]} \sqrt{d \operatorname{Sin}[e+fx]}}{b f} - \\
 & \frac{d g^2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{\operatorname{Sin}[2e + 2fx]}}{2 b f \sqrt{g \operatorname{Cos}[e+fx]} \sqrt{d \operatorname{Sin}[e+fx]}}
 \end{aligned}$$

Result(type 6, 999 leaves):

$$\begin{aligned}
 & - \left(\left((g \cos[e + f x])^{3/2} \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \right. \\
 & \quad \left(- \left(\left(25 (a^2 - b^2)^2 \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) / \right. \right. \\
 & \quad \quad \left(b \left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \quad \quad \left(4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + 3 (-a^2 + b^2) \right. \\
 & \quad \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right) \right) + \\
 & \quad \left(18 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos[e + f x]^2 \sqrt{1 - \cos[e + f x]^2} \right) / \\
 & \quad \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left(-4 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{4}, 2, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \quad \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{5}{4}, 1, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 + \\
 & \quad \left(-5 \left(-4 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{4}, 2, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \quad \left. 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{7}{4}, 1, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \\
 & \quad \cos[e + f x]^2 (-1 + \cos[e + f x]^2) (a^2 + b^2 (-1 + \cos[e + f x]^2)) - \\
 & \quad 9 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \\
 & \quad (a^4 (-5 + 3 \cos[e + f x]^2) + b^4 (-5 + 9 \cos[e + f x]^2 - 5 \cos[e + f x]^4) + \\
 & \quad \left. a^2 b^2 (10 - 12 \cos[e + f x]^2 + 5 \cos[e + f x]^4) \right) \right) / \\
 & \quad \left(b \left(-9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{4}, 2, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + 3 (-a^2 + b^2) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{7}{4}, 1, \frac{13}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right) \right) \\
 & \quad \left. \sqrt{d \sin[e + f x]} \tan[e + f x] \right) / (5 f (1 - \cos[e + f x]^2)^{3/2} \\
 & \quad (a^2 + b^2 (-1 + \cos[e + f x]^2)) \\
 & \quad (a + b \sin[e + f x]))
 \end{aligned}$$

Problem 1418: Result unnecessarily involves higher level functions.

$$\int \frac{(g \cos[e + f x])^{3/2}}{\sqrt{d \sin[e + f x]} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 577 leaves, 18 steps):

$$\frac{g^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{g \cos[e + f x]}}\right]}{\sqrt{2} b \sqrt{d} f} - \frac{g^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{g \cos[e + f x]}}\right]}{\sqrt{2} b \sqrt{d} f} + \left(2 \sqrt{2} \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]}\right. \\ \left. \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}}\right], -1\right]\right) / \\ \left(a b \sqrt{d} f \sqrt{g \cos[e + f x]}\right) - \left(2 \sqrt{2} \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]}\right. \\ \left. \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}}\right], -1\right]\right) / \\ \left(a b \sqrt{d} f \sqrt{g \cos[e + f x]}\right) - \frac{g^{3/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e + f x]}}{\sqrt{g \cos[e + f x]}} + \sqrt{d} \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b \sqrt{d} f} + \\ \frac{g^{3/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e + f x]}}{\sqrt{g \cos[e + f x]}} + \sqrt{d} \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b \sqrt{d} f} + \\ \frac{g^2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\sin[2e + 2fx]}}{a f \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}}$$

Result (type 6, 520 leaves):

$$\begin{aligned}
 & \frac{1}{5 f \sqrt{d \sin [e+f x]} (-a+b \sin [e+f x]) (a+b \sin [e+f x])^2} \\
 & 18 (a^2-b^2) (g \cos [e+f x])^{3/2} \cot [e+f x] \left(a+b \sqrt{\sin [e+f x]^2} \right) \\
 & \left(\left(a \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) / \right. \\
 & \quad \left(9 (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{4}, 2, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 (a^2-b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{7}{4}, 1, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) + \\
 & \quad \left(b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \sqrt{\sin [e+f x]^2} \right) / \\
 & \quad \left(-9 (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{4}, 2, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{5}{4}, 1, \frac{13}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) \Big)
 \end{aligned}$$

Problem 1419: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos [e+f x])^{3/2}}{(d \sin [e+f x])^{3/2} (a+b \sin [e+f x])} dx$$

Optimal (type 4, 321 leaves, 8 steps):

$$\begin{aligned}
 & - \left(\left(2 \sqrt{2} \sqrt{-a^2+b^2} g^2 \sqrt{\cos [e+f x]} \operatorname{EllipticPi} \left[-\frac{a}{b-\sqrt{-a^2+b^2}}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d \sin [e+f x]}}{\sqrt{d} \sqrt{1+\cos [e+f x]}} \right], -1 \right] \right) / \left(a^2 d^{3/2} f \sqrt{g \cos [e+f x]} \right) \Big) + \\
 & \left(2 \sqrt{2} \sqrt{-a^2+b^2} g^2 \sqrt{\cos [e+f x]} \operatorname{EllipticPi} \left[-\frac{a}{b+\sqrt{-a^2+b^2}}, \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d \sin [e+f x]}}{\sqrt{d} \sqrt{1+\cos [e+f x]}} \right], -1 \right] \right) / \left(a^2 d^{3/2} f \sqrt{g \cos [e+f x]} \right) - \\
 & \frac{2 g \sqrt{g \cos [e+f x]}}{a d f \sqrt{d \sin [e+f x]}} - \frac{b g^2 \operatorname{EllipticF} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{\sin [2 e + 2 f x]}}{a^2 d f \sqrt{g \cos [e+f x]} \sqrt{d \sin [e+f x]}}
 \end{aligned}$$

Result (type 6, 1287 leaves):

$$\begin{aligned}
& - \frac{2 (g \cos [e + f x])^{3/2} \tan [e + f x]}{a f (d \sin [e + f x])^{3/2}} - \\
& \frac{1}{a f \cos [e + f x]^{3/2} (d \sin [e + f x])^{3/2}} (g \cos [e + f x])^{3/2} \sin [e + f x]^{3/2} \\
& \left(- \frac{1}{(1 - \cos [e + f x])^{1/4} (a + b \sin [e + f x])} 2 b (a + b \sqrt{1 - \cos [e + f x]^2}) \right. \\
& \left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]^2} \right) / \right. \right. \\
& \left. \left((1 - \cos [e + f x])^{3/4} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos [e + f x]^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 (a^2 + b^2 (-1 + \cos [e + f x]^2)) \left. \right) - \\
& \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\cos [e + f x]^2}}{(-a^2 + b^2)^{1/4} (-1 + \cos [e + f x]^2)^{1/4}} \right] - 2 \right. \right. \\
& \left. \left. \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\cos [e + f x]^2}}{(-a^2 + b^2)^{1/4} (-1 + \cos [e + f x]^2)^{1/4}} \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \right. \right. \\
& \left. \left. \frac{i a \cos [e + f x]}{\sqrt{-1 + \cos [e + f x]^2}} - \frac{(1 + i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]^2}}{(-1 + \cos [e + f x]^2)^{1/4}} \right] - \operatorname{Log} \left[\right. \right. \\
& \left. \left. \sqrt{-a^2 + b^2} + \frac{i a \cos [e + f x]}{\sqrt{-1 + \cos [e + f x]^2}} + \frac{(1 + i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]^2}}{(-1 + \cos [e + f x]^2)^{1/4}} \right] \right) \left. \right) / \\
& \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \sqrt{\sin [e + f x]} + \\
& \left(2 a \sqrt{\sin [e + f x]} \left(b \tan [e + f x] + a \sqrt{1 + \tan [e + f x]^2} \right) \right. \\
& \left. \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]^2}}{\sqrt{a}} \right] + 2 \right. \right. \right. \right. \\
& \left. \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]^2}}{\sqrt{a}} \right] + \operatorname{Log} \left[\right. \right. \right. \\
& \left. \left. -a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]^2} - \sqrt{a^2 - b^2} \tan [e + f x] \right] - \operatorname{Log} \left[\right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. \left. \left. a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right) \right) \right) \right) \right) \right) \bigg/ \\
& \left(4 \sqrt{2} (a^2 - b^2)^{3/4} \right) + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \right. \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. -1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right) \tan[e + f x]^{5/2} \right) \right) \right) \right) \bigg/ \left(5 \sqrt{1 + \tan[e + f x]^2} \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. -9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \left. \left. \left. \left. \left. \left. \left. \left. -1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right) \right) \right) \right) \right) \right) \right) \right) + 2 \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. 2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e + f x]^2, \left. \left. \left. \left. \left. \left. \left. \left. -1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right) \right) \right) \right) \right) \right) \right) \right) + \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e + f x]^2, \left. \left. \left. \left. \left. \left. \left. \left. -1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \\
& \left. \left. \left. \left. \left. \left. \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) \right) \right) \right) \bigg/ \\
& \left. \left. \left. \left. \left. \left. \left. \left. \left(\cos[e + f x]^{5/2} (a + b \sin[e + f x]) \sqrt{\tan[e + f x]} (1 + \tan[e + f x]^2)^{3/2} \right) \right) \right) \right) \right) \right) \right) \bigg)
\end{aligned}$$

Problem 1420: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{3/2}}{(d \sin[e + f x])^{5/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 435 leaves, 12 steps):

$$\begin{aligned}
& \left(2 \sqrt{2} b \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]} \right. \\
& \left. \operatorname{EllipticPi} \left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) \bigg/ \\
& \left(a^3 d^{5/2} f \sqrt{g \cos[e + f x]} \right) - \left(2 \sqrt{2} b \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]} \right. \\
& \left. \operatorname{EllipticPi} \left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) \bigg/ \\
& \left(a^3 d^{5/2} f \sqrt{g \cos[e + f x]} \right) - \frac{2 g \sqrt{g \cos[e + f x]}}{3 a d f (d \sin[e + f x])^{3/2}} + \frac{2 b g \sqrt{g \cos[e + f x]}}{a^2 d^2 f \sqrt{d \sin[e + f x]}} + \\
& \frac{2 g^2 \operatorname{EllipticF} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{\sin[2 e + 2 f x]}}{3 a d^2 f \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}} - \\
& \frac{(a^2 - b^2) g^2 \operatorname{EllipticF} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{\sin[2 e + 2 f x]}}{a^3 d^2 f \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}}
\end{aligned}$$

Result (type 6, 1330 leaves):

$$\frac{(g \cos [e+f x])^{3/2} \left(\frac{2 b \operatorname{Csc}[e+f x]}{a^2} - \frac{2 \operatorname{Csc}[e+f x]^2}{3 a} \right) \sin [e+f x]^2 \tan [e+f x]}{f (d \sin [e+f x])^{5/2}}$$

$$\frac{1}{3 a^2 f \cos [e+f x]^{3/2} (d \sin [e+f x])^{5/2}} (g \cos [e+f x])^{3/2} \sin [e+f x]^{5/2}$$

$$\left(-\frac{1}{(1-\cos [e+f x])^{1/4} (a+b \sin [e+f x])} 2 (a^2-3 b^2) \left(a+b \sqrt{1-\cos [e+f x]^2} \right) \right.$$

$$\left. \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] \sqrt{\cos [e+f x]^2} \right) / \right. \right.$$

$$\left. \left((1-\cos [e+f x])^{3/4} \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] + \left(-4 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] + 3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2}\right] \right) \cos [e+f x]^2 (a^2+b^2 (-1+\cos [e+f x]^2)) \right) \right) -$$

$$\left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos [e+f x]^2}}{(-a^2+b^2)^{1/4} (-1+\cos [e+f x]^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos [e+f x]^2}}{(-a^2+b^2)^{1/4} (-1+\cos [e+f x]^2)^{1/4}}\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + \frac{i a \cos [e+f x]}{\sqrt{-1+\cos [e+f x]^2}} - \frac{(1+i) \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]^2}}{(-1+\cos [e+f x]^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} + \frac{i a \cos [e+f x]}{\sqrt{-1+\cos [e+f x]^2}} + \frac{(1+i) \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\cos [e+f x]^2}}{(-1+\cos [e+f x]^2)^{1/4}}\right] \right) \right) /$$

$$\left(\sqrt{a} (-a^2+b^2)^{3/4} \right) \sqrt{\sin [e+f x]} -$$

$$\left(4 a b \sqrt{\sin [e+f x]} \left(b \tan [e+f x] + a \sqrt{1+\tan [e+f x]^2} \right) \right.$$

$$\left. \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]^2}}{\sqrt{a}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]^2}}{\sqrt{a}}\right] + \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]^2} - \sqrt{a^2-b^2} \tan [e+f x]\right] - \operatorname{Log}\left[\right. \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. \left. a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right) \right) \right) / \\
 & \left(4 \sqrt{2} (a^2 - b^2)^{3/4} + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{5/2} \right) \right) / \left(5 \sqrt{1 + \tan[e + f x]^2} \right. \\
 & \left. \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
 & \left. \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \right. \\
 & \left. \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right) \right) \\
 & \left. \left. \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) \right) / \\
 & \left(\cos[e + f x]^{5/2} (a + b \sin[e + f x]) \sqrt{\tan[e + f x]} (1 + \tan[e + f x]^2)^{3/2} \right)
 \end{aligned}$$

Problem 1421: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{3/2}}{(d \sin[e + f x])^{7/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 525 leaves, 15 steps):

$$\begin{aligned}
 & - \left(\left(2 \sqrt{2} b^2 \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) / \left(a^4 d^{7/2} f \sqrt{g \cos[e + f x]} \right) \Bigg) + \\
 & \left(2 \sqrt{2} b^2 \sqrt{-a^2 + b^2} g^2 \sqrt{\cos[e + f x]} \operatorname{EllipticPi} \left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e + f x]}}{\sqrt{d} \sqrt{1 + \cos[e + f x]}} \right], -1 \right] \right) / \left(a^4 d^{7/2} f \sqrt{g \cos[e + f x]} \right) - \\
 & \frac{2 g \sqrt{g \cos[e + f x]}}{5 a d f (d \sin[e + f x])^{5/2}} + \frac{2 b g \sqrt{g \cos[e + f x]}}{3 a^2 d^2 f (d \sin[e + f x])^{3/2}} - \\
 & \frac{8 g \sqrt{g \cos[e + f x]}}{5 a d^3 f \sqrt{d \sin[e + f x]}} + \\
 & \frac{2 (a^2 - b^2) g \sqrt{g \cos[e + f x]}}{a^3 d^3 f \sqrt{d \sin[e + f x]}} - \\
 & \frac{2 b g^2 \operatorname{EllipticF} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{\sin[2 e + 2 f x]}}{3 a^2 d^3 f \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}} + \\
 & \frac{b (a^2 - b^2) g^2 \operatorname{EllipticF} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{\sin[2 e + 2 f x]}}{a^4 d^3 f \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}}
 \end{aligned}$$

Result (type 6, 1357 leaves):

$$\begin{aligned}
 & \left((g \cos[e + f x])^{3/2} \left(\frac{2 (a^2 - 5 b^2) \operatorname{Csc}[e + f x]}{5 a^3} + \frac{2 b \operatorname{Csc}[e + f x]^2}{3 a^2} - \frac{2 \operatorname{Csc}[e + f x]^3}{5 a} \right) \right. \\
 & \quad \left. \sin[e + f x]^3 \tan[e + f x] \right) / \left(f (d \sin[e + f x])^{7/2} \right) + \\
 & \frac{1}{3 a^3 f \cos[e + f x]^{3/2} (d \sin[e + f x])^{7/2}} b (g \cos[e + f x])^{3/2} \sin[e + f x]^{7/2} \\
 & \left(-\frac{1}{(1 - \cos[e + f x]^2)^{1/4} (a + b \sin[e + f x])} 2 (a^2 - 3 b^2) \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \\
 & \quad \left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos[e + f x]} \right) / \right. \right. \\
 & \quad \left. \left((1 - \cos[e + f x]^2)^{3/4} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e + f x]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos[e + f x]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos[e + f x]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right) \cos[e+fx]^2 (a^2+b^2(-1+\cos[e+fx]^2)) \right) - \\
 & \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4} (-1+\cos[e+fx]^2)^{1/4}} \right] - 2 \right. \right. \\
 & \quad \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4} (-1+\cos[e+fx]^2)^{1/4}} \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + \right. \\
 & \quad \left. \frac{i a \cos[e+fx]}{\sqrt{-1+\cos[e+fx]^2}} - \frac{(1+i) \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1+\cos[e+fx]^2)^{1/4}} \right] - \operatorname{Log} \left[\right. \\
 & \quad \left. \left. \sqrt{-a^2+b^2} + \frac{i a \cos[e+fx]}{\sqrt{-1+\cos[e+fx]^2}} + \frac{(1+i) \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1+\cos[e+fx]^2)^{1/4}} \right] \right) \Bigg) / \\
 & \left(\sqrt{a} (-a^2+b^2)^{3/4} \right) \sqrt{\sin[e+fx]} - \\
 & \left(4 a b \sqrt{\sin[e+fx]} \left(b \tan[e+fx] + a \sqrt{1+\tan[e+fx]^2} \right) \right. \\
 & \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + 2 \right. \right. \right. \\
 & \quad \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + \operatorname{Log} \left[\right. \\
 & \quad \left. -a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2-b^2} \tan[e+fx] \right] - \operatorname{Log} \left[\right. \\
 & \quad \left. \left. \left. a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2-b^2} \tan[e+fx] \right] \right) \right) \Bigg) / \\
 & \left(4 \sqrt{2} (a^2-b^2)^{3/4} \right) + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \tan[e+fx]^{5/2} \right) \right] / \left(5 \sqrt{1+\tan[e+fx]^2} \right. \\
 & \left. \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \right. \\
 & \quad \left. \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \right. \\
 & \left. \left. \left. \tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2 (1+\tan[e+fx]^2) \right) \right) \right) \Bigg) /
 \end{aligned}$$

$$\left(\text{Cos}[e + f x]^{5/2} (a + b \text{Sin}[e + f x]) \sqrt{\text{Tan}[e + f x]} (1 + \text{Tan}[e + f x]^2)^{3/2} \right)$$

Problem 1422: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \text{Cos}[e + f x])^{3/2}}{(d \text{Sin}[e + f x])^{9/2} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 688 leaves, 20 steps):

$$\begin{aligned} & \left(2 \sqrt{2} b^3 \sqrt{-a^2 + b^2} g^2 \sqrt{\text{Cos}[e + f x]} \right. \\ & \quad \left. \text{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{d \text{Sin}[e + f x]}}{\sqrt{d} \sqrt{1 + \text{Cos}[e + f x]}}\right], -1\right] \right) / \\ & \left(a^5 d^{9/2} f \sqrt{g \text{Cos}[e + f x]} \right) - \left(2 \sqrt{2} b^3 \sqrt{-a^2 + b^2} g^2 \sqrt{\text{Cos}[e + f x]} \right. \\ & \quad \left. \text{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{d \text{Sin}[e + f x]}}{\sqrt{d} \sqrt{1 + \text{Cos}[e + f x]}}\right], -1\right] \right) / \\ & \left(a^5 d^{9/2} f \sqrt{g \text{Cos}[e + f x]} \right) - \frac{2 g \sqrt{g \text{Cos}[e + f x]}}{7 a d f (d \text{Sin}[e + f x])^{7/2}} + \frac{2 b g \sqrt{g \text{Cos}[e + f x]}}{5 a^2 d^2 f (d \text{Sin}[e + f x])^{5/2}} - \\ & \frac{4 g \sqrt{g \text{Cos}[e + f x]}}{7 a d^3 f (d \text{Sin}[e + f x])^{3/2}} + \frac{2 (a^2 - b^2) g \sqrt{g \text{Cos}[e + f x]}}{3 a^3 d^3 f (d \text{Sin}[e + f x])^{3/2}} + \\ & \frac{8 b g \sqrt{g \text{Cos}[e + f x]}}{5 a^2 d^4 f \sqrt{d \text{Sin}[e + f x]}} - \frac{2 b (a^2 - b^2) g \sqrt{g \text{Cos}[e + f x]}}{a^4 d^4 f \sqrt{d \text{Sin}[e + f x]}} + \\ & \frac{4 g^2 \text{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\text{Sin}[2 e + 2 f x]}}{7 a d^4 f \sqrt{g \text{Cos}[e + f x]} \sqrt{d \text{Sin}[e + f x]}} - \\ & \frac{2 (a^2 - b^2) g^2 \text{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\text{Sin}[2 e + 2 f x]}}{3 a^3 d^4 f \sqrt{g \text{Cos}[e + f x]} \sqrt{d \text{Sin}[e + f x]}} - \\ & \frac{b^2 (a^2 - b^2) g^2 \text{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\text{Sin}[2 e + 2 f x]}}{a^5 d^4 f \sqrt{g \text{Cos}[e + f x]} \sqrt{d \text{Sin}[e + f x]}} \end{aligned}$$

Result (type 6, 1402 leaves):

$$\begin{aligned} & \left((g \text{Cos}[e + f x])^{3/2} \right. \\ & \quad \left(-\frac{2 b (a^2 - 5 b^2) \text{Csc}[e + f x]}{5 a^4} + \frac{2 (a^2 - 7 b^2) \text{Csc}[e + f x]^2}{21 a^3} + \frac{2 b \text{Csc}[e + f x]^3}{5 a^2} - \frac{2 \text{Csc}[e + f x]^4}{7 a} \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sin[e+fx]^4 \tan[e+fx]}{(f(d \sin[e+fx])^{9/2})} - \right. \\
 & \frac{1}{21 a^4 f \cos[e+fx]^{3/2} (d \sin[e+fx])^{9/2}} (g \cos[e+fx])^{3/2} \sin[e+fx]^{9/2} \\
 & \left(- \frac{1}{(1 - \cos[e+fx])^{1/4} (a+b \sin[e+fx])} 2 (2 a^4 + 7 a^2 b^2 - 21 b^4) (a+b \sqrt{1 - \cos[e+fx]^2}) \right. \\
 & \left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \sqrt{\cos[e+fx]} \right) / \right. \right. \\
 & \left. \left((1 - \cos[e+fx])^{3/4} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right) + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right) + 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \cos[e+fx]^2 (a^2 + b^2 (-1 + \cos[e+fx]^2)) \right) - \\
 & \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4} (-1 + \cos[e+fx]^2)^{1/4}} \right] - 2 \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4} (-1 + \cos[e+fx]^2)^{1/4}} \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \right. \right. \right. \\
 & \left. \left. \left. \frac{i a \cos[e+fx]}{\sqrt{-1 + \cos[e+fx]^2}} - \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1 + \cos[e+fx]^2)^{1/4}} \right] - \operatorname{Log} \left[\right. \right. \right. \\
 & \left. \left. \left. \sqrt{-a^2 + b^2} + \frac{i a \cos[e+fx]}{\sqrt{-1 + \cos[e+fx]^2}} + \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1 + \cos[e+fx]^2)^{1/4}} \right] \right) \right) / \\
 & \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \sqrt{\sin[e+fx]} + \left(2 (2 a^3 b - 14 a b^3) \right. \\
 & \left. \sqrt{\sin[e+fx]} (b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2}) \right) \\
 & \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + 2 \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + \operatorname{Log} \left[\right. \right. \right. \\
 & \left. \left. \left. -a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2 - b^2} \tan[e+fx] \right] - \operatorname{Log} \left[\right. \right. \right. \\
 & \left. \left. \left. a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2 - b^2} \tan[e+fx] \right] \right) \right) /
 \end{aligned}$$

$$\left(4 \sqrt{2} (a^2 - b^2)^{3/4} + \left(9 a^2 b \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \right. \right. \right. \\
\left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] \tan[e + f x]^{5/2} \right) / \left(5 \sqrt{1 + \tan[e + f x]^2} \right. \\
\left. \left(-9 a^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + 2 \right. \right. \\
\left. \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + \right. \right. \right. \\
\left. \left. \left. a^2 \text{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right]\right) \right) \right) \\
\left. \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) \Bigg) / \\
\left(\cos[e + f x]^{5/2} (a + b \sin[e + f x]) \sqrt{\tan[e + f x]} (1 + \tan[e + f x]^2)^{3/2} \right)$$

Problem 1423: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2} \sqrt{d \sin[e + f x]}}{a + b \sin[e + f x]} dx$$

Optimal (type 4, 936 leaves, 31 steps):

$$\begin{aligned}
 & - \frac{\sqrt{d} g^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{4 \sqrt{2} b f} - \frac{(a^2 - b^2) \sqrt{d} g^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b^3 f} + \\
 & \frac{\sqrt{d} g^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{4 \sqrt{2} b f} + \frac{(a^2 - b^2) \sqrt{d} g^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b^3 f} + \\
 & \frac{\sqrt{d} g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{8 \sqrt{2} b f} + \\
 & \frac{(a^2 - b^2) \sqrt{d} g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b^3 f} - \\
 & \frac{\sqrt{d} g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{8 \sqrt{2} b f} - \\
 & \frac{(a^2 - b^2) \sqrt{d} g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b^3 f} - \\
 & \left(2 \sqrt{2} a \sqrt{-a+b} \sqrt{a+b} d g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin[e+fx]}\right) / \left(b^3 f \sqrt{d \sin[e+fx]}\right) + \\
 & \left(2 \sqrt{2} a \sqrt{-a+b} \sqrt{a+b} d g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin[e+fx]}\right) / \left(b^3 f \sqrt{d \sin[e+fx]}\right) + \frac{g (g \cos[e+fx])^{3/2} \sqrt{d \sin[e+fx]}}{2 b f} + \\
 & \frac{a g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e+fx]}}{b^2 f \sqrt{\sin[2e+2fx]}}
 \end{aligned}$$

Result (type 6, 2878 leaves):

$$\begin{aligned}
 & \frac{(g \cos[e+fx])^{5/2} \operatorname{Sec}[e+fx] \sqrt{d \sin[e+fx]}}{2 b f} - \\
 & \frac{1}{4 b f \cos[e+fx]^{5/2} \sqrt{\sin[e+fx]}} (g \cos[e+fx])^{5/2} \sqrt{d \sin[e+fx]} \\
 & \left(1 / \left(\left(1 - \cos[e+fx]^2\right) \left(a^2 + b^2 (-1 + \cos[e+fx]^2)\right) (a + b \sin[e+fx])\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & 14 b (a^2 - b^2) \operatorname{Cos}[e + f x]^{3/2} \left(a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \\
 & \left(\left(b \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) / \right. \\
 & \quad \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] + \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) \operatorname{Cos}[e + f x]^2 \right) + \\
 & \left. \left(a \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) / \right. \\
 & \quad \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] + \right. \\
 & \quad \left(-4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2}\right] \right) \operatorname{Cos}[e + f x]^2 \left. \right) \operatorname{Sin}[e + f x]^{3/2} - \\
 & \left(2 a \sqrt{\operatorname{Tan}[e + f x]} \left(b \operatorname{Tan}[e + f x] + a \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right) \left(\left(-2 \operatorname{ArcTan}\left[1 - \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{a}} \right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]}}{\sqrt{a}} \right] - \right. \\
 & \quad \left. \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] + \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \right. \\
 & \quad \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \operatorname{Tan}[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \quad \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \\
 & \quad \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \\
 & \quad \left. \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2)\right) \right) \right) / \\
 & \left(\operatorname{Cos}[e + f x]^{3/2} \sqrt{\operatorname{Sin}[e + f x]} (a + b \operatorname{Sin}[e + f x]) (1 + \operatorname{Tan}[e + f x]^2)^{3/2} \right) +
 \end{aligned}$$

$$\left(4 a \operatorname{Cos}\left[2(e+f x)\right] \sqrt{\operatorname{Tan}\left[e+f x\right]} \left(b \operatorname{Tan}\left[e+f x\right]+a \sqrt{1+\operatorname{Tan}\left[e+f x\right]^2}\right) \right.$$

$$\left. -\frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2}+2 \sqrt{\operatorname{Tan}\left[e+f x\right]}}{\sqrt{2}}\right]}{\sqrt{2} b^2}-\frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2}+2 \sqrt{\operatorname{Tan}\left[e+f x\right]}}{\sqrt{2}}\right]}{\sqrt{2} b^2}+\right.$$

$$\frac{\left(2 a^2-b^2\right) \operatorname{ArcTan}\left[\frac{-\sqrt{2} \sqrt{a}+2\left(a^2-b^2\right)^{1 / 4} \sqrt{\operatorname{Tan}\left[e+f x\right]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2\left(a^2-b^2\right)^{1 / 4}}+$$

$$\frac{\left(2 a^2-b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{a}+2\left(a^2-b^2\right)^{1 / 4} \sqrt{\operatorname{Tan}\left[e+f x\right]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2\left(a^2-b^2\right)^{1 / 4}}+$$

$$\frac{a \operatorname{Log}\left[1-\sqrt{2} \sqrt{\operatorname{Tan}\left[e+f x\right]}+\operatorname{Tan}\left[e+f x\right]\right]}{2 \sqrt{2} b^2}-$$

$$\frac{a \operatorname{Log}\left[1+\sqrt{2} \sqrt{\operatorname{Tan}\left[e+f x\right]}+\operatorname{Tan}\left[e+f x\right]\right]}{2 \sqrt{2} b^2}-$$

$$\left(\left(2 a^2-b^2\right) \operatorname{Log}\left[-a+\sqrt{2} \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \sqrt{\operatorname{Tan}\left[e+f x\right]}-\sqrt{a^2-b^2} \operatorname{Tan}\left[e+f x\right]\right]\right) /$$

$$\left(4 \sqrt{2} \sqrt{a} b^2\left(a^2-b^2\right)^{1 / 4}\right)+$$

$$\left(\left(2 a^2-b^2\right) \operatorname{Log}\left[a+\sqrt{2} \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \sqrt{\operatorname{Tan}\left[e+f x\right]}+\sqrt{a^2-b^2} \operatorname{Tan}\left[e+f x\right]\right]\right) /$$

$$\left(4 \sqrt{2} \sqrt{a} b^2\left(a^2-b^2\right)^{1 / 4}\right)+\frac{\operatorname{Tan}\left[e+f x\right]^{3 / 2}}{b \sqrt{1+\operatorname{Tan}\left[e+f x\right]^2}}+$$

$$\left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4},-\operatorname{Tan}\left[e+f x\right]^2, \frac{\left(-a^2+b^2\right) \operatorname{Tan}\left[e+f x\right]^2}{a^2}\right] \operatorname{Tan}\left[e+f x\right]^{3 / 2}\right) /$$

$$\left(b \sqrt{1+\operatorname{Tan}\left[e+f x\right]^2}\right.$$

$$\left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4},-\operatorname{Tan}\left[e+f x\right]^2,\left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}\left[e+f x\right]^2\right]+2\right.$$

$$\left. 2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4},-\operatorname{Tan}\left[e+f x\right]^2,\left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}\left[e+f x\right]^2\right]+a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4},-\operatorname{Tan}\left[e+f x\right]^2,\left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}\left[e+f x\right]^2\right]\right)$$

$$\operatorname{Tan}\left[e+f x\right]^2\left(-b^2 \operatorname{Tan}\left[e+f x\right]^2+a^2\left(1+\operatorname{Tan}\left[e+f x\right]^2\right)\right)-$$

$$\left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4},-\operatorname{Tan}\left[e+f x\right]^2, \frac{\left(-a^2+b^2\right) \operatorname{Tan}\left[e+f x\right]^2}{a^2}\right] \operatorname{Tan}\left[e+f x\right]^{3 / 2}\right) /$$

$$\left(3 \sqrt{1+\operatorname{Tan}\left[e+f x\right]^2}\right)$$

$$\begin{aligned}
& \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) \Bigg) + \\
& \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \frac{(-a^2 + b^2) \tan[e+f x]^2}{a^2}\right] \right. \\
& \quad \left. \tan[e+f x]^{7/2} \right) \Bigg) / \left(7 b \sqrt{1 + \tan[e+f x]^2} \right. \\
& \quad \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) \Bigg) - \\
& \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \frac{(-a^2 + b^2) \tan[e+f x]^2}{a^2}\right] \right. \\
& \quad \left. \tan[e+f x]^{7/2} \right) \Bigg) / \left(7 \sqrt{1 + \tan[e+f x]^2} \right. \\
& \quad \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+f x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+f x]^2\right] \right) \\
& \quad \left. \tan[e+f x]^2 \right) \left(-b^2 \tan[e+f x]^2 + a^2 (1 + \tan[e+f x]^2) \right) \Bigg) \Bigg) / \\
& \left(\cos[e+f x]^{3/2} \sqrt{\sin[e+f x]} (a + b \sin[e+f x]) (-1 + \tan[e+f x]^2) \right. \\
& \quad \left. \sqrt{1 + \tan[e+f x]^2} \right)
\end{aligned}$$

Problem 1424: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2}}{\sqrt{d \sin[e + f x]} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 572 leaves, 19 steps):

$$\frac{a g^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{\sqrt{2} b^2 \sqrt{d} f} - \frac{a g^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{d \sin[e + f x]}}\right]}{\sqrt{2} b^2 \sqrt{d} f} -$$

$$\frac{a g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e + f x] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{2 \sqrt{2} b^2 \sqrt{d} f} +$$

$$\frac{a g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e + f x] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e + f x]}}{\sqrt{d \sin[e + f x]}}\right]}{2 \sqrt{2} b^2 \sqrt{d} f} +$$

$$\left(2 \sqrt{2} \sqrt{-a + b} \sqrt{a + b} g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}\right) / (b^2 f \sqrt{d \sin[e + f x]}) -$$

$$\left(2 \sqrt{2} \sqrt{-a + b} \sqrt{a + b} g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}}\right], -1\right] \sqrt{\sin[e + f x]}\right) / (b^2 f \sqrt{d \sin[e + f x]}) -$$

$$\frac{g^2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin[e + f x]}}{b d f \sqrt{\sin[2 e + 2 f x]}}$$

Result (type 6, 2299 leaves):

$$\frac{1}{2 f \cos[e + f x]^{5/2} \sqrt{d \sin[e + f x]}}$$

$$(g \cos[e + f x])^{5/2} \sqrt{\sin[e + f x]} \left(2 \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right.$$

$$\left. \left(\left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}}\right] \right) + \right.$$

$$\left. \left. 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}}\right] \right) - \right.$$

$$\left. \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x]\right] + \right.$$

$$\begin{aligned}
& \left. \left(\text{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\text{Tan}[e + f x]} + \sqrt{a^2 - b^2} \text{Tan}[e + f x] \right] \right) / \right. \\
& \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\text{Tan}[e + f x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \text{Tan}[e + f x]^2 \right] \text{Tan}[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \text{Tan}[e + f x]^2} \right. \\
& \left. \left(-7 a^2 \text{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \text{Tan}[e + f x]^2 \right] + \right. \right. \\
& \left. \left. 2 \left(2 (a^2 - b^2) \text{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \text{Tan}[e + f x]^2 \right] + \right. \right. \right. \\
& \left. \left. \left. a^2 \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \text{Tan}[e + f x]^2 \right] \right) \right) \right) \\
& \left. \left. \left. \text{Tan}[e + f x]^2 \right) \left(-b^2 \text{Tan}[e + f x]^2 + a^2 (1 + \text{Tan}[e + f x]^2) \right) \right) \right) / \right. \\
& \left(\text{Cos}[e + f x]^{3/2} \sqrt{\text{Sin}[e + f x]} (a + b \text{Sin}[e + f x]) (1 + \text{Tan}[e + f x]^2)^{3/2} \right) + \\
& \left(2 \text{Cos}[2(e + f x)] \sqrt{\text{Tan}[e + f x]} \left(b \text{Tan}[e + f x] + a \sqrt{1 + \text{Tan}[e + f x]^2} \right) \right) \\
& \left(-\frac{a \text{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\text{Tan}[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \text{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\text{Tan}[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
& \frac{(2 a^2 - b^2) \text{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\text{Tan}[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
& \frac{(2 a^2 - b^2) \text{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\text{Tan}[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
& \frac{a \text{Log} \left[1 - \sqrt{2} \sqrt{\text{Tan}[e + f x]} + \text{Tan}[e + f x] \right]}{2 \sqrt{2} b^2} - \\
& \frac{a \text{Log} \left[1 + \sqrt{2} \sqrt{\text{Tan}[e + f x]} + \text{Tan}[e + f x] \right]}{2 \sqrt{2} b^2} - \\
& \left. \left((2 a^2 - b^2) \text{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\text{Tan}[e + f x]} - \sqrt{a^2 - b^2} \text{Tan}[e + f x] \right] \right) / \right. \\
& \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
& \left. \left((2 a^2 - b^2) \text{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\text{Tan}[e + f x]} + \sqrt{a^2 - b^2} \text{Tan}[e + f x] \right] \right) / \right. \\
& \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\text{Tan}[e + f x]^{3/2}}{b \sqrt{1 + \text{Tan}[e + f x]^2}} +
\end{aligned}$$

$$\begin{aligned}
 & \left(7 a^4 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+f x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \operatorname{Tan}[e+f x]^{3/2} \right) / \\
 & \left(b \sqrt{1+\operatorname{Tan}[e+f x]^2} \right. \\
 & \quad \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad 2 \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad \quad \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \\
 & \quad \left. \operatorname{Tan}[e+f x]^2 \right) \left(-b^2 \operatorname{Tan}[e+f x]^2 + a^2 (1+\operatorname{Tan}[e+f x]^2) \right) \Big) - \\
 & \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+f x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Tan}[e+f x]^{3/2} \right) / \left(3 \sqrt{1+\operatorname{Tan}[e+f x]^2} \right. \\
 & \quad \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad 2 \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad \quad \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \\
 & \quad \left. \operatorname{Tan}[e+f x]^2 \right) \left(-b^2 \operatorname{Tan}[e+f x]^2 + a^2 (1+\operatorname{Tan}[e+f x]^2) \right) \Big) + \\
 & \left(11 a^4 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Tan}[e+f x]^{7/2} \right) / \left(7 b \sqrt{1+\operatorname{Tan}[e+f x]^2} \right. \\
 & \quad \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad 2 \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \quad \quad \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \\
 & \quad \left. \operatorname{Tan}[e+f x]^2 \right) \left(-b^2 \operatorname{Tan}[e+f x]^2 + a^2 (1+\operatorname{Tan}[e+f x]^2) \right) \Big) - \\
 & \left(11 a^2 b \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Tan}[e+f x]^{7/2} \right) / \left(7 \sqrt{1+\operatorname{Tan}[e+f x]^2} \right. \\
 & \quad \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
 & \quad \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \\
 & \quad \left. \left. \left. \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right] \right] \right] \right) / \\
 & \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (-1 + \tan[e + f x]^2) \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan[e + f x]^2} \right] \right] \right)
 \end{aligned}$$

Problem 1425: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2}}{(d \sin[e + f x])^{3/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 616 leaves, 20 steps):

$$\begin{aligned}
 & - \frac{g^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b d^{3/2} f} + \frac{g^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b d^{3/2} f} + \\
 & \frac{g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b d^{3/2} f} - \\
 & \frac{g^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \cot[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b d^{3/2} f} - \frac{2 g (g \cos[e+fx])^{3/2}}{a d f \sqrt{d \sin[e+fx]}} - \\
 & \left(2 \sqrt{2} \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin[e+fx]} \right) / (a b d f \sqrt{d \sin[e+fx]}) + \\
 & \left(2 \sqrt{2} \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin[e+fx]} \right) / (a b d f \sqrt{d \sin[e+fx]}) - \\
 & \frac{2 g^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin[e+fx]}}{a d^2 f \sqrt{\sin[2e+2fx]}}
 \end{aligned}$$

Result (type 6, 2873 leaves):

$$\begin{aligned}
 & - \frac{2 (g \cos[e+fx])^{5/2} \tan[e+fx]}{a f (d \sin[e+fx])^{3/2}} + \\
 & \frac{1}{a f \cos[e+fx]^{5/2} (d \sin[e+fx])^{3/2}} (g \cos[e+fx])^{5/2} \sin[e+fx]^{3/2} \\
 & \left(\left(1 / \left((1 - \cos[e+fx]^2) (a^2 + b^2 (-1 + \cos[e+fx]^2)) (a + b \sin[e+fx]) \right) \right) \right) \\
 & 14 a (a^2 - b^2) \cos[e+fx]^{3/2} \left(a + b \sqrt{1 - \cos[e+fx]^2} \right) \\
 & \left(\left(b \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \sqrt{1 - \cos[e+fx]^2} \right) / \right. \\
 & \quad \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] + \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2}\right] \right) \cos[e+fx]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) / \\
 & \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + \right. \\
 & \left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] + (a^2-b^2) \operatorname{AppellF1} \left[\right. \right. \\
 & \left. \left. \frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2+b^2} \right] \right) \cos [e+f x]^2 \right) \sin [e+f x]^{3/2} - \\
 & \left(4 b \sqrt{\tan [e+f x]} \left(b \tan [e+f x] + a \sqrt{1+\tan [e+f x]^2} \right) \left(\left(-2 \operatorname{ArcTan} \left[1 - \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]} - \sqrt{a^2-b^2} \tan [e+f x] \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]} + \sqrt{a^2-b^2} \tan [e+f x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+f x]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right) \tan [e+f x]^{3/2} \right) / \left(3 \sqrt{1+\tan [e+f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + 2 \right. \right. \\
 & \left. \left((a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] \right) \right) \right) \right) / \\
 & \left(\cos [e+f x]^{3/2} \sqrt{\sin [e+f x]} (a+b \sin [e+f x]) (1+\tan [e+f x]^2)^{3/2} \right) + \\
 & \left(2 b \cos [2 (e+f x)] \sqrt{\tan [e+f x]} \left(b \tan [e+f x] + a \sqrt{1+\tan [e+f x]^2} \right) \right) \\
 & \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2}+2 \sqrt{\tan [e+f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2}+2 \sqrt{\tan [e+f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
 & \left. \frac{(2 a^2-b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a}+2 (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2-b^2)^{1/4}} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & (4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}) + \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & (4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}) + \frac{\operatorname{Tan}[e+fx]^{3/2}}{b\sqrt{1 + \operatorname{Tan}[e+fx]^2}} + \\
 & \left(7a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2} \right) / \\
 & \left(b\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \left. \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) - \\
 & \left(7a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e+fx]^{3/2} \right) / \left(3\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \left. \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) + \\
 & \left(11a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{\tan[e + f x]^{7/2}}{7 b \sqrt{1 + \tan[e + f x]^2}} \right) \right/ \left(\left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + 2 \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + \right. \\
 & \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] \right) \\
 & \quad \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) - \\
 & \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \frac{(-a^2 + b^2) \tan[e + f x]^2}{a^2} \right] \right. \\
 & \left. \frac{\tan[e + f x]^{7/2}}{7 \sqrt{1 + \tan[e + f x]^2}} \right) \left(\left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + 2 \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] + \right. \\
 & \quad \quad \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e + f x]^2\right] \right) \\
 & \quad \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) \right/ \\
 & \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (-1 + \tan[e + f x]^2) \right. \\
 & \quad \left. \sqrt{1 + \tan[e + f x]^2} \right)
 \end{aligned}$$

Problem 1426: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2}}{(d \sin[e + f x])^{5/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 359 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{2 g (g \cos [e+f x])^{3/2}}{3 a d f (d \sin [e+f x])^{3/2}} + \frac{2 b g (g \cos [e+f x])^{3/2}}{a^2 d^2 f \sqrt{d \sin [e+f x]}} + \\
 & \left(2 \sqrt{2} \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g} \sqrt{1+\sin [e+f x]}}\right], -1\right] \right. \\
 & \left. \sqrt{\sin [e+f x]} \right) / \left(a^2 d^2 f \sqrt{d \sin [e+f x]} \right) - \\
 & \left(2 \sqrt{2} \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g} \sqrt{1+\sin [e+f x]}}\right], -1\right] \right. \\
 & \left. \sqrt{\sin [e+f x]} \right) / \left(a^2 d^2 f \sqrt{d \sin [e+f x]} \right) + \\
 & \frac{2 b g^2 \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[e-\frac{\pi}{4}+f x, 2\right] \sqrt{d \sin [e+f x]}}{a^2 d^3 f \sqrt{\sin [2 e+2 f x]}}
 \end{aligned}$$

Result (type 6, 2923 leaves):

$$\begin{aligned}
 & \left((g \cos [e+f x])^{5/2} \left(\frac{2 b \cot [e+f x]}{a^2} - \frac{2 \cot [e+f x] \csc [e+f x]}{3 a} \right) \sin [e+f x] \tan [e+f x]^2 \right) / \\
 & \left(f (d \sin [e+f x])^{5/2} \right) - \frac{1}{a^2 f \cos [e+f x]^{5/2} (d \sin [e+f x])^{5/2}} \\
 & (g \cos [e+f x])^{5/2} \sin [e+f x]^{5/2} \left(\left(28 a b (a^2 - b^2) \cos [e+f x]^{3/2} \left(a + b \sqrt{1 - \cos [e+f x]^2} \right) \right. \right. \\
 & \left. \left(\left(b \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \sqrt{1 - \cos [e+f x]^2} \right) / \right. \right. \\
 & \left. \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + \right. \right. \\
 & \left. \left(4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \right) \cos [e+f x]^2 \right) + \\
 & \left. \left(a \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \right) / \right. \\
 & \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + \right. \right. \\
 & \left. \left(-4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \right) \cos [e+f x]^2 \right) \right) \\
 & \sin [e+f x]^{3/2} \left. \right) / \left(3 (1 - \cos [e+f x]^2) (a^2 + b^2 (-1 + \cos [e+f x]^2)) \right) \\
 & (a + b \sin [e+f x]) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 (a^2 - 2 b^2) \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right. \\
 & \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + \right. \right. \\
 & \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e + f x]^2} \right. \\
 & \quad \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
 & \quad \left. \left((a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right) \right) / \\
 & \quad \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) / \\
 & \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (1 + \tan[e + f x]^2)^{3/2} \right) + \\
 & \left(2 b^2 \cos[2(e + f x)] \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right) \\
 & \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \left. \frac{a \operatorname{Log} \left[1 - \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[e + f x]} + \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b^2} - \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\operatorname{Tan}[e + f x]^{3/2}}{b \sqrt{1 + \operatorname{Tan}[e + f x]^2}} + \\
 & \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \operatorname{Tan}[e + f x]^{3/2} \right) / \\
 & \left(b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) - \\
 & \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) + \\
 & \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{7/2} \right) / \left(7 b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \\
& \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right) - \\
& \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
& \left. \tan[e+fx]^{7/2}\right) / \left(7 \sqrt{1 + \tan[e+fx]^2}\right. \\
& \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \\
& \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \right. \\
& \left. \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right]\right) \right. \\
& \left. \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right)\right) / \\
& \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (-1 + \tan[e+fx]^2) \right. \\
& \left. \sqrt{1 + \tan[e+fx]^2}\right)
\end{aligned}$$

Problem 1427: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{5/2}}{(d \sin[e+fx])^{7/2} (a + b \sin[e+fx])} dx$$

Optimal (type 4, 519 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{2 g (g \cos [e+f x])^{3/2}}{5 a d f (d \sin [e+f x])^{5/2}} + \frac{2 b g (g \cos [e+f x])^{3/2}}{3 a^2 d^2 f (d \sin [e+f x])^{3/2}} - \\
 & \frac{4 g (g \cos [e+f x])^{3/2}}{5 a d^3 f \sqrt{d \sin [e+f x]}} + \frac{2 (a^2 - b^2) g (g \cos [e+f x])^{3/2}}{a^3 d^3 f \sqrt{d \sin [e+f x]}} - \\
 & \left(2 \sqrt{2} b \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g} \sqrt{1+\sin [e+f x]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin [e+f x]} \right) / \left(a^3 d^3 f \sqrt{d \sin [e+f x]} \right) + \\
 & \left(2 \sqrt{2} b \sqrt{-a+b} \sqrt{a+b} g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e+f x]}}{\sqrt{g} \sqrt{1+\sin [e+f x]}}\right], -1\right] \right. \\
 & \quad \left. \sqrt{\sin [e+f x]} \right) / \left(a^3 d^3 f \sqrt{d \sin [e+f x]} \right) - \\
 & \frac{4 g^2 \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin [e+f x]}}{5 a d^4 f \sqrt{\sin [2 e + 2 f x]}} + \\
 & \left(2 (a^2 - b^2) g^2 \sqrt{g \cos [e+f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin [e+f x]} \right) / \\
 & \left(a^3 d^4 f \sqrt{\sin [2 e + 2 f x]} \right)
 \end{aligned}$$

Result (type 6, 2995 leaves):

$$\begin{aligned}
 & \left((g \cos [e+f x])^{5/2} \left(\frac{2 (3 a^2 \cos [e+f x] - 5 b^2 \cos [e+f x]) \operatorname{Csc}[e+f x]}{5 a^3} + \right. \right. \\
 & \quad \left. \left. \frac{2 b \operatorname{Cot}[e+f x] \operatorname{Csc}[e+f x]}{3 a^2} - \frac{2 \operatorname{Cot}[e+f x] \operatorname{Csc}[e+f x]^2}{5 a} \right) \sin [e+f x]^2 \tan [e+f x]^2 \right) / \\
 & \left(f (d \sin [e+f x])^{7/2} \right) + \frac{1}{5 a^3 f \cos [e+f x]^{5/2} (d \sin [e+f x])^{7/2}} (g \cos [e+f x])^{5/2} \\
 & \sin [e+f x]^{7/2} \left(- \left(\left(14 (a^2 - b^2) (6 a^3 - 10 a b^2) \cos [e+f x]^{3/2} \left(a + b \sqrt{1 - \cos [e+f x]^2} \right) \right. \right. \right. \\
 & \quad \left. \left(\left(b \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \sqrt{1 - \cos [e+f x]^2} \right) \right) / \right. \\
 & \quad \left(-7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + \right. \\
 & \quad \left(4 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] + (a^2 - b^2) \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \right) \cos [e+f x]^2 \right) + \right. \\
 & \quad \left. \left(a \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e+f x]^2, \frac{b^2 \cos [e+f x]^2}{-a^2 + b^2}\right] \right) \right) / \left(7 (a^2 - b^2) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \left(-4b^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right]\right) \cos[e+fx]^2 \Bigg) \sin[e+fx]^{3/2} \Bigg) / \\
& \left(3(1-\cos[e+fx]^2)(a^2+b^2(-1+\cos[e+fx]^2))(a+b\sin[e+fx])\right) \Bigg) + \\
& \left(2(8a^2b-10b^3)\sqrt{\tan[e+fx]}(b\tan[e+fx]+a\sqrt{1+\tan[e+fx]^2})\right. \\
& \left(\left(-2\text{ArcTan}\left[1-\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] + \right. \right. \\
& \left. \left. 2\text{ArcTan}\left[1+\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] - \right. \right. \\
& \left. \left. \text{Log}\left[-a+\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}-\sqrt{a^2-b^2}\tan[e+fx]\right] + \right. \right. \\
& \left. \left. \text{Log}\left[a+\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}+\sqrt{a^2-b^2}\tan[e+fx]\right]\right)\right) / \\
& \left(4\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\right) + \left(7a^2b \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \right. \right. \\
& \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] \tan[e+fx]^{3/2}\right) / \left(3\sqrt{1+\tan[e+fx]^2}\right. \\
& \left(-7a^2 \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + 2 \right. \\
& \left. \left(2(a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + \right. \right. \\
& \left. \left. a^2 \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]\right) \right. \\
& \left. \left. \tan[e+fx]^2\right) (-b^2\tan[e+fx]^2+a^2(1+\tan[e+fx]^2))\right) \Bigg) \Bigg) / \\
& \left(\cos[e+fx]^{3/2}\sqrt{\sin[e+fx]}(a+b\sin[e+fx])(1+\tan[e+fx]^2)^{3/2}\right) + \\
& \left(2(-3a^2b+5b^3)\cos[2(e+fx)]\sqrt{\tan[e+fx]}\right. \\
& \left.(b\tan[e+fx]+a\sqrt{1+\tan[e+fx]^2})\right. \\
& \left(-\frac{a\text{ArcTan}\left[\frac{-\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2}b^2} - \frac{a\text{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2}b^2} + \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} + \right. \\
 & \left. (2a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} + \frac{\operatorname{Tan}[e+fx]^{3/2}}{b\sqrt{1 + \operatorname{Tan}[e+fx]^2}} + \right. \\
 & \left. \left(7a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2} \right) / \right. \\
 & \left. \left(b\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \right. \\
 & \left. \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) - \\
 & \left(7a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e+fx]^{3/2} \right) / \left(3\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \\
 & \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right)
 \end{aligned}$$

$$\left(\begin{aligned} & \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \Big) + \\ & \left(11 a^4 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right. \\ & \tan[e+fx]^{7/2} \Big) / \left(7 b \sqrt{1 + \tan[e+fx]^2} \right. \\ & \left. \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \right. \\ & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) + \right. \\ & \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \\ & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) - \\ & \left(11 a^2 b \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right. \\ & \tan[e+fx]^{7/2} \Big) / \left(7 \sqrt{1 + \tan[e+fx]^2} \right. \\ & \left. \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \right. \\ & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) + \right. \\ & \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \\ & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) \Big) / \end{aligned} \right) \\ \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (-1 + \tan[e+fx]^2) \sqrt{1 + \tan[e+fx]^2} \right)$$

Problem 1428: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{5/2}}{(d \sin[e+fx])^{9/2} (a + b \sin[e+fx])} dx$$

Optimal (type 4, 612 leaves, 18 steps):

$$\begin{aligned}
 & -\frac{2g(g\cos[e+fx])^{3/2}}{7adf(d\sin[e+fx])^{7/2}} + \frac{2bg(g\cos[e+fx])^{3/2}}{5a^2d^2f(d\sin[e+fx])^{5/2}} - \frac{8g(g\cos[e+fx])^{3/2}}{21ad^3f(d\sin[e+fx])^{3/2}} + \\
 & \frac{2(a^2-b^2)g(g\cos[e+fx])^{3/2}}{3a^3d^3f(d\sin[e+fx])^{3/2}} + \frac{4bg(g\cos[e+fx])^{3/2}}{5a^2d^4f\sqrt{d\sin[e+fx]}} - \frac{2b(a^2-b^2)g(g\cos[e+fx])^{3/2}}{a^4d^4f\sqrt{d\sin[e+fx]}} + \\
 & \left(2\sqrt{2}b^2\sqrt{-a+b}\sqrt{a+b}g^{5/2}\text{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \text{ArcSin}\left[\frac{\sqrt{g\cos[e+fx]}}{\sqrt{g}\sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \left. \sqrt{\sin[e+fx]} \right) / \left(a^4d^4f\sqrt{d\sin[e+fx]} \right) - \\
 & \left(2\sqrt{2}b^2\sqrt{-a+b}\sqrt{a+b}g^{5/2}\text{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \text{ArcSin}\left[\frac{\sqrt{g\cos[e+fx]}}{\sqrt{g}\sqrt{1+\sin[e+fx]}}\right], -1\right] \right. \\
 & \left. \sqrt{\sin[e+fx]} \right) / \left(a^4d^4f\sqrt{d\sin[e+fx]} \right) + \\
 & \frac{4bg^2\sqrt{g\cos[e+fx]}\text{EllipticE}\left[e-\frac{\pi}{4}+fx, 2\right]\sqrt{d\sin[e+fx]}}{5a^2d^5f\sqrt{\sin[2e+2fx]}} - \\
 & \left(\frac{2b(a^2-b^2)g^2\sqrt{g\cos[e+fx]}\text{EllipticE}\left[e-\frac{\pi}{4}+fx, 2\right]\sqrt{d\sin[e+fx]}}{a^4d^5f\sqrt{\sin[2e+2fx]}} \right) /
 \end{aligned}$$

Result (type 6, 3037 leaves):

$$\begin{aligned}
 & \left((g\cos[e+fx])^{5/2} \left(-\frac{2(3a^2b\cos[e+fx]-5b^3\cos[e+fx])\csc[e+fx]}{5a^4} + \right. \right. \\
 & \frac{2(3a^2\cos[e+fx]-7b^2\cos[e+fx])\csc[e+fx]^2}{21a^3} + \frac{2b\cot[e+fx]\csc[e+fx]^2}{5a^2} - \\
 & \left. \left. \frac{2\cot[e+fx]\csc[e+fx]^3}{7a} \right) \sin[e+fx]^3 \tan[e+fx]^2 \right) / \left(f(d\sin[e+fx])^{9/2} \right) - \\
 & \frac{1}{5a^4f\cos[e+fx]^{5/2}(d\sin[e+fx])^{9/2}} b(g\cos[e+fx])^{5/2}\sin[e+fx]^{9/2} \\
 & \left(- \left(\left(14(a^2-b^2)(6a^3-10ab^2)\cos[e+fx]^{3/2}(a+b\sqrt{1-\cos[e+fx]^2}) \right. \right. \right. \\
 & \left. \left(\left(b\text{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right]\sqrt{1-\cos[e+fx]^2} \right) / \right. \right. \\
 & \left. \left(-7(a^2-b^2)\text{AppellF1}\left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \left. \left(4b^2\text{AppellF1}\left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] + (a^2-b^2) \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2\cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \left(a \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) / \left(7(a^2-b^2) \right. \\
& \quad \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \left(-4b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \right. \right. \\
& \quad \quad \left. \frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{4}, 1, \right. \\
& \quad \quad \left. \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \cos[e+fx]^2 \left. \right) \sin[e+fx]^{3/2} \left. \right) / \\
& \left(3(1-\cos[e+fx]^2)(a^2+b^2(-1+\cos[e+fx]^2))(a+b\sin[e+fx]) \right) + \\
& \left(2(8a^2b-10b^3)\sqrt{\tan[e+fx]} \left(b \tan[e+fx] + a\sqrt{1+\tan[e+fx]^2} \right) \right. \\
& \left(\left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] + \right. \right. \\
& \quad \left. \left. 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]} - \sqrt{a^2-b^2}\tan[e+fx]\right] + \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]} + \sqrt{a^2-b^2}\tan[e+fx]\right] \right) \right) / \\
& \left(4\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4} + \left(7a^2b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2 \right) \tan[e+fx]^{3/2} \right) / \left(3\sqrt{1+\tan[e+fx]^2} \right. \\
& \quad \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2 \right] + 2 \right. \\
& \quad \left(2(a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2 \right] \right) \\
& \quad \left. \left. \left. \tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2(1+\tan[e+fx]^2) \right) \right) \right) / \\
& \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a+b\sin[e+fx]) (1+\tan[e+fx]^2)^{3/2} \right) + \\
& \left(2(-3a^2b+5b^3)\cos[2(e+fx)]\sqrt{\tan[e+fx]} \right. \\
& \quad \left. \left(b \tan[e+fx] + a\sqrt{1+\tan[e+fx]^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2}+2\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} + \right. \\
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2}\sqrt{a}+2(a^2-b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2-b^2)^{1/4}} + \\
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2}\sqrt{a}+2(a^2-b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2-b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \left. \frac{a \operatorname{Log}\left[1 + \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \right. \\
 & \left. \frac{\left((2a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right]\right)}{\left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}\right)} + \right. \\
 & \left. \frac{\left((2a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right]\right)}{\left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}\right)} + \frac{\operatorname{Tan}[e+fx]^{3/2}}{b\sqrt{1 + \operatorname{Tan}[e+fx]^2}} + \right. \\
 & \left. \frac{\left(7a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2}\right)}{\left(b\sqrt{1 + \operatorname{Tan}[e+fx]^2}\right)} \right. \\
 & \left. \frac{\left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2\right)}{\left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right.} \right. \\
 & \left. \frac{a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right]}{\operatorname{Tan}[e+fx]^2} \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2)\right) - \\
 & \left. \frac{\left(7a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2}\right)}{\left(3\sqrt{1 + \operatorname{Tan}[e+fx]^2}\right)} \right. \\
 & \left. \frac{\left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2\right)}{\right.}
 \end{aligned}$$

$$\begin{aligned}
& \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \quad \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \\
& \quad \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) + \\
& \left(11 a^4 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \frac{(-a^2 + b^2) \tan[e + f x]^2}{a^2} \right] \right. \\
& \quad \left. \tan[e + f x]^{7/2} \right) / \left(7 b \sqrt{1 + \tan[e + f x]^2} \right) \\
& \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \\
& \quad \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) - \\
& \left(11 a^2 b \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \frac{(-a^2 + b^2) \tan[e + f x]^2}{a^2} \right] \right. \\
& \quad \left. \tan[e + f x]^{7/2} \right) / \left(7 \sqrt{1 + \tan[e + f x]^2} \right) \\
& \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \quad \quad \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \\
& \quad \left. \tan[e + f x]^2 \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) / \\
& \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (-1 + \tan[e + f x]^2) \right. \\
& \quad \left. \sqrt{1 + \tan[e + f x]^2} \right)
\end{aligned}$$

Problem 1429: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e + f x])^{5/2}}{(d \sin[e + f x])^{11/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 822 leaves, 24 steps):

$$\begin{aligned} & -\frac{2 g (g \cos [e + f x])^{3/2}}{9 a d f (d \sin [e + f x])^{9/2}} + \frac{2 b g (g \cos [e + f x])^{3/2}}{7 a^2 d^2 f (d \sin [e + f x])^{7/2}} - \frac{4 g (g \cos [e + f x])^{3/2}}{15 a d^3 f (d \sin [e + f x])^{5/2}} + \\ & \frac{2 (a^2 - b^2) g (g \cos [e + f x])^{3/2}}{5 a^3 d^3 f (d \sin [e + f x])^{5/2}} + \frac{8 b g (g \cos [e + f x])^{3/2}}{21 a^2 d^4 f (d \sin [e + f x])^{3/2}} - \frac{2 b (a^2 - b^2) g (g \cos [e + f x])^{3/2}}{3 a^4 d^4 f (d \sin [e + f x])^{3/2}} - \\ & \frac{8 g (g \cos [e + f x])^{3/2}}{15 a d^5 f \sqrt{d \sin [e + f x]}} + \frac{4 (a^2 - b^2) g (g \cos [e + f x])^{3/2}}{5 a^3 d^5 f \sqrt{d \sin [e + f x]}} + \frac{2 b^2 (a^2 - b^2) g (g \cos [e + f x])^{3/2}}{a^5 d^5 f \sqrt{d \sin [e + f x]}} - \\ & \left(2 \sqrt{2} b^3 \sqrt{-a + b} \sqrt{a + b} g^{5/2} \operatorname{EllipticPi}\left[-\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e + f x]}}{\sqrt{g} \sqrt{1 + \sin [e + f x]}}\right], -1\right] \right. \\ & \left. \sqrt{\sin [e + f x]} \right) / \left(a^5 d^5 f \sqrt{d \sin [e + f x]} \right) + \\ & \left(2 \sqrt{2} b^3 \sqrt{-a + b} \sqrt{a + b} g^{5/2} \operatorname{EllipticPi}\left[\frac{\sqrt{-a + b}}{\sqrt{a + b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos [e + f x]}}{\sqrt{g} \sqrt{1 + \sin [e + f x]}}\right], -1\right] \right. \\ & \left. \sqrt{\sin [e + f x]} \right) / \left(a^5 d^5 f \sqrt{d \sin [e + f x]} \right) - \\ & \frac{8 g^2 \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin [e + f x]}}{15 a d^6 f \sqrt{\sin [2 e + 2 f x]}} + \\ & \left(4 (a^2 - b^2) g^2 \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin [e + f x]} \right) / \\ & \left(5 a^3 d^6 f \sqrt{\sin [2 e + 2 f x]} \right) + \\ & \left(2 b^2 (a^2 - b^2) g^2 \sqrt{g \cos [e + f x]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{d \sin [e + f x]} \right) / \\ & \left(a^5 d^6 f \sqrt{\sin [2 e + 2 f x]} \right) \end{aligned}$$

Result (type 6, 3111 leaves):

$$\begin{aligned} & \left((g \cos [e + f x])^{5/2} \left(\frac{1}{15 a^5} 2 (2 a^4 \cos [e + f x] + 9 a^2 b^2 \cos [e + f x] - 15 b^4 \cos [e + f x]) \operatorname{Csc}[e + f x] - \right. \right. \\ & \frac{2 (3 a^2 b \cos [e + f x] - 7 b^3 \cos [e + f x]) \operatorname{Csc}[e + f x]^2}{21 a^4} + \\ & \frac{2 (a^2 \cos [e + f x] - 3 b^2 \cos [e + f x]) \operatorname{Csc}[e + f x]^3}{15 a^3} + \frac{2 b \cot [e + f x] \operatorname{Csc}[e + f x]^3}{7 a^2} - \\ & \left. \left. \frac{2 \cot [e + f x] \operatorname{Csc}[e + f x]^4}{9 a} \right) \sin [e + f x]^4 \tan [e + f x]^2 \right) / \\ & \left(f (d \sin [e + f x])^{11/2} \right) + \frac{1}{15 a^5 f \cos [e + f x]^{5/2} (d \sin [e + f x])^{11/2}} \\ & (g \cos [e + f x])^{5/2} \sin [e + f x]^{11/2} \end{aligned}$$

$$\begin{aligned}
& \left(- \left(\left(14 (a^2 - b^2) (4 a^5 + 18 a^3 b^2 - 30 a b^4) \cos [e + f x]^{3/2} \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \right. \right. \right. \\
& \quad \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos [e + f x]^2} \right) / \right. \\
& \quad \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
& \quad \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \\
& \quad \left. \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) + \right. \\
& \quad \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) / \left(7 (a^2 - b^2) \right. \\
& \quad \left. \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{4}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) \sin [e + f x]^{3/2} \Big/ \\
& \quad \left. \left(3 (1 - \cos [e + f x]^2) (a^2 + b^2 (-1 + \cos [e + f x]^2)) (a + b \sin [e + f x]) \right) \right) + \\
& \left(2 (2 a^4 b + 24 a^2 b^3 - 30 b^5) \sqrt{\tan [e + f x]} \left(b \tan [e + f x] + a \sqrt{1 + \tan [e + f x]^2} \right) \right. \\
& \quad \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]}}{\sqrt{a}} \right] + \right. \right. \\
& \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]}}{\sqrt{a}} \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]} - \sqrt{a^2 - b^2} \tan [e + f x] \right] + \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan [e + f x]} + \sqrt{a^2 - b^2} \tan [e + f x] \right] \right) \Big/ \right. \\
& \quad \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e + f x]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [e + f x]^2 \right] \tan [e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan [e + f x]^2} \right. \\
& \quad \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e + f x]^2 \right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan [e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e + f x]^2 \right] + \right. \\
& \quad \left. \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan [e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e + f x]^2 \right] \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \left. \tan [e+fx]^2 \right) \left(-b^2 \tan [e+fx]^2 + a^2 \left(1 + \tan [e+fx]^2\right)\right) \right) \right) \right) \right) \right) \Big/ \\
 & \left(\cos [e+fx]^{3/2} \sqrt{\sin [e+fx]} (a+b \sin [e+fx]) \left(1 + \tan [e+fx]^2\right)^{3/2} \right) + \\
 & \left(2 \left(-2 a^4 b - 9 a^2 b^3 + 15 b^5\right) \cos [2(e+fx)] \sqrt{\tan [e+fx]} \right. \\
 & \left. \left(b \tan [e+fx] + a \sqrt{1 + \tan [e+fx]^2} \right) \right. \\
 & \left. \left(-\frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2}+2\sqrt{\tan [e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\tan [e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} \right) + \right. \\
 & \left. \frac{\left(2 a^2 - b^2\right) \operatorname{ArcTan}\left[\frac{-\sqrt{2} \sqrt{a} + 2\left(a^2 - b^2\right)^{1/4} \sqrt{\tan [e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 \left(a^2 - b^2\right)^{1/4}} + \right. \\
 & \left. \frac{\left(2 a^2 - b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} + 2\left(a^2 - b^2\right)^{1/4} \sqrt{\tan [e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} \sqrt{a} b^2 \left(a^2 - b^2\right)^{1/4}} + \right. \\
 & \left. \frac{a \log \left[1 - \sqrt{2} \sqrt{\tan [e+fx]} + \tan [e+fx]\right]}{2 \sqrt{2} b^2} - \right. \\
 & \left. \frac{a \log \left[1 + \sqrt{2} \sqrt{\tan [e+fx]} + \tan [e+fx]\right]}{2 \sqrt{2} b^2} \right. \\
 & \left. \left(\left(2 a^2 - b^2\right) \log \left[-a + \sqrt{2} \sqrt{a} \left(a^2 - b^2\right)^{1/4} \sqrt{\tan [e+fx]} - \sqrt{a^2 - b^2} \tan [e+fx]\right] \right) \Big/ \right. \\
 & \left. \left(4 \sqrt{2} \sqrt{a} b^2 \left(a^2 - b^2\right)^{1/4} \right) + \right. \\
 & \left. \left(\left(2 a^2 - b^2\right) \log \left[a + \sqrt{2} \sqrt{a} \left(a^2 - b^2\right)^{1/4} \sqrt{\tan [e+fx]} + \sqrt{a^2 - b^2} \tan [e+fx]\right] \right) \Big/ \right. \\
 & \left. \left(4 \sqrt{2} \sqrt{a} b^2 \left(a^2 - b^2\right)^{1/4} \right) + \frac{\tan [e+fx]^{3/2}}{b \sqrt{1 + \tan [e+fx]^2}} + \right. \\
 & \left. \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+fx]^2, \frac{\left(-a^2 + b^2\right) \tan [e+fx]^2}{a^2}\right] \tan [e+fx]^{3/2} \right) \Big/ \right. \\
 & \left. \left(b \sqrt{1 + \tan [e+fx]^2} \right) \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan [e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan [e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left(2 \left(a^2 - b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan [e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan [e+fx]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan [e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan [e+fx]^2\right] \right) \right)
 \end{aligned}$$

$$\left. \sqrt{1 + \tan[e + fx]^2} \right)$$

Problem 1430: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(d \sin[e + fx])^{5/2}}{\sqrt{g \cos[e + fx]} (a + b \sin[e + fx])} dx$$

Optimal (type 4, 616 leaves, 19 steps):

$$\frac{a d^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{g \cos[e+fx]}}\right]}{\sqrt{2} b^2 f \sqrt{g}} - \frac{a d^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{g \cos[e+fx]}}\right]}{\sqrt{2} b^2 f \sqrt{g}} - \left(2 \sqrt{2} a^2 d^{5/2} \sqrt{\cos[e + fx]} \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e + fx]}}{\sqrt{d} \sqrt{1 + \cos[e + fx]}}\right], -1\right]\right) / \left(b^2 \sqrt{-a^2 + b^2} f \sqrt{g \cos[e + fx]}\right) + \left(2 \sqrt{2} a^2 d^{5/2} \sqrt{\cos[e + fx]} \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e + fx]}}{\sqrt{d} \sqrt{1 + \cos[e + fx]}}\right], -1\right]\right) / \left(b^2 \sqrt{-a^2 + b^2} f \sqrt{g \cos[e + fx]}\right) - \frac{a d^{5/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e+fx]}}{\sqrt{g \cos[e+fx]}} + \sqrt{d} \tan[e + fx]\right]}{2 \sqrt{2} b^2 f \sqrt{g}} + \frac{a d^{5/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \sin[e+fx]}}{\sqrt{g \cos[e+fx]}} + \sqrt{d} \tan[e + fx]\right]}{2 \sqrt{2} b^2 f \sqrt{g}} - \frac{d^2 \sqrt{g \cos[e + fx]} \sqrt{d \sin[e + fx]}}{b f g} + \frac{d^3 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{\sin[2e + 2fx]}}{2 b f \sqrt{g \cos[e + fx]} \sqrt{d \sin[e + fx]}}$$

Result (type 6, 1790 leaves):

$$\frac{1}{2 f \sqrt{g \cos[e + fx]} \sin[e + fx]^{5/2}} \left(\sqrt{\cos[e + fx]} (d \sin[e + fx])^{5/2} \left(- \left(\left(2 \cos[2(e + fx)] \sqrt{\sin[e + fx]} \right) \left(b \tan[e + fx] + a \sqrt{1 + \tan[e + fx]^2} \right) \left(- \frac{a \operatorname{ArcTan}\left[\frac{-\sqrt{2} + 2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} - \right. \right. \right. \right.$$

$$\begin{aligned}
& \frac{a \operatorname{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2} b^2} + \frac{\sqrt{a} (2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} b^2 (a^2 - b^2)^{3/4}} + \\
& \frac{\sqrt{a} (2 a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} b^2 (a^2 - b^2)^{3/4}} - \\
& \frac{a \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b^2} + \\
& \frac{a \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b^2} + \left(\sqrt{a} (2 a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} \right. \right. \\
& \left. \left. (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e+fx]\right]\right) / \left(4 \sqrt{2} b^2 (a^2 - b^2)^{3/4}\right) - \\
& \left(\sqrt{a} (2 a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e+fx]\right]\right) / \\
& \left(4 \sqrt{2} b^2 (a^2 - b^2)^{3/4}\right) - \frac{\sqrt{\operatorname{Tan}[e+fx]}}{b \sqrt{1 + \operatorname{Tan}[e+fx]^2}} - \left(5 a^4 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
& \left. \left. -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e+fx]^2}{a^2}\right] \sqrt{\operatorname{Tan}[e+fx]}\right) / \left(b \sqrt{1 + \operatorname{Tan}[e+fx]^2}\right) \\
& \left(-5 a^2 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right] + \right. \\
& \left. 2 \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
& \left. \left. a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right]\right) \right. \\
& \left. \operatorname{Tan}[e+fx]^2\right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2 (1 + \operatorname{Tan}[e+fx]^2)\right) + \\
& \left(9 a^4 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e+fx]^2}{a^2}\right] \right. \\
& \left. \operatorname{Tan}[e+fx]^{5/2}\right) / \left(5 b \sqrt{1 + \operatorname{Tan}[e+fx]^2}\right) \\
& \left(-9 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right] + \right. \\
& \left. 2 \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
& \left. \left. a^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e+fx]^2\right]\right) \right. \\
& \left. \operatorname{Tan}[e+fx]^2\right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2 (1 + \operatorname{Tan}[e+fx]^2)\right) \Big) \Big) /
\end{aligned}$$

$$\begin{aligned}
 & \left(\cos [e+f x]^{5/2} (a+b \sin [e+f x]) \sqrt{\tan [e+f x]} (-1+\tan [e+f x]^2) \right. \\
 & \quad \left. \sqrt{1+\tan [e+f x]^2} \right) + \\
 & \left(2 \sqrt{\sin [e+f x]} \left(b \tan [e+f x] + a \sqrt{1+\tan [e+f x]^2} \right) \right. \\
 & \quad \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] + \right. \right. \right. \\
 & \quad \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]}}{\sqrt{a}} \right] + \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]} - \sqrt{a^2-b^2} \tan [e+f x] \right] - \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\tan [e+f x]} + \sqrt{a^2-b^2} \tan [e+f x] \right] \right) \right) / \\
 & \quad \left(4 \sqrt{2} (a^2-b^2)^{3/4} + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan [e+f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] \tan [e+f x]^{5/2} \right) / \left(5 \sqrt{1+\tan [e+f x]^2} \right. \\
 & \quad \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + \right. \\
 & \quad \quad \left. 2 \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] + \right. \right. \\
 & \quad \quad \quad \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan [e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [e+f x]^2 \right] \right) \right) \\
 & \quad \left. \left. \tan [e+f x]^2 \right) (-b^2 \tan [e+f x]^2 + a^2 (1 + \tan [e+f x]^2)) \right) \right) / \\
 & \left(\cos [e+f x]^{5/2} (a+b \sin [e+f x]) \sqrt{\tan [e+f x]} (1+\tan [e+f x]^2)^{3/2} \right)
 \end{aligned}$$

Problem 1431: Result unnecessarily involves higher level functions.

$$\int \frac{(d \sin [e+f x])^{3/2}}{\sqrt{g \cos [e+f x]} (a+b \sin [e+f x])} dx$$

Optimal (type 4, 508 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{d^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+fx]}}\right]}{\sqrt{2} b f \sqrt{g}} + \frac{d^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{g \operatorname{Cos}[e+fx]}}\right]}{\sqrt{2} b f \sqrt{g}} + \\
 & \left(2 \sqrt{2} a d^{3/2} \sqrt{\operatorname{Cos}[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+fx]}}\right], -1\right]\right) / \\
 & \left(b \sqrt{-a^2 + b^2} f \sqrt{g \operatorname{Cos}[e+fx]}\right) - \\
 & \left(2 \sqrt{2} a d^{3/2} \sqrt{\operatorname{Cos}[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{d} \sqrt{1 + \operatorname{Cos}[e+fx]}}\right], -1\right]\right) / \\
 & \left(b \sqrt{-a^2 + b^2} f \sqrt{g \operatorname{Cos}[e+fx]}\right) + \frac{d^{3/2} \operatorname{Log}\left[\sqrt{d} - \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{g \operatorname{Cos}[e+fx]}} + \sqrt{d} \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b f \sqrt{g}} - \\
 & \frac{d^{3/2} \operatorname{Log}\left[\sqrt{d} + \frac{\sqrt{2} \sqrt{g} \sqrt{d \operatorname{Sin}[e+fx]}}{\sqrt{g \operatorname{Cos}[e+fx]}} + \sqrt{d} \operatorname{Tan}[e+fx]\right]}{2 \sqrt{2} b f \sqrt{g}}
 \end{aligned}$$

Result(type 6, 518 leaves):

$$\begin{aligned}
 & \frac{1}{f \sqrt{g \operatorname{Cos}[e+fx]} (-a + b \operatorname{Sin}[e+fx]) (a + b \operatorname{Sin}[e+fx])^2} \\
 & 10 (a^2 - b^2) \operatorname{Cot}[e+fx] (d \operatorname{Sin}[e+fx])^{3/2} \left(a + b \sqrt{\operatorname{Sin}[e+fx]^2}\right) \\
 & \left(\left(a \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right]\right) / \right. \\
 & \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right] + \right. \\
 & \left(-4 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{4}, 2, \frac{9}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right] + \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{4}, 1, \frac{9}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right]\right) \operatorname{Cos}[e+fx]^2\right) + \\
 & \left(b \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right] \sqrt{\operatorname{Sin}[e+fx]^2}\right) / \\
 & \left(-5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{3}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right] + \right. \\
 & \left(4 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{3}{4}, 2, \frac{9}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right] + \right. \\
 & \left. \left. 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{4}, 1, \frac{9}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2 + b^2}\right]\right) \operatorname{Cos}[e+fx]^2\right)
 \end{aligned}$$

Problem 1433: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{g \cos[e+fx]} \sqrt{d \sin[e+fx]} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 273 leaves, 7 steps):

$$\begin{aligned} & \left(2 \sqrt{2} b \sqrt{\cos[e+fx]} \operatorname{EllipticPi} \left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{1 + \cos[e+fx]}} \right], -1 \right] \right) / \\ & \left(a \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \cos[e+fx]} \right) - \\ & \left(2 \sqrt{2} b \sqrt{\cos[e+fx]} \operatorname{EllipticPi} \left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{1 + \cos[e+fx]}} \right], -1 \right] \right) / \\ & \left(a \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \cos[e+fx]} \right) + \frac{\operatorname{EllipticF} \left[e - \frac{\pi}{4} + fx, 2 \right] \sqrt{\sin[2e + 2fx]}}{a f \sqrt{g \cos[e+fx]} \sqrt{d \sin[e+fx]}} \end{aligned}$$

Result (type 6, 664 leaves):

$$\begin{aligned}
& - \left(\left(2 \sqrt{\cos[e+fx]} \left(a + b \sqrt{1 - \cos[e+fx]^2} \right) \right. \right. \\
& \quad \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \sqrt{\cos[e+fx]} \right) / \right. \\
& \quad \left((1 - \cos[e+fx]^2)^{3/4} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \right. \right. \right. \\
& \quad \quad \left. \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] + \right. \\
& \quad \quad \left. \left. 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2 + b^2} \right] \right) \right) \\
& \quad \left. \left. \cos[e+fx]^2 \right) (a^2 + b^2 (-1 + \cos[e+fx]^2)) \right) - \\
& \quad \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4} (-1 + \cos[e+fx]^2)^{1/4}} \right] - \right. \right. \\
& \quad \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2 + b^2)^{1/4} (-1 + \cos[e+fx]^2)^{1/4}} \right] + \right. \\
& \quad \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \cos[e+fx]}{\sqrt{-1 + \cos[e+fx]^2}} - \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1 + \cos[e+fx]^2)^{1/4}} \right] - \right. \\
& \quad \left. \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \cos[e+fx]}{\sqrt{-1 + \cos[e+fx]^2}} + \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1 + \cos[e+fx]^2)^{1/4}} \right] \right) \right) / \\
& \quad \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \left. \operatorname{Sin}[e+fx] \right) / \\
& \quad \left(f \sqrt{g \cos[e+fx]} (1 - \cos[e+fx]^2)^{1/4} \sqrt{d \operatorname{Sin}[e+fx]} \right. \\
& \quad \left. (a + b \operatorname{Sin}[e+fx]) \right) \Big)
\end{aligned}$$

Problem 1434: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{g \cos[e+fx]} (d \operatorname{Sin}[e+fx])^{3/2} (a + b \operatorname{Sin}[e+fx])} dx$$

Optimal (type 4, 320 leaves, 9 steps):

$$\begin{aligned}
 & - \left(\left(2\sqrt{2} b^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi} \left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d} \sin[e+fx]}{\sqrt{d} \sqrt{1 + \cos[e+fx]}} \right], -1 \right] \right) / \right. \\
 & \quad \left. \left(a^2 \sqrt{-a^2 + b^2} d^{3/2} f \sqrt{g \cos[e+fx]} \right) \right) + \\
 & \left(2\sqrt{2} b^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi} \left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin} \left[\frac{\sqrt{d} \sin[e+fx]}{\sqrt{d} \sqrt{1 + \cos[e+fx]}} \right], -1 \right] \right) / \\
 & \quad \left(a^2 \sqrt{-a^2 + b^2} d^{3/2} f \sqrt{g \cos[e+fx]} \right) - \\
 & \frac{2\sqrt{g \cos[e+fx]}}{a d f g \sqrt{d \sin[e+fx]}} - \frac{b \operatorname{EllipticF} \left[e - \frac{\pi}{4} + fx, 2 \right] \sqrt{\sin[2e + 2fx]}}{a^2 d f \sqrt{g \cos[e+fx]} \sqrt{d \sin[e+fx]}}
 \end{aligned}$$

Result (type 6, 715 leaves):

$$\begin{aligned}
 & - \frac{2 \operatorname{Cos}[e + f x] \operatorname{Sin}[e + f x]}{a f \sqrt{g \operatorname{Cos}[e + f x]} (d \operatorname{Sin}[e + f x])^{3/2}} + \left(2 b \sqrt{\operatorname{Cos}[e + f x]} \left(a + b \sqrt{1 - \operatorname{Cos}[e + f x]^2} \right) \right. \\
 & \left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \sqrt{\operatorname{Cos}[e + f x]} \right) / \right. \\
 & \left((1 - \operatorname{Cos}[e + f x]^2)^{3/4} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left. 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \operatorname{Cos}[e + f x]^2, \frac{b^2 \operatorname{Cos}[e + f x]^2}{-a^2 + b^2} \right] \right) \right. \\
 & \left. \left. \operatorname{Cos}[e + f x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[e + f x]^2)) \right) - \\
 & \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\operatorname{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} (-1 + \operatorname{Cos}[e + f x]^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\operatorname{Cos}[e + f x]}}{(-a^2 + b^2)^{1/4} (-1 + \operatorname{Cos}[e + f x]^2)^{1/4}} \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \operatorname{Cos}[e + f x]}{\sqrt{-1 + \operatorname{Cos}[e + f x]^2}} - \frac{(1 + i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]}}{(-1 + \operatorname{Cos}[e + f x]^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \operatorname{Cos}[e + f x]}{\sqrt{-1 + \operatorname{Cos}[e + f x]^2}} + \frac{(1 + i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Cos}[e + f x]}}{(-1 + \operatorname{Cos}[e + f x]^2)^{1/4}} \right] \right) \right) / \\
 & \left. \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \operatorname{Sin}[e + f x]^2 \right) / \\
 & (a f \sqrt{g \operatorname{Cos}[e + f x]} (1 - \operatorname{Cos}[e + f x]^2)^{1/4} (d \operatorname{Sin}[e + f x])^{3/2} \\
 & (a + b \operatorname{Sin}[e + f x]))
 \end{aligned}$$

Problem 1435: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{g \operatorname{Cos}[e + f x]} (d \operatorname{Sin}[e + f x])^{5/2} (a + b \operatorname{Sin}[e + f x])} dx$$

Optimal (type 4, 424 leaves, 13 steps):

$$\begin{aligned} & \left(2\sqrt{2} b^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b-\sqrt{-a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{1+\cos[e+fx]}}\right], -1\right] \right) / \\ & \left(a^3 \sqrt{-a^2+b^2} d^{5/2} f \sqrt{g \cos[e+fx]} \right) - \\ & \left(2\sqrt{2} b^3 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b-\sqrt{-a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d \sin[e+fx]}}{\sqrt{d} \sqrt{1+\cos[e+fx]}}\right], -1\right] \right) / \\ & \left(a^3 \sqrt{-a^2+b^2} d^{5/2} f \sqrt{g \cos[e+fx]} \right) - \frac{2\sqrt{g \cos[e+fx]}}{3 a d f g (d \sin[e+fx])^{3/2}} + \\ & \frac{2 b \sqrt{g \cos[e+fx]}}{a^2 d^2 f g \sqrt{d \sin[e+fx]}} + \frac{2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\sin[2e+2fx]}}{3 a d^2 f \sqrt{g \cos[e+fx]} \sqrt{d \sin[e+fx]}} + \\ & \frac{b^2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + f x, 2\right] \sqrt{\sin[2e+2fx]}}{a^3 d^2 f \sqrt{g \cos[e+fx]} \sqrt{d \sin[e+fx]}} \end{aligned}$$

Result (type 6, 1332 leaves):

$$\begin{aligned} & \frac{\cos[e+fx] \left(\frac{2 b \operatorname{Csc}[e+fx]}{a^2} - \frac{2 \operatorname{Csc}[e+fx]^2}{3 a} \right) \sin[e+fx]^3}{f \sqrt{g \cos[e+fx]} (d \sin[e+fx])^{5/2}} + \\ & \frac{1}{3 a^2 f \sqrt{g \cos[e+fx]} (d \sin[e+fx])^{5/2}} \sqrt{\cos[e+fx]} \sin[e+fx]^{5/2} \\ & \left(-\frac{1}{(1-\cos[e+fx]^2)^{1/4} (a+b \sin[e+fx])} 2 (2 a^2+3 b^2) \left(a+b \sqrt{1-\cos[e+fx]^2} \right) \right. \\ & \left. \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \sqrt{\cos[e+fx]} \right) / \right. \right. \\ & \left. \left((1-\cos[e+fx]^2)^{3/4} \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right) + \left(-4 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right) + 3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] \right) \cos[e+fx]^2 \right) (a^2+b^2 (-1+\cos[e+fx]^2)) \left. \right) - \\ & \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4} (-1+\cos[e+fx]^2)^{1/4}}\right] - 2 \right. \right. \\ & \left. \left. \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos[e+fx]}}{(-a^2+b^2)^{1/4} (-1+\cos[e+fx]^2)^{1/4}}\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + \right. \right. \right. \\ & \left. \left. \left. \frac{i a \cos[e+fx]}{\sqrt{-1+\cos[e+fx]^2}} - \frac{(1+i) \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\cos[e+fx]}}{(-1+\cos[e+fx]^2)^{1/4}} \right] - \operatorname{Log}\left[\right. \right. \right. \end{aligned}$$

$$\begin{aligned}
& \left. \left(\sqrt{-a^2 + b^2} + \frac{i a \cos[e + f x]}{\sqrt{-1 + \cos[e + f x]^2}} + \frac{(1 + i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos[e + f x]}}{(-1 + \cos[e + f x]^2)^{1/4}} \right) \right) / \\
& \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \sqrt{\sin[e + f x]} + \\
& \left(4 a b \sqrt{\sin[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right. \\
& \left(\left(\sqrt{a} \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + 2 \right. \right. \right. \\
& \left. \left. \left. \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + \operatorname{Log} \left[\right. \right. \right. \right. \\
& \left. \left. \left. -a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] - \operatorname{Log} \left[\right. \right. \right. \right. \\
& \left. \left. \left. a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) \right) \right) / \\
& \left(4 \sqrt{2} (a^2 - b^2)^{3/4} \right) + \left(9 a^2 b \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{5/2} \right) / \left(5 \sqrt{1 + \tan[e + f x]^2} \right. \\
& \left. \left(-9 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
& \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \\
& \left. \left. a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right) \\
& \left. \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) \right) / \\
& \left(\cos[e + f x]^{5/2} (a + b \sin[e + f x]) \sqrt{\tan[e + f x]} (1 + \tan[e + f x]^2)^{3/2} \right)
\end{aligned}$$

Problem 1436: Attempted integration timed out after 120 seconds.

$$\int \frac{(d \sin[e + f x])^{5/2}}{(g \cos[e + f x])^{3/2} (a + b \sin[e + f x])} dx$$

Optimal (type 4, 1064 leaves, 31 steps):

$$\begin{aligned}
 & - \frac{a^2 d^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b (a^2 - b^2) f g^{3/2}} + \frac{b d^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} (a^2 - b^2) f g^{3/2}} + \\
 & \frac{a^2 d^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} b (a^2 - b^2) f g^{3/2}} - \frac{b d^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{d \sin[e+fx]}}\right]}{\sqrt{2} (a^2 - b^2) f g^{3/2}} + \\
 & \frac{a^2 d^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b (a^2 - b^2) f g^{3/2}} - \\
 & \frac{b d^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] - \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} (a^2 - b^2) f g^{3/2}} - \\
 & \frac{a^2 d^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} b (a^2 - b^2) f g^{3/2}} + \\
 & \frac{b d^{5/2} \operatorname{Log}\left[\sqrt{g} + \sqrt{g} \operatorname{Cot}[e+fx] + \frac{\sqrt{2} \sqrt{d} \sqrt{g \cos[e+fx]}}{\sqrt{d \sin[e+fx]}}\right]}{2 \sqrt{2} (a^2 - b^2) f g^{3/2}} - \\
 & \left(2 \sqrt{2} a^3 d^3 \operatorname{EllipticPi}\left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]}\right) / \\
 & \left(b (-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \sin[e+fx]}\right) + \\
 & \left(2 \sqrt{2} a^3 d^3 \operatorname{EllipticPi}\left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin}\left[\frac{\sqrt{g \cos[e+fx]}}{\sqrt{g} \sqrt{1+\sin[e+fx]}}\right], -1\right] \sqrt{\sin[e+fx]}\right) / \\
 & \left(b (-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \sin[e+fx]}\right) - \frac{2 b d^2 \sqrt{d \sin[e+fx]}}{(a^2 - b^2) f g \sqrt{g \cos[e+fx]}} + \\
 & \frac{2 a d (d \sin[e+fx])^{3/2}}{(a^2 - b^2) f g \sqrt{g \cos[e+fx]}} - \frac{2 a d^2 \sqrt{g \cos[e+fx]} \operatorname{EllipticE}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{d \sin[e+fx]}}{(a^2 - b^2) f g^2 \sqrt{\sin[2e+2fx]}}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

Problem 1437: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(d \sin[e+fx])^{3/2}}{(g \cos[e+fx])^{3/2} (a+b \sin[e+fx])} dx$$

Optimal (type 4, 379 leaves, 10 steps):

$$\begin{aligned} & \left(2 \sqrt{2} a^2 d^2 \operatorname{EllipticPi} \left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+fx]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+fx]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+fx]} \right) / \\ & \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+fx]} \right) - \\ & \left(2 \sqrt{2} a^2 d^2 \operatorname{EllipticPi} \left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+fx]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+fx]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+fx]} \right) / \\ & \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+fx]} \right) + \frac{2 a d \sqrt{d \operatorname{Sin}[e+fx]}}{(a^2-b^2) f g \sqrt{g \operatorname{Cos}[e+fx]}} - \\ & \frac{2 b (d \operatorname{Sin}[e+fx])^{3/2}}{(a^2-b^2) f g \sqrt{g \operatorname{Cos}[e+fx]}} + \frac{2 b d \sqrt{g \operatorname{Cos}[e+fx]} \operatorname{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \operatorname{Sin}[e+fx]}}{(a^2-b^2) f g^2 \sqrt{\operatorname{Sin}[2e+2fx]}} \end{aligned}$$

Result (type 6, 2915 leaves):

$$\begin{aligned} & \frac{2 \operatorname{Cot}[e+fx] (d \operatorname{Sin}[e+fx])^{3/2} (a-b \operatorname{Sin}[e+fx])}{(a^2-b^2) f (g \operatorname{Cos}[e+fx])^{3/2}} - \\ & \frac{1}{(a-b) (a+b) f (g \operatorname{Cos}[e+fx])^{3/2} \operatorname{Sin}[e+fx]^{3/2}} \\ & \operatorname{Cos}[e+fx]^{3/2} (d \operatorname{Sin}[e+fx])^{3/2} \left(\left(28 a b (a^2-b^2) \operatorname{Cos}[e+fx]^{3/2} \left(a+b \sqrt{1-\operatorname{Cos}[e+fx]^2} \right) \right. \right. \\ & \left. \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] \sqrt{1-\operatorname{Cos}[e+fx]^2} \right) / \right. \right. \\ & \left. \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] + \right. \right. \\ & \left. \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] + (a^2-b^2) \right. \right. \\ & \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] \right) \operatorname{Cos}[e+fx]^2 \right) + \\ & \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] \right) / \\ & \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] + \right. \\ & \left. \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] + (a^2-b^2) \right. \right. \\ & \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \operatorname{Cos}[e+fx]^2, \frac{b^2 \operatorname{Cos}[e+fx]^2}{-a^2+b^2} \right] \right) \operatorname{Cos}[e+fx]^2 \right) \right) \\ & \operatorname{Sin}[e+fx]^{3/2} \left(3 (1-\operatorname{Cos}[e+fx]^2) (a^2+b^2) (-1+\operatorname{Cos}[e+fx]^2) \right) \\ & (a+b \operatorname{Sin}[e+fx]) \right) + \end{aligned}$$

$$\begin{aligned}
 & \left(2 (a^2 - b^2) \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right. \\
 & \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] + \right. \right. \\
 & \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{a}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} - \sqrt{a^2 - b^2} \tan[e + f x] \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]} + \sqrt{a^2 - b^2} \tan[e + f x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \tan[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \tan[e + f x]^2} \right. \\
 & \quad \left. \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + 2 \right. \right. \\
 & \quad \left. \left((a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan[e + f x]^2 \right) \left(-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2) \right) \right) \right) / \\
 & \left(\cos[e + f x]^{3/2} \sqrt{\sin[e + f x]} (a + b \sin[e + f x]) (1 + \tan[e + f x]^2)^{3/2} \right) + \\
 & \left(2 b^2 \cos[2(e + f x)] \sqrt{\tan[e + f x]} \left(b \tan[e + f x] + a \sqrt{1 + \tan[e + f x]^2} \right) \right) \\
 & \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e + f x]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \\
 & \quad \left. \frac{a \operatorname{Log} \left[1 - \sqrt{2} \sqrt{\tan[e + f x]} + \tan[e + f x] \right]}{2 \sqrt{2} b^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[e + f x]} + \operatorname{Tan}[e + f x]\right]}{2 \sqrt{2} b^2} - \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} - \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \\
 & \left((2 a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Tan}[e + f x]} + \sqrt{a^2 - b^2} \operatorname{Tan}[e + f x]\right] \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4} \right) + \frac{\operatorname{Tan}[e + f x]^{3/2}}{b \sqrt{1 + \operatorname{Tan}[e + f x]^2}} + \\
 & \left(7 a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \operatorname{Tan}[e + f x]^{3/2} \right) / \\
 & \left(b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) - \\
 & \left(7 a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{3/2} \right) / \left(3 \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-7 a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}[e + f x]^2 \right) \left(-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2) \right) \right) + \\
 & \left(11 a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e + f x]^{7/2} \right) / \left(7 b \sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \\
 & \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right) - \\
 & \left(11 a^2 b \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
 & \left. \tan[e+fx]^{7/2}\right) / \left(7 \sqrt{1 + \tan[e+fx]^2}\right. \\
 & \left(-11 a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2\right. \\
 & \left.2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] +\right. \\
 & \left. a^2 \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right]\right) \\
 & \left. \tan[e+fx]^2 \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)\right)\right) / \\
 & \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (-1 + \tan[e+fx]^2)\right. \\
 & \left. \sqrt{1 + \tan[e+fx]^2}\right)
 \end{aligned}$$

Problem 1438: Attempted integration timed out after 120 seconds.

$$\int \frac{\sqrt{d \sin[e+fx]}}{(g \cos[e+fx])^{3/2} (a + b \sin[e+fx])} dx$$

Optimal (type 4, 374 leaves, 11 steps):

$$\begin{aligned}
 & - \left(\left(2 \sqrt{2} a b d \operatorname{EllipticPi} \left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+f x]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+f x]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+f x]} \right) / \right. \\
 & \quad \left. \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+f x]} \right) \right) + \\
 & \left(2 \sqrt{2} a b d \operatorname{EllipticPi} \left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+f x]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+f x]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+f x]} \right) / \\
 & \quad \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+f x]} \right) - \\
 & \quad \frac{2 b \sqrt{d \operatorname{Sin}[e+f x]}}{(a^2-b^2) f g \sqrt{g \operatorname{Cos}[e+f x]}} + \frac{2 a (d \operatorname{Sin}[e+f x])^{3/2}}{(a^2-b^2) d f g \sqrt{g \operatorname{Cos}[e+f x]}} - \\
 & \quad \frac{2 a \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \operatorname{Sin}[e+f x]}}{(a^2-b^2) f g^2 \sqrt{\operatorname{Sin}[2 e+2 f x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 1439: Attempted integration timed out after 120 seconds.

$$\int \frac{1}{(g \operatorname{Cos}[e+f x])^{3/2} \sqrt{d \operatorname{Sin}[e+f x]} (a+b \operatorname{Sin}[e+f x])} dx$$

Optimal (type 4, 380 leaves, 11 steps):

$$\begin{aligned}
 & \left(2 \sqrt{2} b^2 \operatorname{EllipticPi} \left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+f x]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+f x]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+f x]} \right) / \\
 & \quad \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+f x]} \right) - \\
 & \left(2 \sqrt{2} b^2 \operatorname{EllipticPi} \left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \operatorname{Cos}[e+f x]}}{\sqrt{g} \sqrt{1+\operatorname{Sin}[e+f x]}} \right], -1 \right] \sqrt{\operatorname{Sin}[e+f x]} \right) / \\
 & \quad \left((-a+b)^{3/2} (a+b)^{3/2} f g^{3/2} \sqrt{d \operatorname{Sin}[e+f x]} \right) + \frac{2 a \sqrt{d \operatorname{Sin}[e+f x]}}{(a^2-b^2) d f g \sqrt{g \operatorname{Cos}[e+f x]}} - \\
 & \quad \frac{2 b (d \operatorname{Sin}[e+f x])^{3/2}}{(a^2-b^2) d^2 f g \sqrt{g \operatorname{Cos}[e+f x]}} + \frac{2 b \sqrt{g \operatorname{Cos}[e+f x]} \operatorname{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \operatorname{Sin}[e+f x]}}{(a^2-b^2) d f g^2 \sqrt{\operatorname{Sin}[2 e+2 f x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 1440: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(g \operatorname{Cos}[e+f x])^{3/2} (d \operatorname{Sin}[e+f x])^{3/2} (a+b \operatorname{Sin}[e+f x])} dx$$

Optimal (type 4, 568 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{2 a}{(a^2 - b^2) d f g \sqrt{g \cos[e + f x]} \sqrt{d \sin[e + f x]}} + \frac{2 b^2 (g \cos[e + f x])^{3/2}}{a (a^2 - b^2) d f g^3 \sqrt{d \sin[e + f x]}} - \\
 & \left(2 \sqrt{2} b^3 \operatorname{EllipticPi} \left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}} \right], -1 \right] \sqrt{\sin[e + f x]} \right) / \\
 & \left(a (-a+b)^{3/2} (a+b)^{3/2} d f g^{3/2} \sqrt{d \sin[e + f x]} \right) + \\
 & \left(2 \sqrt{2} b^3 \operatorname{EllipticPi} \left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \operatorname{ArcSin} \left[\frac{\sqrt{g \cos[e + f x]}}{\sqrt{g} \sqrt{1 + \sin[e + f x]}} \right], -1 \right] \sqrt{\sin[e + f x]} \right) / \\
 & \left(a (-a+b)^{3/2} (a+b)^{3/2} d f g^{3/2} \sqrt{d \sin[e + f x]} \right) - \frac{2 b \sqrt{d \sin[e + f x]}}{(a^2 - b^2) d^2 f g \sqrt{g \cos[e + f x]}} + \\
 & \frac{4 a (d \sin[e + f x])^{3/2}}{(a^2 - b^2) d^3 f g \sqrt{g \cos[e + f x]}} - \frac{4 a \sqrt{g \cos[e + f x]} \operatorname{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \sin[e + f x]}}{(a^2 - b^2) d^2 f g^2 \sqrt{\sin[2 e + 2 f x]}} + \\
 & \frac{2 b^2 \sqrt{g \cos[e + f x]} \operatorname{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \sin[e + f x]}}{a (a^2 - b^2) d^2 f g^2 \sqrt{\sin[2 e + 2 f x]}}
 \end{aligned}$$

Result (type 6, 2968 leaves):

$$\begin{aligned}
 & \frac{\cos[e + f x]^2 \sin[e + f x]^2 \left(-\frac{2 \cot[e + f x]}{a} + \frac{2 \sec[e + f x] (-b + a \sin[e + f x])}{a^2 - b^2} \right)}{f (g \cos[e + f x])^{3/2} (d \sin[e + f x])^{3/2}} - \\
 & \frac{1}{a (a - b) (a + b) f (g \cos[e + f x])^{3/2} (d \sin[e + f x])^{3/2}} \cos[e + f x]^{3/2} \sin[e + f x]^{3/2} \\
 & \left(- \left(\left(14 (a^2 - b^2) (4 a^3 - 2 a b^2) \cos[e + f x]^{3/2} \left(a + b \sqrt{1 - \cos[e + f x]^2} \right) \right. \right. \right. \\
 & \left. \left(\left(b \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos[e + f x]^2} \right) / \right. \right. \\
 & \left. \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left(4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) \cos[e + f x]^2 \right) + \\
 & \left(a \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] \right) / \left(7 (a^2 - b^2) \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + \left(-4 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{4}, 2, \frac{11}{4}, \cos[e + f x]^2, \frac{b^2 \cos[e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{4}, 1, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left(\frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2} \right) \cos[e+fx]^2 \right) \sin[e+fx]^{3/2} \Big/ \\
& \left(3 (1 - \cos[e+fx]^2) (a^2 + b^2 (-1 + \cos[e+fx]^2)) (a + b \sin[e+fx]) \right) + \\
& \left(2 (2 a^2 b - 2 b^3) \sqrt{\tan[e+fx]} \left(b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2} \right) \right. \\
& \left(\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] + \right. \right. \\
& \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{a}} \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[-a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} - \sqrt{a^2 - b^2} \tan[e+fx] \right] + \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[a + \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]} + \sqrt{a^2 - b^2} \tan[e+fx] \right] \right) \Big/ \\
& \left(4 \sqrt{2} \sqrt{a} (a^2 - b^2)^{1/4} \right) + \left(7 a^2 b \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \tan[e+fx]^{3/2} \right) \Big/ \left(3 \sqrt{1 + \tan[e+fx]^2} \right. \\
& \left(-7 a^2 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left. a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \\
& \quad \left. \left. \tan[e+fx]^2 \right) (-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2)) \right) \Big/ \\
& \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a + b \sin[e+fx]) (1 + \tan[e+fx]^2)^{3/2} \right) + \\
& \left(2 (-2 a^2 b + b^3) \cos[2(e+fx)] \sqrt{\tan[e+fx]} \right. \\
& \quad \left. \left(b \tan[e+fx] + a \sqrt{1 + \tan[e+fx]^2} \right) \right. \\
& \left(-\frac{a \operatorname{ArcTan} \left[\frac{-\sqrt{2} + 2 \sqrt{\tan[e+fx]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} - \frac{a \operatorname{ArcTan} \left[\frac{\sqrt{2} + 2 \sqrt{\tan[e+fx]}}{\sqrt{2}} \right]}{\sqrt{2} b^2} + \right. \\
& \quad \left. \frac{(2 a^2 - b^2) \operatorname{ArcTan} \left[\frac{-\sqrt{2} \sqrt{a} + 2 (a^2 - b^2)^{1/4} \sqrt{\tan[e+fx]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} \sqrt{a} b^2 (a^2 - b^2)^{1/4}} + \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} \right) + \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} \right) + \frac{\operatorname{Tan}[e+fx]^{3/2}}{b\sqrt{1 + \operatorname{Tan}[e+fx]^2}} + \\
 & \left(7a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2} \right) / \\
 & \left(b\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \quad \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \\
 & \quad \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) - \\
 & \left(7a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right. \\
 & \quad \left. \operatorname{Tan}[e+fx]^{3/2} \right) / \left(3\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \quad \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \\
 & \quad \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \quad \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) + \\
 & \left(11a^4 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right)
 \end{aligned}$$

$$\left(\frac{\text{Tan}[e + f x]^{7/2}}{7 b \sqrt{1 + \text{Tan}[e + f x]^2}} \left(-11 a^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + 2 \right. \right. \right. \\ \left. \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + a^2 \text{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right) \right. \right. \\ \left. \left. \text{Tan}[e + f x]^2 \right) (-b^2 \text{Tan}[e + f x]^2 + a^2 (1 + \text{Tan}[e + f x]^2)) \right) - \\ \left(11 a^2 b \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\text{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \text{Tan}[e + f x]^2}{a^2}\right] \right. \\ \left. \frac{\text{Tan}[e + f x]^{7/2}}{7 \sqrt{1 + \text{Tan}[e + f x]^2}} \left(-11 a^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + 2 \right. \right. \\ \left. \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + a^2 \text{AppellF1}\left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right) \right. \right. \\ \left. \left. \text{Tan}[e + f x]^2 \right) (-b^2 \text{Tan}[e + f x]^2 + a^2 (1 + \text{Tan}[e + f x]^2)) \right) \right) \bigg) \bigg) \bigg) \bigg) / \\ \left(\text{Cos}[e + f x]^{3/2} \sqrt{\text{Sin}[e + f x]} (a + b \text{Sin}[e + f x]) (-1 + \text{Tan}[e + f x]^2) \right. \\ \left. \sqrt{1 + \text{Tan}[e + f x]^2} \right)$$

Problem 1441: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(g \text{Cos}[e + f x])^{3/2} (d \text{Sin}[e + f x])^{5/2} (a + b \text{Sin}[e + f x])} dx$$

Optimal (type 4, 673 leaves, 19 steps):

$$\begin{aligned}
 & - \frac{2 a}{3 (a^2 - b^2) d f g \sqrt{g \cos [e + f x]} (d \sin [e + f x])^{3/2}} + \frac{2 b^2 (g \cos [e + f x])^{3/2}}{3 a (a^2 - b^2) d f g^3 (d \sin [e + f x])^{3/2}} + \\
 & \frac{2 b}{(a^2 - b^2) d^2 f g \sqrt{g \cos [e + f x]} \sqrt{d \sin [e + f x]}} - \frac{2 b^3 (g \cos [e + f x])^{3/2}}{a^2 (a^2 - b^2) d^2 f g^3 \sqrt{d \sin [e + f x]}} + \\
 & \left(2 \sqrt{2} b^4 \text{EllipticPi} \left[-\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \text{ArcSin} \left[\frac{\sqrt{g \cos [e + f x]}}{\sqrt{g} \sqrt{1 + \sin [e + f x]}} \right], -1 \right] \sqrt{\sin [e + f x]} \right) / \\
 & \left(a^2 (-a+b)^{3/2} (a+b)^{3/2} d^2 f g^{3/2} \sqrt{d \sin [e + f x]} \right) - \\
 & \left(2 \sqrt{2} b^4 \text{EllipticPi} \left[\frac{\sqrt{-a+b}}{\sqrt{a+b}}, \text{ArcSin} \left[\frac{\sqrt{g \cos [e + f x]}}{\sqrt{g} \sqrt{1 + \sin [e + f x]}} \right], -1 \right] \sqrt{\sin [e + f x]} \right) / \\
 & \left(a^2 (-a+b)^{3/2} (a+b)^{3/2} d^2 f g^{3/2} \sqrt{d \sin [e + f x]} \right) + \frac{8 a \sqrt{d \sin [e + f x]}}{3 (a^2 - b^2) d^3 f g \sqrt{g \cos [e + f x]}} - \\
 & \frac{4 b (d \sin [e + f x])^{3/2}}{(a^2 - b^2) d^4 f g \sqrt{g \cos [e + f x]}} + \frac{4 b \sqrt{g \cos [e + f x]} \text{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \sin [e + f x]}}{(a^2 - b^2) d^3 f g^2 \sqrt{\sin [2 e + 2 f x]}} - \\
 & \frac{2 b^3 \sqrt{g \cos [e + f x]} \text{EllipticE} \left[e - \frac{\pi}{4} + f x, 2 \right] \sqrt{d \sin [e + f x]}}{a^2 (a^2 - b^2) d^3 f g^2 \sqrt{\sin [2 e + 2 f x]}}
 \end{aligned}$$

Result (type 6, 2988 leaves):

$$\begin{aligned}
 & \left(\cos [e + f x]^2 \sin [e + f x]^3 \right. \\
 & \left. \left(\frac{2 b \cot [e + f x]}{a^2} - \frac{2 \cot [e + f x] \csc [e + f x]}{3 a} + \frac{2 \sec [e + f x] (a - b \sin [e + f x])}{a^2 - b^2} \right) \right) / \\
 & \left(f (g \cos [e + f x])^{3/2} (d \sin [e + f x])^{5/2} \right) - \\
 & \frac{1}{a^2 (-a+b) (a+b) f (g \cos [e + f x])^{3/2} (d \sin [e + f x])^{5/2}} b \cos [e + f x]^{3/2} \\
 & \sin [e + f x]^{5/2} \left(- \left(\left(14 (a^2 - b^2) (4 a^3 - 2 a b^2) \cos [e + f x]^{3/2} \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \right. \right. \right. \\
 & \left. \left(b \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{1 - \cos [e + f x]^2} \right) \right) / \\
 & \left(-7 (a^2 - b^2) \text{AppellF1} \left[\frac{3}{4}, -\frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \left(4 b^2 \text{AppellF1} \left[\frac{7}{4}, -\frac{1}{4}, 2, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \\
 & \left. \left. \left. \text{AppellF1} \left[\frac{7}{4}, \frac{3}{4}, 1, \frac{11}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \cos [e + f x]^2 \right) + \right. \\
 & \left. \left(a \text{AppellF1} \left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) / \left(7 (a^2 - b^2) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{3}{4}, \frac{1}{4}, 1, \frac{7}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + \left(-4b^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{4}, 2, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right] + (a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{5}{4}, 1, \frac{11}{4}, \cos[e+fx]^2, \frac{b^2 \cos[e+fx]^2}{-a^2+b^2}\right]\right) \cos[e+fx]^2 \Bigg) \sin[e+fx]^{3/2} \Bigg) / \\
& \left(3(1-\cos[e+fx]^2)(a^2+b^2(-1+\cos[e+fx]^2))(a+b\sin[e+fx])\right) + \\
& \left(2(2a^2b-2b^3)\sqrt{\tan[e+fx]}(b\tan[e+fx]+a\sqrt{1+\tan[e+fx]^2})\right. \\
& \left(\left(-2\text{ArcTan}\left[1-\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] + \right. \right. \\
& \left. \left. 2\text{ArcTan}\left[1+\frac{\sqrt{2}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}}{\sqrt{a}}\right] - \right. \right. \\
& \left. \left. \text{Log}\left[-a+\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}-\sqrt{a^2-b^2}\tan[e+fx]\right] + \right. \right. \\
& \left. \left. \text{Log}\left[a+\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\sqrt{\tan[e+fx]}+\sqrt{a^2-b^2}\tan[e+fx]\right]\right)\right) / \\
& \left(4\sqrt{2}\sqrt{a}(a^2-b^2)^{1/4}\right) + \left(7a^2b \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \right. \right. \\
& \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] \tan[e+fx]^{3/2}\right) / \left(3\sqrt{1+\tan[e+fx]^2}\right) + \\
& \left(-7a^2 \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + 2 \right. \\
& \left. \left(2(a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + \right. \right. \\
& \left. \left. a^2 \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right]\right) \right. \\
& \left. \left. \tan[e+fx]^2\right) (-b^2\tan[e+fx]^2+a^2(1+\tan[e+fx]^2))\right) \Bigg) \Bigg) / \\
& \left(\cos[e+fx]^{3/2}\sqrt{\sin[e+fx]}(a+b\sin[e+fx])(1+\tan[e+fx]^2)^{3/2}\right) + \\
& \left(2(-2a^2b+b^3)\cos[2(e+fx)]\sqrt{\tan[e+fx]}\right. \\
& \left.(b\tan[e+fx]+a\sqrt{1+\tan[e+fx]^2})\right. \\
& \left(-\frac{a\text{ArcTan}\left[\frac{-\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2}b^2} - \frac{a\text{ArcTan}\left[\frac{\sqrt{2}+2\sqrt{\tan[e+fx]}}{\sqrt{2}}\right]}{\sqrt{2}b^2} + \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{(2a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{2}\sqrt{a} + 2(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]}}{\sqrt{2}\sqrt{a}}\right]}{2\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4}} + \\
 & \frac{a \operatorname{Log}\left[1 - \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \frac{a \operatorname{Log}\left[1 + \sqrt{2}\sqrt{\operatorname{Tan}[e+fx]} + \operatorname{Tan}[e+fx]\right]}{2\sqrt{2}b^2} - \\
 & \left((2a^2 - b^2) \operatorname{Log}\left[-a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} - \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} + \right. \\
 & \left. (2a^2 - b^2) \operatorname{Log}\left[a + \sqrt{2}\sqrt{a}(a^2 - b^2)^{1/4}\sqrt{\operatorname{Tan}[e+fx]} + \sqrt{a^2 - b^2}\operatorname{Tan}[e+fx]\right] \right) / \\
 & \left(4\sqrt{2}\sqrt{a}b^2(a^2 - b^2)^{1/4} + \frac{\operatorname{Tan}[e+fx]^{3/2}}{b\sqrt{1 + \operatorname{Tan}[e+fx]^2}} + \right. \\
 & \left. \left(7a^4 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \operatorname{Tan}[e+fx]^{3/2} \right) / \right. \\
 & \left. \left(b\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \right. \\
 & \left. \left. \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \right. \right. \\
 & \left. \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right) \right. \\
 & \left. \left. \operatorname{Tan}[e+fx]^2 \right) \left(-b^2 \operatorname{Tan}[e+fx]^2 + a^2(1 + \operatorname{Tan}[e+fx]^2) \right) \right) - \\
 & \left(7a^2 b \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \frac{(-a^2 + b^2)\operatorname{Tan}[e+fx]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Tan}[e+fx]^{3/2} \right) / \left(3\sqrt{1 + \operatorname{Tan}[e+fx]^2} \right. \\
 & \left. \left(-7a^2 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + 2 \right. \right. \\
 & \left. \left(2(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] + \right. \right. \\
 & \left. \left. a^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, -\operatorname{Tan}[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right)\operatorname{Tan}[e+fx]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \right) + \\
 & \left(11 a^4 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right. \\
 & \left. \tan[e+fx]^{7/2} \right) / \left(7 b \sqrt{1 + \tan[e+fx]^2} \right. \\
 & \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \\
 & \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
 & \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \\
 & \left. \tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \Big) - \\
 & \left(11 a^2 b \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2} \right] \right. \\
 & \left. \tan[e+fx]^{7/2} \right) / \left(7 \sqrt{1 + \tan[e+fx]^2} \right. \\
 & \left(-11 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + 2 \right. \\
 & \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{1}{2}, 2, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
 & \left. a^2 \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2}, 1, \frac{15}{4}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \\
 & \left. \tan[e+fx]^2 \right) \left(-b^2 \tan[e+fx]^2 + a^2 (1 + \tan[e+fx]^2) \right) \Big) \Big) / \\
 & \left(\cos[e+fx]^{3/2} \sqrt{\sin[e+fx]} (a+b \sin[e+fx]) (-1 + \tan[e+fx]^2) \right. \\
 & \left. \sqrt{1 + \tan[e+fx]^2} \right)
 \end{aligned}$$

Problem 1442: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^{3/2}}{\sqrt{d \sin[e+fx]} (a+b \sin[e+fx])^2} dx$$

Optimal (type 4, 331 leaves, 8 steps):

$$\begin{aligned}
 & \left(\sqrt{2} b g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b - \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d} \sin[e+fx]}{\sqrt{d} \sqrt{1 + \cos[e+fx]}}\right], -1\right] \right) / \\
 & \left(a^2 \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \cos[e+fx]} \right) - \\
 & \left(\sqrt{2} b g^2 \sqrt{\cos[e+fx]} \operatorname{EllipticPi}\left[-\frac{a}{b + \sqrt{-a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{d} \sin[e+fx]}{\sqrt{d} \sqrt{1 + \cos[e+fx]}}\right], -1\right] \right) / \\
 & \left(a^2 \sqrt{-a^2 + b^2} \sqrt{d} f \sqrt{g \cos[e+fx]} \right) + \\
 & \frac{g \sqrt{g \cos[e+fx]} \sqrt{d} \sin[e+fx]}{a d f (a + b \sin[e+fx])} + \frac{g^2 \operatorname{EllipticF}\left[e - \frac{\pi}{4} + fx, 2\right] \sqrt{\sin[2e + 2fx]}}{2 a^2 f \sqrt{g \cos[e+fx]} \sqrt{d} \sin[e+fx]}
 \end{aligned}$$

Result(type 6, 717 leaves):

$$\begin{aligned}
 & - \left(\left((g \cos [e + f x])^{3/2} \left(a + b \sqrt{1 - \cos [e + f x]^2} \right) \right. \right. \\
 & \quad \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \sqrt{\cos [e + f x]} \right) \right) / \\
 & \quad \left((1 - \cos [e + f x]^2)^{3/4} \right. \\
 & \quad \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{3}{4}, 1, \frac{5}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left(-4 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{4}, 2, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. 3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{7}{4}, 1, \frac{9}{4}, \cos [e + f x]^2, \frac{b^2 \cos [e + f x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \quad \left. \cos [e + f x]^2 \right) (a^2 + b^2 (-1 + \cos [e + f x]^2)) \Big) - \\
 & \quad \left(\left(\frac{1}{8} - \frac{i}{8} \right) b \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4} (-1 + \cos [e + f x]^2)^{1/4}} \right] - \right. \right. \\
 & \quad \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\cos [e + f x]}}{(-a^2 + b^2)^{1/4} (-1 + \cos [e + f x]^2)^{1/4}} \right] + \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \cos [e + f x]}{\sqrt{-1 + \cos [e + f x]^2}} - \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]}}{(-1 + \cos [e + f x]^2)^{1/4}} \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \frac{i a \cos [e + f x]}{\sqrt{-1 + \cos [e + f x]^2}} + \right. \right. \\
 & \quad \left. \left. \frac{(1+i) \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\cos [e + f x]}}{(-1 + \cos [e + f x]^2)^{1/4}} \right] \right) \Big) / \left(\sqrt{a} (-a^2 + b^2)^{3/4} \right) \\
 & \quad \left. \sin [e + f x] \right) / \left(a f \cos [e + f x]^{3/2} (1 - \cos [e + f x]^2)^{1/4} \sqrt{d \sin [e + f x]} \right) \\
 & \quad \left. (a + b \sin [e + f x]) \right) \Big) + \\
 & \quad \frac{(g \cos [e + f x])^{3/2} \tan [e + f x]}{a f \sqrt{d \sin [e + f x]} (a + b \sin [e + f x])}
 \end{aligned}$$

Problem 1449: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c + d x]^3 \operatorname{Sec}[c + d x]^2 (a + b \sin [c + d x]) dx$$

Optimal (type 3, 75 leaves, 8 steps):

$$-\frac{3 a \operatorname{ArcTanh}[\cos [c+d x]]}{2 d}-\frac{b \cot [c+d x]}{d}+\frac{3 a \sec [c+d x]}{2 d}-\frac{a \csc [c+d x]^2 \sec [c+d x]}{2 d}+\frac{b \tan [c+d x]}{d}$$

Result (type 3, 172 leaves):

$$-\frac{2 b \cot [2(c+d x)]}{d}-\frac{a \csc \left[\frac{1}{2}(c+d x)\right]^2}{8 d}-\frac{3 a \log \left[\cos \left[\frac{1}{2}(c+d x)\right]\right]}{2 d}+\frac{3 a \log \left[\sin \left[\frac{1}{2}(c+d x)\right]\right]}{2 d}+\frac{a \sec \left[\frac{1}{2}(c+d x)\right]^2}{8 d}+\frac{a \sin \left[\frac{1}{2}(c+d x)\right]}{d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)}-\frac{a \sin \left[\frac{1}{2}(c+d x)\right]}{d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)}$$

Problem 1455: Result more than twice size of optimal antiderivative.

$$\int \csc [c+d x]^3 \sec [c+d x]^2 (a+b \sin [c+d x])^2 dx$$

Optimal (type 3, 100 leaves, 10 steps):

$$-\frac{\left(3 a^2+2 b^2\right) \operatorname{ArcTanh}[\cos [c+d x]]}{2 d}-\frac{2 a b \cot [c+d x]}{d}+\frac{\left(3 a^2+2 b^2\right) \sec [c+d x]}{2 d}-\frac{a^2 \csc [c+d x]^2 \sec [c+d x]}{2 d}+\frac{2 a b \tan [c+d x]}{d}$$

Result (type 3, 238 leaves):

$$\frac{1}{2 d\left(\csc \left[\frac{1}{2}(c+d x)\right]^2-\sec \left[\frac{1}{2}(c+d x)\right]^2\right)} \csc [c+d x]^4\left(2 a^2+4 b^2-2\left(3 a^2+2 b^2\right) \cos [2(c+d x)]\right)+3 a^2 \cos [3(c+d x)] \log \left[\cos \left[\frac{1}{2}(c+d x)\right]\right]+2 b^2 \cos [3(c+d x)] \log \left[\cos \left[\frac{1}{2}(c+d x)\right]\right]-\left(3 a^2+2 b^2\right) \cos [c+d x]\left(\log \left[\cos \left[\frac{1}{2}(c+d x)\right]\right]-\log \left[\sin \left[\frac{1}{2}(c+d x)\right]\right]\right)-3 a^2 \cos [3(c+d x)] \log \left[\sin \left[\frac{1}{2}(c+d x)\right]\right]-2 b^2 \cos [3(c+d x)] \log \left[\sin \left[\frac{1}{2}(c+d x)\right]\right]+8 a b \sin [c+d x]-8 a b \sin [3(c+d x)]$$

Problem 1462: Result more than twice size of optimal antiderivative.

$$\int \csc [c+d x]^3 \sec [c+d x]^2 (a+b \sin [c+d x])^3 dx$$

Optimal (type 3, 132 leaves, 14 steps):

$$-\frac{3 a^3 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{2 d}-\frac{3 a b^2 \operatorname{ArcTanh}[\operatorname{Cos}[c+d x]]}{d}-\frac{3 a^2 b \operatorname{Cot}[c+d x]}{d}+\frac{3 a^3 \operatorname{Sec}[c+d x]}{2 d}+\frac{3 a b^2 \operatorname{Sec}[c+d x]}{d}-\frac{a^3 \operatorname{Csc}[c+d x]^2 \operatorname{Sec}[c+d x]}{2 d}+\frac{3 a^2 b \operatorname{Tan}[c+d x]}{d}+\frac{b^3 \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 267 leaves):

$$\frac{1}{2 d\left(\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2-\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)} \operatorname{Csc}[c+d x]^4\left(2 a^3+12 a b^2-6\left(a^3+2 a b^2\right) \operatorname{Cos}[2(c+d x)]+\right. \\ \left.3 a^3 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]+6 a b^2 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]-\right. \\ \left.3 a\left(a^2+2 b^2\right) \operatorname{Cos}[c+d x]\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)-\right. \\ \left.3 a^3 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-6 a b^2 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]+12 a^2 b \operatorname{Sin}[c+d x]+6 b^3 \operatorname{Sin}[c+d x]-12 a^2 b \operatorname{Sin}[3(c+d x)]-2 b^3 \operatorname{Sin}[3(c+d x)]\right)$$

Problem 1479: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[e+f x]^2(a+b \operatorname{Sin}[e+f x])^{3 / 2}}{\sqrt{d \operatorname{Sin}[e+f x]}} d x$$

Optimal (type 4, 312 leaves, ? steps):

$$\frac{\operatorname{Sec}[e+f x](b+a \operatorname{Sin}[e+f x]) \sqrt{a+b \operatorname{Sin}[e+f x]}}{f \sqrt{d \operatorname{Sin}[e+f x]}}-\frac{1}{\sqrt{d} f}(a+b)^{3 / 2} \sqrt{-\frac{a(-1+\operatorname{Csc}[e+f x])}{a+b}} \\ \sqrt{\frac{a(1+\operatorname{Csc}[e+f x])}{a-b}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+b \operatorname{Sin}[e+f x]}}{\sqrt{a+b} \sqrt{d \operatorname{Sin}[e+f x]}}\right],-\frac{a+b}{a-b}\right] \operatorname{Tan}[e+f x]- \\ \left(b(a+b) \sqrt{-\frac{a(-1+\operatorname{Csc}[e+f x])}{a+b}} \sqrt{\frac{b+a \operatorname{Csc}[e+f x]}{-a+b}}\right. \\ \left.\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{-\frac{b+a \operatorname{Csc}[e+f x]}{a-b}}\right],-\frac{-a+b}{a+b}\right](1+\operatorname{Sin}[e+f x]) \operatorname{Tan}[e+f x]\right) / \\ \left(f \sqrt{\frac{a(1+\operatorname{Csc}[e+f x])}{a-b}} \sqrt{d \operatorname{Sin}[e+f x]} \sqrt{a+b \operatorname{Sin}[e+f x]}\right)$$

Result (type 4, 1515 leaves):

$$\begin{aligned}
 & -\frac{1}{f \sqrt{d \sin[e+fx]}} 2 a^2 \sqrt{\sin[e+fx]} \\
 & \left(\left(\sqrt{\cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sin[e+fx]}{a}}}{\sqrt{2}}}\right], \frac{2a}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) / \\
 & \quad \left(\sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - \left(b \sqrt{\cot\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2} \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{a}{a+b}, \operatorname{ArcSin}\left[\sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sin[e+fx]}{a}}}{\sqrt{2}}}\right], \frac{2a}{a+b}\right] \operatorname{Sec}[e+fx] \right. \\
 & \quad \left. \sin\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 \sin[e+fx]}{a}} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e+\frac{\pi}{2}-fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) \right) / \\
 & \quad \left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - \\
 & \quad \left(\frac{1}{f \sqrt{d \sin[e+fx]}} b \sqrt{\sin[e+fx]} \sqrt{2} \tan\left[\frac{1}{2}(e+fx)\right] \sqrt{\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} \right)
 \end{aligned}$$

$$\sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}} -$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}} \sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}}}} \sqrt{2} \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right] \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}}$$

$$\left(\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}} \left(a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + i \left(b - \sqrt{-a^2 + b^2} \right)} \right.$$

$$\left. \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \left(\operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} \right], \right. \right.$$

$$\left. \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} - \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right)$$

$$\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^{3/2} \sqrt{1 + \frac{a}{b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] - \sqrt{-a^2 + b^2} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} -$$

$$a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[-\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right]$$

$$\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^{3/2} \sqrt{1 + \frac{a}{b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] - \sqrt{-a^2 + b^2} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} +$$

$$a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^{3/2} \right. \\ \left. \sqrt{\frac{1 + \frac{a}{b \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] - \sqrt{-a^2 + b^2} \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}}{a}} \right) + \right. \\ \left. \frac{(a + b \operatorname{Sin}[e + f x])^{3/2} \operatorname{Tan}[e + f x]}{f \sqrt{d \operatorname{Sin}[e + f x]}} \right.$$

Problem 1480: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[e + f x]^4 (a + b \operatorname{Sin}[e + f x])^{5/2}}{\sqrt{d \operatorname{Sin}[e + f x]}} dx$$

Optimal (type 4, 366 leaves, ? steps):

$$\frac{5 a \operatorname{Sec}[e + f x] (b + a \operatorname{Sin}[e + f x]) \sqrt{a + b \operatorname{Sin}[e + f x]}}{6 f \sqrt{d \operatorname{Sin}[e + f x]}} + \\ \frac{\operatorname{Sec}[e + f x]^3 \sqrt{d \operatorname{Sin}[e + f x]} (a + b \operatorname{Sin}[e + f x])^{5/2}}{3 d f} - \frac{1}{6 \sqrt{d} f} \\ 5 a (a + b)^{3/2} \sqrt{-\frac{a (-1 + \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \\ \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}} \right], -\frac{a + b}{a - b} \right] \operatorname{Tan}[e + f x] - \\ \left(5 a b (a + b) \sqrt{-\frac{a (-1 + \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{b + a \operatorname{Csc}[e + f x]}{-a + b}} \right. \\ \left. \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\sqrt{-\frac{b + a \operatorname{Csc}[e + f x]}{a - b}} \right], \frac{-a + b}{a + b} \right] (1 + \operatorname{Sin}[e + f x]) \operatorname{Tan}[e + f x] \right) / \\ \left(6 f \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \sqrt{d \operatorname{Sin}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]} \right)$$

Result (type 4, 9121 leaves):

$$\begin{aligned}
 & - \frac{1}{3 f \sqrt{d \sin [e+f x]}} 5 a^3 \sqrt{\sin [e+f x]} \\
 & \left(\left(\sqrt{\cot \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}}}{\sqrt{2}} \right], \frac{2 a}{a+b} \right] \right. \right. \\
 & \left. \left. \operatorname{Sec} [e+f x] \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}} \right. \right. \\
 & \left. \left. \sqrt{\frac{\operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}} \right] \right) \right) \\
 & \left(\sqrt{\sin [e+f x]} \sqrt{a+b \sin [e+f x]} \right) - \left(b \sqrt{\cot \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2} \right. \\
 & \left. \operatorname{EllipticPi} \left[\frac{a}{a+b}, \operatorname{ArcSin} \left[\frac{\sqrt{-\frac{(a+b) \operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}}}{\sqrt{2}} \right], \frac{2 a}{a+b} \right] \operatorname{Sec} [e+f x] \right. \\
 & \left. \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e+f x]}{a}} \right. \right. \\
 & \left. \left. \sqrt{\frac{\operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e+f x])}{a}} \right] \right) \right) \\
 & \left((a+b) \sqrt{\sin [e+f x]} \sqrt{a+b \sin [e+f x]} \right) + \\
 & \left(\sin [e+f x] \sqrt{a+b \sin [e+f x]} \left(\frac{1}{3} \operatorname{Sec} [e+f x]^3 (a^2+b^2+2 a b \sin [e+f x]) + \right. \right. \\
 & \left. \left. \frac{1}{6} \operatorname{Sec} [e+f x] (5 a^2-2 b^2+5 a b \sin [e+f x]) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(f \sqrt{d \sin[e + f x]} \right) - \left(5 a b \sin[e + f x] \sqrt{a + b \sin[e + f x]} \right. \\
 & \left. \left(\sqrt{2} \tan\left[\frac{1}{2}(e + f x)\right] \sqrt{\frac{\tan\left[\frac{1}{2}(e + f x)\right]}{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2}} \sqrt{\frac{a + 2 b \tan\left[\frac{1}{2}(e + f x)\right] + a \tan\left[\frac{1}{2}(e + f x)\right]^2}{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2}} \right. \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} (a + 2 b \tan\left[\frac{1}{2}(e + f x)\right] + a \tan\left[\frac{1}{2}(e + f x)\right]^2)} \right. \\
 & \left. \sqrt{2} \left(\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} (a + 2 b \cot\left[\frac{1}{2}(e + f x)\right] + a \cot\left[\frac{1}{2}(e + f x)\right]^2) + \right. \right. \\
 & \left. \left(i (b - \sqrt{-a^2 + b^2}) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e + f x)\right]}{b - \sqrt{-a^2 + b^2}}} \right. \right. \\
 & \left. \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e + f x)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \text{EllipticF}\left[\right. \right. \\
 & \left. \left. i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e + f x)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \left/ \left(\sqrt{\tan\left[\frac{1}{2}(e + f x)\right]} \right) \right. \\
 & \left. \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e + f x)\right]}{b - \sqrt{-a^2 + b^2}}} \right. \right. \\
 & \left. \left. \text{EllipticPi}\left[-\frac{i (b + \sqrt{-a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e + f x)\right]}} \right], \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right) \right/ \left(\sqrt{\tan\left[\frac{1}{2}(e + fx)\right]} \right) + \right. \right.$$

$$\left. \left. \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e + fx)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e + fx)\right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[\right. \right. \right. \right.$$

$$\left. \left. \left. \frac{i(b + \sqrt{-a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e + fx)\right]}}\right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \right/ \right.$$

$$\left. \left. \left(\sqrt{\tan\left[\frac{1}{2}(e + fx)\right]} \right) \right) \left(\frac{\tan\left[\frac{1}{2}(e + fx)\right]}{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2} \right)^{3/2} \right.$$

$$\left. \left. \left(1 + \tan\left[\frac{1}{2}(e + fx)\right]^2 \right)^2 \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(e + fx)\right] + a \tan\left[\frac{1}{2}(e + fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2}} \right) \right) \right/ \right.$$

$$\left(6 f \sqrt{d \sin[e + fx]} \left(\frac{1}{\sqrt{2}} \sec\left[\frac{1}{2}(e + fx)\right]^2 \sqrt{\frac{\tan\left[\frac{1}{2}(e + fx)\right]}{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2}} \right. \right.$$

$$\left. \left. \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(e + fx)\right] + a \tan\left[\frac{1}{2}(e + fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2}} + \right. \right.$$

$$\left. \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}} \left(a + 2b \tan\left[\frac{1}{2}(e + fx)\right] + a \tan\left[\frac{1}{2}(e + fx)\right]^2 \right)^2 \right) \right)$$

$$\begin{aligned}
 & \sqrt{2} \left(\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2 b \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right] + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]^2 \right) + \right. \\
 & \left. i \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \right. \\
 & \left. \left(\operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \operatorname{EllipticF} \left[\right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \right) / \left(\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) - \\
 & \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi} \left[\right. \right. \\
 & \left. \left. - \frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) / \\
 & \left(\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) + \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi} \left[\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) / \left(\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(b \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + a \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \left(\frac{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^{3/2} \\
 & \frac{\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \sqrt{\frac{a + 2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}}}{1} \\
 & \sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & 2\sqrt{2} \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2b \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right] + a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]^2 \right) + \right. \\
 & \left. \left(i \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b - \sqrt{-a^2 + b^2}}} \right) \right. \\
 & \left. \left(\operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \operatorname{EllipticF}\left[\right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \right) / \left(\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} \right) - \\
 & \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[\right. \right. \\
 & \left. \left. - \frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]} \right) + \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{-a^2 + b^2})}{a}\right], \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}}\right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] / \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]} \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right] \left(\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{3/2} \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(e+fx)\right] + a \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2b \tan\left[\frac{1}{2}(e+fx)\right] + a \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)} \\
 & \sqrt{2} \left(\frac{i a \sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{Csc}\left[\frac{1}{2}(e+fx)\right]^2}{4 \left(1 - i \cot\left[\frac{1}{2}(e+fx)\right] \right) \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}}} \right) - \\
 & \left(i a \sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{Csc}\left[\frac{1}{2}(e+fx)\right]^2 \right) / \\
 & \left(4 \left(1 + i \cot\left[\frac{1}{2}(e+fx)\right] \right) \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \right) + \\
 & \sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(-b \operatorname{Csc}\left[\frac{1}{2}(e+fx)\right]^2 - a \cot\left[\frac{1}{2}(e+fx)\right] \operatorname{Csc}\left[\frac{1}{2}(e+fx)\right]^2 \right) -
 \end{aligned}$$

$$\left(i \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \right.$$

$$\left. \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \operatorname{EllipticF} \left[\right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 \right) /$$

$$\left(4 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^{3/2} \right) + \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \right.$$

$$\left. \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi} \left[-\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 \right) /$$

$$\left(4 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]^{3/2} \right) - \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \right.$$

$$\left. \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi} \left[\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \operatorname{Sec} \left[\frac{1}{2} (e + f x) \right]^2 \right) /$$

$$\begin{aligned}
 & \left(4 \operatorname{Tan} \left[\frac{1}{2} (e + f x) \right] \right)^{3/2} - \left(i a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \right. \\
 & \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \left(\operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \right. \\
 & \left. \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \Bigg/ \\
 & \left(4 \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) - \\
 & \left(i a (b - \sqrt{-a^2 + b^2}) \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \right. \\
 & \left(\operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \right. \\
 & \left. \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \Bigg/ \\
 & \left(4 (b + \sqrt{-a^2 + b^2}) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) + \\
 & \left(a^2 \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{EllipticPi} \left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. - \frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] / \\
 & \left(4 \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) + \\
 & \left(a^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{EllipticPi} \left[- \frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) / \\
 & \left(4 \left(b + \sqrt{-a^2 + b^2} \right) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) - \\
 & \left(a^2 \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b + \sqrt{-a^2 + b^2}}} \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{EllipticPi} \left[\right. \right. \\
 & \left. \left. \frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) / \\
 & \left(4 \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \sqrt{\operatorname{Tan} \left[\frac{1}{2} (e + f x) \right]} \right) - \\
 & \left(a^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[\frac{1}{2} (e + f x) \right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{Csc} \left[\frac{1}{2} (e + f x) \right]^2 \operatorname{EllipticPi} \left[\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(i \operatorname{ArcSinh} \left[\frac{\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2} (e+fx) \right]}} \right], \frac{b+\sqrt{-a^2+b^2}}{b-\sqrt{-a^2+b^2}} \right) / \\
 & \left(4 \left(b+\sqrt{-a^2+b^2} \right) \sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b+\sqrt{-a^2+b^2}}} \sqrt{\tan \left[\frac{1}{2} (e+fx) \right]} \right) + \\
 & \left(i \left(b-\sqrt{-a^2+b^2} \right) \sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b+\sqrt{-a^2+b^2}}} \right) \\
 & \sqrt{1+\frac{a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b-\sqrt{-a^2+b^2}}} \left(i \sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}} \operatorname{Sec} \left[\frac{1}{2} (e+fx) \right]^2 \right) / \\
 & \left(4 \sqrt{1+\frac{a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b-\sqrt{-a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b+\sqrt{-a^2+b^2}}} \tan \left[\frac{1}{2} (e+fx) \right]^{3/2} \right) - \\
 & \left(i \sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b-\sqrt{-a^2+b^2}}} \operatorname{Sec} \left[\frac{1}{2} (e+fx) \right]^2 \right) / \\
 & \left(4 \sqrt{1+\frac{a \operatorname{Cot} \left[\frac{1}{2} (e+fx) \right]}{b+\sqrt{-a^2+b^2}}} \tan \left[\frac{1}{2} (e+fx) \right]^{3/2} \right) / \\
 & \left(\sqrt{\tan \left[\frac{1}{2} (e+fx) \right]} \right) \left(\frac{\tan \left[\frac{1}{2} (e+fx) \right]}{1+\tan \left[\frac{1}{2} (e+fx) \right]^2} \right)^{3/2} \\
 & \left(1+\tan \left[\frac{1}{2} (e+fx) \right]^2 \right)^2 \sqrt{\frac{a+2b \tan \left[\frac{1}{2} (e+fx) \right]+a \tan \left[\frac{1}{2} (e+fx) \right]^2}{1+\tan \left[\frac{1}{2} (e+fx) \right]^2}} +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \sqrt{\frac{a+2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}} \right. \\
 & \left. \left(-\frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)} \right) \right) / \\
 & \left(\sqrt{2} \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}} \right) - \\
 & \left(1 / \left(\sqrt{2} \sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}} \left(a+2b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \\
 & 3 \left(\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}} \left(a+2b \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]+a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]^2 \right) + \right. \\
 & \left. \left(i \left(b-\sqrt{-a^2+b^2} \right) \sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b-\sqrt{-a^2+b^2}}} \right) \right. \\
 & \left. \left(\operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b+\sqrt{-a^2+b^2}}{b-\sqrt{-a^2+b^2}} \right] - \operatorname{EllipticF}\left[\right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b+\sqrt{-a^2+b^2}}{b-\sqrt{-a^2+b^2}} \right] \right) \right) / \left(\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} \right) - \\
 & \left(a \sqrt{\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(e+fx)\right]}{b-\sqrt{-a^2+b^2}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i\left(b+\sqrt{-a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}}\right],\right. \\
 & \left.\frac{b+\sqrt{-a^2+b^2}}{b-\sqrt{-a^2+b^2}}\right] / \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right) + \\
 & \left(a \sqrt{\frac{b+\sqrt{-a^2+b^2}+a \cot\left[\frac{1}{2}(e+fx)\right]}{b+\sqrt{-a^2+b^2}}}\sqrt{1+\frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b-\sqrt{-a^2+b^2}}}\right) \text{EllipticPi}\left[\right. \\
 & \left. \frac{i\left(b+\sqrt{-a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{-a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}}\right], \frac{b+\sqrt{-a^2+b^2}}{b-\sqrt{-a^2+b^2}}\right] / \\
 & \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}\right) \sqrt{\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} \\
 & \left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(e+fx)\right]+a \tan\left[\frac{1}{2}(e+fx)\right]^2}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} \\
 & \left(-\frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}+\frac{\sec\left[\frac{1}{2}(e+fx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}\right) + \\
 & \left(\tan\left[\frac{1}{2}(e+fx)\right]\sqrt{\frac{\tan\left[\frac{1}{2}(e+fx)\right]}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}}\right. \\
 & \left.\frac{b \sec\left[\frac{1}{2}(e+fx)\right]^2+a \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}-\right. \\
 & \left.\left(\sec\left[\frac{1}{2}(e+fx)\right]\right)^2 \tan\left[\frac{1}{2}(e+fx)\right]\left(a+2b \tan\left[\frac{1}{2}(e+fx)\right]+a \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \Bigg) / \\
 & \left(\sqrt{2} \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(e+fx)\right] + a \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}} \right) - \\
 & \left(\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2b \cot\left[\frac{1}{2}(e+fx)\right] + a \cot\left[\frac{1}{2}(e+fx)\right]^2 \right) + \right. \\
 & \left. \left(i \left(b - \sqrt{-a^2 + b^2} \right) \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b - \sqrt{-a^2 + b^2}}} \right) \right. \\
 & \left. \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) \right) / \\
 & \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]} \right) - \left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \cot\left[\frac{1}{2}(e+fx)\right]}{b + \sqrt{-a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(e+fx)\right]}{b - \sqrt{-a^2 + b^2}}} \text{EllipticPi}\left[-\frac{i \left(b + \sqrt{-a^2 + b^2} \right)}{a}, i \right. \right. \\
 & \left. \left. \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]}} \right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}} \right] \right) / \left(\sqrt{\tan\left[\frac{1}{2}(e+fx)\right]} \right) +
 \end{aligned}$$

$$\left(a \sqrt{\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right]}{b + \sqrt{-a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(e + f x)\right]}{b - \sqrt{-a^2 + b^2}}} \operatorname{EllipticPi}\left[\frac{i\left(b + \sqrt{-a^2 + b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}}\right], \frac{b + \sqrt{-a^2 + b^2}}{b - \sqrt{-a^2 + b^2}}\right] \right) / \left(\sqrt{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]} \right) \left(\frac{\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} \right)^{3/2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right)^2 \left(\frac{b \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + a \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} - \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \left(a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \right) \right) / \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right)^2 \right) / \left(\sqrt{2} \sqrt{\frac{a}{b + \sqrt{-a^2 + b^2}}} \left(a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}} \right) \right)$$

Problem 1483: Result more than twice size of optimal antiderivative.

$$\int (a + b \sin[c + d x]) \operatorname{Tan}[c + d x]^5 dx$$

Optimal (type 3, 116 leaves, 7 steps):

$$\frac{(8a + 15b) \operatorname{Log}[1 - \operatorname{Sin}[c + dx]]}{16d} - \frac{(8a - 15b) \operatorname{Log}[1 + \operatorname{Sin}[c + dx]]}{16d} - \frac{15b \operatorname{Sin}[c + dx]}{8d} - \frac{(4a + 5b \operatorname{Sin}[c + dx]) \operatorname{Tan}[c + dx]^2}{8d} + \frac{(a + b \operatorname{Sin}[c + dx]) \operatorname{Tan}[c + dx]^4}{4d}$$

Result (type 3, 246 leaves):

$$\frac{a \operatorname{Log}[\operatorname{Cos}[c + dx]]}{d} - \frac{15b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8d} + \frac{15b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8d} - \frac{a \operatorname{Sec}[c + dx]^2}{d} + \frac{a \operatorname{Sec}[c + dx]^4}{4d} + \frac{b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} - \frac{b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{9b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{b \operatorname{Sin}[c + dx]}{d} - \frac{9b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2}$$

Problem 1484: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + dx] (a + b \operatorname{Sin}[c + dx]) \operatorname{Tan}[c + dx]^4 dx$$

Optimal (type 3, 103 leaves, 7 steps):

$$\frac{3a \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} - \frac{b \operatorname{Log}[\operatorname{Cos}[c + dx]]}{d} - \frac{3a \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{8d} - \frac{b \operatorname{Tan}[c + dx]^2}{2d} + \frac{a \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]^3}{4d} + \frac{b \operatorname{Tan}[c + dx]^4}{4d}$$

Result (type 3, 234 leaves):

$$\frac{b \operatorname{Log}[\operatorname{Cos}[c + dx]]}{d} - \frac{3a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8d} + \frac{3a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8d} - \frac{b \operatorname{Sec}[c + dx]^2}{d} + \frac{b \operatorname{Sec}[c + dx]^4}{4d} + \frac{5a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} - \frac{5a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} + \frac{5a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{5a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2}$$

Problem 1486: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 (a + b \sin[c + dx]) \tan[c + dx]^2 dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$-\frac{a \operatorname{ArcTanh}[\sin[c + dx]]}{8d} - \frac{a \sec[c + dx] \tan[c + dx]}{8d} + \frac{a \sec[c + dx]^3 \tan[c + dx]}{4d} + \frac{b \tan[c + dx]^4}{4d}$$

Result (type 3, 207 leaves):

$$\begin{aligned} & \frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8d} - \\ & \frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8d} + \frac{a}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} - \\ & \frac{a}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{a}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\ & \frac{a}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \frac{b \tan[c + dx]^4}{4d} \end{aligned}$$

Problem 1487: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^4 (a + b \sin[c + dx]) \tan[c + dx] dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$-\frac{b \operatorname{ArcTanh}[\sin[c + dx]]}{8d} + \frac{a \sec[c + dx]^4}{4d} - \frac{b \sec[c + dx] \tan[c + dx]}{8d} + \frac{b \sec[c + dx]^3 \tan[c + dx]}{4d}$$

Result (type 3, 207 leaves):

$$\begin{aligned} & \frac{b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8d} - \\ & \frac{b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8d} + \frac{a \sec[c + dx]^4}{4d} + \\ & \frac{b}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} - \frac{b}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} - \\ & \frac{b}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{b}{16d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} \end{aligned}$$

Problem 1488: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx] \text{Sec}[c + dx]^5 (a + b \text{Sin}[c + dx]) dx$$

Optimal (type 3, 99 leaves, 8 steps):

$$\frac{3 b \text{ArcTanh}[\text{Sin}[c + dx]]}{8 d} + \frac{a \text{Log}[\text{Tan}[c + dx]]}{d} + \frac{3 b \text{Sec}[c + dx] \text{Tan}[c + dx]}{8 d} + \frac{b \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{4 d} + \frac{a \text{Tan}[c + dx]^2}{d} + \frac{a \text{Tan}[c + dx]^4}{4 d}$$

Result (type 3, 248 leaves):

$$\frac{a \text{Log}[\text{Cos}[c + dx]]}{d} - \frac{3 b \text{Log}[\text{Cos}[\frac{1}{2}(c + dx)] - \text{Sin}[\frac{1}{2}(c + dx)]]}{8 d} + \frac{3 b \text{Log}[\text{Cos}[\frac{1}{2}(c + dx)] + \text{Sin}[\frac{1}{2}(c + dx)]]}{8 d} + \frac{a \text{Log}[\text{Sin}[c + dx]]}{d} + \frac{a \text{Sec}[c + dx]^2}{2 d} + \frac{a \text{Sec}[c + dx]^4}{4 d} + \frac{b}{16 d (\text{Cos}[\frac{1}{2}(c + dx)] - \text{Sin}[\frac{1}{2}(c + dx)])^4} + \frac{3 b}{16 d (\text{Cos}[\frac{1}{2}(c + dx)] - \text{Sin}[\frac{1}{2}(c + dx)])^2} - \frac{b}{16 d (\text{Cos}[\frac{1}{2}(c + dx)] + \text{Sin}[\frac{1}{2}(c + dx)])^4} - \frac{3 b}{16 d (\text{Cos}[\frac{1}{2}(c + dx)] + \text{Sin}[\frac{1}{2}(c + dx)])^2}$$

Problem 1489: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^2 \text{Sec}[c + dx]^5 (a + b \text{Sin}[c + dx]) dx$$

Optimal (type 3, 115 leaves, 10 steps):

$$\frac{15 a \text{ArcTanh}[\text{Sin}[c + dx]]}{8 d} - \frac{15 a \text{Csc}[c + dx]}{8 d} + \frac{b \text{Log}[\text{Tan}[c + dx]]}{d} + \frac{5 a \text{Csc}[c + dx] \text{Sec}[c + dx]^2}{8 d} + \frac{a \text{Csc}[c + dx] \text{Sec}[c + dx]^4}{4 d} + \frac{b \text{Tan}[c + dx]^2}{d} + \frac{b \text{Tan}[c + dx]^4}{4 d}$$

Result (type 3, 284 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{2d} - \frac{b \operatorname{Log}[\operatorname{Cos}[c+dx]]}{d} - \frac{15 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{15 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{b \operatorname{Log}[\operatorname{Sin}[c+dx]]}{d} + \\
 & \frac{b \operatorname{Sec}[c+dx]^2}{2d} + \frac{b \operatorname{Sec}[c+dx]^4}{4d} + \frac{a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \\
 & \frac{7a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\
 & \frac{7a}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d}
 \end{aligned}$$

Problem 1490: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^3 \operatorname{Sec}[c+dx]^5 (a+b \operatorname{Sin}[c+dx]) dx$$

Optimal (type 3, 135 leaves, 10 steps):

$$\begin{aligned}
 & \frac{15 b \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} - \frac{a \operatorname{Cot}[c+dx]^2}{2d} - \frac{15 b \operatorname{Csc}[c+dx]}{8d} + \frac{3 a \operatorname{Log}[\operatorname{Tan}[c+dx]]}{d} + \\
 & \frac{5 b \operatorname{Csc}[c+dx] \operatorname{Sec}[c+dx]^2}{8d} + \frac{b \operatorname{Csc}[c+dx] \operatorname{Sec}[c+dx]^4}{4d} + \frac{3 a \operatorname{Tan}[c+dx]^2}{2d} + \frac{a \operatorname{Tan}[c+dx]^4}{4d}
 \end{aligned}$$

Result (type 3, 298 leaves):

$$\begin{aligned}
 & - \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{2d} - \frac{a \operatorname{Csc}[c+dx]^2}{2d} - \\
 & \frac{3 a \operatorname{Log}[\operatorname{Cos}[c+dx]]}{d} - \frac{15 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{15 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{3 a \operatorname{Log}[\operatorname{Sin}[c+dx]]}{d} + \\
 & \frac{a \operatorname{Sec}[c+dx]^2}{d} + \frac{a \operatorname{Sec}[c+dx]^4}{4d} + \frac{b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} + \\
 & \frac{7b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\
 & \frac{7b}{16d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d}
 \end{aligned}$$

Problem 1491: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^4 \text{Sec}[c + dx]^5 (a + b \text{Sin}[c + dx]) dx$$

Optimal (type 3, 155 leaves, 11 steps):

$$\frac{35 a \text{ArcTanh}[\text{Sin}[c + dx]]}{8 d} - \frac{b \text{Cot}[c + dx]^2}{2 d} - \frac{35 a \text{Csc}[c + dx]}{8 d} - \frac{35 a \text{Csc}[c + dx]^3}{24 d} + \frac{3 b \text{Log}[\text{Tan}[c + dx]]}{d} + \frac{7 a \text{Csc}[c + dx]^3 \text{Sec}[c + dx]^2}{8 d} + \frac{a \text{Csc}[c + dx]^3 \text{Sec}[c + dx]^4}{4 d} + \frac{3 b \text{Tan}[c + dx]^2}{2 d} + \frac{b \text{Tan}[c + dx]^4}{4 d}$$

Result (type 3, 358 leaves):

$$\frac{19 a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{12 d} - \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right] \text{Csc}\left[\frac{1}{2}(c + dx)\right]^2}{24 d} - \frac{b \text{Csc}[c + dx]^2}{2 d} - \frac{3 b \text{Log}[\text{Cos}[c + dx]]}{d} - \frac{35 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} + \frac{35 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} + \frac{3 b \text{Log}[\text{Sin}[c + dx]]}{d} + \frac{b \text{Sec}[c + dx]^2}{d} + \frac{b \text{Sec}[c + dx]^4}{4 d} + \frac{a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{11 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{11 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^4} - \frac{11 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{19 a \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{12 d} - \frac{a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c + dx)\right]}{24 d}$$

Problem 1495: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + dx]^2 (a + b \text{Sin}[c + dx])^2 \text{Tan}[c + dx]^3 dx$$

Optimal (type 3, 116 leaves, 7 steps):

$$\frac{b(3a + 4b) \text{Log}[1 - \text{Sin}[c + dx]]}{8 d} + \frac{(3a - 4b) b \text{Log}[1 + \text{Sin}[c + dx]]}{8 d} + \frac{\text{Sec}[c + dx]^4 (a + b \text{Sin}[c + dx])^2}{4 d} - \frac{\text{Sec}[c + dx]^2 (a + b \text{Sin}[c + dx]) (2a + 3b \text{Sin}[c + dx])}{4 d}$$

Result (type 3, 264 leaves):

$$\begin{aligned}
 & - \frac{b^2 \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{3 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{4 d} + \\
 & \frac{3 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{4 d} - \frac{b^2 \operatorname{Sec}[c + d x]^2}{d} + \\
 & \frac{b^2 \operatorname{Sec}[c + d x]^4}{4 d} + \frac{a b}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \\
 & \frac{a b}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \\
 & \frac{5 a b}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{a b}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \\
 & \frac{a^2 \operatorname{Tan}[c + d x]^4}{4 d}
 \end{aligned}$$

Problem 1496: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^2 \operatorname{Tan}[c + d x]^2 dx$$

Optimal (type 3, 93 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{(a^2 - 3 b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} - \\
 & \frac{\operatorname{Sec}[c + d x]^2 (4 a b + (a^2 + 3 b^2) \operatorname{Sin}[c + d x])}{8 d} + \frac{\operatorname{Sec}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^2 \operatorname{Tan}[c + d x]}{4 d}
 \end{aligned}$$

Result (type 3, 216 leaves):

$$\begin{aligned}
 & \frac{1}{16 d} \left(2 (a^2 - 3 b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \\
 & \left. 2 (a^2 - 3 b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \\
 & \left. \frac{(a + b)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{a^2 + 6 a b + 5 b^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} \right. \\
 & \left. \frac{(a - b)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{a^2 - 6 a b + 5 b^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} \right)
 \end{aligned}$$

Problem 1497: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^4 (a + b \operatorname{Sin}[c + d x])^2 \operatorname{Tan}[c + d x] dx$$

Optimal (type 3, 72 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{a b \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{4 d} + \frac{\operatorname{Sec}[c + d x]^4 (a + b \operatorname{Sin}[c + d x])^2}{4 d} - \frac{\operatorname{Sec}[c + d x]^2 (b^2 + a b \operatorname{Sin}[c + d x])}{4 d}
 \end{aligned}$$

Result (type 3, 200 leaves):

$$\frac{1}{16 d} \left(4 a b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right] - 4 a b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right] + \frac{(a+b)^2}{\left(\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right)^4} + \frac{a^2 - 2 a b - 3 b^2}{\left(\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right)^2} + \frac{(a-b)^2}{\left(\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right)^4} + \frac{a^2 + 2 a b - 3 b^2}{\left(\operatorname{Cos} \left[\frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c+d x) \right] \right)^2} \right)$$

Problem 1500: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x]^5 (a+b \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 185 leaves, 6 steps):

$$\begin{aligned} & - \frac{2 a b \operatorname{Csc}[c+d x]}{d} - \frac{a^2 \operatorname{Csc}[c+d x]^2}{2 d} - \frac{(12 a^2 + 15 a b + 4 b^2) \operatorname{Log}[1 - \operatorname{Sin}[c+d x]]}{8 d} + \\ & \frac{(3 a^2 + b^2) \operatorname{Log}[\operatorname{Sin}[c+d x]]}{d} - \frac{(12 a^2 - 15 a b + 4 b^2) \operatorname{Log}[1 + \operatorname{Sin}[c+d x]]}{8 d} + \\ & \frac{\operatorname{Sec}[c+d x]^4 (a^2 + b^2 + 2 a b \operatorname{Sin}[c+d x])}{4 d} + \frac{\operatorname{Sec}[c+d x]^2 (2 (2 a^2 + b^2) + 7 a b \operatorname{Sin}[c+d x])}{4 d} \end{aligned}$$

Result (type 3, 717 leaves):

$$\begin{aligned}
 & - \frac{a b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{d (a+b \operatorname{Sin}[c+d x])^2} - \\
 & \frac{a^2 \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{8 d (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \left((-12 a^2 - 15 a b - 4 b^2) (b+a \operatorname{Csc}[c+d x])^2 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x]^2\right) / (4 d (a+b \operatorname{Sin}[c+d x])^2) + \\
 & \left((-12 a^2 + 15 a b - 4 b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right. \\
 & \quad \left. \operatorname{Sin}[c+d x]^2\right) / (4 d (a+b \operatorname{Sin}[c+d x])^2) + \\
 & \frac{(3 a^2 + b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Log}[\operatorname{Sin}[c+d x]] \operatorname{Sin}[c+d x]^2}{d (a+b \operatorname{Sin}[c+d x])^2} - \\
 & \frac{a^2 (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]^2}{8 d (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \frac{(a^2 + 2 a b + b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4 (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \frac{(9 a^2 + 14 a b + 5 b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \frac{(a^2 - 2 a b + b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4 (a+b \operatorname{Sin}[c+d x])^2} + \\
 & \frac{(9 a^2 - 14 a b + 5 b^2) (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 (a+b \operatorname{Sin}[c+d x])^2} - \\
 & \frac{a b (b+a \operatorname{Csc}[c+d x])^2 \operatorname{Sin}[c+d x]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{d (a+b \operatorname{Sin}[c+d x])^2}
 \end{aligned}$$

Problem 1505: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^4 (a+b \operatorname{Sin}[c+d x])^3 \operatorname{Tan}[c+d x] dx$$

Optimal (type 3, 90 leaves, 5 steps):

$$\frac{3 b (a^2 - b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{\operatorname{Sec}[c+d x]^4 (a+b \operatorname{Sin}[c+d x])^3}{4 d} - \frac{3 \operatorname{Sec}[c+d x]^2 (a+b \operatorname{Sin}[c+d x]) (b^2 + a b \operatorname{Sin}[c+d x])}{8 d}$$

Result (type 3, 212 leaves):

$$\frac{1}{16d} \left(6b(a^2 - b^2) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] - \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. 6b(-a^2 + b^2) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] + \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. \frac{(a+b)^3}{\left(\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] - \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right)^4} + \frac{(a-5b)(a+b)^2}{\left(\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] - \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right)^2} + \right. \\ \left. \frac{(a-b)^3}{\left(\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] + \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right)^4} + \frac{(a-b)^2(a+5b)}{\left(\operatorname{Cos} \left[\frac{1}{2}(c + dx) \right] + \operatorname{Sin} \left[\frac{1}{2}(c + dx) \right] \right)^2} \right)$$

Problem 1508: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c + dx]^3 \operatorname{Sec}[c + dx]^5 (a + b \operatorname{Sin}[c + dx])^3 dx$$

Optimal (type 3, 221 leaves, 6 steps):

$$\frac{3a^2 b \operatorname{Csc}[c + dx]}{d} - \frac{a^3 \operatorname{Csc}[c + dx]^2}{2d} - \frac{3(a+b)(8a^2 + 7ab + b^2) \operatorname{Log}[1 - \operatorname{Sin}[c + dx]]}{16d} + \\ \frac{3a(a^2 + b^2) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{d} - \frac{3(a-b)(8a^2 - 7ab + b^2) \operatorname{Log}[1 + \operatorname{Sin}[c + dx]]}{16d} + \\ \frac{b^2 \operatorname{Sec}[c + dx]^4 \left(a \left(3 + \frac{a^2}{b^2} \right) + \left(1 + \frac{3a^2}{b^2} \right) b \operatorname{Sin}[c + dx] \right)}{4d} + \\ \frac{b^2 \operatorname{Sec}[c + dx]^2 \left(4a \left(3 + \frac{2a^2}{b^2} \right) + 3 \left(1 + \frac{7a^2}{b^2} \right) b \operatorname{Sin}[c + dx] \right)}{8d}$$

Result (type 3, 772 leaves):

$$\begin{aligned}
 & - \frac{3 a^2 b \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{2 d (a+b \operatorname{Sin}[c+d x])^3} - \\
 & \frac{a^3 \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{8 d (a+b \operatorname{Sin}[c+d x])^3} - \\
 & \left(3\left(8 a^3+15 a^2 b+8 a b^2+b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[c+d x]^3\right) / (8 d (a+b \operatorname{Sin}[c+d x])^3) - \\
 & \left(3\left(8 a^3-15 a^2 b+8 a b^2-b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right. \\
 & \quad \left. \operatorname{Sin}[c+d x]^3\right) / (8 d (a+b \operatorname{Sin}[c+d x])^3) + \\
 & \frac{3\left(a^3+a b^2\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Log}[\operatorname{Sin}[c+d x]] \operatorname{Sin}[c+d x]^3}{d (a+b \operatorname{Sin}[c+d x])^3} - \\
 & \frac{a^3 (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]^3}{8 d (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \frac{\left(a^3+3 a^2 b+3 a b^2+b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4 (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \frac{3\left(3 a^3+7 a^2 b+5 a b^2+b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \frac{\left(a^3-3 a^2 b+3 a b^2-b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4 (a+b \operatorname{Sin}[c+d x])^3} + \\
 & \frac{3\left(3 a^3-7 a^2 b+5 a b^2-b^3\right)(b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 (a+b \operatorname{Sin}[c+d x])^3} - \\
 & \frac{3 a^2 b (b+a \operatorname{Csc}[c+d x])^3 \operatorname{Sin}[c+d x]^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{2 d (a+b \operatorname{Sin}[c+d x])^3}
 \end{aligned}$$

Problem 1509: Unable to integrate problem.

$$\int \operatorname{Sec}[c+d x]^5 \operatorname{Sin}[c+d x]^n (a+b \operatorname{Sin}[c+d x])^4 dx$$

Optimal (type 5, 295 leaves, 6 steps):

$$\begin{aligned}
& -\frac{1}{8d(1+n)}(6a^2b^2(1-n^2) - a^4(3-4n+n^2) - b^4(3+4n+n^2)) \\
& \quad \text{Hypergeometric2F1}\left[1, \frac{1+n}{2}, \frac{3+n}{2}, \text{Sin}[c+dx]^2\right] \text{Sin}[c+dx]^{1+n} - \frac{1}{2d(2+n)} \\
& a b n (a^2(2-n) - b^2(2+n)) \text{Hypergeometric2F1}\left[1, \frac{2+n}{2}, \frac{4+n}{2}, \text{Sin}[c+dx]^2\right] \text{Sin}[c+dx]^{2+n} + \\
& \frac{1}{4d} \text{Sec}[c+dx]^4 \text{Sin}[c+dx]^{1+n} (a^4 + 6a^2b^2 + b^4 + 4ab(a^2+b^2) \text{Sin}[c+dx]) + \frac{1}{8d} \text{Sec}[c+dx]^2 \\
& \quad \text{Sin}[c+dx]^{1+n} (a^4(3-n) - 6a^2b^2(1+n) - b^4(5+n) + 4ab(a^2(2-n) - b^2(2+n)) \text{Sin}[c+dx])
\end{aligned}$$

Result (type 8, 31 leaves):

$$\int \text{Sec}[c+dx]^5 \text{Sin}[c+dx]^n (a+b \text{Sin}[c+dx])^4 dx$$

Problem 1513: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c+dx]^5 \text{Sin}[c+dx]^n}{a+b \text{Sin}[c+dx]} dx$$

Optimal (type 5, 360 leaves, 10 steps):

$$\begin{aligned}
& ((3a^2 - 9ab + 8b^2) \text{Hypergeometric2F1}[1, 1+n, 2+n, -\text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}) / \\
& \quad (16(a-b)^3 d(1+n)) + \\
& ((3a^2 + 9ab + 8b^2) \text{Hypergeometric2F1}[1, 1+n, 2+n, \text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}) / \\
& \quad (16(a+b)^3 d(1+n)) - \frac{b^6 \text{Hypergeometric2F1}\left[1, 1+n, 2+n, -\frac{b \text{Sin}[c+dx]}{a}\right] \text{Sin}[c+dx]^{1+n}}{a(a^2-b^2)^3 d(1+n)} + \\
& ((3a-5b) \text{Hypergeometric2F1}[2, 1+n, 2+n, -\text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}) / \\
& \quad (16(a-b)^2 d(1+n)) + \\
& ((3a+5b) \text{Hypergeometric2F1}[2, 1+n, 2+n, \text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}) / \\
& \quad (16(a+b)^2 d(1+n)) + \frac{\text{Hypergeometric2F1}[3, 1+n, 2+n, -\text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}}{8(a-b)d(1+n)} + \\
& \frac{\text{Hypergeometric2F1}[3, 1+n, 2+n, \text{Sin}[c+dx]] \text{Sin}[c+dx]^{1+n}}{8(a+b)d(1+n)}
\end{aligned}$$

Result (type 6, 16959 leaves):

$$\left(\text{Sec}[c+dx]^5 \text{Sin}[c+dx]^n \right. \\
\left. - \left(\left(a^3(3+n) \text{AppellF1}\left[\frac{1+n}{2}, \frac{1}{2}(-1+n), 1, \frac{3+n}{2}, -\text{Tan}[c+dx]^2, \frac{(-a^2+b^2) \text{Tan}[c+dx]^2}{a^2}\right] \right) \right) \right)$$

$$\begin{aligned}
 & \left. \left(\tan [c+d x]^2 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^{-1+n} \right) / \right. \\
 & \left((1+n) \left(-a^2 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \left(2 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{5+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + a^2 (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1+n}{2}, 1, \frac{5+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c+d x]^2 \right) \left(-b^2 \tan [c+d x]^2 + a^2 (1+\tan [c+d x]^2) \right) \right) \Bigg] + \\
 & \left(a^2 b (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2+b^2 \right) \tan [c+d x]^2}{a^2} \right] \right) \\
 & \left. \left(\tan [c+d x]^2 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^n \right) / \right. \\
 & \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \right. \\
 & \quad \left(2 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c+d x]^2 \right) \left(-b^2 \tan [c+d x]^2 + a^2 (1+\tan [c+d x]^2) \right) \right) - \\
 & \left(2 a^3 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2+b^2 \right) \tan [c+d x]^2}{a^2} \right] \right) \\
 & \left. \left(\tan [c+d x]^4 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^{-1+n} \right) / \right. \\
 & \left((3+n) \left(-a^2 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \left(2 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{7+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + a^2 (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1+n}{2}, 1, \frac{7+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \tan [c+d x]^2 \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right) \right) + \\
& \left(2 a^2 b (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \right. \\
& \quad \left. \tan [c+d x]^4 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^n \right) / \\
& \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \right. \\
& \quad \left(2 \left(a^2 - b^2 \right) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
& \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
& \quad \left. \tan [c+d x]^2 \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right) \right) - \\
& \left(a^3 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \right. \\
& \quad \left. \tan [c+d x]^6 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^{-1+n} \right) / \\
& \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
& \quad \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right) + \left(2 \left(a^2 - b^2 \right) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), \right. \right. \\
& \quad \left. \left. 2, \frac{9+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + a^2 (-1+n) \right. \\
& \quad \left. \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1+n}{2}, 1, \frac{9+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
& \quad \left. \tan [c+d x]^2 \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right) \right) + \\
& \left(a^2 b (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \right. \\
& \quad \left. \tan [c+d x]^6 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^n \right) / \\
& \left((6+n) \left(-a^2 (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \right. \\
& \quad \left(2 \left(a^2 - b^2 \right) \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{n}{2}, 2, 5 + \frac{n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & a^2 n \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5+\frac{n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \\
 & \left. \tan[c+dx]^2 \left(-b^2 \tan[c+dx]^2 + a^2 (1+\tan[c+dx]^2)\right)\right] \Bigg) \Bigg) \Bigg) / \\
 & \left(d (a+b \sin[c+dx]) \left(\left(a^3 (3+n) \operatorname{AppellF1}\left[\frac{1+n}{2}, \frac{1}{2}(-1+n), 1, \frac{3+n}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2}\right] \tan[c+dx]^2 \right. \right. \right. \\
 & \left. \left. \left. (2 a^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 2 b^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx]) \right. \right. \right. \\
 & \left. \left. \left. \left(\frac{\tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}} \right)^{-1+n} \right) \right) \Bigg) / \\
 & \left((1+n) \left(-a^2 (3+n) \operatorname{AppellF1}\left[\frac{1+n}{2}, \frac{1}{2}(-1+n), 1, \frac{3+n}{2}, -\tan[c+dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \left(2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3+n}{2}, \frac{1}{2}(-1+n), \right. \right. \right. \right. \\
 & \left. \left. \left. 2, \frac{5+n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2 + a^2 (-1+n) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{3+n}{2}, \frac{1+n}{2}, 1, \frac{5+n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \tan[c+dx]^2 \left(-b^2 \tan[c+dx]^2 + a^2 (1+\tan[c+dx]^2)\right)^2 \right) \right) - \\
 & \left(a^2 b (4+n) \operatorname{AppellF1}\left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2}\right] \right. \\
 & \left. \tan[c+dx]^2 (2 a^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 2 b^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx]) \right. \\
 & \left. \left(\frac{\tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}} \right)^n \right) \Bigg) / \\
 & \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1}\left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \right. \\
 & \left. \left(2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \right. \\
 & \left. \left. a^2 n \operatorname{AppellF1}\left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right) \right. \\
 & \left. \tan[c+dx]^2 \left(-b^2 \tan[c+dx]^2 + a^2 (1+\tan[c+dx]^2)\right)^2 \right) \Bigg) + \\
 & \left(2 a^3 (5+n) \operatorname{AppellF1}\left[\frac{3+n}{2}, \frac{1}{2}(-1+n), 1, \frac{5+n}{2}, -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2}\right] \right. \\
 & \left. \tan[c+dx]^4 (2 a^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 2 b^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx]) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(\frac{\tan[c+dx]}{\sqrt{1+\tan^2[c+dx]}} \right)^{-1+n} / \\
& \left((3+n) \left(-a^2 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\tan[c+dx]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
& \quad \left. \left. \left. 2, \frac{7+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + a^2 (-1+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1+n}{2}, 1, \frac{7+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 \right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2) \right)^2 \Big) - \\
& \left(2 a^2 b (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan[c+dx]^2, \frac{(-a^2 + b^2) \tan[c+dx]^2}{a^2} \right] \right. \\
& \quad \left. \tan[c+dx]^4 \left(2 a^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 2 b^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right. \\
& \quad \left. \left(\frac{\tan[c+dx]}{\sqrt{1+\tan^2[c+dx]}} \right)^n \right) / \\
& \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \right. \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \right. \\
& \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 \right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2) \right)^2 \Big) + \\
& \left(a^3 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan[c+dx]^2, \frac{(-a^2 + b^2) \tan[c+dx]^2}{a^2} \right] \right. \\
& \quad \left. \tan[c+dx]^6 \left(2 a^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 2 b^2 \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right. \\
& \quad \left. \left(\frac{\tan[c+dx]}{\sqrt{1+\tan^2[c+dx]}} \right)^{-1+n} \right) / \\
& \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan[c+dx]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
& \quad \left. \left. \left. 2, \frac{9+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + a^2 (-1+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1+n}{2}, 1, \frac{9+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \tan [c+d x]^2 \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right)^2 \right) - \\
 & \left(a^2 b (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \right. \\
 & \quad \tan [c+d x]^6 \left(2 a^2 \operatorname{Sec} [c+d x]^2 \tan [c+d x] - 2 b^2 \operatorname{Sec} [c+d x]^2 \tan [c+d x] \right) \\
 & \quad \left. \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^n \right) / \\
 & \left((6+n) \left(-a^2 (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \right. \\
 & \quad \left(2 \left(a^2 - b^2 \right) \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{n}{2}, 2, 5 + \frac{n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5 + \frac{n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
 & \quad \left. \tan [c+d x]^2 \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right)^2 \right) - \\
 & \left(2 a^3 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec} [c+d x]^2 \tan [c+d x] \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^{-1+n} \right) / \\
 & \left((1+n) \left(-a^2 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \left. + \left(2 \left(a^2 - b^2 \right) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 2, \frac{5+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1+n}{2}, 1, \frac{5+n}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \tan [c+d x]^2 \right) \\
 & \quad \left(-b^2 \tan [c+d x]^2 + a^2 \left(1 + \tan [c+d x]^2 \right) \right) \left. - \left(a^3 (3+n) \tan [c+d x]^2 \right. \right. \\
 & \quad \left. \left(-\frac{1}{3+n} (-1+n) (1+n) \operatorname{AppellF1} \left[1 + \frac{1+n}{2}, 1 + \frac{1}{2} (-1+n), 1, 1 + \frac{3+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan [c+d x]^2, \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \operatorname{Sec} [c+d x]^2 \tan [c+d x] + \frac{1}{a^2 (3+n)} \right. \\
 & \quad \left. 2 \left(-a^2 + b^2 \right) (1+n) \operatorname{AppellF1} \left[1 + \frac{1+n}{2}, \frac{1}{2} (-1+n), 2, 1 + \frac{3+n}{2}, -\tan [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{\left(-a^2 + b^2 \right) \tan [c+d x]^2}{a^2} \right] \operatorname{Sec} [c+d x]^2 \tan [c+d x] \right) \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^{-1+n} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((1+n) \left(-a^2 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{5+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + a^2 (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1+n}{2}, 1, \frac{5+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right. \\
 & \quad \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1 + \tan [c+dx]^2) \right) \Big) + \\
 & \left(2 a^2 b (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+dx]^2, \frac{(-a^2 + b^2) \tan [c+dx]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec} [c+dx]^2 \tan [c+dx] \left(\frac{\tan [c+dx]}{\sqrt{1 + \tan [c+dx]^2}} \right)^n \right) / \\
 & \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
 & \quad \left. a^2 n \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \\
 & \quad \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1 + \tan [c+dx]^2) \right) \Big) + \\
 & \left(a^2 b (4+n) \tan [c+dx]^2 \left(-\frac{1}{4+n} n (2+n) \operatorname{AppellF1} \left[1 + \frac{2+n}{2}, 1 + \frac{n}{2}, 1, 1 + \frac{4+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan [c+dx]^2, \frac{(-a^2 + b^2) \tan [c+dx]^2}{a^2} \right] \operatorname{Sec} [c+dx]^2 \tan [c+dx] + \frac{1}{a^2 (4+n)} \right. \\
 & \quad \left. 2 (-a^2 + b^2) (2+n) \operatorname{AppellF1} \left[1 + \frac{2+n}{2}, \frac{n}{2}, 2, 1 + \frac{4+n}{2}, -\tan [c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2 + b^2) \tan [c+dx]^2}{a^2} \right] \operatorname{Sec} [c+dx]^2 \tan [c+dx] \right) \left(\frac{\tan [c+dx]}{\sqrt{1 + \tan [c+dx]^2}} \right)^n \Big) / \\
 & \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
 & \quad \left. a^2 n \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \\
 & \quad \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1 + \tan [c+dx]^2) \right) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(8 a^3 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\operatorname{Tan}[c+d x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]^3 \left(\frac{\operatorname{Tan}[c+d x]}{\sqrt{1+\operatorname{Tan}[c+d x]^2}} \right)^{-1+n} \right) / \\
 & \left((3+n) \left(-a^2 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 2, \frac{7+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1+n}{2}, 1, \frac{7+n}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right) \operatorname{Tan}[c+d x]^2 \right) \\
 & \quad \left. \left(-b^2 \operatorname{Tan}[c+d x]^2 + a^2 (1 + \operatorname{Tan}[c+d x]^2) \right) \right) - \left(2 a^3 (5+n) \operatorname{Tan}[c+d x]^4 \right. \\
 & \quad \left(-\frac{1}{5+n} (-1+n) (3+n) \operatorname{AppellF1} \left[1 + \frac{3+n}{2}, 1 + \frac{1}{2} (-1+n), 1, 1 + \frac{5+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+d x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2} \right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] + \frac{1}{a^2 (5+n)} \right. \\
 & \quad \left. 2 (-a^2+b^2) (3+n) \operatorname{AppellF1} \left[1 + \frac{3+n}{2}, \frac{1}{2} (-1+n), 2, 1 + \frac{5+n}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2} \right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] \right) \left(\frac{\operatorname{Tan}[c+d x]}{\sqrt{1+\operatorname{Tan}[c+d x]^2}} \right)^{-1+n} \right) / \\
 & \left((3+n) \left(-a^2 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. 2, \frac{7+n}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + a^2 (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1+n}{2}, 1, \frac{7+n}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Tan}[c+d x]^2 \right) \left(-b^2 \operatorname{Tan}[c+d x]^2 + a^2 (1 + \operatorname{Tan}[c+d x]^2) \right) \right) + \\
 & \left(8 a^2 b (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\operatorname{Tan}[c+d x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]^3 \left(\frac{\operatorname{Tan}[c+d x]}{\sqrt{1+\operatorname{Tan}[c+d x]^2}} \right)^n \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right. \\
 & \quad \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1+\tan [c+dx]^2) \right) \Big) + \\
 & \left(2 a^2 b (6+n) \tan [c+dx]^4 \left(-\frac{1}{6+n} n (4+n) \operatorname{AppellF1} \left[1+\frac{4+n}{2}, 1+\frac{n}{2}, 1, 1+\frac{6+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan [c+dx]^2, \frac{(-a^2+b^2) \tan [c+dx]^2}{a^2} \right] \operatorname{Sec} [c+dx]^2 \tan [c+dx] + \frac{1}{a^2 (6+n)} \right. \\
 & \quad \left. 2 (-a^2+b^2) (4+n) \operatorname{AppellF1} \left[1+\frac{4+n}{2}, \frac{n}{2}, 2, 1+\frac{6+n}{2}, -\tan [c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2+b^2) \tan [c+dx]^2}{a^2} \right] \operatorname{Sec} [c+dx]^2 \tan [c+dx] \right) \left(\frac{\tan [c+dx]}{\sqrt{1+\tan [c+dx]^2}} \right)^n \Big) / \\
 & \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right. \\
 & \quad \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1+\tan [c+dx]^2) \right) \Big) - \\
 & \left(6 a^3 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan [c+dx]^2, \frac{(-a^2+b^2) \tan [c+dx]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec} [c+dx]^2 \tan [c+dx]^5 \left(\frac{\tan [c+dx]}{\sqrt{1+\tan [c+dx]^2}} \right)^{-1+n} \right) / \\
 & \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan [c+dx]^2, \right. \right. \right. \\
 & \quad \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right) + \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), 2, \frac{9+n}{2}, \right. \right. \\
 & \quad \left. \left. -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{7+n}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1+n}{2}, 1, \frac{9+n}{2}, -\tan [c+dx]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \tan [c+dx]^2 \right) \\
 & \left(-b^2 \tan [c+dx]^2 + a^2 (1+\tan [c+dx]^2) \right) \Big) - \left(a^3 (7+n) \tan [c+dx]^6 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{1}{7+n} (-1+n) (5+n) \operatorname{AppellF1}\left[1 + \frac{5+n}{2}, 1 + \frac{1}{2} (-1+n), 1, 1 + \frac{7+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \frac{1}{a^2 (7+n)} \right. \\
 & \quad \left. 2 (-a^2+b^2) (5+n) \operatorname{AppellF1}\left[1 + \frac{5+n}{2}, \frac{1}{2} (-1+n), 2, 1 + \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \left(\frac{\operatorname{Tan}[c+dx]}{\sqrt{1+\operatorname{Tan}[c+dx]^2}} \right)^{-1+n} \Big/ \\
 & \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1}\left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right) + \left(2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{7+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. 2, \frac{9+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right) + a^2 (-1+n) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{7+n}{2}, \frac{1+n}{2}, 1, \frac{9+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Tan}[c+dx]^2 \right) (-b^2 \operatorname{Tan}[c+dx]^2 + a^2 (1 + \operatorname{Tan}[c+dx]^2)) \right) + \\
 & \left(6 a^2 b (8+n) \operatorname{AppellF1}\left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]^5 \left(\frac{\operatorname{Tan}[c+dx]}{\sqrt{1+\operatorname{Tan}[c+dx]^2}} \right)^n \right) \Big/ \\
 & \left((6+n) \left(-a^2 (8+n) \operatorname{AppellF1}\left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \right. \right. \\
 & \quad \left. \left(2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{n}{2}, 2, 5 + \frac{n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5 + \frac{n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[c+dx]^2 \right) (-b^2 \operatorname{Tan}[c+dx]^2 + a^2 (1 + \operatorname{Tan}[c+dx]^2)) \right) + \\
 & \left(a^2 b (8+n) \operatorname{Tan}[c+dx]^6 \left(-\frac{1}{8+n} n (6+n) \operatorname{AppellF1}\left[1 + \frac{6+n}{2}, 1 + \frac{n}{2}, 1, 1 + \frac{8+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \frac{1}{a^2 (8+n)} \right. \\
 & \quad \left. 2 (-a^2+b^2) (6+n) \operatorname{AppellF1}\left[1 + \frac{6+n}{2}, \frac{n}{2}, 2, 1 + \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \left(\frac{\operatorname{Tan}[c+dx]}{\sqrt{1+\operatorname{Tan}[c+dx]^2}} \right)^n \Big/
 \end{aligned}$$

$$\begin{aligned}
& \left((6+n) \left(-a^2 (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{n}{2}, 2, 5 + \frac{n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
& \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5 + \frac{n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right. \\
& \quad \left. \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1 + \tan [c+dx]^2) \right) \right) - \\
& \left(a^3 (-1+n) (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+dx]^2, \right. \right. \\
& \quad \left. \left. \frac{(-a^2 + b^2) \tan [c+dx]^2}{a^2} \right] \tan [c+dx]^2 \left(\frac{\tan [c+dx]}{\sqrt{1 + \tan [c+dx]^2}} \right)^{-2+n} \right. \\
& \quad \left. \left. \left(-\frac{\sec [c+dx]^2 \tan [c+dx]^2}{(1 + \tan [c+dx]^2)^{3/2}} + \frac{\sec [c+dx]^2}{\sqrt{1 + \tan [c+dx]^2}} \right) \right) \right) / \\
& \left((1+n) \left(-a^2 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan [c+dx]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right) + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
& \quad \left. \left. \left. 2, \frac{5+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + a^2 (-1+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1+n}{2}, 1, \frac{5+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right. \\
& \quad \left. \left. \tan [c+dx]^2 \right) \left(-b^2 \tan [c+dx]^2 + a^2 (1 + \tan [c+dx]^2) \right) \right) + \\
& \left(a^2 b n (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+dx]^2, \frac{(-a^2 + b^2) \tan [c+dx]^2}{a^2} \right] \right. \\
& \quad \left. \tan [c+dx]^2 \left(\frac{\tan [c+dx]}{\sqrt{1 + \tan [c+dx]^2}} \right)^{-1+n} \right. \\
& \quad \left. \left. \left(-\frac{\sec [c+dx]^2 \tan [c+dx]^2}{(1 + \tan [c+dx]^2)^{3/2}} + \frac{\sec [c+dx]^2}{\sqrt{1 + \tan [c+dx]^2}} \right) \right) \right) / \\
& \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1} \left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] + \right. \\
& \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\tan [c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+dx]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2) \right) \right) - \\
 & \left(2 a^3 (-1+n) (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\tan[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2} \right] \tan[c+dx]^4 \left(\frac{\tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}} \right)^{-2+n} \right. \\
 & \quad \left. \left(-\frac{\sec[c+dx]^2 \tan[c+dx]^2}{(1+\tan[c+dx]^2)^{3/2}} + \frac{\sec[c+dx]^2}{\sqrt{1+\tan[c+dx]^2}} \right) \right) / \\
 & \left((3+n) \left(-a^2 (5+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\tan[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{7+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + a^2 (-1+n) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1+n}{2}, 1, \frac{7+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] \right. \right. \\
 & \quad \left. \left. \tan[c+dx]^2 \right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2) \right) \right) + \\
 & \left(2 a^2 b n (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2} \right] \right. \\
 & \quad \left. \tan[c+dx]^4 \left(\frac{\tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}} \right)^{-1+n} \right. \\
 & \quad \left. \left(-\frac{\sec[c+dx]^2 \tan[c+dx]^2}{(1+\tan[c+dx]^2)^{3/2}} + \frac{\sec[c+dx]^2}{\sqrt{1+\tan[c+dx]^2}} \right) \right) / \\
 & \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2-b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] + \right. \\
 & \quad \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c+dx]^2 \right] \right) \\
 & \quad \left. \tan[c+dx]^2 \right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2) \right) \right) - \\
 & \left(a^3 (-1+n) (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan[c+dx]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \tan[c + dx]^6 \left(\frac{\tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right)^{-2+n} \\
& \left(-\frac{\sec[c + dx]^2 \tan[c + dx]^2}{(1 + \tan[c + dx]^2)^{3/2}} + \frac{\sec[c + dx]^2}{\sqrt{1 + \tan[c + dx]^2}} \right) \Big/ \\
& \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), \right. \right. \right. \\
& \quad \left. \left. 2, \frac{9+n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + a^2 (-1+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1+n}{2}, 1, \frac{9+n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \right. \\
& \quad \left. \tan[c + dx]^2 \right) \left(-b^2 \tan[c + dx]^2 + a^2 (1 + \tan[c + dx]^2) \right) \Big) + \\
& \left(a^2 b n (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \right. \\
& \quad \tan[c + dx]^6 \left(\frac{\tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right)^{-1+n} \\
& \quad \left(-\frac{\sec[c + dx]^2 \tan[c + dx]^2}{(1 + \tan[c + dx]^2)^{3/2}} + \frac{\sec[c + dx]^2}{\sqrt{1 + \tan[c + dx]^2}} \right) \Big/ \\
& \quad \left((6+n) \left(-a^2 (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{n}{2}, 2, 5 + \frac{n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \\
& \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5 + \frac{n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \right. \\
& \quad \left. \tan[c + dx]^2 \right) \left(-b^2 \tan[c + dx]^2 + a^2 (1 + \tan[c + dx]^2) \right) \Big) + \\
& \quad \left(a^3 (3+n) \operatorname{AppellF1} \left[\frac{1+n}{2}, \frac{1}{2} (-1+n), 1, \frac{3+n}{2}, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \right. \\
& \quad \tan[c + dx]^2 \left(\frac{\tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right)^{-1+n} \\
& \quad \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 2, \frac{5+n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \right. \right. \right. \\
& \quad \left. \left. \tan[c + dx]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{3+n}{2}, \frac{1+n}{2}, 1, \frac{5+n}{2}, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \left) \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \\
& a^2 (3 + n) \left(-\frac{1}{3 + n} (-1 + n) (1 + n) \operatorname{AppellF1}\left[1 + \frac{1 + n}{2}, 1 + \frac{1}{2} (-1 + n), 1, \right. \right. \\
& \left. \left. 1 + \frac{3 + n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] + \right. \\
& \left. \frac{1}{3 + n} 2 \left(-1 + \frac{b^2}{a^2} \right) (1 + n) \operatorname{AppellF1}\left[1 + \frac{1 + n}{2}, \frac{1}{2} (-1 + n), 2, 1 + \frac{3 + n}{2}, \right. \right. \\
& \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) + \\
& \tan[c + dx]^2 \left(2 (a^2 - b^2) \left(-\frac{1}{5 + n} (-1 + n) (3 + n) \operatorname{AppellF1}\left[1 + \frac{3 + n}{2}, 1 + \frac{1}{2} (-1 + n), 2, \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{5 + n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] + \right. \right. \\
& \left. \left. \frac{1}{5 + n} 4 \left(-1 + \frac{b^2}{a^2} \right) (3 + n) \operatorname{AppellF1}\left[1 + \frac{3 + n}{2}, \frac{1}{2} (-1 + n), 3, 1 + \frac{5 + n}{2}, \right. \right. \right. \\
& \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) + \right. \\
& \left. a^2 (-1 + n) \left(\frac{1}{5 + n} 2 \left(-1 + \frac{b^2}{a^2} \right) (3 + n) \operatorname{AppellF1}\left[1 + \frac{3 + n}{2}, \frac{1 + n}{2}, 2, 1 + \frac{5 + n}{2}, \right. \right. \right. \\
& \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \right. \right. \\
& \left. \left. \frac{1}{5 + n} (1 + n) (3 + n) \operatorname{AppellF1}\left[1 + \frac{3 + n}{2}, 1 + \frac{1 + n}{2}, 1, 1 + \frac{5 + n}{2}, \right. \right. \right. \\
& \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) \right) \right) \bigg) \bigg) \bigg) \bigg) \bigg) / \\
& \left((1 + n) \left(-a^2 (3 + n) \operatorname{AppellF1}\left[\frac{1 + n}{2}, \frac{1}{2} (-1 + n), 1, \frac{3 + n}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3 + n}{2}, \frac{1}{2} (-1 + n), 2, \frac{5 + n}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + a^2 (-1 + n) \operatorname{AppellF1}\left[\frac{3 + n}{2}, \right. \right. \right. \\
& \left. \left. \left. \frac{1 + n}{2}, 1, \frac{5 + n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \tan[c + dx]^2 \right)^2 \\
& \left(-b^2 \tan[c + dx]^2 + a^2 (1 + \tan[c + dx]^2) \right) \bigg) - \left(a^2 b (4 + n) \operatorname{AppellF1}\left[\frac{2 + n}{2}, \frac{n}{2}, \right. \right. \\
& \left. \left. 1, \frac{4 + n}{2}, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \tan[c + dx]^2 \left(\frac{\tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right)^n \right. \\
& \left. \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{4 + n}{2}, \frac{n}{2}, 2, \frac{6 + n}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & a^2 n \operatorname{AppellF1}\left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \\
 & \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - a^2 (4+n) \left(-\frac{1}{4+n} n (2+n) \operatorname{AppellF1}\left[1+\frac{2+n}{2}, 1+\frac{n}{2}, \right.\right. \\
 & \quad \left.1, 1+\frac{4+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \\
 & \quad \frac{1}{4+n} 2 \left(-1+\frac{b^2}{a^2}\right) (2+n) \operatorname{AppellF1}\left[1+\frac{2+n}{2}, \frac{n}{2}, 2, 1+\frac{4+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \\
 & \quad \left.\left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]\left.\right) + \operatorname{Tan}[c+dx]^2 \\
 & \left(2 (a^2-b^2) \left(-\frac{1}{6+n} n (4+n) \operatorname{AppellF1}\left[1+\frac{4+n}{2}, 1+\frac{n}{2}, 2, 1+\frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \right.\right.\right. \\
 & \quad \left.\left.\left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \frac{1}{6+n} 4 \left(-1+\frac{b^2}{a^2}\right) (4+n) \right. \\
 & \quad \left.\operatorname{AppellF1}\left[1+\frac{4+n}{2}, \frac{n}{2}, 3, 1+\frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \right. \\
 & \quad \left.\operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]\right) + a^2 n \left(\frac{1}{6+n} 2 \left(-1+\frac{b^2}{a^2}\right) (4+n) \operatorname{AppellF1}\left[1+\frac{4+n}{2}, \right.\right. \\
 & \quad \left.\frac{2+n}{2}, 2, 1+\frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \\
 & \quad \left.\operatorname{Tan}[c+dx] - \frac{1}{6+n} (2+n) (4+n) \operatorname{AppellF1}\left[1+\frac{4+n}{2}, 1+\frac{2+n}{2}, 1, 1+\frac{6+n}{2}, \right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]\right)\left.\right)\left.\right) / \\
 & \left((2+n) \left(-a^2 (4+n) \operatorname{AppellF1}\left[\frac{2+n}{2}, \frac{n}{2}, 1, \frac{4+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] + \right.\right. \\
 & \quad \left.2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{4+n}{2}, \frac{n}{2}, 2, \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] + \right. \\
 & \quad \left. a^2 n \operatorname{AppellF1}\left[\frac{4+n}{2}, \frac{2+n}{2}, 1, \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+dx]^2\right] \right) \\
 & \quad \left. \operatorname{Tan}[c+dx]^2 \right)^2 \left(-b^2 \operatorname{Tan}[c+dx]^2 + a^2 (1+\operatorname{Tan}[c+dx]^2)\right) \left. \right) + \\
 & \left[2 a^3 (5+n) \operatorname{AppellF1}\left[\frac{3+n}{2}, \frac{1}{2} (-1+n), 1, \frac{5+n}{2}, -\operatorname{Tan}[c+dx]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+dx]^2}{a^2}\right] \right] \\
 & \operatorname{Tan}[c+dx]^4 \left(\frac{\operatorname{Tan}[c+dx]}{\sqrt{1+\operatorname{Tan}[c+dx]^2}}\right)^{-1+n} \\
 & \left(2 \left(2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 2, \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \right.\right.\right. \\
 & \quad \left.\left.\operatorname{Tan}[c+dx]^2\right] + a^2 (-1+n) \operatorname{AppellF1}\left[\frac{5+n}{2}, \frac{1+n}{2}, 1, \frac{7+n}{2}, \right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\left.\right\} \sec [c+d x]^2 \tan [c+d x]- \\
 & a^2(5+n)\left(-\frac{1}{5+n}(-1+n)(3+n) \operatorname{AppellF1}\left[1+\frac{3+n}{2}, 1+\frac{1}{2}(-1+n), 1,\right.\right. \\
 & \quad \left.1+\frac{5+n}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]+ \\
 & \quad \left.\frac{1}{5+n} 2\left(-1+\frac{b^2}{a^2}\right)(3+n) \operatorname{AppellF1}\left[1+\frac{3+n}{2}, \frac{1}{2}(-1+n), 2, 1+\frac{5+n}{2},\right.\right. \\
 & \quad \left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]\left.\right\}+ \\
 & \tan [c+d x]^2\left(2\left(a^2-b^2\right)\left(-\frac{1}{7+n}(-1+n)(5+n) \operatorname{AppellF1}\left[1+\frac{5+n}{2}, 1+\frac{1}{2}(-1+n), 2,\right.\right.\right. \\
 & \quad \left.1+\frac{7+n}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]+ \\
 & \quad \left.\frac{1}{7+n} 4\left(-1+\frac{b^2}{a^2}\right)(5+n) \operatorname{AppellF1}\left[1+\frac{5+n}{2}, \frac{1}{2}(-1+n), 3, 1+\frac{7+n}{2},\right.\right. \\
 & \quad \left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]\left.\right\}+ \\
 & a^2(-1+n)\left(\frac{1}{7+n} 2\left(-1+\frac{b^2}{a^2}\right)(5+n) \operatorname{AppellF1}\left[1+\frac{5+n}{2}, \frac{1+n}{2}, 2, 1+\frac{7+n}{2},\right.\right. \\
 & \quad \left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]- \\
 & \quad \left.\frac{1}{7+n}(1+n)(5+n) \operatorname{AppellF1}\left[1+\frac{5+n}{2}, 1+\frac{1+n}{2}, 1, 1+\frac{7+n}{2},\right.\right. \\
 & \quad \left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]\left.\right\}\left.\right\} / \\
 & \left((3+n)\left(-a^2(5+n) \operatorname{AppellF1}\left[\frac{3+n}{2}, \frac{1}{2}(-1+n), 1, \frac{5+n}{2},-\tan [c+d x]^2,\right.\right.\right. \\
 & \quad \left.\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5+n}{2}, \frac{1}{2}(-1+n), 2, \frac{7+n}{2},\right.\right. \\
 & \quad \left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right)+a^2(-1+n) \operatorname{AppellF1}\left[\frac{5+n}{2},\right. \\
 & \quad \left.\frac{1+n}{2}, 1, \frac{7+n}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\left.\right) \tan [c+d x]^2)^2 \\
 & \left(-b^2 \tan [c+d x]^2+a^2\left(1+\tan [c+d x]^2\right)\right)\left.-\left(2 a^2 b(6+n) \operatorname{AppellF1}\left[\frac{4+n}{2},\right.\right.\right. \\
 & \quad \left.\frac{n}{2}, 1, \frac{6+n}{2},-\tan [c+d x]^2,\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \\
 & \tan [c+d x]^4\left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}}\right)^n
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right) \right. \\
 & \quad \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - a^2 (6+n) \left(-\frac{1}{6+n} n (4+n) \operatorname{AppellF1} \left[1 + \frac{4+n}{2}, 1 + \frac{n}{2}, \right. \right. \\
 & \quad \left. \left. 1, 1 + \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \right. \\
 & \quad \left. \frac{1}{6+n} 2 \left(-1 + \frac{b^2}{a^2} \right) (4+n) \operatorname{AppellF1} \left[1 + \frac{4+n}{2}, \frac{n}{2}, 2, 1 + \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) + \operatorname{Tan}[c+dx]^2 \\
 & \left(2 (a^2 - b^2) \left(-\frac{1}{8+n} n (6+n) \operatorname{AppellF1} \left[1 + \frac{6+n}{2}, 1 + \frac{n}{2}, 2, 1 + \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \frac{1}{8+n} 4 \left(-1 + \frac{b^2}{a^2} \right) (6+n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[1 + \frac{6+n}{2}, \frac{n}{2}, 3, 1 + \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) + a^2 n \left(\frac{1}{8+n} 2 \left(-1 + \frac{b^2}{a^2} \right) (6+n) \operatorname{AppellF1} \left[1 + \frac{6+n}{2}, \right. \right. \\
 & \quad \left. \left. \frac{2+n}{2}, 2, 1 + \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \right. \\
 & \quad \left. \operatorname{Tan}[c+dx] - \frac{1}{8+n} (2+n) (6+n) \operatorname{AppellF1} \left[1 + \frac{6+n}{2}, 1 + \frac{2+n}{2}, 1, 1 + \frac{8+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \right) \Bigg) / \\
 & \left((4+n) \left(-a^2 (6+n) \operatorname{AppellF1} \left[\frac{4+n}{2}, \frac{n}{2}, 1, \frac{6+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{n}{2}, 2, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1} \left[\frac{6+n}{2}, \frac{2+n}{2}, 1, \frac{8+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Tan}[c+dx]^2 \right)^2 \left(-b^2 \operatorname{Tan}[c+dx]^2 + a^2 (1 + \operatorname{Tan}[c+dx]^2) \right) \Bigg) + \\
 & \left(a^3 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[c+dx]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Tan}[c+dx]^6 \left(\frac{\operatorname{Tan}[c+dx]}{\sqrt{1 + \operatorname{Tan}[c+dx]^2}} \right)^{-1+n} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), 2, \frac{9+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}[c+dx]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1+n}{2}, 1, \frac{9+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \right. \\
 & a^2 (7+n) \left(-\frac{1}{7+n} (-1+n) (5+n) \operatorname{AppellF1} \left[1 + \frac{5+n}{2}, 1 + \frac{1}{2} (-1+n), 1, \right. \right. \\
 & \quad \left. \left. 1 + \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \right. \\
 & \quad \left. \frac{1}{7+n} 2 \left(-1 + \frac{b^2}{a^2} \right) (5+n) \operatorname{AppellF1} \left[1 + \frac{5+n}{2}, \frac{1}{2} (-1+n), 2, 1 + \frac{7+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) + \\
 & \operatorname{Tan}[c+dx]^2 \left(2 (a^2 - b^2) \left(-\frac{1}{9+n} (-1+n) (7+n) \operatorname{AppellF1} \left[1 + \frac{7+n}{2}, 1 + \frac{1}{2} (-1+n), 2, \right. \right. \right. \\
 & \quad \left. \left. 1 + \frac{9+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] + \right. \\
 & \quad \left. \frac{1}{9+n} 4 \left(-1 + \frac{b^2}{a^2} \right) (7+n) \operatorname{AppellF1} \left[1 + \frac{7+n}{2}, \frac{1}{2} (-1+n), 3, 1 + \frac{9+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) + \\
 & a^2 (-1+n) \left(\frac{1}{9+n} 2 \left(-1 + \frac{b^2}{a^2} \right) (7+n) \operatorname{AppellF1} \left[1 + \frac{7+n}{2}, \frac{1+n}{2}, 2, 1 + \frac{9+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \right. \\
 & \quad \left. \frac{1}{9+n} (1+n) (7+n) \operatorname{AppellF1} \left[1 + \frac{7+n}{2}, 1 + \frac{1+n}{2}, 1, 1 + \frac{9+n}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \right) \Bigg) / \\
 & \left((5+n) \left(-a^2 (7+n) \operatorname{AppellF1} \left[\frac{5+n}{2}, \frac{1}{2} (-1+n), 1, \frac{7+n}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7+n}{2}, \frac{1}{2} (-1+n), 2, \frac{9+n}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] + a^2 (-1+n) \operatorname{AppellF1} \left[\frac{7+n}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1+n}{2}, 1, \frac{9+n}{2}, -\operatorname{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+dx]^2 \right] \right) \operatorname{Tan}[c+dx]^2 \right)^2 \\
 & \left. \left(-b^2 \operatorname{Tan}[c+dx]^2 + a^2 (1 + \operatorname{Tan}[c+dx]^2) \right) \right) - \left(a^2 b (8+n) \operatorname{AppellF1} \left[\frac{6+n}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2} \right] \\
 & \tan [c+d x]^6 \left(\frac{\tan [c+d x]}{\sqrt{1+\tan [c+d x]^2}} \right)^n \\
 & \left(2 \left(2 \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{n}{2}, 2, 5+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
 & \quad \left. \left. a^2 n \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \tan [c+d x] - a^2(8+n) \left(-\frac{1}{8+n} n(6+n) \operatorname{AppellF1}\left[1+\frac{6+n}{2}, 1+\frac{n}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1, 1+\frac{8+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] + \right. \right. \\
 & \quad \left. \left. \frac{1}{8+n} 2 \left(-1+\frac{b^2}{a^2}\right) (6+n) \operatorname{AppellF1}\left[1+\frac{6+n}{2}, \frac{n}{2}, 2, 1+\frac{8+n}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + \tan [c+d x]^2 \right. \\
 & \quad \left. \left(2 \left(a^2-b^2\right) \left(-\frac{1}{2\left(5+\frac{n}{2}\right)} n(8+n) \operatorname{AppellF1}\left[1+\frac{8+n}{2}, 1+\frac{n}{2}, 2, 6+\frac{n}{2}, -\tan [c+d x]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] + \frac{1}{5+\frac{n}{2}} 2 \left(-1+\frac{b^2}{a^2}\right) (8+n) \right. \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1}\left[1+\frac{8+n}{2}, \frac{n}{2}, 3, 6+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + a^2 n \left(\frac{1}{5+\frac{n}{2}} \left(-1+\frac{b^2}{a^2}\right) (8+n) \operatorname{AppellF1}\left[1+\frac{8+n}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{2+n}{2}, 2, 6+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \right. \right. \\
 & \quad \quad \left. \left. \tan [c+d x] - \frac{1}{2\left(5+\frac{n}{2}\right)} (2+n) (8+n) \operatorname{AppellF1}\left[1+\frac{8+n}{2}, 1+\frac{2+n}{2}, 1, 6+\frac{n}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) \right) \right) \right) \right) / \\
 & \left((6+n) \left(-a^2(8+n) \operatorname{AppellF1}\left[\frac{6+n}{2}, \frac{n}{2}, 1, \frac{8+n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
 & \quad \left. \left(2 \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{n}{2}, 2, 5+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. a^2 n \operatorname{AppellF1}\left[\frac{8+n}{2}, \frac{2+n}{2}, 1, 5+\frac{n}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \right) \right)
 \end{aligned}$$

Optimal (type 4, 502 leaves, ? steps):

$$\begin{aligned} & - \frac{3 a b (-2 a^2 + b^2) \operatorname{Cos}[e + f x] \sqrt{a + b \operatorname{Sin}[e + f x]}}{5 f \sqrt{d \operatorname{Sin}[e + f x]}} + \\ & \frac{\operatorname{Sec}[e + f x]^5 \sqrt{d \operatorname{Sin}[e + f x]} (a + b \operatorname{Sin}[e + f x])^{9/2}}{5 d f} - \frac{1}{20 d f} \\ & 3 a \operatorname{Sec}[e + f x]^3 \sqrt{d \operatorname{Sin}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]} (-a (7 a^2 + b^2) + \\ & 2 b (-7 a^2 + b^2) \operatorname{Sin}[e + f x] + 5 a (a^2 - b^2) \operatorname{Sin}[e + f x]^2 + (8 a^2 b - 4 b^3) \operatorname{Sin}[e + f x]^3) - \\ & \frac{1}{20 \sqrt{d} f} 3 a (a + b)^{3/2} (5 a^2 + 3 a b - 4 b^2) \sqrt{-\frac{a (-1 + \operatorname{Csc}[e + f x])}{a + b}} \sqrt{\frac{a (1 + \operatorname{Csc}[e + f x])}{a - b}} \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a + b \operatorname{Sin}[e + f x]}}{\sqrt{a + b} \sqrt{d \operatorname{Sin}[e + f x]}}\right], -\frac{a + b}{a - b}\right] \operatorname{Tan}[e + f x] - \\ & \left(3 b (2 a^4 - 3 a^2 b^2 + b^4) \sqrt{-\frac{a (-1 + \operatorname{Csc}[e + f x])}{a + b}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{-\frac{b + a \operatorname{Csc}[e + f x]}{a - b}}\right], \right. \right. \\ & \left. \left. 1 - \frac{2 a}{a + b}\right] \sqrt{d \operatorname{Sin}[e + f x]} \sqrt{-\frac{a \operatorname{Csc}[e + f x]^2 (1 + \operatorname{Sin}[e + f x]) (a + b \operatorname{Sin}[e + f x])}{(a - b)^2}} \right. \\ & \left. \left. \operatorname{Tan}[e + f x] \right) / (5 d f \sqrt{a + b \operatorname{Sin}[e + f x]}) \end{aligned}$$

Result (type 4, 1600 leaves):

$$\begin{aligned} & \left(\operatorname{Sin}[e + f x] \sqrt{a + b \operatorname{Sin}[e + f x]} \right. \\ & \left(\frac{1}{20} \operatorname{Sec}[e + f x] (15 a^4 - 15 a^2 b^2 + 4 b^4 + 24 a^3 b \operatorname{Sin}[e + f x] - 12 a b^3 \operatorname{Sin}[e + f x]) + \right. \\ & \frac{1}{10} \operatorname{Sec}[e + f x]^3 (3 a^4 - 3 a^2 b^2 - 4 b^4 + 9 a^3 b \operatorname{Sin}[e + f x] - 5 a b^3 \operatorname{Sin}[e + f x]) + \\ & \left. \left. \frac{1}{5} \operatorname{Sec}[e + f x]^5 (a^4 + 6 a^2 b^2 + b^4 + 4 a^3 b \operatorname{Sin}[e + f x] + 4 a b^3 \operatorname{Sin}[e + f x]) \right) \right) / \\ & \left(f \sqrt{d \operatorname{Sin}[e + f x]} \right) + \frac{1}{40 f \sqrt{d \operatorname{Sin}[e + f x]}} 3 a \sqrt{\operatorname{Sin}[e + f x]} \\ & \left(\left(4 a (5 a^4 - 9 a^2 b^2 + 4 b^4) \sqrt{\frac{(a + b) \operatorname{Cot}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2}{-a + b}} \right. \right. \\ & \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x\right)\right]^2 (a + b \operatorname{Sin}[e + f x])}}{a}}\right], -\frac{2 a}{-a + b}\right] \operatorname{Sec}[e + f x] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[ex+fx]}{a}} \right. \\
 & \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[ex+fx])}{a}} \right) / \\
 & \left((a+b) \sqrt{\sin[ex+fx]} \sqrt{a+b \sin[ex+fx]} \right) + \\
 & 4a(-8a^3b + 4ab^3) \left(\left(\sqrt{\frac{(a+b) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-a+b}} \right) \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[ex+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \operatorname{Sec}[ex+fx] \right. \\
 & \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[ex+fx]}{a}} \right. \\
 & \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[ex+fx])}{a}} \right) / \\
 & \left((a+b) \sqrt{\sin[ex+fx]} \sqrt{a+b \sin[ex+fx]} \right) - \left(\sqrt{\frac{(a+b) \operatorname{Cot}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-a+b}} \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{a}{b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[ex+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \operatorname{Sec}[ex+fx] \right. \\
 & \left. \sin\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[ex+fx]}{a}} \right. \\
 & \left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2}\left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[ex+fx])}{a}} \right) /
 \end{aligned}$$

$$\left(b \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) + 2 (8 a^2 b^2 - 4 b^4)$$

$$\left(\frac{\cos[e+fx] \sqrt{a+b \sin[e+fx]}}{b \sqrt{\sin[e+fx]}} + \left(i \cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right] \operatorname{Csc}[e+fx] \right. \right.$$

$$\left. \left. \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sin\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]}{\sqrt{\sin[e+fx]}}\right], -\frac{2a}{-a-b}\right] \sqrt{a+b \sin[e+fx]} \right) \right) /$$

$$\left(b \sqrt{\cos\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \operatorname{Csc}[e+fx]} \sqrt{\frac{\operatorname{Csc}[e+fx] (a+b \sin[e+fx])}{a+b}} \right) +$$

$$\frac{1}{b} 2 a \left(\left(a \sqrt{\frac{(a+b) \operatorname{Cot}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-a+b}} \operatorname{EllipticF}\left[$$

$$\operatorname{ArcSin}\left[\frac{\sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \operatorname{Sec}[e+fx]$$

$$\sin\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 \sin[e+fx]}{a}}$$

$$\left. \sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}} \right) /$$

$$\left((a+b) \sqrt{\sin[e+fx]} \sqrt{a+b \sin[e+fx]} \right) - a \sqrt{\frac{(a+b) \operatorname{Cot}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2}{-a+b}}$$

$$\operatorname{EllipticPi}\left[-\frac{a}{b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{\operatorname{Csc}\left[\frac{1}{2} \left(-e + \frac{\pi}{2} - fx\right)\right]^2 (a+b \sin[e+fx])}{a}}}{\sqrt{2}}}\right], -\frac{2a}{-a+b}\right] \operatorname{Sec}[$$

$$\left. \begin{aligned} & e + f x \sin \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^4 \sqrt{-\frac{(a+b) \operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 \sin [e + f x]}{a}} \\ & \sqrt{\frac{\operatorname{Csc} \left[\frac{1}{2} \left(-e + \frac{\pi}{2} - f x \right) \right]^2 (a+b \sin [e + f x])}{a}} \right) / \\ & \left(b \sqrt{\sin [e + f x]} \sqrt{a+b \sin [e + f x]} \right) \end{aligned} \right) \left. \right) \left. \right) \left. \right)$$

Problem 1516: Result more than twice size of optimal antiderivative.

$$\int \cos [e + f x]^2 (a + b \sin [e + f x])^2 (c + d \sin [e + f x])^{4/3} dx$$

Optimal (type 6, 458 leaves, 11 steps):

$$\begin{aligned} & -\frac{1}{2080 d^3 f} 9 (64 a b c d - 26 a^2 d^2 - b^2 (18 c^2 - 13 d^2)) \cos [e + f x] (c + d \sin [e + f x])^{7/3} - \\ & \frac{9 b (3 b c - 2 a d) \cos [e + f x] \sin [e + f x] (c + d \sin [e + f x])^{7/3}}{208 d^2 f} + \\ & \frac{3 \cos [e + f x] (a + b \sin [e + f x])^2 (c + d \sin [e + f x])^{7/3}}{16 d f} - \\ & \left(3 (c + d)^2 (208 a^2 c d^2 - 64 a b d (3 c^2 - 5 d^2) + b^2 c (54 c^2 + d^2)) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1}{2}, -\frac{7}{3}, \frac{3}{2}, \right. \right. \\ & \left. \left. \frac{1}{2} (1 - \sin [e + f x]), \frac{d (1 - \sin [e + f x])}{c + d} \right] \cos [e + f x] (c + d \sin [e + f x])^{1/3} \right) / \\ & \left(1040 \sqrt{2} d^4 f \sqrt{1 + \sin [e + f x]} \left(\frac{c + d \sin [e + f x]}{c + d} \right)^{1/3} \right) - \\ & \left(3 (c - d) (c + d)^2 (192 a b c d - 208 a^2 d^2 - b^2 (54 c^2 + 91 d^2)) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1}{2}, -\frac{4}{3}, \frac{3}{2}, \right. \right. \\ & \left. \left. \frac{1}{2} (1 - \sin [e + f x]), \frac{d (1 - \sin [e + f x])}{c + d} \right] \cos [e + f x] (c + d \sin [e + f x])^{1/3} \right) / \\ & \left(1040 \sqrt{2} d^4 f \sqrt{1 + \sin [e + f x]} \left(\frac{c + d \sin [e + f x]}{c + d} \right)^{1/3} \right) \end{aligned}$$

Result (type 6, 3522 leaves):

$$\frac{1}{455 f} 513 a b c \operatorname{AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \sin [e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \sin [e + f x]}{(-1 - \frac{c}{d}) d} \right]$$

$$\begin{aligned}
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \\
& \frac{1}{7280 d^3 f} 81 b^2 c^4 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} - \\
& \frac{1}{455 d^2 f} 18 a b c^3 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \\
& \frac{1}{35 d f} 54 a^2 c^2 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \\
& \frac{1}{14560 d f} 5211 b^2 c^2 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \\
& \frac{1}{40 f} 9 a^2 d \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \\
& \frac{1}{640 f} 63 b^2 d \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \\
& \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \frac{1}{65 f} \\
& 9 a b c^2 \left(-\frac{1}{d^2} 3 c \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d\sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d\sin[e+fx]}{(-1-\frac{c}{d})d}\right] \right. \\
& \left. \text{Sec}[e+fx] \sqrt{\frac{-d-d\sin[e+fx]}{c-d}} \sqrt{\frac{d-d\sin[e+fx]}{c+d}} (c+d\sin[e+fx])^{1/3} + \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{4 d^2} {}_3\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \sec [e+f x] \\
 & \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \Bigg) + \frac{1}{7280 d^3 f} \\
 81 b^2 c^5 & \left(-\frac{1}{d^2} {}_3\text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \right. \\
 & \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \left. \frac{1}{4 d^2} {}_3\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \sec [e+f x] \right. \\
 & \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) - \frac{1}{455 d^2 f} \\
 18 a b c^4 & \left(-\frac{1}{d^2} {}_3\text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \right. \\
 & \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \left. \frac{1}{4 d^2} {}_3\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \sec [e+f x] \right. \\
 & \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) + \frac{1}{70 d f} \\
 3 a^2 c^3 & \left(-\frac{1}{d^2} {}_3\text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \right. \\
 & \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \left. \frac{1}{4 d^2} {}_3\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \sec [e+f x] \right. \\
 & \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) - \frac{1}{1040 d f}
 \end{aligned}$$

$$21 b^2 c^3 \left(-\frac{1}{d^2} {}_3F_3 \text{ AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \right. \\ \left. \sec[e+fx] \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{1/3} + \right. \\ \left. \frac{1}{4 d^2} {}_3F_3 \text{ AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \sec[e+fx] \right. \\ \left. \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{4/3} \right) + \frac{1}{280 f}$$

$$153 a^2 c d \left(-\frac{1}{d^2} {}_3F_3 \text{ AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \right. \\ \left. \sec[e+fx] \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{1/3} + \right. \\ \left. \frac{1}{4 d^2} {}_3F_3 \text{ AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \sec[e+fx] \right. \\ \left. \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{4/3} \right) + \frac{1}{58240 f}$$

$$9603 b^2 c d \left(-\frac{1}{d^2} {}_3F_3 \text{ AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \right. \\ \left. \sec[e+fx] \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{1/3} + \right. \\ \left. \frac{1}{4 d^2} {}_3F_3 \text{ AppellF1} \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \sec[e+fx] \right. \\ \left. \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{4/3} \right) + \frac{1}{91 f}$$

$$24 a b d^2 \left(-\frac{1}{d^2} {}_3F_3 \text{ AppellF1} \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin[e+fx]}{(1-\frac{c}{d})d}, -\frac{c+d \sin[e+fx]}{(-1-\frac{c}{d})d} \right] \right. \\ \left. \sec[e+fx] \sqrt{\frac{-d-d \sin[e+fx]}{c-d}} \sqrt{\frac{d-d \sin[e+fx]}{c+d}} (c+d \sin[e+fx])^{1/3} + \right.$$

$$\frac{1}{4 d^2} {}_3\text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin[e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin[e+f x]}{\left(-1-\frac{c}{d}\right) d}\right] \sec[e+f x]$$

$$\sqrt{\frac{-d-d \sin[e+f x]}{c-d}} \sqrt{\frac{d-d \sin[e+f x]}{c+d}} (c+d \sin[e+f x])^{4/3} +$$

$$\frac{1}{f} (c+d \sin[e+f x])^{1/3} \left(-\frac{1}{58240 d^3} {}_3\left(-216 b^2 c^4+768 a b c^3 d-832 a^2 c^2 d^2+\right.\right.$$

$$\left.332 b^2 c^2 d^2+7232 a b c d^3+2912 a^2 d^4+1729 b^2 d^4\right) \cos[e+f x]-$$

$$\frac{3\left(8 b^2 c^2+896 a b c d+416 a^2 d^2+117 b^2 d^2\right) \cos\left[3(e+f x)\right]}{16640 d} +\frac{3}{256} b^2 d \cos\left[5(e+f x)\right]+$$

$$\frac{1}{14560 d^2} {}_3\left(-18 b^2 c^3+64 a b c^2 d+1144 a^2 c d^2+23 b^2 c d^2+80 a b d^3\right) \sin\left[2(e+f x)\right]-$$

$$\left. \frac{3 b\left(17 b c+32 a d\right) \sin\left[4(e+f x)\right]}{1664}\right)$$

Problem 1517: Result more than twice size of optimal antiderivative.

$$\int \cos [e+f x]^2 (a+b \sin [e+f x]) (c+d \sin [e+f x])^{4 / 3} d x$$

Optimal (type 6, 341 leaves, 10 steps):

$$-\frac{3(6 b c-13 a d) \cos [e+f x](c+d \sin [e+f x])^{7 / 3}}{130 d^2 f} +$$

$$\frac{3 b \cos [e+f x] \sin [e+f x](c+d \sin [e+f x])^{7 / 3}}{13 d f} +$$

$$\left(3(c+d)^2(6 b c^2-13 a c d-10 b d^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2},-\frac{7}{3}, \frac{3}{2},\right.\right.$$

$$\left.\frac{1}{2}(1-\sin [e+f x]), \frac{d(1-\sin [e+f x])}{c+d}\right] \cos [e+f x](c+d \sin [e+f x])^{1 / 3}\left.\right) /$$

$$\left(65 \sqrt{2} d^3 f \sqrt{1+\sin [e+f x]}\left(\frac{c+d \sin [e+f x]}{c+d}\right)^{1 / 3}\right)-$$

$$\left(3(c-d)(c+d)^2(6 b c-13 a d) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2},-\frac{4}{3}, \frac{3}{2}, \frac{1}{2}(1-\sin [e+f x]),\right.\right.$$

$$\left.\frac{d(1-\sin [e+f x])}{c+d}\right] \cos [e+f x](c+d \sin [e+f x])^{1 / 3}\left.\right) /$$

$$\left(65 \sqrt{2} d^3 f \sqrt{1+\sin [e+f x]}\left(\frac{c+d \sin [e+f x]}{c+d}\right)^{1 / 3}\right)$$

Result (type 6, 2110 leaves):

$$\frac{1}{910 f} {}_5\text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d}\right]$$

$$\begin{aligned}
 & \text{Sec}[e + f x] \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} - \\
 & \frac{1}{455 d^2 f} 9 b c^3 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \\
 & \text{Sec}[e + f x] \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} + \\
 & \frac{1}{35 d f} 54 a c^2 \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \\
 & \text{Sec}[e + f x] \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} + \frac{1}{40 f} \\
 & 9 a d \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \text{Sec}[e + f x] \\
 & \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} + \frac{1}{130 f} \\
 & 9 b c^2 \left(-\frac{1}{d^2} 3 c \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \right. \\
 & \text{Sec}[e + f x] \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} + \\
 & \left. \frac{1}{4 d^2} 3 \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \text{Sec}[e + f x] \right. \\
 & \left. \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{4/3} \right) - \frac{1}{455 d^2 f} \\
 & 9 b c^4 \left(-\frac{1}{d^2} 3 c \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \right. \\
 & \text{Sec}[e + f x] \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{1/3} + \\
 & \left. \frac{1}{4 d^2} 3 \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c + d \text{Sin}[e + f x]}{(1 - \frac{c}{d}) d}, -\frac{c + d \text{Sin}[e + f x]}{(-1 - \frac{c}{d}) d}\right] \text{Sec}[e + f x] \right. \\
 & \left. \sqrt{\frac{-d - d \text{Sin}[e + f x]}{c - d}} \sqrt{\frac{d - d \text{Sin}[e + f x]}{c + d}} (c + d \text{Sin}[e + f x])^{4/3} \right) + \frac{1}{70 d f}
 \end{aligned}$$

$$\begin{aligned}
 & 3 a c^3 \left(-\frac{1}{d^2} {}_3 F_4 \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \right. \\
 & \quad \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \quad \frac{1}{4 d^2} {}_3 F_4 \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \sec [e+f x] \\
 & \quad \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) + \frac{1}{280 f} \\
 & 153 a c d \left(-\frac{1}{d^2} {}_3 F_4 \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \right. \\
 & \quad \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \quad \frac{1}{4 d^2} {}_3 F_4 \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \sec [e+f x] \\
 & \quad \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) + \frac{1}{91 f} \\
 & 12 b d^2 \left(-\frac{1}{d^2} {}_3 F_4 \left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \right. \\
 & \quad \sec [e+f x] \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{1/3} + \\
 & \quad \frac{1}{4 d^2} {}_3 F_4 \left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, -\frac{c+d \sin [e+f x]}{\left(1-\frac{c}{d}\right) d}, -\frac{c+d \sin [e+f x]}{\left(-1-\frac{c}{d}\right) d} \right] \sec [e+f x] \\
 & \quad \left. \sqrt{\frac{-d-d \sin [e+f x]}{c-d}} \sqrt{\frac{d-d \sin [e+f x]}{c+d}} (c+d \sin [e+f x])^{4/3} \right) + \frac{1}{f} (c+d \sin [e+f x])^{1/3} \\
 & \left(-\frac{3\left(12 b c^3-26 a c^2 d+113 b c d^2+91 a d^3\right) \cos [e+f x]}{1820 d^2}-\frac{3}{520}(14 b c+13 a d) \cos [3(e+f x)]+\right. \\
 & \quad \left. \frac{3\left(4 b c^2+143 a c d+5 b d^2\right) \sin [2(e+f x)]}{1820 d}-\frac{3}{104} b d \sin [4(e+f x)] \right)
 \end{aligned}$$

Problem 1518: Result more than twice size of optimal antiderivative.

$$\int \text{Cos}[e + f x]^2 (c + d \text{Sin}[e + f x])^{4/3} dx$$

Optimal (type 6, 125 leaves, 2 steps):

$$\left(3 \text{AppellF1}\left[\frac{7}{3}, -\frac{1}{2}, -\frac{1}{2}, \frac{10}{3}, \frac{c + d \text{Sin}[e + f x]}{c - d}, \frac{c + d \text{Sin}[e + f x]}{c + d}\right] \text{Cos}[e + f x] \right. \\ \left. (c + d \text{Sin}[e + f x])^{7/3} \right) / \left(7 d f \sqrt{1 - \frac{c + d \text{Sin}[e + f x]}{c - d}} \sqrt{1 - \frac{c + d \text{Sin}[e + f x]}{c + d}} \right)$$

Result (type 6, 301 leaves):

$$-\frac{1}{1120 d^3 f} 3 \text{Sec}[e + f x] (c + d \text{Sin}[e + f x])^{1/3} \\ \left(12 (4 c^4 + 3 c^2 d^2 - 7 d^4) \text{AppellF1}\left[\frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, \frac{c + d \text{Sin}[e + f x]}{c - d}, \frac{c + d \text{Sin}[e + f x]}{c + d}\right] \right. \\ \sqrt{-\frac{d (-1 + \text{Sin}[e + f x])}{c + d}} \sqrt{-\frac{d (1 + \text{Sin}[e + f x])}{c - d}} - \\ 3 c (4 c^2 + 51 d^2) \text{AppellF1}\left[\frac{4}{3}, \frac{1}{2}, \frac{1}{2}, \frac{7}{3}, \frac{c + d \text{Sin}[e + f x]}{c - d}, \frac{c + d \text{Sin}[e + f x]}{c + d}\right] \\ \sqrt{-\frac{d (-1 + \text{Sin}[e + f x])}{c + d}} \sqrt{-\frac{d (1 + \text{Sin}[e + f x])}{c - d}} (c + d \text{Sin}[e + f x]) + \\ \left. 4 d^2 \text{Cos}[e + f x]^2 (-4 c^2 + 7 d^2 + 14 d^2 \text{Cos}[2 (e + f x)] - 44 c d \text{Sin}[e + f x]) \right)$$

Problem 1523: Unable to integrate problem.

$$\int \text{Cos}[e + f x]^2 (a + b \text{Sin}[e + f x])^2 (c + d \text{Sin}[e + f x])^n dx$$

Optimal (type 6, 552 leaves, 11 steps):

$$\begin{aligned}
 & \left((2 a^2 d^2 (3+n) - 4 a b c d (4+n) + b^2 (6 c^2 - d^2 (3+n))) \operatorname{Cos}[e+f x] (c+d \operatorname{Sin}[e+f x])^{1+n} \right) / \\
 & \left(d^3 f (2+n) (3+n) (4+n) \right) - \frac{b (3 b c - 2 a d) \operatorname{Cos}[e+f x] \operatorname{Sin}[e+f x] (c+d \operatorname{Sin}[e+f x])^{1+n}}{d^2 f (3+n) (4+n)} + \\
 & \frac{\operatorname{Cos}[e+f x] (a+b \operatorname{Sin}[e+f x])^2 (c+d \operatorname{Sin}[e+f x])^{1+n}}{d f (4+n)} - \\
 & \left(\sqrt{2} (c+d) (a^2 c d^2 (12+7 n+n^2) - 2 a b d (4+n) (2 c^2 - d^2 (2+n)) + b^2 c (6 c^2 - d^2 (3-n-n^2))) \right) \\
 & \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -1-n, \frac{3}{2}, \frac{1}{2} (1-\operatorname{Sin}[e+f x]), \frac{d (1-\operatorname{Sin}[e+f x])}{c+d}\right] \operatorname{Cos}[e+f x] \\
 & (c+d \operatorname{Sin}[e+f x])^n \left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d} \right)^{-n} \left/ \left(d^4 f (2+n) (3+n) (4+n) \sqrt{1+\operatorname{Sin}[e+f x]} \right) \right. - \\
 & \left(\sqrt{2} (c^2 - d^2) (4 a b c d (4+n) - a^2 d^2 (12+7 n+n^2) - b^2 (6 c^2 + d^2 (3+4 n+n^2))) \right) \\
 & \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -n, \frac{3}{2}, \frac{1}{2} (1-\operatorname{Sin}[e+f x]), \frac{d (1-\operatorname{Sin}[e+f x])}{c+d}\right] \operatorname{Cos}[e+f x] \\
 & (c+d \operatorname{Sin}[e+f x])^n \left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d} \right)^{-n} \left/ \left(d^4 f (2+n) (3+n) (4+n) \sqrt{1+\operatorname{Sin}[e+f x]} \right) \right.
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \operatorname{Cos}[e+f x]^2 (a+b \operatorname{Sin}[e+f x])^2 (c+d \operatorname{Sin}[e+f x])^n dx$$

Problem 1524: Unable to integrate problem.

$$\int \operatorname{Cos}[e+f x]^2 (a+b \operatorname{Sin}[e+f x]) (c+d \operatorname{Sin}[e+f x])^n dx$$

Optimal (type 6, 375 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{(2 b c - a d (3+n)) \operatorname{Cos}[e+f x] (c+d \operatorname{Sin}[e+f x])^{1+n}}{d^2 f (2+n) (3+n)} + \\
 & \frac{b \operatorname{Cos}[e+f x] \operatorname{Sin}[e+f x] (c+d \operatorname{Sin}[e+f x])^{1+n}}{d f (3+n)} - \\
 & \left(\sqrt{2} (c+d) (a c d (3+n) - b (2 c^2 - d^2 (2+n))) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -1-n, \frac{3}{2}, \frac{1}{2} (1-\operatorname{Sin}[e+f x]), \frac{d (1-\operatorname{Sin}[e+f x])}{c+d}\right], \right. \\
 & \left. \frac{d (1-\operatorname{Sin}[e+f x])}{c+d} \right] \operatorname{Cos}[e+f x] (c+d \operatorname{Sin}[e+f x])^n \left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d} \right)^{-n} \left/ \right. \\
 & \left(d^3 f (2+n) (3+n) \sqrt{1+\operatorname{Sin}[e+f x]} \right) - \left(\sqrt{2} (c^2 - d^2) (2 b c - a d (3+n)) \right) \\
 & \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -n, \frac{3}{2}, \frac{1}{2} (1-\operatorname{Sin}[e+f x]), \frac{d (1-\operatorname{Sin}[e+f x])}{c+d}\right] \operatorname{Cos}[e+f x] \\
 & (c+d \operatorname{Sin}[e+f x])^n \left(\frac{c+d \operatorname{Sin}[e+f x]}{c+d} \right)^{-n} \left/ \left(d^3 f (2+n) (3+n) \sqrt{1+\operatorname{Sin}[e+f x]} \right) \right.
 \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \cos [e+f x]^2 (a+b \sin [e+f x]) (c+d \sin [e+f x])^n dx$$

Problem 1525: Unable to integrate problem.

$$\int \cos [e+f x]^2 (c+d \sin [e+f x])^n dx$$

Optimal (type 6, 127 leaves, 2 steps):

$$\left(\text{AppellF1} \left[1+n, -\frac{1}{2}, -\frac{1}{2}, 2+n, \frac{c+d \sin [e+f x]}{c-d}, \frac{c+d \sin [e+f x]}{c+d} \right] \cos [e+f x] \right. \\ \left. (c+d \sin [e+f x])^{1+n} \right) / \left(d f (1+n) \sqrt{1-\frac{c+d \sin [e+f x]}{c-d}} \sqrt{1-\frac{c+d \sin [e+f x]}{c+d}} \right)$$

Result (type 8, 23 leaves):

$$\int \cos [e+f x]^2 (c+d \sin [e+f x])^n dx$$

Problem 1532: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x] (a+b \sin [c+d x]) (A+B \sin [c+d x]) dx$$

Optimal (type 3, 64 leaves, 5 steps):

$$-\frac{(a+b)(A+B) \log [1-\sin [c+d x]]}{2 d} + \frac{(a-b)(A-B) \log [1+\sin [c+d x]]}{2 d} - \frac{b B \sin [c+d x]}{d}$$

Result (type 3, 172 leaves):

$$-\frac{A b \log [\cos [c+d x]]}{d} - \frac{a B \log [\cos [c+d x]]}{d} - \frac{a A \log \left[\cos \left[\frac{c}{2} + \frac{d x}{2} \right] - \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right]}{d} + \\ \frac{a A \log \left[\cos \left[\frac{c}{2} + \frac{d x}{2} \right] + \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right]}{d} - \frac{b B \log \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right]}{d} + \\ \frac{b B \log \left[\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right]}{d} - \frac{b B \sin [c+d x]}{d}$$

Problem 1533: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^3 (a+b \sin [c+d x]) (A+B \sin [c+d x]) dx$$

Optimal (type 3, 59 leaves, 3 steps):

$$\frac{(a-B) \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \frac{\sec [c+d x]^2 (A b+a B+(a A+b B) \sin [c+d x])}{2 d}$$

Result (type 3, 141 leaves):

$$\frac{1}{4d} \left(2(-aA + bB) \operatorname{Log} \left[\cos \left[\frac{1}{2}(c + dx) \right] - \sin \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. 2(aA - bB) \operatorname{Log} \left[\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. \frac{(a+b)(A+B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] - \sin \left[\frac{1}{2}(c + dx) \right] \right)^2} - \frac{(a-b)(A-B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right)^2} \right)$$

Problem 1534: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^5 (a + b \sin[c + dx]) (A + B \sin[c + dx]) dx$$

Optimal (type 3, 88 leaves, 4 steps):

$$\frac{(3aA - bB) \operatorname{ArcTanh}[\sin[c + dx]]}{8d} + \frac{\sec[c + dx]^4 (Ab + aB + (aA + bB) \sin[c + dx])}{4d} + \frac{(3aA - bB) \sec[c + dx] \tan[c + dx]}{8d}$$

Result (type 3, 220 leaves):

$$\frac{1}{16d} \left(2(-3aA + bB) \operatorname{Log} \left[\cos \left[\frac{1}{2}(c + dx) \right] - \sin \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. 2(3aA - bB) \operatorname{Log} \left[\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right] + \right. \\ \left. \frac{(a+b)(A+B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] - \sin \left[\frac{1}{2}(c + dx) \right] \right)^4} + \frac{b(A-B) + a(3A+B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] - \sin \left[\frac{1}{2}(c + dx) \right] \right)^2} - \right. \\ \left. \frac{(a-b)(A-B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right)^4} + \frac{a(-3A+B) + b(A+B)}{\left(\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right)^2} \right)$$

Problem 1535: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^7 (a + b \sin[c + dx]) (A + B \sin[c + dx]) dx$$

Optimal (type 3, 118 leaves, 5 steps):

$$\frac{(5aA - bB) \operatorname{ArcTanh}[\sin[c + dx]]}{16d} + \frac{\sec[c + dx]^6 (Ab + aB + (aA + bB) \sin[c + dx])}{6d} + \frac{(5aA - bB) \sec[c + dx] \tan[c + dx]}{16d} + \frac{(5aA - bB) \sec[c + dx]^3 \tan[c + dx]}{24d}$$

Result (type 3, 297 leaves):

$$\frac{1}{96 d} \left(6 (-5 a A + b B) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \right. \\
6 (5 a A - b B) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \\
\frac{2 (a + b) (A + B)}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{3 (A b + a (2 A + B))}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} + \\
\frac{3 (b (A - B) + a (5 A + B))}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} - \frac{2 (a - b) (A - B)}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^6} + \\
\left. \frac{3 (A b + a (-2 A + B))}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{3 (a (-5 A + B) + b (A + B))}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 1542: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^5 (a + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Sin}[c + d x]) dx$$

Optimal (type 3, 122 leaves, 4 steps):

$$\frac{(3 a^2 A - A b^2 - 2 a b B) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \\
\frac{\operatorname{Sec}[c + d x]^4 (B + A \operatorname{Sin}[c + d x]) (a + b \operatorname{Sin}[c + d x])^2}{4 d} + \\
\frac{\operatorname{Sec}[c + d x]^2 (2 b (2 a A - b B) + (3 a^2 A + A b^2 - 2 a b B) \operatorname{Sin}[c + d x])}{8 d}$$

Result (type 3, 255 leaves):

$$\frac{1}{16 d} \left(2 (-3 a^2 A + A b^2 + 2 a b B) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \right. \\
2 (3 a^2 A - A b^2 - 2 a b B) \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] + \\
\frac{(a + b)^2 (A + B)}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{(a + b) (a (3 A + B) - b (A + 3 B))}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} - \\
\left. \frac{(a - b)^2 (A - B)}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{(a - b) (3 a A + A b - a B - 3 b B)}{\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 1543: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^7 (a + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Sin}[c + d x]) dx$$

Optimal (type 3, 160 leaves, 5 steps):

$$\frac{(5 a^2 A - A b^2 - 2 a b B) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{16 d} +$$

$$\frac{\operatorname{Sec}[c + d x]^6 (B + A \operatorname{Sin}[c + d x]) (a + b \operatorname{Sin}[c + d x])^2}{6 d} +$$

$$\frac{\operatorname{Sec}[c + d x]^4 (2 b (4 a A - b B) + (5 a^2 A + 3 A b^2 - 2 a b B) \operatorname{Sin}[c + d x])}{24 d} +$$

$$\frac{(5 a^2 A - A b^2 - 2 a b B) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{16 d}$$

Result (type 3, 459 leaves):

$$\frac{(-5 a^2 A + A b^2 + 2 a b B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{16 d} +$$

$$\frac{(5 a^2 A - A b^2 - 2 a b B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{16 d} +$$

$$\frac{a^2 A + 2 a A b + A b^2 + a^2 B + 2 a b B + b^2 B}{48 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^6} + \frac{2 a^2 A + 2 a A b + a^2 B - b^2 B}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} +$$

$$\frac{5 a^2 A + 2 a A b - A b^2 + a^2 B - 2 a b B - b^2 B}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{-a^2 A + 2 a A b - A b^2 + a^2 B - 2 a b B + b^2 B}{48 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^6} +$$

$$\frac{-2 a^2 A + 2 a A b + a^2 B - b^2 B}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{-5 a^2 A + 2 a A b + A b^2 + a^2 B + 2 a b B - b^2 B}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2}$$

Problem 1557: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^3 (A + B \operatorname{Sin}[c + d x])}{(a + b \operatorname{Sin}[c + d x])^2} dx$$

Optimal (type 3, 228 leaves, 4 steps):

$$-\frac{(a A + 3 A b + 2 b B) \operatorname{Log}[1 - \operatorname{Sin}[c + d x]]}{4 (a + b)^3 d} +$$

$$\frac{(a A - 3 A b + 2 b B) \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{4 (a - b)^3 d} + \frac{b^2 (4 a A b - 3 a^2 B - b^2 B) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^3 d} -$$

$$\frac{b (a^2 A + 3 A b^2 - 4 a b B)}{2 (a^2 - b^2)^2 d (a + b \operatorname{Sin}[c + d x])} - \frac{\operatorname{Sec}[c + d x]^2 (A b - a B - (a A - b B) \operatorname{Sin}[c + d x])}{2 (a^2 - b^2) d (a + b \operatorname{Sin}[c + d x])}$$

Result (type 3, 347 leaves):

$$\frac{1}{4d} \left(\frac{8 \text{ i } b^2 (-4 a A b + 3 a^2 B + b^2 B) (c + d x)}{(a - b)^3 (a + b)^3} + \frac{2 \text{ i } (a A - 3 A b + 2 b B) \text{ ArcTan}[\text{Cot}[c + d x]]}{(a - b)^3} - \frac{2 \text{ i } (a A + 3 A b + 2 b B) \text{ ArcTan}[\text{Cot}[c + d x]]}{(a + b)^3} - \frac{(a A + 3 A b + 2 b B) \text{ Log}\left[\left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2\right]}{(a + b)^3} + \frac{(a A - 3 A b + 2 b B) \text{ Log}\left[\left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2\right]}{(a - b)^3} + \frac{4 b^2 (-4 a A b + 3 a^2 B + b^2 B) \text{ Log}[a + b \text{ Sin}[c + d x]]}{(-a^2 + b^2)^3} + \frac{A + B}{(a + b)^2 \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{-A + B}{(a - b)^2 \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{4 b^2 (-A b + a B)}{(a - b)^2 (a + b)^2 (a + b \text{ Sin}[c + d x])} \right)$$

Problem 1558: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x]^5 (A + B \text{ Sin}[c + d x])}{(a + b \text{ Sin}[c + d x])^2} dx$$

Optimal (type 3, 372 leaves, 5 steps):

$$\frac{(3 a^2 A + 2 a b (6 A + B) + b^2 (15 A + 8 B)) \text{ Log}[1 - \text{Sin}[c + d x]]}{16 (a + b)^4 d} + \frac{(3 a^2 A + b^2 (15 A - 8 B) - 2 a b (6 A - B)) \text{ Log}[1 + \text{Sin}[c + d x]]}{16 (a - b)^4 d} - \frac{b^4 (6 a A b - 5 a^2 B - b^2 B) \text{ Log}[a + b \text{ Sin}[c + d x]]}{(a^2 - b^2)^4 d} - \frac{b (3 a^4 A - 12 a^2 A b^2 - 15 A b^4 + 2 a^3 b B + 22 a b^3 B)}{8 (a^2 - b^2)^3 d (a + b \text{ Sin}[c + d x])} + \frac{\text{Sec}[c + d x]^4 (A b - a B - (a A - b B) \text{ Sin}[c + d x])}{4 (a^2 - b^2) d (a + b \text{ Sin}[c + d x])} + \frac{(\text{Sec}[c + d x]^2 (b (a^2 A + 5 A b^2 - 6 a b B) + (3 a^3 A - 9 a A b^2 + 2 a^2 b B + 4 b^3 B) \text{ Sin}[c + d x]))}{(8 (a^2 - b^2)^2 d (a + b \text{ Sin}[c + d x]))}$$

Result (type 3, 642 leaves):

$$\begin{aligned}
 & \frac{1}{64 d} \left(-\frac{128 i b^4 (-6 a A b + 5 a^2 B + b^2 B) (c + d x)}{(a - b)^4 (a + b)^4} + \right. \\
 & \frac{8 i (3 a^2 A + b^2 (15 A - 8 B) + 2 a b (-6 A + B)) \operatorname{ArcTan}[\operatorname{Cot}[c + d x]]}{(a - b)^4} - \\
 & \frac{8 i (3 a^2 A + 2 a b (6 A + B) + b^2 (15 A + 8 B)) \operatorname{ArcTan}[\operatorname{Cot}[c + d x]]}{(a + b)^4} - \frac{1}{(a + b)^4} \\
 & 4 (3 a^2 A + 2 a b (6 A + B) + b^2 (15 A + 8 B)) \operatorname{Log}\left[\left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^2\right] + \frac{1}{(a - b)^4} \\
 & 4 (3 a^2 A + b^2 (15 A - 8 B) + 2 a b (-6 A + B)) \operatorname{Log}\left[\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^2\right] + \\
 & \frac{64 b^4 (-6 a A b + 5 a^2 B + b^2 B) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^4} + \\
 & \frac{1}{(a^2 - b^2)^3 (a + b \operatorname{Sin}[c + d x])} \operatorname{Sec}[c + d x]^4 (-21 a^4 A b + 84 a^2 A b^3 + 9 A b^5 + 16 a^5 B - \\
 & 62 a^3 b^2 B - 26 a b^4 B - 8 b (a^4 A - 8 a^2 A b^2 - 5 A b^4 + 4 a^3 b B + 8 a b^3 B) \operatorname{Cos}[2(c + d x)] + \\
 & b (-3 a^4 A + 12 a^2 A b^2 + 15 A b^4 - 2 a^3 b B - 22 a b^3 B) \operatorname{Cos}[4(c + d x)] + 22 a^5 A \operatorname{Sin}[c + d x] - \\
 & 56 a^3 A b^2 \operatorname{Sin}[c + d x] + 34 a A b^4 \operatorname{Sin}[c + d x] - 12 a^4 b B \operatorname{Sin}[c + d x] + 36 a^2 b^3 B \operatorname{Sin}[c + d x] - \\
 & 24 b^5 B \operatorname{Sin}[c + d x] + 6 a^5 A \operatorname{Sin}[3(c + d x)] - 24 a^3 A b^2 \operatorname{Sin}[3(c + d x)] + 18 a A b^4 \operatorname{Sin}[\\
 & \left. 3(c + d x)] + 4 a^4 b B \operatorname{Sin}[3(c + d x)] + 4 a^2 b^3 B \operatorname{Sin}[3(c + d x)] - 8 b^5 B \operatorname{Sin}[3(c + d x)] \right) \Big)
 \end{aligned}$$

Problem 1559: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + d x]^7 (A + B \operatorname{Sin}[c + d x])}{(a + b \operatorname{Sin}[c + d x])^2} dx$$

Optimal (type 3, 550 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{1}{32 (a+b)^5 d} (5 a^3 A + a^2 b (25 A + 2 B) + a b^2 (47 A + 10 B) + b^3 (35 A + 16 B)) \operatorname{Log}[1 - \operatorname{Sin}[c + d x]] + \\
 & \frac{1}{32 (a-b)^5 d} (5 a^3 A - b^3 (35 A - 16 B) + a b^2 (47 A - 10 B) - a^2 (25 A b - 2 b B)) \operatorname{Log}[1 + \operatorname{Sin}[c + d x]] + \\
 & \frac{b^6 (8 a A b - 7 a^2 B - b^2 B) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^5 d} - \\
 & (b (5 a^6 A - 23 a^4 A b^2 + 47 a^2 A b^4 + 35 A b^6 + 2 a^5 b B - 12 a^3 b^3 B - 54 a b^5 B)) / \\
 & (16 (a^2 - b^2)^4 d (a + b \operatorname{Sin}[c + d x])) - \frac{\operatorname{Sec}[c + d x]^6 (A b - a B - (a A - b B) \operatorname{Sin}[c + d x])}{6 (a^2 - b^2) d (a + b \operatorname{Sin}[c + d x])} + \\
 & (\operatorname{Sec}[c + d x]^4 (b (a^2 A + 7 A b^2 - 8 a b B) + (5 a^3 A - 13 a A b^2 + 2 a^2 b B + 6 b^3 B) \operatorname{Sin}[c + d x])) / \\
 & (24 (a^2 - b^2)^2 d (a + b \operatorname{Sin}[c + d x])) + \\
 & (\operatorname{Sec}[c + d x]^2 (b (5 a^4 A - 18 a^2 A b^2 - 35 A b^4 + 2 a^3 b B + 46 a b^3 B) + 3 (5 a^5 A - 18 a^3 A b^2 + 29 a A b^4 + \\
 & 2 a^4 b B - 10 a^2 b^3 B - 8 b^5 B) \operatorname{Sin}[c + d x])) / (48 (a^2 - b^2)^3 d (a + b \operatorname{Sin}[c + d x]))
 \end{aligned}$$

Result (type 3, 1293 leaves):

$$\begin{aligned}
 & \frac{2i(-8aAb^7 + 7a^2b^6B + b^8B)(c+dx)}{(a-b)^5(a+b)^5d} + \frac{1}{16(a+b)^5d} \\
 & i(-5a^3A - 25a^2Ab - 47aAb^2 - 35Ab^3 - 2a^2bB - 10ab^2B - 16b^3B) \text{ArcTan} \left[\right. \\
 & \quad \left. \text{Csc}[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right] + \\
 & \frac{1}{16(a-b)^5d} i(5a^3A - 25a^2Ab + 47aAb^2 - 35Ab^3 + 2a^2bB - 10ab^2B + 16b^3B) \text{ArcTan} \left[\right. \\
 & \quad \left. \text{Csc}[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right] + \\
 & \frac{1}{32(a+b)^5d} (-5a^3A - 25a^2Ab - 47aAb^2 - 35Ab^3 - 2a^2bB - 10ab^2B - 16b^3B) \\
 & \quad \text{Log} \left[\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right] + \frac{1}{32(a-b)^5d} \\
 & (5a^3A - 25a^2Ab + 47aAb^2 - 35Ab^3 + 2a^2bB - 10ab^2B + 16b^3B) \\
 & \quad \text{Log} \left[\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right] + \\
 & \frac{(8aAb^7 - 7a^2b^6B - b^8B) \text{Log}[a+b \text{Sin}[c+dx]]}{(a^2 - b^2)^5d} + \frac{1}{1536(a^2 - b^2)^4d(a+b \text{Sin}[c+dx])} \\
 & \text{Sec}[c+dx]^6 (-314a^6Ab + 1342a^4Ab^3 - 2798a^2Ab^5 - 150Ab^7 + 256a^7B - 1060a^5b^2B + \\
 & \quad 2168a^3b^4B + 556ab^6B - 113a^6Ab \cos[2(c+dx)] + 827a^4Ab^3 \cos[2(c+dx)] - \\
 & \quad 2803a^2Ab^5 \cos[2(c+dx)] - 791Ab^7 \cos[2(c+dx)] - 314a^5b^2B \cos[2(c+dx)] + \\
 & \quad 1756a^3b^4B \cos[2(c+dx)] + 1438ab^6B \cos[2(c+dx)] - 70a^6Ab \cos[4(c+dx)] + \\
 & \quad 322a^4Ab^3 \cos[4(c+dx)] - 914a^2Ab^5 \cos[4(c+dx)] - 490Ab^7 \cos[4(c+dx)] - \\
 & \quad 28a^5b^2B \cos[4(c+dx)] + 392a^3b^4B \cos[4(c+dx)] + 788ab^6B \cos[4(c+dx)] - \\
 & \quad 15a^6Ab \cos[6(c+dx)] + 69a^4Ab^3 \cos[6(c+dx)] - 141a^2Ab^5 \cos[6(c+dx)] - \\
 & \quad 105Ab^7 \cos[6(c+dx)] - 6a^5b^2B \cos[6(c+dx)] + 36a^3b^4B \cos[6(c+dx)] + \\
 & \quad 162ab^6B \cos[6(c+dx)] + 396a^7A \sin[c+dx] - 1412a^5Ab^2 \sin[c+dx] + \\
 & \quad 1828a^3Ab^4 \sin[c+dx] - 812aAb^6 \sin[c+dx] - 200a^6bB \sin[c+dx] + 656a^4b^3B \\
 & \quad \sin[c+dx] - 904a^2b^5B \sin[c+dx] + 448b^7B \sin[c+dx] + 170a^7A \sin[3(c+dx)] - \\
 & \quad 782a^5Ab^2 \sin[3(c+dx)] + 1342a^3Ab^4 \sin[3(c+dx)] - 730aAb^6 \sin[3(c+dx)] + \\
 & \quad 68a^6bB \sin[3(c+dx)] - 184a^4b^3B \sin[3(c+dx)] - 124a^2b^5B \sin[3(c+dx)] + \\
 & \quad 240b^7B \sin[3(c+dx)] + 30a^7A \sin[5(c+dx)] - 138a^5Ab^2 \sin[5(c+dx)] + \\
 & \quad 282a^3Ab^4 \sin[5(c+dx)] - 174aAb^6 \sin[5(c+dx)] + 12a^6bB \sin[5(c+dx)] - \\
 & \quad 72a^4b^3B \sin[5(c+dx)] + 12a^2b^5B \sin[5(c+dx)] + 48b^7B \sin[5(c+dx)]
 \end{aligned}$$

Problem 1561: Result more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^p}{(a+b \sin[e+fx])(c+d \sin[e+fx])} dx$$

Optimal (type 6, 330 leaves, 4 steps):

$$\begin{aligned}
& - \left(\left[g \operatorname{AppellF1} \left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{a+b}{a+b \sin[e+fx]}, \frac{a-b}{a+b \sin[e+fx]} \right] (g \cos[e+fx])^{-1+p} \right. \right. \\
& \quad \left. \left. \left(-\frac{b(1-\sin[e+fx])}{a+b \sin[e+fx]} \right)^{\frac{1-p}{2}} \left(\frac{b(1+\sin[e+fx])}{a+b \sin[e+fx]} \right)^{\frac{1-p}{2}} \right] / ((bc-ad) f (1-p)) \right) + \\
& \left(g \operatorname{AppellF1} \left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{c+d}{c+d \sin[e+fx]}, \frac{c-d}{c+d \sin[e+fx]} \right] \right. \\
& \quad \left. (g \cos[e+fx])^{-1+p} \left(-\frac{d(1-\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \left(\frac{d(1+\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \right] / ((bc-ad) f (1-p))
\end{aligned}$$

Result (type 6, 9347 leaves):

$$\begin{aligned}
& - \left(\left(a^2 b^2 (g \cos[e+fx])^p \tan[e+fx] (1+\tan[e+fx]^2)^{-p/2} \right. \right. \\
& \quad \left(- \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) / \right. \right. \\
& \quad \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \tan[e+fx]^2 \right) \right) + \\
& \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e+fx]^2, \frac{(-a^2+b^2) \tan[e+fx]^2}{a^2} \right] \tan[e+fx] \right) / \\
& \left(\sqrt{1+\tan[e+fx]^2} \right. \\
& \quad \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] + \right. \\
& \quad \left. a^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, 1, 3, -\tan[e+fx]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e+fx]^2 \right] \right) \tan[e+fx]^2 \right) \right) \right) / \\
& \left((bc-ad) (-bc+ad) f (a+b \sin[e+fx]) (-b^2 \tan[e+fx]^2 + a^2 (1+\tan[e+fx]^2)) \right. \\
& \quad \left(-\frac{1}{(bc-ad) (-b^2 \tan[e+fx]^2 + a^2 (1+\tan[e+fx]^2))^2} a^2 b \tan[e+fx] \right. \\
& \quad \left. (2 a^2 \operatorname{Sec}[e+fx]^2 \tan[e+fx] - 2 b^2 \operatorname{Sec}[e+fx]^2 \tan[e+fx]) (1+\tan[e+fx]^2)^{-p/2} \right)
\end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) / \right. \right. \\
 & \quad \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+f x]^2 \right) \right) + \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \operatorname{Tan}[e+f x] \right) / \left(\sqrt{1 + \operatorname{Tan}[e+f x]^2} \right) \\
 & \quad \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[e+f x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + a^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, 1, 3, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \operatorname{Tan}[e+f x]^2 \right) \Bigg) - \\
 & \frac{1}{(b c - a d) (-b^2 \operatorname{Tan}[e+f x]^2 + a^2 (1 + \operatorname{Tan}[e+f x]^2))} a^2 b p \operatorname{Sec}[e+f x]^2 \\
 & \operatorname{Tan}[e+f x]^2 (1 + \operatorname{Tan}[e+f x]^2)^{-1-\frac{p}{2}} \\
 & \left(- \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) / \right. \right. \\
 & \quad \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+f x]^2 \right) \right) + \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e+f x]^2}{a^2} \right] \operatorname{Tan}[e+f x] \right) / \left(\sqrt{1 + \operatorname{Tan}[e+f x]^2} \right) \\
 & \quad \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[e+f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e+f x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[e+f x]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \Big) \tan[e + f x]^2 \Big) \Big) + \\
& \frac{1}{(b c - a d) (-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2))} a^2 b \sec[e + f x]^2 \\
& (1 + \tan[e + f x]^2)^{-p/2} \\
& \left(- \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) / \right. \right. \\
& \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right. \\
& \left. \tan[e + f x]^2 \right) \Big) + \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \right. \right. \\
& \left. \left. \frac{(-a^2 + b^2) \tan[e + f x]^2}{a^2} \right] \tan[e + f x] \right) \Big) / \left(\sqrt{1 + \tan[e + f x]^2} \right. \\
& \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left. \left. a^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, 1, 3, -\tan[e + f x]^2, \right. \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right) \right) \tan[e + f x]^2 \Big) \Big) + \\
& \frac{1}{(b c - a d) (-b^2 \tan[e + f x]^2 + a^2 (1 + \tan[e + f x]^2))} a^2 b \tan[e + f x] \\
& (1 + \tan[e + f x]^2)^{-p/2} \\
& \left(- \left(\left(3 a \left(-\frac{1}{3} p \operatorname{AppellF1} \left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right. \right. \right. \right. \\
& \left. \left. \sec[e + f x]^2 \tan[e + f x] + \frac{2}{3} \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \sec[e + f x]^2 \tan[e + f x] \right) \right) \right) / \right. \\
& \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan[e + f x]^2 \right] \right) \right. \\
& \left. \tan[e + f x]^2 \right) \Big) - \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x]^2 \Big/ \\
 & \left((1 + \operatorname{Tan}[e + f x]^2)^{3/2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + a^2 (1+p) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \operatorname{Tan}[e + f x]^2 \right) \right) + \\
 & \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e + f x]^2 \right) \Big/ \left(\sqrt{1 + \operatorname{Tan}[e + f x]^2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + a^2 (1+p) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \operatorname{Tan}[e + f x]^2 \right) \right) + \\
 & \left(2 b \operatorname{Tan}[e + f x] \left(\frac{1}{a^2} (-a^2 + b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] - \right. \right. \\
 & \quad \left. \frac{1}{2} (1+p) \operatorname{AppellF1}\left[2, 1 + \frac{1+p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \right) \Big/ \\
 & \left(\sqrt{1 + \operatorname{Tan}[e + f x]^2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + a^2 (1+p) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \operatorname{Tan}[e + f x]^2 \right) \right) + \\
 & \left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right. \\
 & \quad \left. \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - 3 a^2 \left(-\frac{1}{3} p \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \right. \\
& \quad \left. \frac{2}{3} \left(-1 + \frac{b^2}{a^2}\right) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \right. \right. \\
& \quad \left. \left. \text{Tan}[e + f x]^2\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \text{Tan}[e + f x]^2 \left(2 (a^2 - b^2) \right. \\
& \quad \left(-\frac{3}{5} p \text{AppellF1}\left[\frac{5}{2}, 1 + \frac{p}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right. \\
& \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{12}{5} \left(-1 + \frac{b^2}{a^2}\right) \text{AppellF1}\left[\frac{5}{2}, \frac{p}{2}, 3, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \\
& \quad a^2 p \left(\frac{6}{5} \left(-1 + \frac{b^2}{a^2}\right) \text{AppellF1}\left[\frac{5}{2}, \frac{2+p}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \right. \\
& \quad \left. \frac{3}{5} (2+p) \text{AppellF1}\left[\frac{5}{2}, 1 + \frac{2+p}{2}, 1, \frac{7}{2}, -\text{Tan}[e + f x]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) \right) \Big/ \\
& \left(-3 a^2 \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + \right. \\
& \quad \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + \right. \\
& \quad \left. a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right) \text{Tan}[e + f x]^2 \Big)^2 - \\
& \left(2 b \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \text{Tan}[e + f x]^2}{a^2}\right] \right. \\
& \quad \text{Tan}[e + f x] \left(2 \left(2 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] + a^2 (1+p) \text{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right) \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - 4 a^2 \\
& \quad \left(\left(-1 + \frac{b^2}{a^2}\right) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\text{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[e + f x]^2\right] \right. \\
& \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \frac{1}{2} (1+p) \text{AppellF1}\left[2, 1 + \frac{1+p}{2}, 1, 3, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & e + f x \Big) / \left(\sqrt{1 + \tan[e + f x]^2} \right. \\
 & \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + \right. \\
 & \left(2 (c^2 - d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + \right. \\
 & \left. c^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[e + f x]^2, \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] \right) \tan[e + f x]^2 \Big) \Big) / \\
 & \left((b c - a d) (-b c + a d) f (c + d \sin[e + f x]) (-d^2 \tan[e + f x]^2 + \right. \\
 & \left. c^2 (1 + \tan[e + f x]^2) \right) \\
 & \left(-\frac{1}{(-b c + a d) (-d^2 \tan[e + f x]^2 + c^2 (1 + \tan[e + f x]^2))^2} \right. \\
 & \left. c^2 \right. \\
 & \left. d \right. \\
 & \left. \tan[e + f x] \right. \\
 & \left. (2 c^2 \sec[e + f x]^2 \tan[e + f x] - 2 d^2 \sec[e + f x]^2 \tan[e + f x]) \right. \\
 & \left. (1 + \tan[e + f x]^2)^{-p/2} \right. \\
 & \left(-\left(\left(3 c \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] \right) / \right. \right. \\
 & \left. \left(-3 c^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + \right. \right. \\
 & \left. \left(2 (c^2 - d^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + \right. \right. \\
 & \left. c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] \right) \tan[e + f x]^2 \Big) \Big) + \\
 & \left(2 d \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \frac{(-c^2 + d^2) \tan[e + f x]^2}{c^2}\right] \tan[e + f x] \right) / \\
 & \left(\sqrt{1 + \tan[e + f x]^2} \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + \left(2 (c^2 - d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] + c^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, \right. \right. \\
 & \left. \left. 1, 3, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + f x]^2\right] \right) \tan[e + f x]^2 \Big) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(-bc + ad) (-d^2 \tan[e + fx]^2 + c^2 (1 + \tan[e + fx]^2))} \\
 & \frac{d}{c^2} \\
 & \frac{p}{\sec[e + fx]^2} \\
 & \frac{\tan[e + fx]^2}{(1 + \tan[e + fx]^2)^{-1-\frac{p}{2}}} \\
 & \left(- \left(\left(3c \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] \right) / \right. \right. \\
 & \quad \left(-3c^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + \right. \\
 & \quad \left(2(c^2 - d^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + \right. \\
 & \quad \left. \left. c^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] \right) \tan[e + fx]^2 \right) \right) + \\
 & \left(2d \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + fx]^2, \frac{(-c^2 + d^2) \tan[e + fx]^2}{c^2} \right] \tan[e + fx] \right) / \\
 & \left(\sqrt{1 + \tan[e + fx]^2} \left(-4c^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + \right. \right. \\
 & \quad \left(2(c^2 - d^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + c^2(1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, \right. \right. \\
 & \quad \left. \left. 1, 3, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] \right) \tan[e + fx]^2 \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(-bc + ad) (-d^2 \tan[e + fx]^2 + c^2 (1 + \tan[e + fx]^2))} \\
 & \frac{d}{c^2} \\
 & \frac{p}{\sec[e + fx]^2} \\
 & \frac{\tan[e + fx]^2}{(1 + \tan[e + fx]^2)^{-p/2}} \\
 & \left(- \left(\left(3c \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] \right) / \right. \right. \\
 & \quad \left(-3c^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + \right. \\
 & \quad \left(2(c^2 - d^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] + \right. \\
 & \quad \left. \left. c^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + fx]^2 \right] \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \Bigg) \tan[e + f x]^2 \Bigg) + \\
& \left(2 d \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \frac{(-c^2 + d^2) \tan[e + f x]^2}{c^2} \right] \tan[e + f x] \right) / \\
& \left(\sqrt{1 + \tan[e + f x]^2} \left(-4 c^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \right. \right. \right. \\
& \left. \left. \left. \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right) + \left(2 (c^2 - d^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right) + c^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, \right. \right. \right. \\
& \left. \left. \left. 1, 3, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right) \right] \tan[e + f x]^2 \right) \Bigg) + \\
& \frac{1}{(-b c + a d) (-d^2 \tan[e + f x]^2 + c^2 (1 + \tan[e + f x]^2))} \\
& \frac{d}{c^2} \\
& \tan[\\
& e + f x] (1 + \tan[e + f x]^2)^{-p/2} \\
& \left(- \left(\left(3 c \left(-\frac{1}{3} p \operatorname{AppellF1} \left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right] \right. \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x] + \frac{2}{3} \left(-1 + \frac{d^2}{c^2} \right) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) \right) \Bigg) / \\
& \left(-3 c^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left(2 (c^2 - d^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right] + \right. \\
& \left. c^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right] \right) \tan[e + f x]^2 \Bigg) - \\
& \left(2 d \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \frac{(-c^2 + d^2) \tan[e + f x]^2}{c^2} \right] \right. \\
& \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x]^2 \right) / \\
& \left((1 + \tan[e + f x]^2)^{3/2} \left(-4 c^2 \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\tan[e + f x]^2, \right. \right. \right. \\
& \left. \left. \left. \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right) + \left(2 (c^2 - d^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan[e + f x]^2, \left(-1 + \frac{d^2}{c^2} \right) \tan[e + f x]^2 \right) + c^2 (1+p) \operatorname{AppellF1} \left[2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{3+p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right) \tan[e+fx]^2 \right) + \\
 & \left(2 d \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e+fx]^2, \frac{(-c^2+d^2) \tan[e+fx]^2}{c^2}\right] \operatorname{Sec}[e+fx]^2 \right) / \\
 & \left(\sqrt{1+\tan[e+fx]^2} \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] + \left(2 (c^2-d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] + c^2 (1+p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \left. \left. \frac{3+p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \right) \tan[e+fx]^2 \right) + \\
 & \left(2 d \tan[e+fx] \left(\frac{1}{c^2} (-c^2+d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{(-c^2+d^2) \tan[e+fx]^2}{c^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] - \frac{1}{2} \right. \\
 & \left. (1+p) \operatorname{AppellF1}\left[2, 1 + \frac{1+p}{2}, 1, 3, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{(-c^2+d^2) \tan[e+fx]^2}{c^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) \right) / \\
 & \left(\sqrt{1+\tan[e+fx]^2} \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] + \left(2 (c^2-d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] + c^2 (1+p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \left. \left. \frac{3+p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \right) \tan[e+fx]^2 \right) + \\
 & \left(3 c \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \right. \\
 & \left(2 \left(2 (c^2-d^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] + \right. \right. \\
 & \left. \left. c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \right) \right. \\
 & \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] - 3 c^2 \left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \right. \\
 & \left. \frac{2}{3} \left(-1 + \frac{d^2}{c^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e+fx]^2 \right] \right. \\
 & \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) + \tan[e+fx]^2 \left(2 (c^2-d^2) \left(-\frac{3}{5} p \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 + \frac{p}{2}, 2, \frac{7}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \\
 & \tan[e + fx] + \frac{12}{5} \left(-1 + \frac{d^2}{c^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{p}{2}, 3, \frac{7}{2}, -\tan[e + fx]^2, \right. \\
 & \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \tan[e + fx]\right] + c^2 p \left(\frac{6}{5} \left(-1 + \frac{d^2}{c^2}\right) \right. \\
 & \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2+p}{2}, 2, \frac{7}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \right] \\
 & \operatorname{Sec}[e + fx]^2 \tan[e + fx] - \frac{3}{5} (2+p) \operatorname{AppellF1}\left[\frac{5}{2}, 1 + \frac{2+p}{2}, 1, \frac{7}{2}, \right. \\
 & \left. -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \tan[e + fx]\right] \Big) \Big) \Big) \Big) \Big) / \\
 & \left(-3 c^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \\
 & \left. \left(2 (c^2 - d^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \right. \\
 & \left. \left. c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) \tan[e + fx]^2\right) - \\
 & \left(2 d \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[e + fx]^2, \frac{(-c^2 + d^2) \tan[e + fx]^2}{c^2}\right] \tan[e + fx] \right. \\
 & \left. \left(2 \left(2 (c^2 - d^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \right. \right. \\
 & \left. \left. c^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) \right) \\
 & \operatorname{Sec}[e + fx]^2 \tan[e + fx] - 4 c^2 \left(\left(-1 + \frac{d^2}{c^2}\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \\
 & \left. \left. -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \tan[e + fx] - \right. \right. \\
 & \left. \left. \frac{1}{2} (1+p) \operatorname{AppellF1}\left[2, 1 + \frac{1+p}{2}, 1, 3, -\tan[e + fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \tan[e + fx]\right] + \tan[e + fx]^2 \right) \\
 & \left(2 (c^2 - d^2) \left(\frac{8}{3} \left(-1 + \frac{d^2}{c^2}\right) \operatorname{AppellF1}\left[3, \frac{1+p}{2}, 3, 4, -\tan[e + fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \operatorname{Sec}[e + fx]^2 \tan[e + fx] - \frac{2}{3} (1+p) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[3, 1 + \frac{1+p}{2}, 2, 4, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \right] \right. \right. \\
 & \left. \left. \operatorname{Sec}[e + fx]^2 \tan[e + fx]\right) + c^2 (1+p) \left(\frac{4}{3} \left(-1 + \frac{d^2}{c^2}\right) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[3, \frac{3+p}{2}, 2, 4, -\text{Tan}[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \\
 & \text{Sec}[e+fx]^2 \text{Tan}[e+fx] - \frac{2}{3}(3+p) \text{AppellF1}\left[3, 1 + \frac{3+p}{2}, 1, 4, \right. \\
 & \quad \left. -\text{Tan}[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left(\sqrt{1 + \text{Tan}[e+fx]^2} \left(-4c^2 \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] + \left(2(c^2 - d^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] + c^2(1+p) \text{AppellF1}\left[2, \frac{3+p}{2}, \right. \right. \\
 & \quad \left. \left. 1, 3, -\text{Tan}[e+fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Tan}[e+fx]^2 \right)^2 \right) \Bigg) \Bigg) \Bigg) \Bigg) /
 \end{aligned}$$

Problem 1562: Result more than twice size of optimal antiderivative.

$$\int \frac{(g \cos[e+fx])^p}{(a+b \sin[e+fx]) (c+d \sin[e+fx])^2} dx$$

Optimal (type 6, 508 leaves, 5 steps):

$$\begin{aligned}
 & - \left(\left[b g \text{AppellF1}\left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{a+b}{a+b \sin[e+fx]}, \frac{a-b}{a+b \sin[e+fx]}\right] \right. \right. \\
 & \quad \left. \left(g \cos[e+fx] \right)^{-1+p} \left(-\frac{b(1-\sin[e+fx])}{a+b \sin[e+fx]} \right)^{\frac{1-p}{2}} \right. \\
 & \quad \left. \left. \left(\frac{b(1+\sin[e+fx])}{a+b \sin[e+fx]} \right)^{\frac{1-p}{2}} \right) \right] / \left((bc-ad)^2 f(1-p) \right) \Bigg) + \\
 & \left(b g \text{AppellF1}\left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{c+d}{c+d \sin[e+fx]}, \frac{c-d}{c+d \sin[e+fx]}\right] \left(g \cos[e+fx] \right)^{-1+p} \right. \\
 & \quad \left. \left(-\frac{d(1-\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \left(\frac{d(1+\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \right] / \left((bc-ad)^2 f(1-p) \right) + \\
 & \left(g \text{AppellF1}\left[2-p, \frac{1-p}{2}, \frac{1-p}{2}, 3-p, \frac{c+d}{c+d \sin[e+fx]}, \frac{c-d}{c+d \sin[e+fx]}\right] \left(g \cos[e+fx] \right)^{-1+p} \right. \\
 & \quad \left. \left(-\frac{d(1-\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \left(\frac{d(1+\sin[e+fx])}{c+d \sin[e+fx]} \right)^{\frac{1-p}{2}} \right] / \left((bc-ad) f(2-p) (c+d \sin[e+fx]) \right) \Bigg)
 \end{aligned}$$

Result (type 6, 23548 leaves): Display of huge result suppressed!

Problem 1563: Result more than twice size of optimal antiderivative.

$$\int \frac{(g \operatorname{Sec}[e + f x])^p}{(a + b \operatorname{Sin}[e + f x]) (c + d \operatorname{Sin}[e + f x])} dx$$

Optimal (type 6, 308 leaves, 5 steps):

$$\begin{aligned} & - \left(\left(\operatorname{AppellF1} \left[1 + p, \frac{1 + p}{2}, \frac{1 + p}{2}, 2 + p, \frac{a + b}{a + b \operatorname{Sin}[e + f x]}, \frac{a - b}{a + b \operatorname{Sin}[e + f x]} \right] \right. \right. \\ & \quad \operatorname{Sec}[e + f x] (g \operatorname{Sec}[e + f x])^p \left(- \frac{b (1 - \operatorname{Sin}[e + f x])}{a + b \operatorname{Sin}[e + f x]} \right)^{\frac{1-p}{2}} \\ & \quad \left. \left. \left(\frac{b (1 + \operatorname{Sin}[e + f x])}{a + b \operatorname{Sin}[e + f x]} \right)^{\frac{1-p}{2}} \right) / ((b c - a d) f (1 + p)) \right) + \\ & \left(\operatorname{AppellF1} \left[1 + p, \frac{1 + p}{2}, \frac{1 + p}{2}, 2 + p, \frac{c + d}{c + d \operatorname{Sin}[e + f x]}, \frac{c - d}{c + d \operatorname{Sin}[e + f x]} \right] \operatorname{Sec}[e + f x] \right. \\ & \quad \left. (g \operatorname{Sec}[e + f x])^p \left(- \frac{d (1 - \operatorname{Sin}[e + f x])}{c + d \operatorname{Sin}[e + f x]} \right)^{\frac{1-p}{2}} \left(\frac{d (1 + \operatorname{Sin}[e + f x])}{c + d \operatorname{Sin}[e + f x]} \right)^{\frac{1-p}{2}} \right) / ((b c - a d) f (1 + p)) \end{aligned}$$

Result (type 6, 9549 leaves):

$$\begin{aligned} & - \left(\left(a^2 b^2 (g \operatorname{Sec}[e + f x])^p \operatorname{Tan}[e + f x] (1 + \operatorname{Tan}[e + f x]^2)^{p/2} \right. \right. \\ & \quad \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + f x]^2 \right] \right) / \right. \\ & \quad \left(3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + f x]^2 \right] + \right. \\ & \quad \left(a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + f x]^2 \right] + \right. \\ & \quad \left. 2 (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \right. \right. \\ & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + f x]^2 \right] \right) \operatorname{Tan}[e + f x]^2 \right) + \\ & \quad \left(2 b \operatorname{AppellF1} \left[1, \frac{1 - p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \right] \operatorname{Tan}[e + f x] \right) / \\ & \quad \left(\sqrt{1 + \operatorname{Tan}[e + f x]^2} \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1 - p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2} \right) \right. \right. \right. \\ & \quad \left. \left. \operatorname{Tan}[e + f x]^2 \right) + \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1 - p}{2}, 2, 3, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\ & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[e + f x]^2 \right] - a^2 (-1 + p) \operatorname{AppellF1} \left[2, \frac{3 - p}{2}, 1, 3, \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \operatorname{Tan}[e + f x] \right) / \left(\sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \\
 & \left. \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] - \right. \right. \\
 & \left. \left. a^2 (-1+p) \operatorname{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \operatorname{Tan}[e + f x]^2 \right) \right) + \\
 & \frac{1}{(b c - a d) (-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2))} a^2 b \operatorname{Sec}[e + f x]^2 \\
 & (1 + \operatorname{Tan}[e + f x]^2)^{p/2} \\
 & \left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) / \right. \\
 & \left(3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \\
 & \left(a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + 2 \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \right. \\
 & \left. \operatorname{Tan}[e + f x]^2 \right) + \left(2 b \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{(-a^2 + b^2) \operatorname{Tan}[e + f x]^2}{a^2} \operatorname{Tan}[e + f x] \right) / \left(\sqrt{1 + \operatorname{Tan}[e + f x]^2} \right. \right. \\
 & \left. \left. \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] + \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] - \right. \right. \\
 & \left. \left. a^2 (-1+p) \operatorname{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, -\operatorname{Tan}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right) \operatorname{Tan}[e + f x]^2 \right) \right) + \\
 & \frac{1}{(b c - a d) (-b^2 \operatorname{Tan}[e + f x]^2 + a^2 (1 + \operatorname{Tan}[e + f x]^2))} a^2 b \operatorname{Tan}[e + f x] \\
 & (1 + \operatorname{Tan}[e + f x]^2)^{p/2} \\
 & \left(\left(3 a \left(\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \right. \right. \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{2}{3} \left(-1 + \frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}[e + f x]^2, \left(-1 + \frac{b^2}{a^2}\right) \operatorname{Tan}[e + f x]^2\right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \right. \\
 & \left(a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + 2 \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \right. \\
 & \left. \tan[e+fx]^2\right) - \left(2 b \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 \right) / \\
 & \left((1 + \tan[e+fx]^2)^{3/2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] - a^2 (-1+p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \left. \left. \frac{3-p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \tan[e+fx]^2 \right) + \\
 & \left(2 b \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \right. \\
 & \left. \operatorname{Sec}[e+fx]^2 \right) / \left(\sqrt{1 + \tan[e+fx]^2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, \right. \right. \right. \\
 & \left. \left. 2, 3, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] - a^2 (-1+p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \left. \left. \frac{3-p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right) \tan[e+fx]^2 \right) + \\
 & \left(2 b \tan[e+fx] \left(-\frac{1}{2} (1-p) \operatorname{AppellF1}\left[2, 1 + \frac{1-p}{2}, 1, 3, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \right. \\
 & \left. \frac{1}{a^2} (-a^2 + b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{(-a^2 + b^2) \tan[e+fx]^2}{a^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) \right) / \\
 & \left(\sqrt{1 + \tan[e+fx]^2} \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[e+fx]^2\right] - a^2 (-1+p) \operatorname{AppellF1}\left[2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{3-p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right) \tan[e+fx]^2 \right) \right) - \\
 & \left(3a \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] \right. \\
 & \left(2 \left(a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + \right. \right. \\
 & \left. \left. 2(-a^2+b^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right) \right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \right. \\
 & \left. 3a^2 \left(\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \frac{2}{3} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) + \right. \\
 & \left. \tan[e+fx]^2 \left(a^2 p \left(\frac{6}{5} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, 1-\frac{p}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left(1-\frac{p}{2}\right) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, 2-\frac{p}{2}, 1, \frac{7}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) + 2(-a^2+b^2) \left(\frac{3}{5} p \operatorname{AppellF1}\left[\frac{5}{2}, 1-\frac{p}{2}, \right. \right. \right. \\
 & \left. \left. \left. 2, \frac{7}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right] \operatorname{Sec}[e+fx]^2 \right. \right. \\
 & \left. \left. \tan[e+fx] + \frac{12}{5} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{p}{2}, 3, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) \right) \right) \right) / \\
 & \left(3a^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + \right. \\
 & \left(a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] + \right. \\
 & \left. 2(-a^2+b^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2 \right) \right] \tan[e+fx]^2 \right)^2 - \\
 & \left(2b \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \frac{(-a^2+b^2)\tan[e+fx]^2}{a^2}\right] \tan[e+fx] \right. \\
 & \left. \left(2 \left(2(a^2-b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right)\tan[e+fx]^2\right] - \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 (-1+p) \operatorname{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \right. \\
 & \quad \left. \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] - 4a^2 \left(-\frac{1}{2}(1-p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \quad \left. \left. 1+\frac{1-p}{2}, 1, 3, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \right. \\
 & \quad \left. \tan[e+fx] + \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx]\right] + \tan[e+fx]^2 \\
 & \quad \left(2(a^2-b^2) \left(-\frac{2}{3}(1-p) \operatorname{AppellF1}\left[3, 1+\frac{1-p}{2}, 2, 4, -\tan[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \frac{8}{3} \left(-1+\frac{b^2}{a^2}\right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[3, \frac{1-p}{2}, 3, 4, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx]\right) - a^2 (-1+p) \left(-\frac{2}{3}(3-p) \operatorname{AppellF1}\left[3, \right. \right. \\
 & \quad \left. \left. 1+\frac{3-p}{2}, 1, 4, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \right. \\
 & \quad \left. \tan[e+fx] + \frac{4}{3} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[3, \frac{3-p}{2}, 2, 4, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx]\right) \Big) \Big) \Big) \Big) \Big) \Big) / \\
 & \left(\sqrt{1+\tan[e+fx]^2} \left(-4a^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \right. \right. \right. \\
 & \quad \left. \left. \tan[e+fx]^2\right] + \left(2(a^2-b^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\tan[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] - a^2 (-1+p) \operatorname{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, \right. \right. \\
 & \quad \left. \left. -\tan[e+fx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[e+fx]^2\right] \tan[e+fx]^2\right)^2\right) \Big) \Big) \Big) \Big) - \\
 & \left(c^2 d^2 (g \operatorname{Sec}[e+fx])^p \tan[e+fx] (1+\tan[e+fx]^2)^{p/2}\right) \\
 & \left(\left(3\right.\right. \\
 & \quad c \\
 & \quad \left.\operatorname{AppellF1}\left[\right.\right. \\
 & \quad \left.\left.\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, \right.\right. \\
 & \quad \left.\left.-\tan[e+fx]^2, \right.\right. \\
 & \quad \left.\left.\left(-1+\frac{d^2}{c^2}\right) \tan[e+fx]^2\right]\right) \Big) \Big) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 c^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \left(c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \quad 2\left(-c^2+d^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \right. \\
 & \quad \quad \quad \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \left. \right) \operatorname{Tan}[e+f x]^2 \left. + \right. \\
 & \left. \left(2 d \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \frac{\left(-c^2+d^2\right) \operatorname{Tan}[e+f x]^2}{c^2}\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+f x] \right) \right) / \left(\sqrt{1+\operatorname{Tan}[e+f x]^2} \right. \\
 & \quad \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \left(2\left(c^2-d^2\right) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] - \right. \\
 & \quad \quad c^2(-1+p) \operatorname{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, -\operatorname{Tan}[e+f x]^2, \right. \\
 & \quad \quad \quad \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \left. \right) \left. \right) \left. \right) \left. \right) / \\
 & \left((b c-a d)(-b c+a d) f(c+d \operatorname{Sin}[e+f x])\left(-d^2 \operatorname{Tan}[e+f x]^2+\right. \right. \\
 & \quad \left. \left. c^2\left(1+\operatorname{Tan}[e+f x]^2\right)\right) \right. \\
 & \left. \left(-\frac{1}{(-b c+a d)\left(-d^2 \operatorname{Tan}[e+f x]^2+c^2\left(1+\operatorname{Tan}[e+f x]^2\right)\right)^2} \right. \right. \\
 & \quad \left. \left. \frac{d \operatorname{Tan}[e+f x]}{\left(1+\operatorname{Tan}[e+f x]^2\right)^{p / 2}} \right. \right. \\
 & \quad \left. \left(\left(3 c \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \right) / \right. \right. \\
 & \quad \left(3 c^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \left(c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \quad 2\left(-c^2+d^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \right. \\
 & \quad \quad \quad \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \left. \right) \operatorname{Tan}[e+f x]^2 \left. + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 d \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \frac{(-c^2+d^2) \operatorname{Tan}[e+f x]^2}{c^2}\right] \operatorname{Tan}[e+f x] \right) / \\
 & \left(\sqrt{1+\operatorname{Tan}[e+f x]^2} \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \left(2 \left(c^2-d^2\right) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] - c^2(-1+p) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3-p}{2}, 1, 3, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \operatorname{Tan}[e+f x]^2 \right) \right) \right) + \\
 & \frac{1}{(-b c+a d)\left(-d^2 \operatorname{Tan}[e+f x]^2+c^2\left(1+\operatorname{Tan}[e+f x]^2\right)\right)} \\
 & \frac{d}{c^2} \\
 & \frac{p}{\operatorname{Sec}[e+f x]^2} \\
 & \frac{\operatorname{Tan}[e+f x]^2}{\left(1+\operatorname{Tan}[e+f x]^2\right)^{-1+\frac{p}{2}}} \\
 & \left(\left(3 c \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \right) / \right. \\
 & \quad \left(3 c^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \\
 & \quad \left. \left(c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \right. \right. \\
 & \quad \left. \left. 2\left(-c^2+d^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \operatorname{Tan}[e+f x]^2 \right) \right) + \\
 & \left. \left(2 d \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \frac{(-c^2+d^2) \operatorname{Tan}[e+f x]^2}{c^2}\right] \operatorname{Tan}[e+f x] \right) / \right. \\
 & \left. \left(\sqrt{1+\operatorname{Tan}[e+f x]^2} \left(-4 c^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\operatorname{Tan}[e+f x]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] + \left(2 \left(c^2-d^2\right) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] - c^2(-1+p) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3-p}{2}, 1, 3, -\operatorname{Tan}[e+f x]^2, \left(-1+\frac{d^2}{c^2}\right) \operatorname{Tan}[e+f x]^2\right] \operatorname{Tan}[e+f x]^2 \right) \right) \right) + \\
 & \frac{1}{(-b c+a d)\left(-d^2 \operatorname{Tan}[e+f x]^2+c^2\left(1+\operatorname{Tan}[e+f x]^2\right)\right)} \\
 & \frac{d}{c^2} \\
 & \frac{p}{\operatorname{Sec}[e+f x]^2}
 \end{aligned}$$

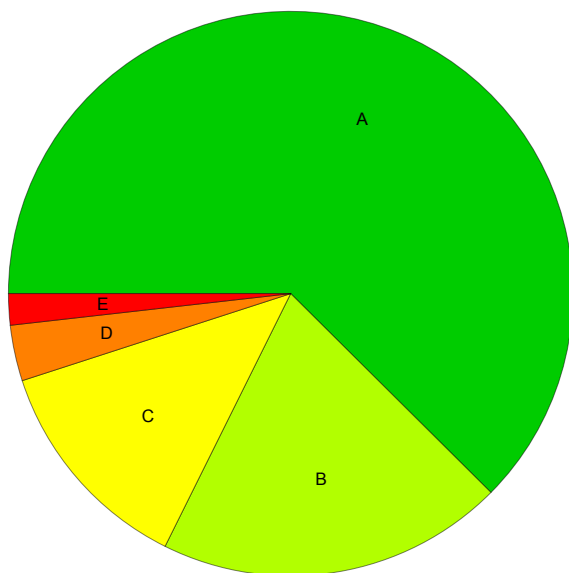
$$\begin{aligned}
 & (1 + \tan[e + fx]^2)^{p/2} \\
 & \left(\left(3c \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) / \right. \\
 & \quad \left(3c^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \\
 & \quad \left(c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \\
 & \quad \left. 2(-c^2 + d^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\tan[e + fx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) \tan[e + fx]^2 \right) + \\
 & \left. \left(2d \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e + fx]^2, \frac{(-c^2 + d^2) \tan[e + fx]^2}{c^2}\right] \tan[e + fx] \right) / \right. \\
 & \left. \left(\sqrt{1 + \tan[e + fx]^2} \left(-4c^2 \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e + fx]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2 \right) + \left(2(c^2 - d^2) \operatorname{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \\
 & \quad \left. \left. -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] - c^2(-1+p) \operatorname{AppellF1}\left[2, \right. \right. \\
 & \quad \left. \left. \frac{3-p}{2}, 1, 3, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) \tan[e + fx]^2 \right) \right) \right) + \\
 & \frac{1}{(-bc + ad) (-d^2 \tan[e + fx]^2 + c^2 (1 + \tan[e + fx]^2))} \\
 & \frac{d}{c^2} \\
 & \frac{d}{\tan[e + fx] (1 + \tan[e + fx]^2)^{p/2}} \\
 & \left(\left(3c \left(\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e + fx]^2 \tan[e + fx] + \frac{2}{3} \left(-1 + \frac{d^2}{c^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \operatorname{Sec}[e + fx]^2 \tan[e + fx] \right) \right) / \right. \\
 & \quad \left(3c^2 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \\
 & \quad \left(c^2 p \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\tan[e + fx]^2, \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] + \right. \\
 & \quad \left. 2(-c^2 + d^2) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\tan[e + fx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \tan[e + fx]^2\right] \right) \tan[e + fx]^2 \right) - \\
 & \left. \left(2d \operatorname{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\tan[e + fx]^2, \frac{(-c^2 + d^2) \tan[e + fx]^2}{c^2}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x]^2 \right) / \\
 & \left((1 + \text{Tan}[e + f x]^2)^{3/2} \left(-4 c^2 \text{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] + \left(2 (c^2 - d^2) \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] - c^2 (-1+p) \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3-p}{2}, 1, 3, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right]\right) \text{Tan}[e + f x]^2 \right) \right) + \\
 & \left(2 d \text{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\text{Tan}[e + f x]^2, \frac{(-c^2 + d^2) \text{Tan}[e + f x]^2}{c^2}\right] \text{Sec}[e + f x]^2 \right) / \\
 & \left(\sqrt{1 + \text{Tan}[e + f x]^2} \left(-4 c^2 \text{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] + \left(2 (c^2 - d^2) \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] - c^2 (-1+p) \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3-p}{2}, 1, 3, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right]\right) \text{Tan}[e + f x]^2 \right) \right) + \\
 & \left(2 d \text{Tan}[e + f x] \left(-\frac{1}{2} (1-p) \text{AppellF1}\left[2, 1 + \frac{1-p}{2}, 1, 3, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-c^2 + d^2) \text{Tan}[e + f x]^2}{c^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{1}{c^2} (-c^2 + d^2) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\text{Tan}[e + f x]^2, \frac{(-c^2 + d^2) \text{Tan}[e + f x]^2}{c^2}\right] \right. \right. \\
 & \quad \left. \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) \right) / \\
 & \left(\sqrt{1 + \text{Tan}[e + f x]^2} \left(-4 c^2 \text{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] + \left(2 (c^2 - d^2) \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] - c^2 (-1+p) \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3-p}{2}, 1, 3, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right]\right) \text{Tan}[e + f x]^2 \right) \right) - \\
 & \left(3 c \text{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] \right. \\
 & \quad \left(2 \left(c^2 p \text{AppellF1}\left[\frac{3}{2}, 1 - \frac{p}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] + 2 \right. \right. \\
 & \quad \left. \left. (-c^2 + d^2) \text{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \left(-1 + \frac{d^2}{c^2}\right) \text{Tan}[e + f x]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Sec}[e+fx]^2 \text{Tan}[e+fx] + 3c^2 \left(\frac{1}{3} p \text{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] + \right. \\
& \quad \left. \frac{2}{3} \left(-1+\frac{d^2}{c^2}\right) \text{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \right. \\
& \quad \left. \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \right) + \text{Tan}[e+fx]^2 \left(c^2 p \left(\frac{6}{5} \left(-1+\frac{d^2}{c^2}\right) \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. 1-\frac{p}{2}, 2, \frac{7}{2}, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \right. \\
& \quad \left. \text{Tan}[e+fx] - \frac{6}{5} \left(1-\frac{p}{2}\right) \text{AppellF1}\left[\frac{5}{2}, 2-\frac{p}{2}, 1, \frac{7}{2}, -\text{Tan}[e+fx]^2, \right. \right. \\
& \quad \left. \left. \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \right) + 2(-c^2+d^2) \\
& \quad \left(\frac{3}{5} p \text{AppellF1}\left[\frac{5}{2}, 1-\frac{p}{2}, 2, \frac{7}{2}, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \right. \\
& \quad \left. \text{Sec}[e+fx]^2 \text{Tan}[e+fx] + \frac{12}{5} \left(-1+\frac{d^2}{c^2}\right) \text{AppellF1}\left[\frac{5}{2}, -\frac{p}{2}, 3, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
& \left(3c^2 \text{AppellF1}\left[\frac{1}{2}, -\frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] + \right. \\
& \quad \left(c^2 p \text{AppellF1}\left[\frac{3}{2}, 1-\frac{p}{2}, 1, \frac{5}{2}, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] + \right. \\
& \quad \left. 2(-c^2+d^2) \text{AppellF1}\left[\frac{3}{2}, -\frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[e+fx]^2, \right. \right. \\
& \quad \left. \left. \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \right) \text{Tan}[e+fx]^2 \Bigg) - \\
& \left(2d \text{AppellF1}\left[1, \frac{1-p}{2}, 1, 2, -\text{Tan}[e+fx]^2, \frac{(-c^2+d^2) \text{Tan}[e+fx]^2}{c^2}\right] \text{Tan}[e+fx] \right. \\
& \quad \left. \left(2 \left(2(c^2-d^2) \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] - \right. \right. \right. \\
& \quad \left. \left. c^2(-1+p) \text{AppellF1}\left[2, \frac{3-p}{2}, 1, 3, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \right) \right. \\
& \quad \left. \text{Sec}[e+fx]^2 \text{Tan}[e+fx] - 4c^2 \left(-\frac{1}{2} (1-p) \text{AppellF1}\left[2, 1+\frac{1-p}{2}, 1, \right. \right. \right. \\
& \quad \left. \left. 3, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] + \right. \\
& \quad \left. \left. \left(-1+\frac{d^2}{c^2}\right) \text{AppellF1}\left[2, \frac{1-p}{2}, 2, 3, -\text{Tan}[e+fx]^2, \left(-1+\frac{d^2}{c^2}\right) \right. \right. \right. \\
& \quad \left. \left. \text{Tan}[e+fx]^2\right] \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \right) + \text{Tan}[e+fx]^2 \right)
\end{aligned}$$

Summary of Integration Test Results

1563 integration problems



A - 976 optimal antiderivatives

B - 311 more than twice size of optimal antiderivatives

C - 198 unnecessarily complex antiderivatives

D - 50 unable to integrate problems

E - 28 integration timeouts